

HPGe DETECTOR APPENDIX

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Abstract

The objective of this project was to identify an unknown gamma ray source by using a high-purity germanium (HPGe) detector. We calibrated the detector by using three known sources, ^{22}Na , ^{60}Co & ^{133}Ba , and then measured the energy spectrum from the unknown source. We determined the unknown source to have contained a sample of ^{238}U at some point in its lifetime, due to the fact that we detected many emissions from elements in the ^{238}U decay chain, such as ^{214}Bi & ^{214}Pb . We were also tasked with identifying radioactive sources present in the environmental background and what decay chains they might belong to. By running the detector without a source present, we found that there were many peaks from ^{214}Pb & ^{214}Bi which would point to the ^{238}U decay chain, along with peaks from sources such as ^{40}K & ^{137}Cs . We believe that we carried out the experiment successfully, completing all objectives – and if we had more time on the experiment it would have been nice to investigate the detector properties in more detail and how this would affect the obtained spectrum, especially in the low-energy limit.

1 Fitted Peaks

All of these are for the 24 hour data runs, hence the high count numbers

1.1 Barium-133

1.1.1 Gaussian Fit Only

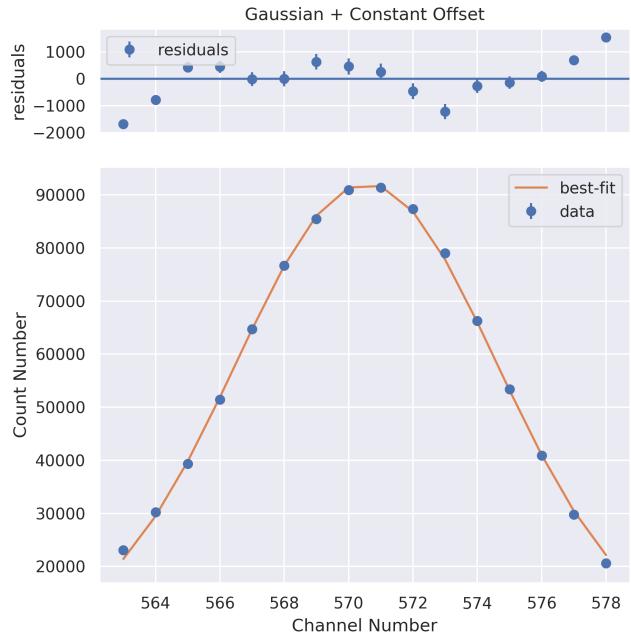
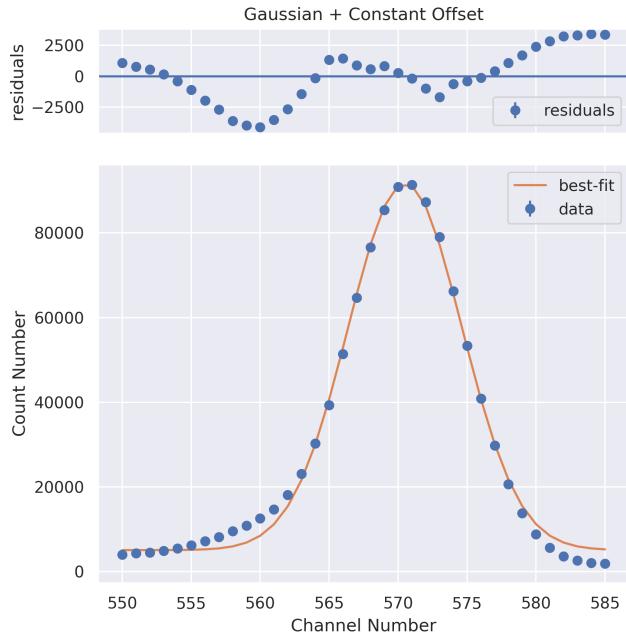


Figure 1: Fit of full & zoomed in peak of ^{133}Ba 81 keV peak

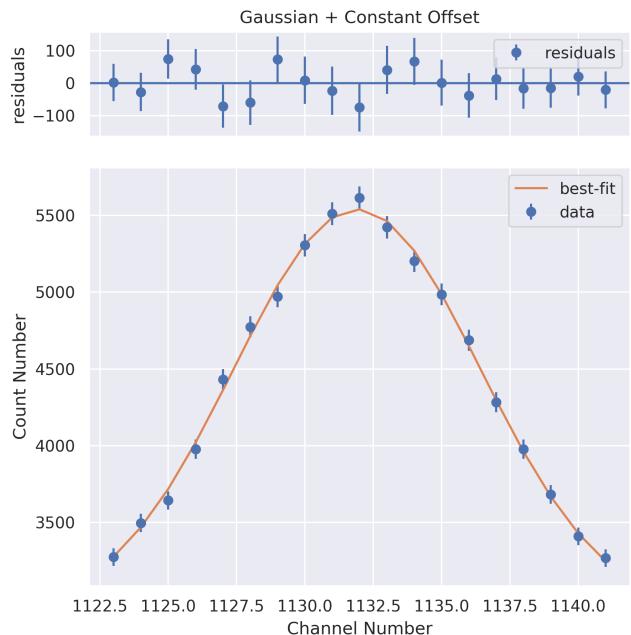
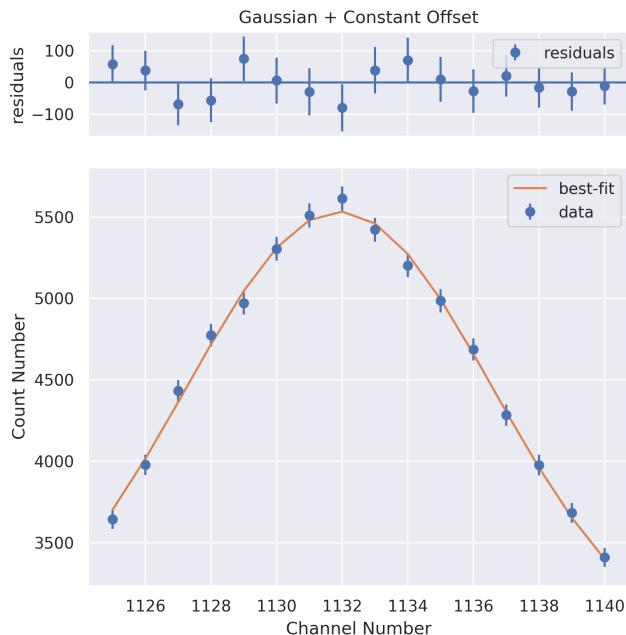
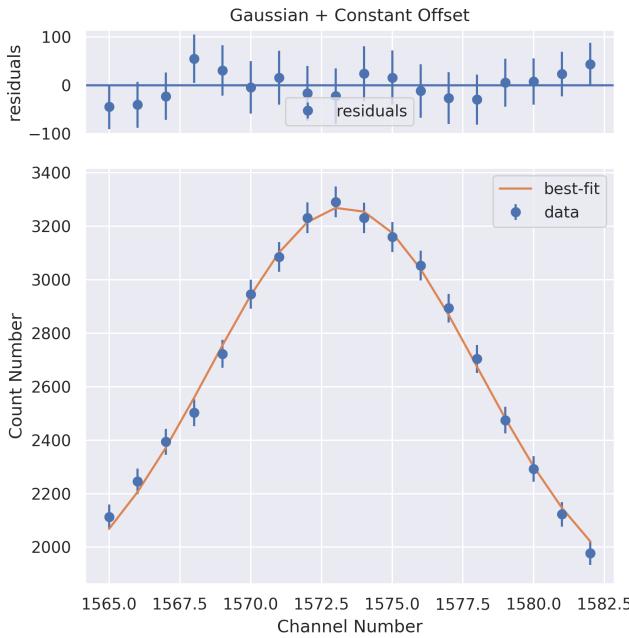
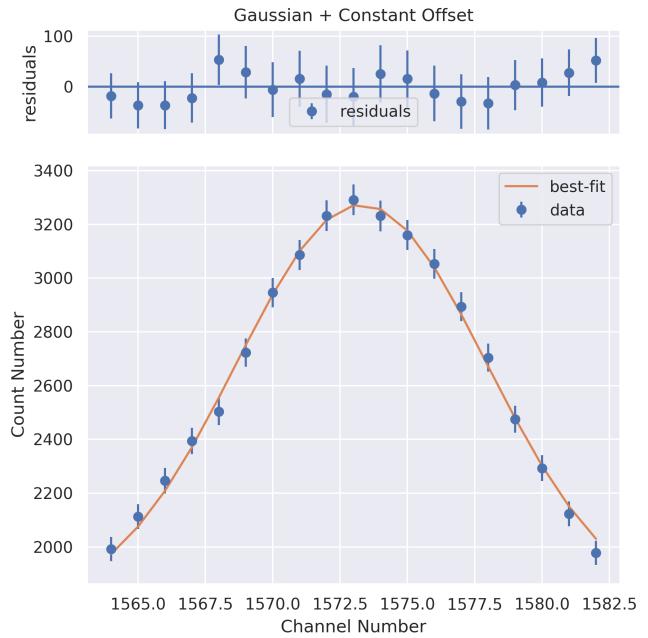


Figure 2: Fit of full & zoomed in peak of ^{133}Ba 161 keV peak

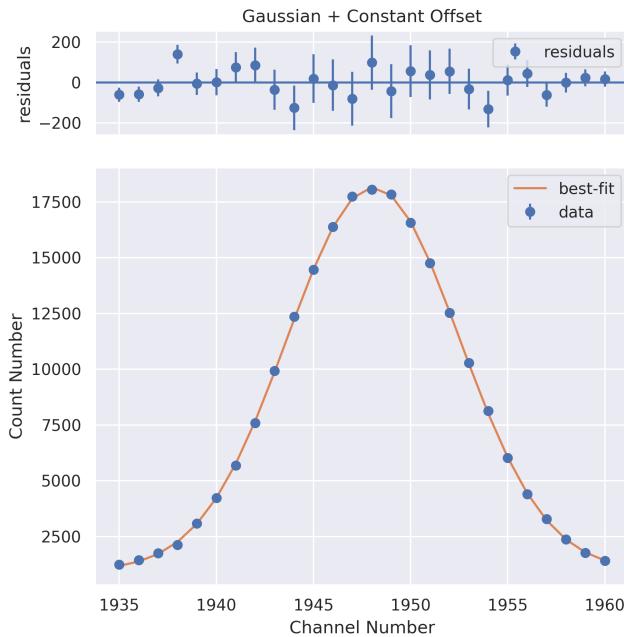


(a) Full peak with fit

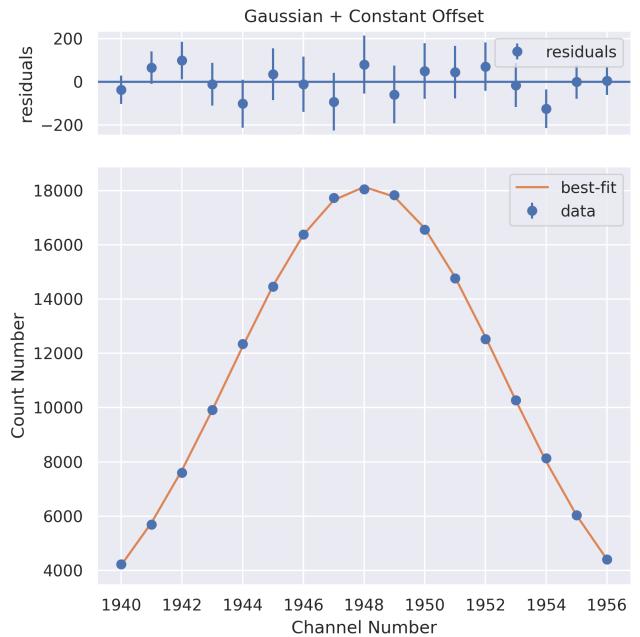


(b) Zoomed in peak with fit

Figure 3: Fit of full & zoomed in peak of ^{133}Ba 223 keV peak

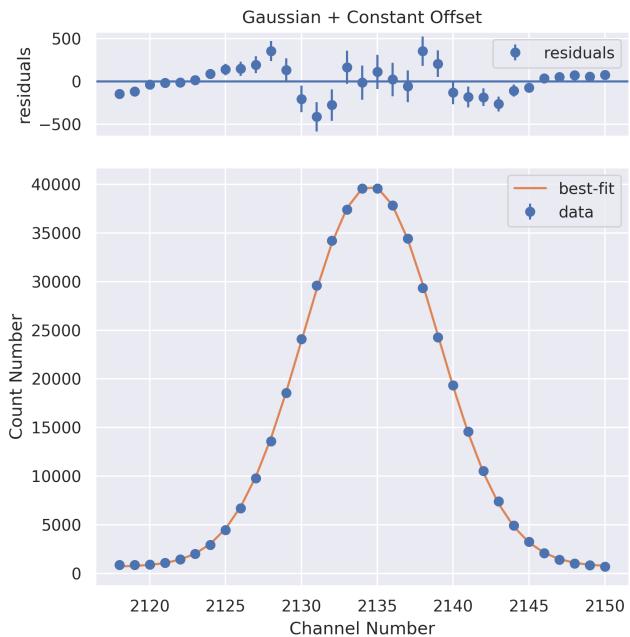


(a) Full peak with fit

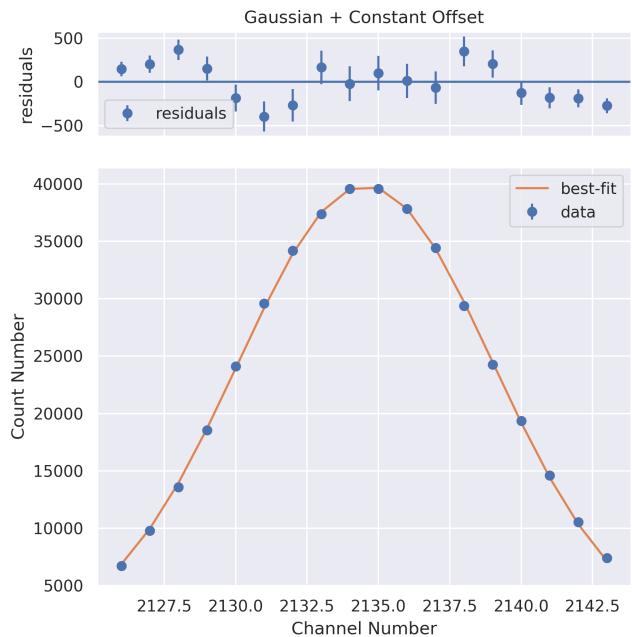


(b) Zoomed in peak with fit

Figure 4: Fit of full & zoomed in peak of ^{133}Ba 276 keV peak

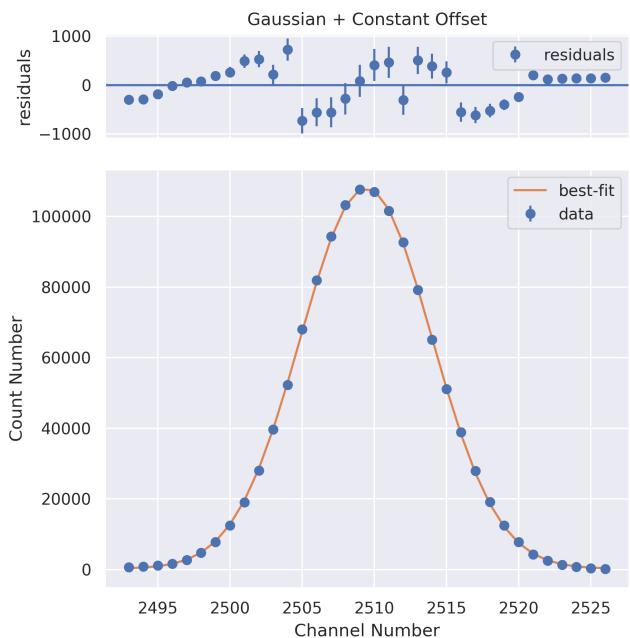


(a) Full peak with fit

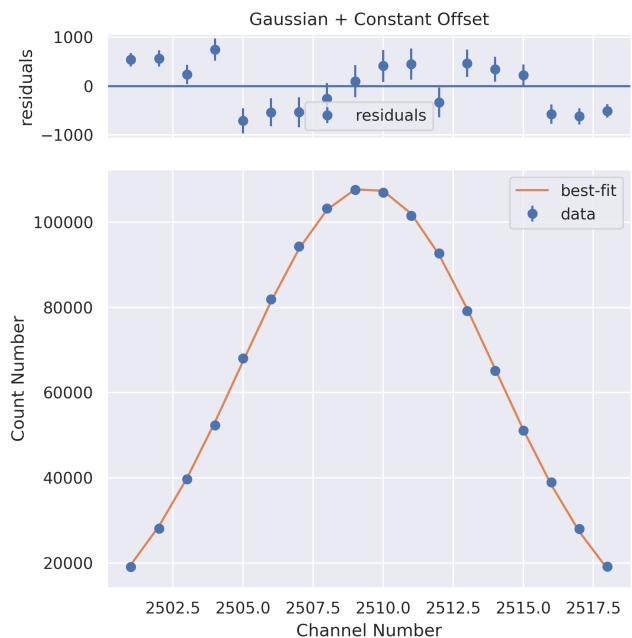


(b) Zoomed in peak with fit

Figure 5: Fit of full & zoomed in peak of ^{133}Ba 303 keV peak

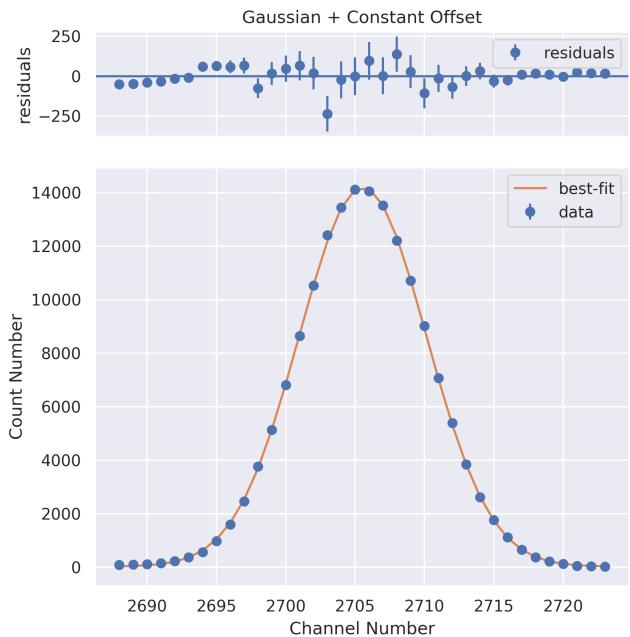


(a) Full peak with fit

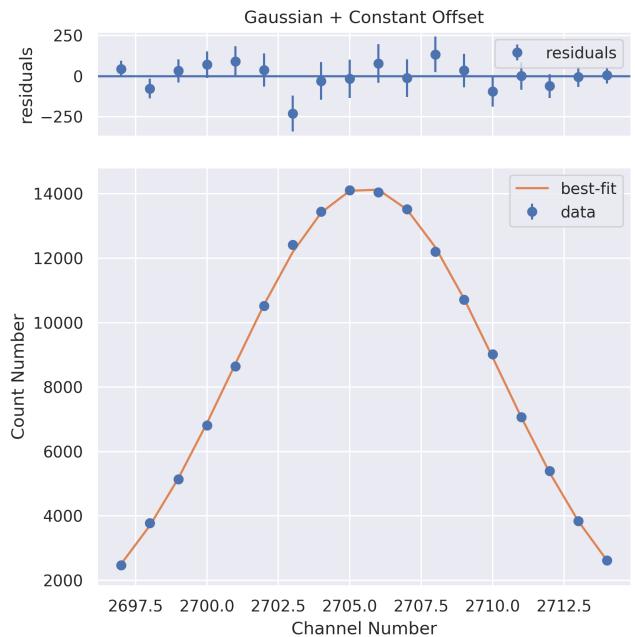


(b) Zoomed in peak with fit

Figure 6: Fit of full & zoomed in peak of ^{133}Ba 356 keV peak



(a) Full peak with fit



(b) Zoomed in peak with fit

Figure 7: Fit of full & zoomed in peak of ^{133}Ba 384 keV peak

1.1.2 Linear + Gaussian Fit

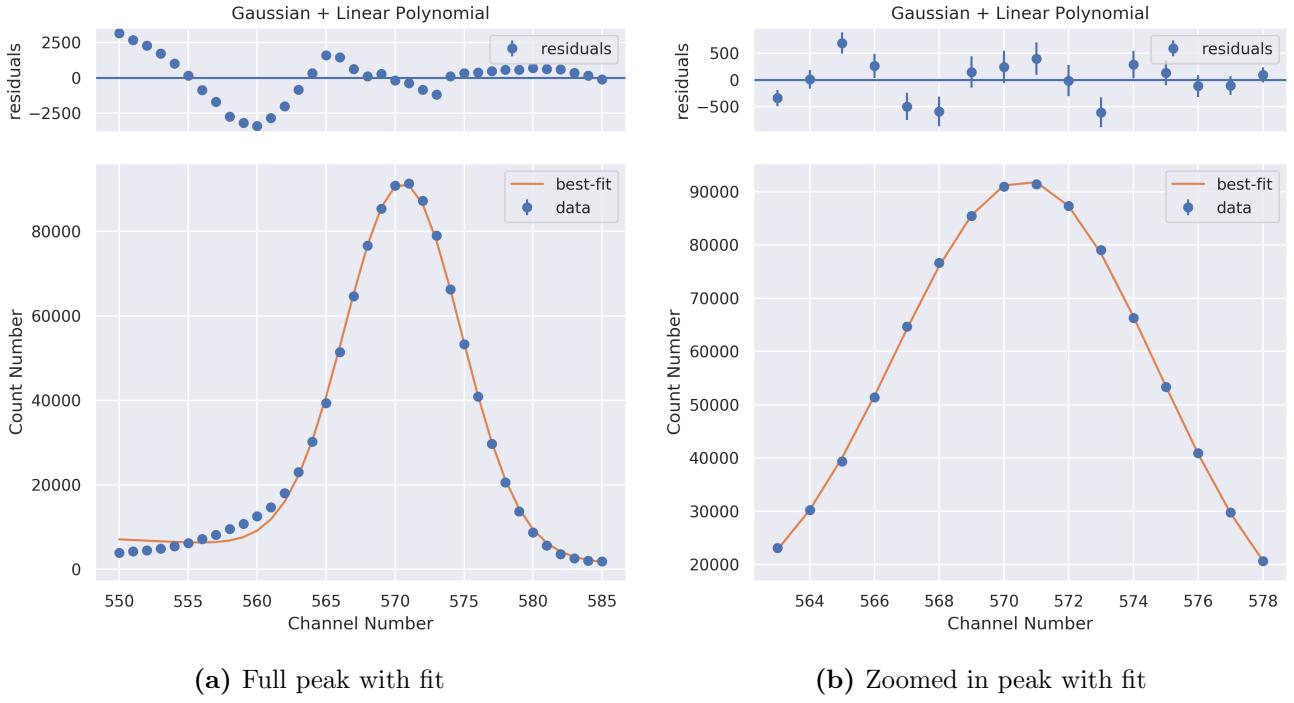


Figure 8: Fit of full & zoomed in peak of ^{133}Ba 81 keV peak

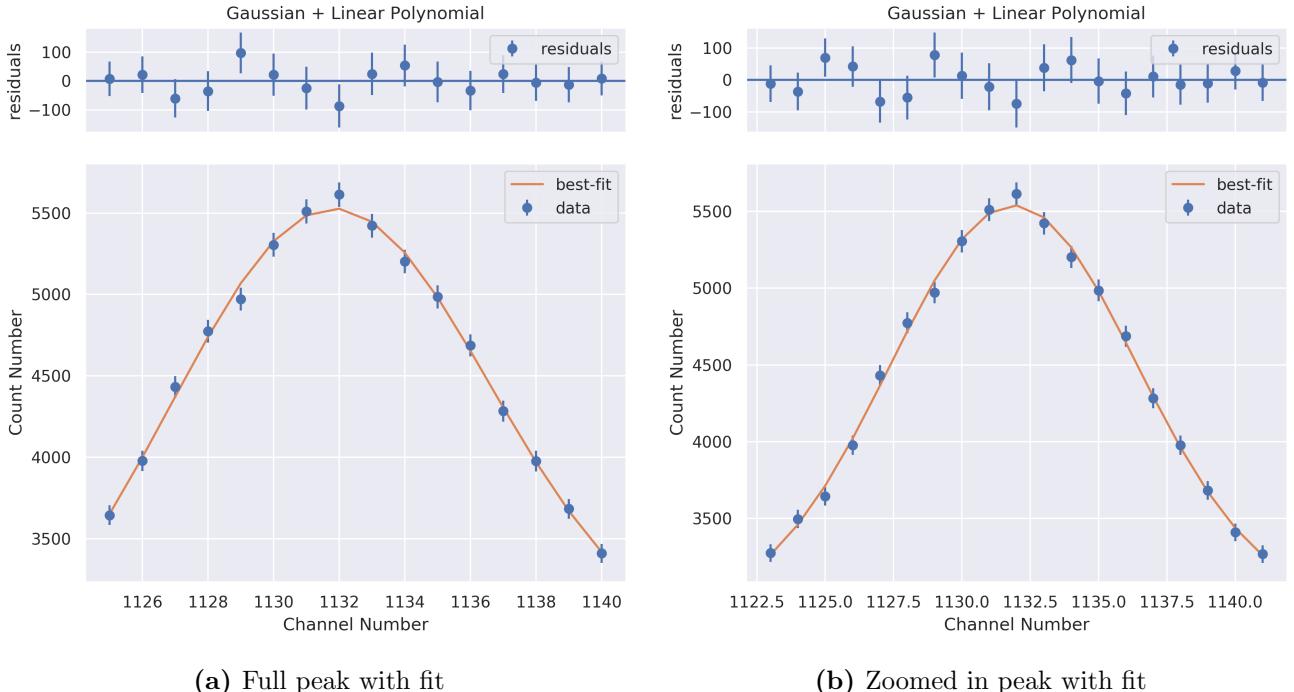
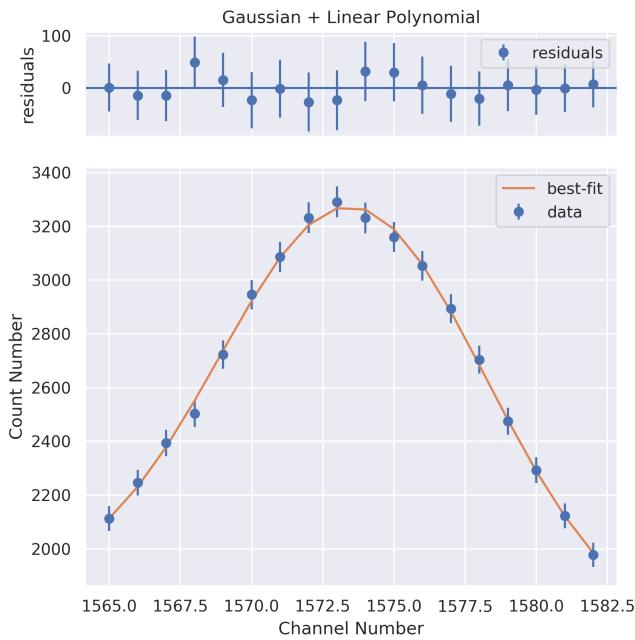
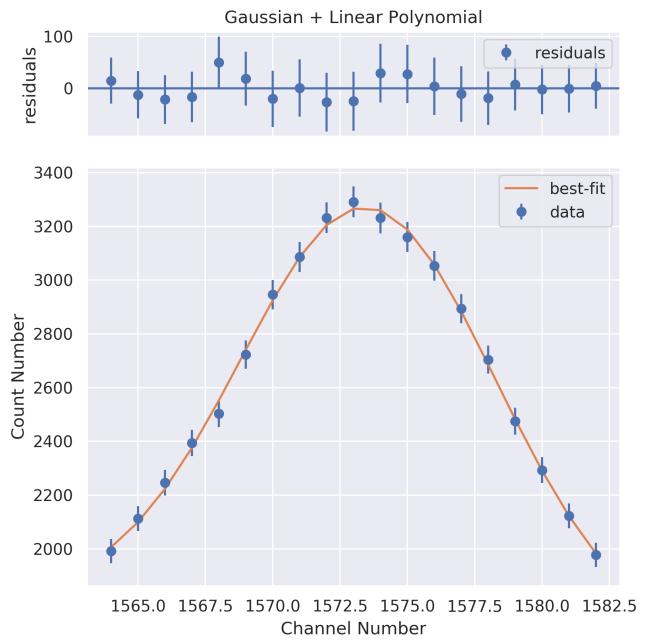


Figure 9: Fit of full & zoomed in peak of ^{133}Ba 161 keV peak

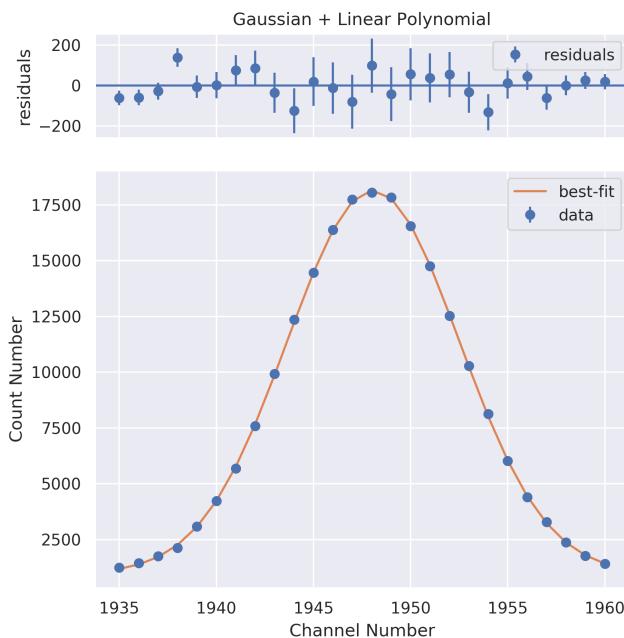


(a) Full peak with fit

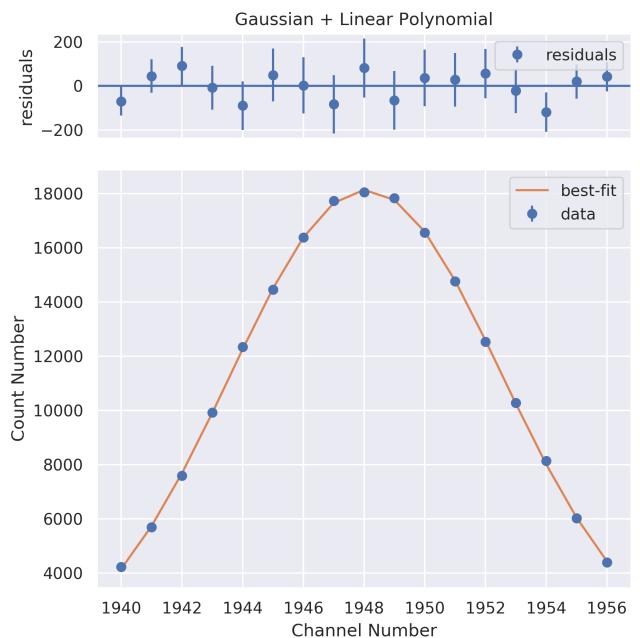


(b) Zoomed in peak with fit

Figure 10: Fit of full & zoomed in peak of ^{133}Ba 223 keV peak

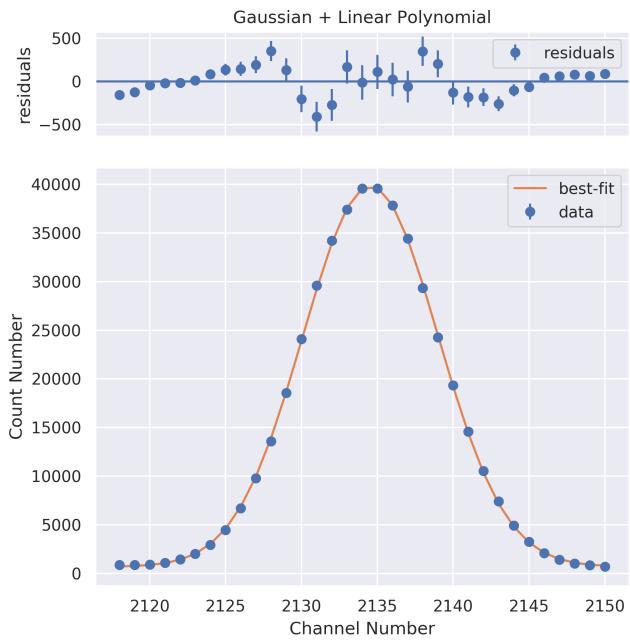


(a) Full peak with fit

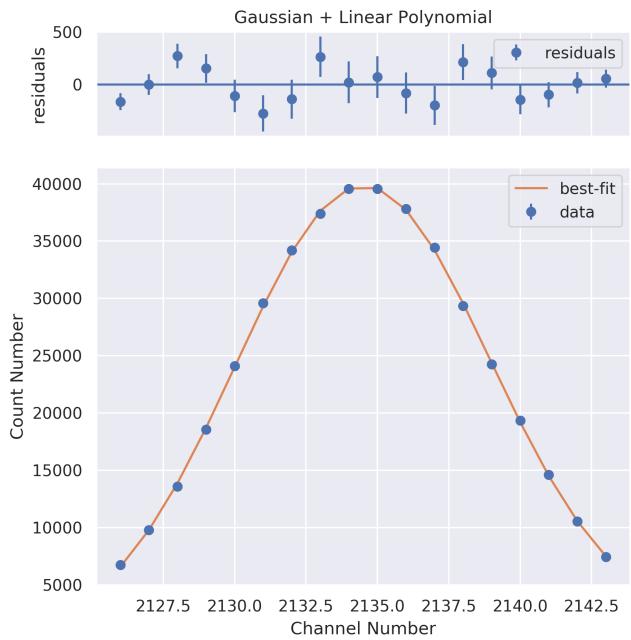


(b) Zoomed in peak with fit

Figure 11: Fit of full & zoomed in peak of ^{133}Ba 276 keV peak

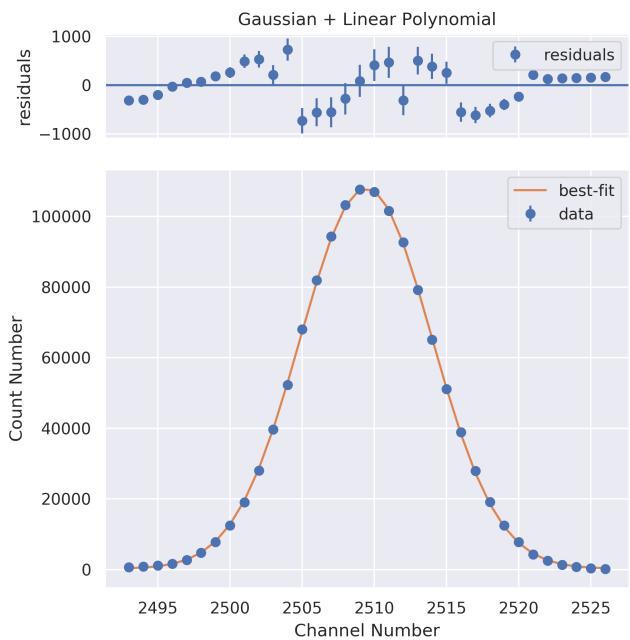


(a) Full peak with fit

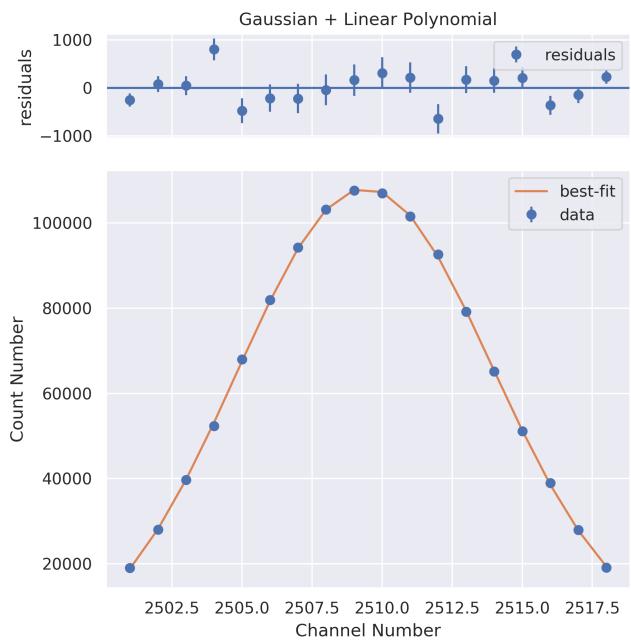


(b) Zoomed in peak with fit

Figure 12: Fit of full & zoomed in peak of ^{133}Ba 303 keV peak

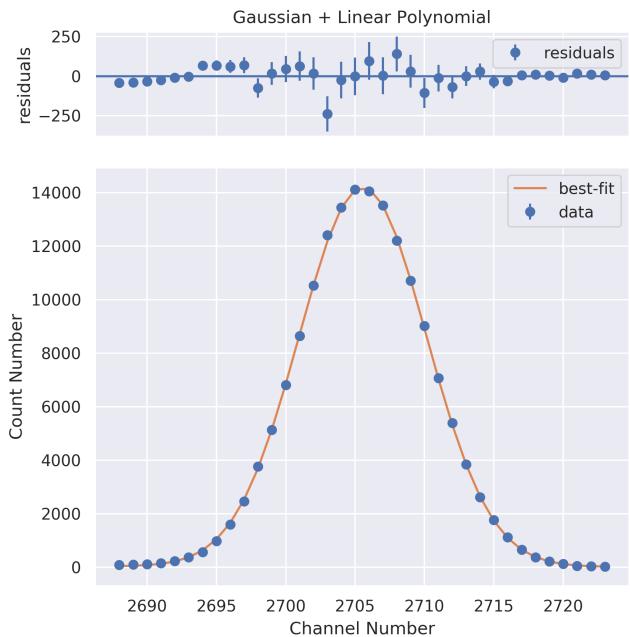


(a) Full peak with fit

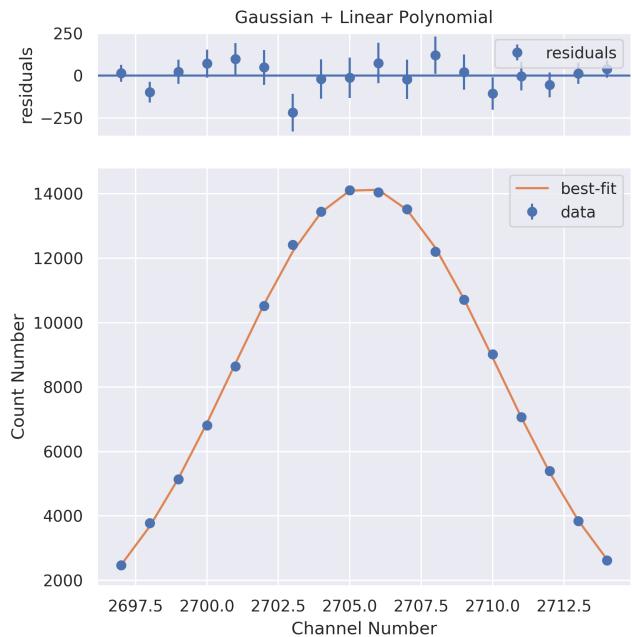


(b) Zoomed in peak with fit

Figure 13: Fit of full & zoomed in peak of ^{133}Ba 356 keV peak



(a) Full peak with fit



(b) Zoomed in peak with fit

Figure 14: Fit of full & zoomed in peak of ^{133}Ba 384 keV peak

1.1.3 Quadratic + Gaussian Fit

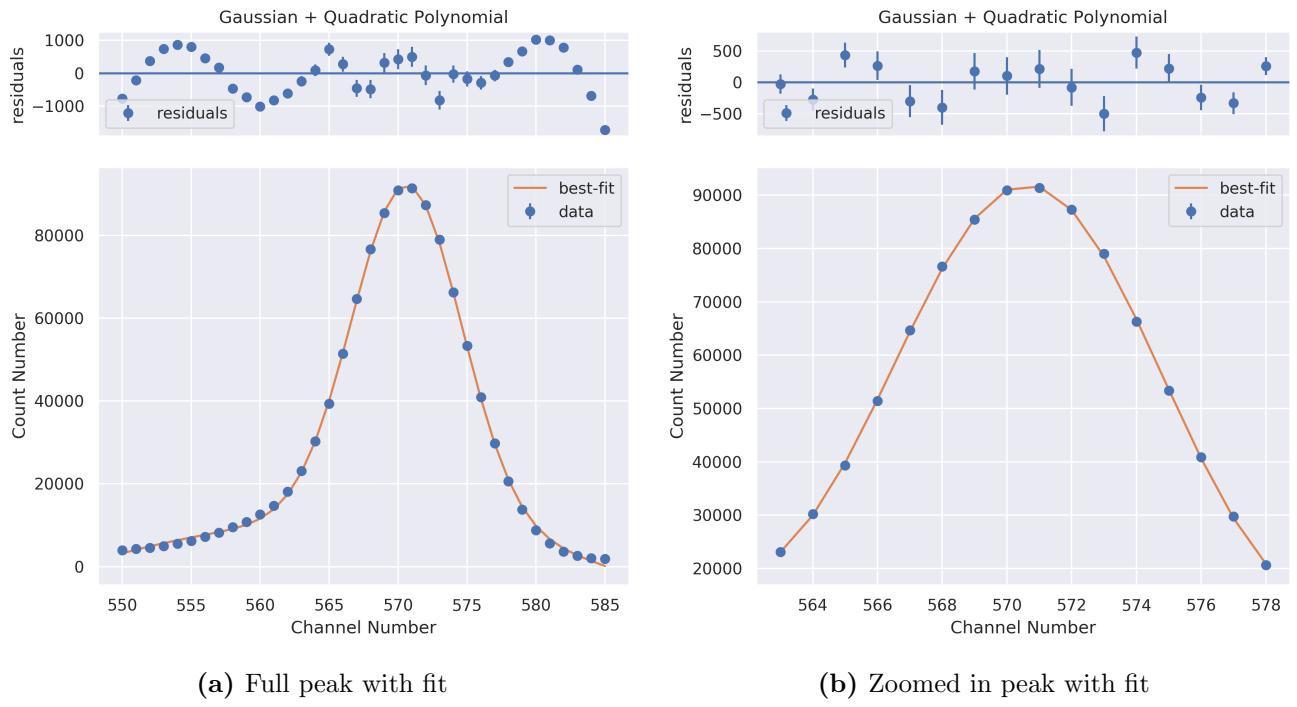


Figure 15: Fit of full & zoomed in peak of ^{133}Ba 81 keV peak

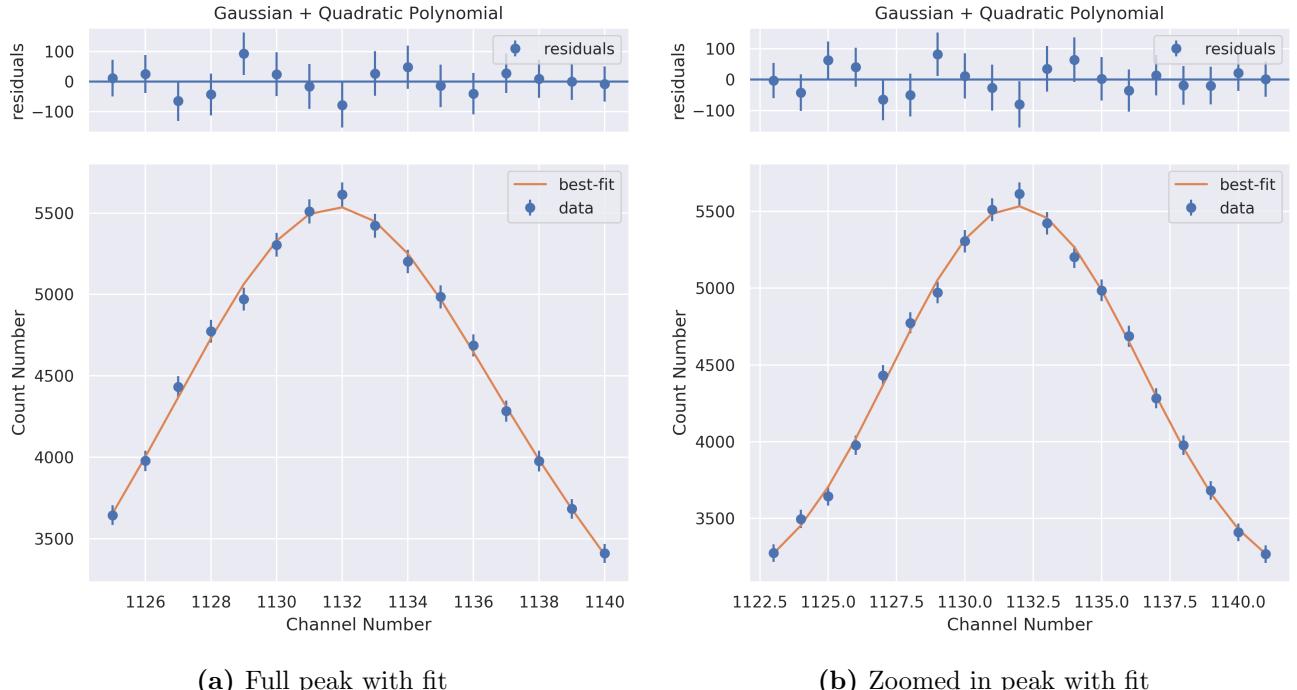
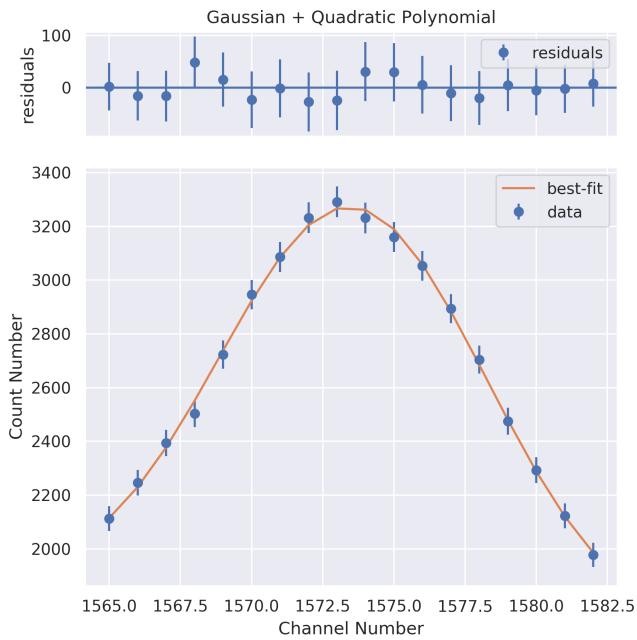
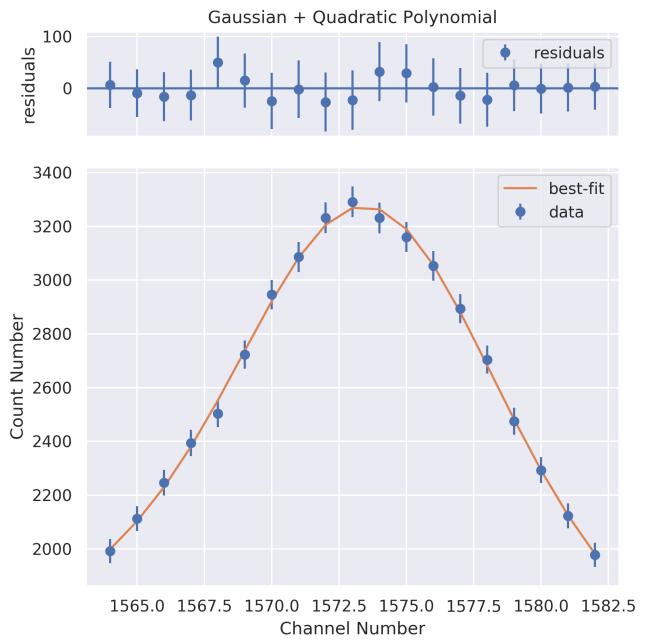


Figure 16: Fit of full & zoomed in peak of ^{133}Ba 161 keV peak

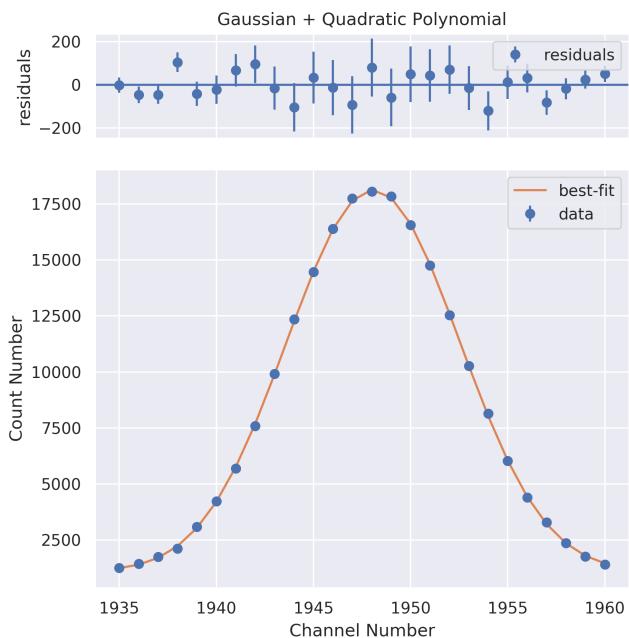


(a) Full peak with fit

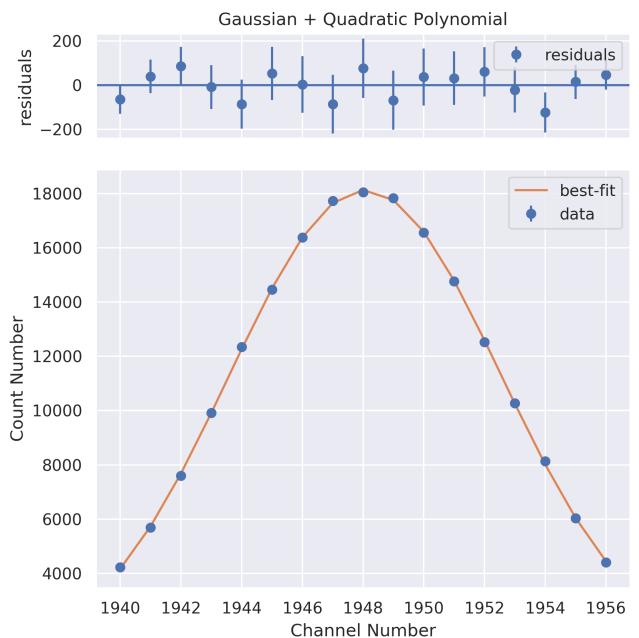


(b) Zoomed in peak with fit

Figure 17: Fit of full & zoomed in peak of ^{133}Ba 223 keV peak

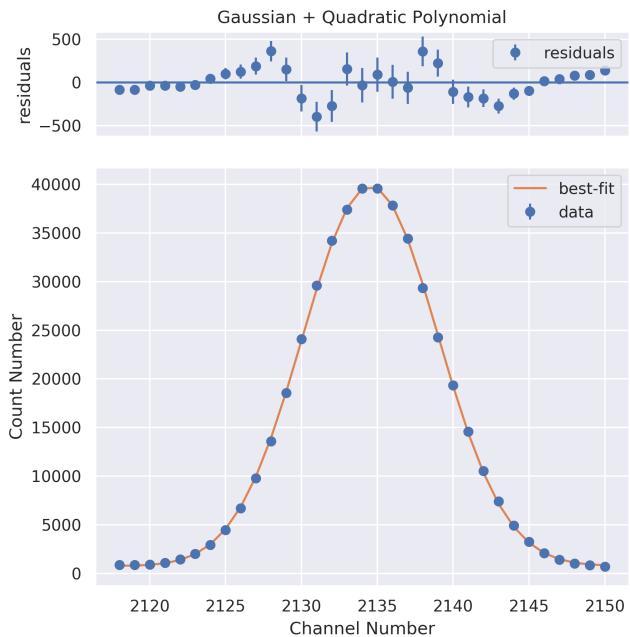


(a) Full peak with fit

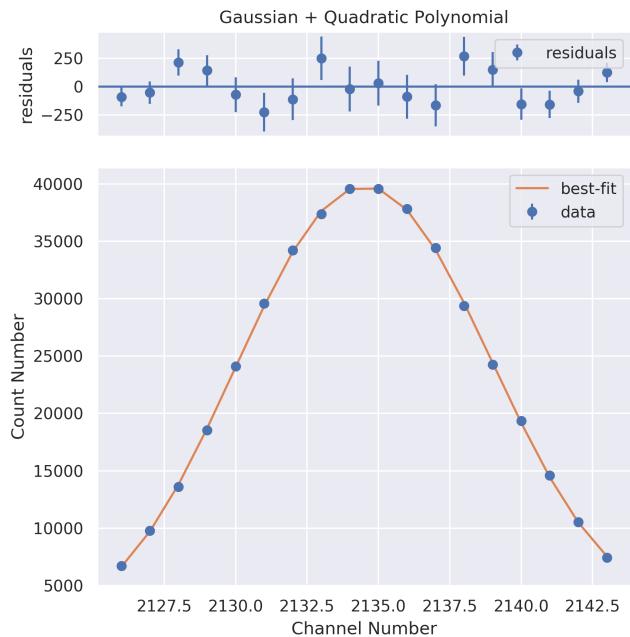


(b) Zoomed in peak with fit

Figure 18: Fit of full & zoomed in peak of ^{133}Ba 276 keV peak

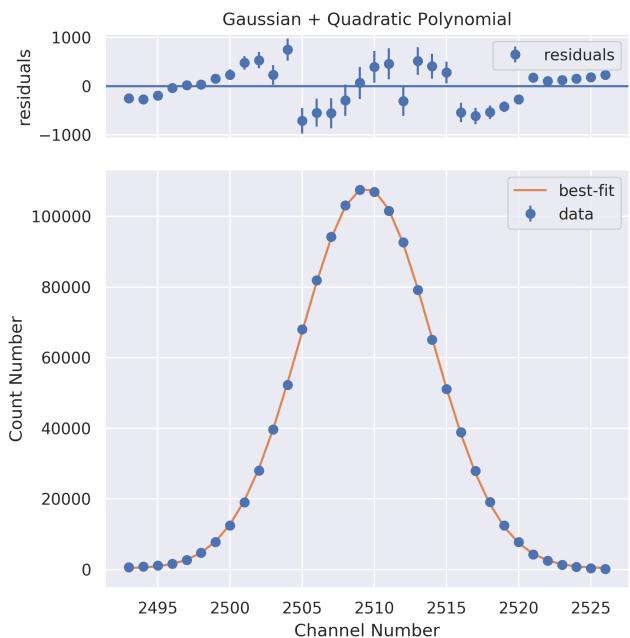


(a) Full peak with fit

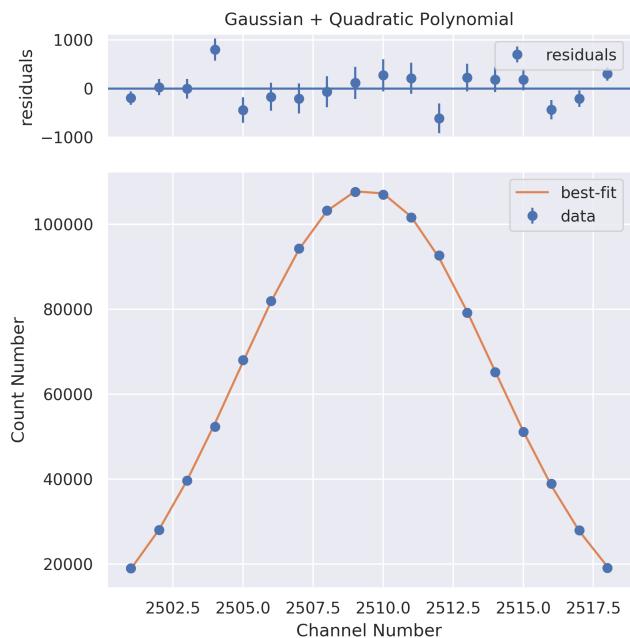


(b) Zoomed in peak with fit

Figure 19: Fit of full & zoomed in peak of ^{133}Ba 303 keV peak

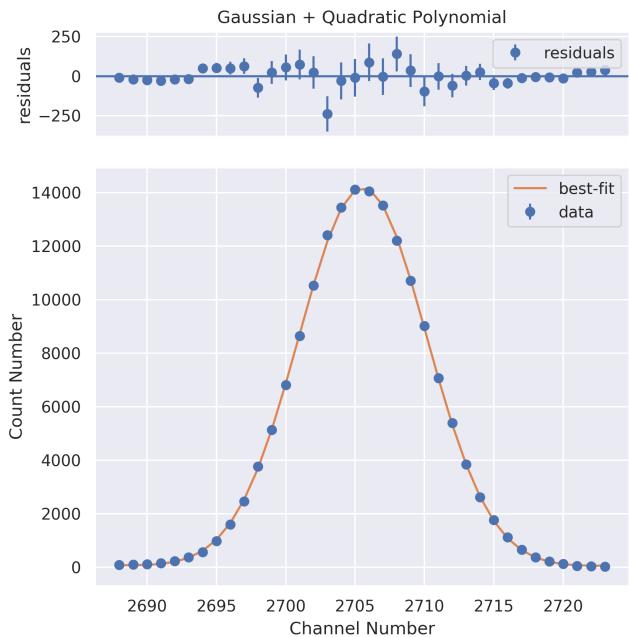


(a) Full peak with fit

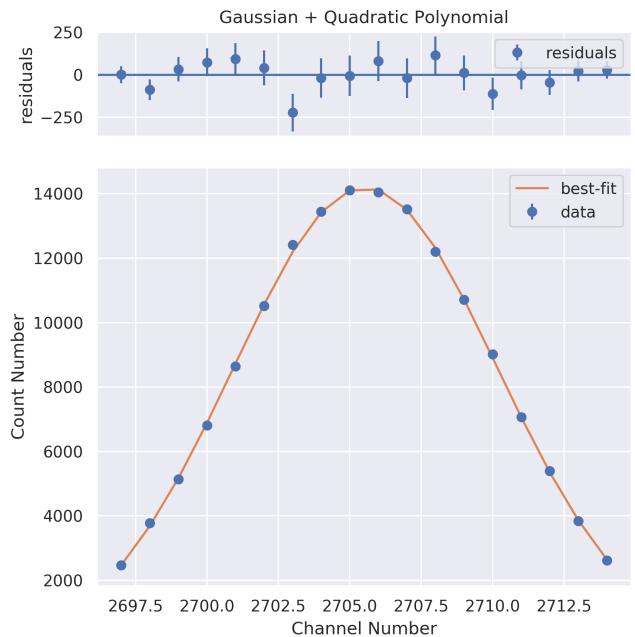


(b) Zoomed in peak with fit

Figure 20: Fit of full & zoomed in peak of ^{133}Ba 356 keV peak



(a) Full peak with fit

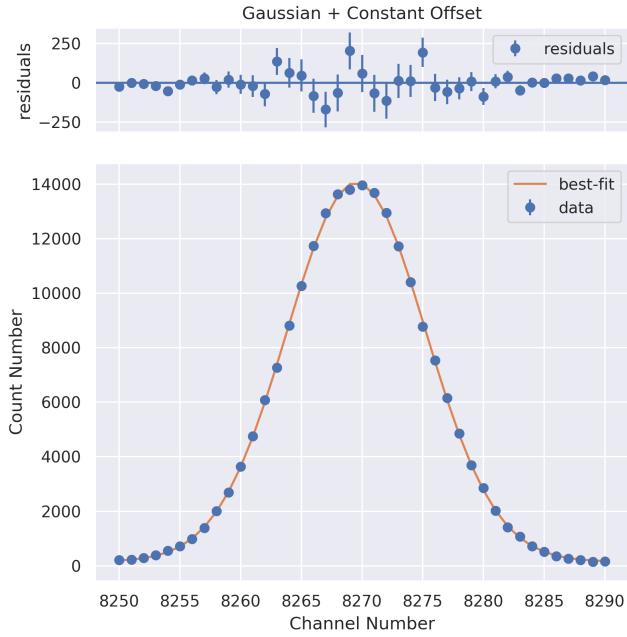


(b) Zoomed in peak with fit

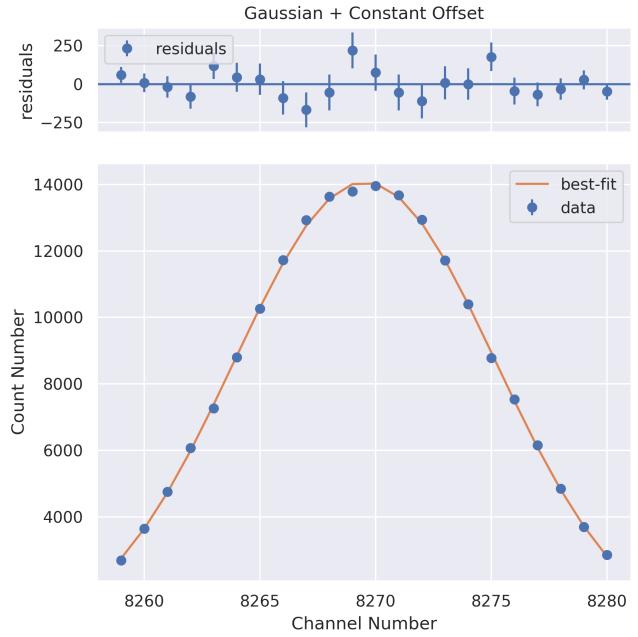
Figure 21: Fit of full & zoomed in peak of ^{133}Ba 384 keV peak

1.2 Cobalt-60

1.2.1 Gaussian Fit Only

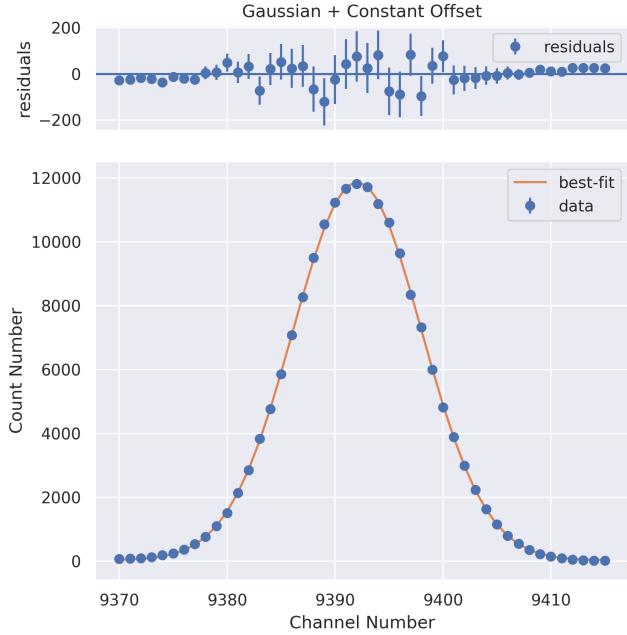


(a) Full peak with fit

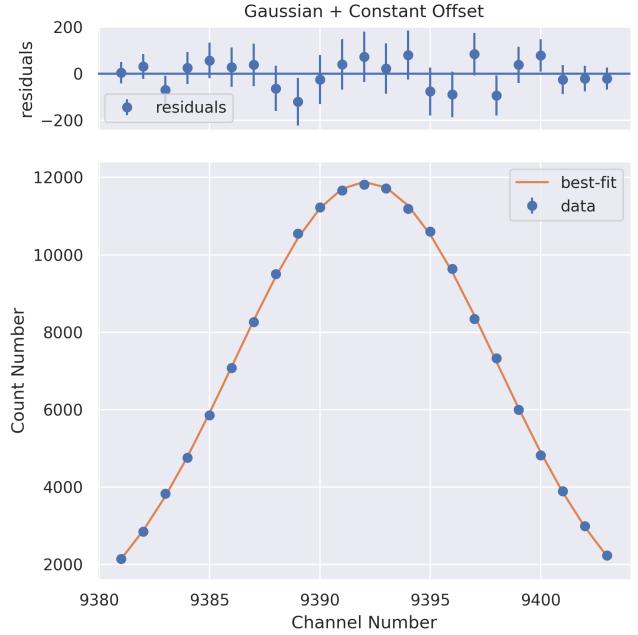


(b) Zoomed in peak with fit

Figure 22: Fit of full & zoomed in peak of ^{60}Co 1173 keV peak



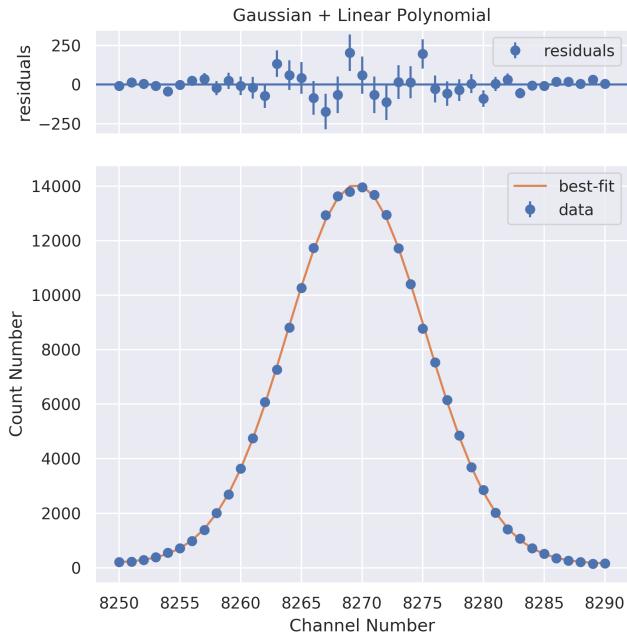
(a) Full peak with fit



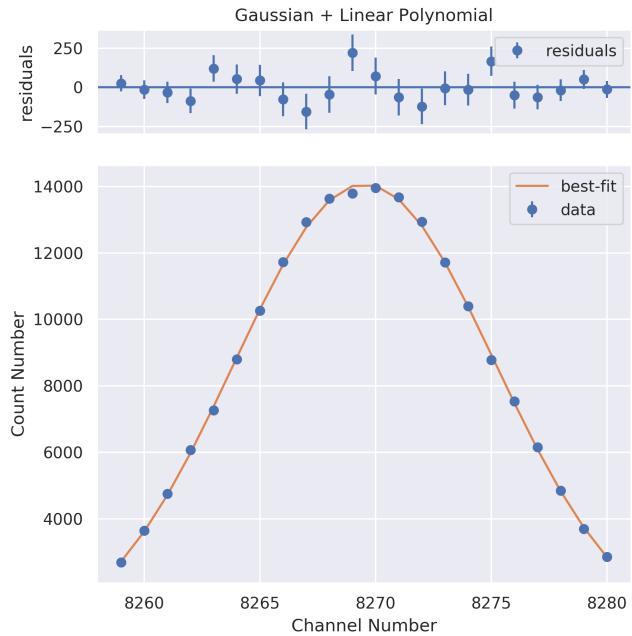
(b) Zoomed in peak with fit

Figure 23: Fit of full & zoomed in peak of ^{60}Co 1332 keV peak

1.2.2 Linear + Gaussian Fit

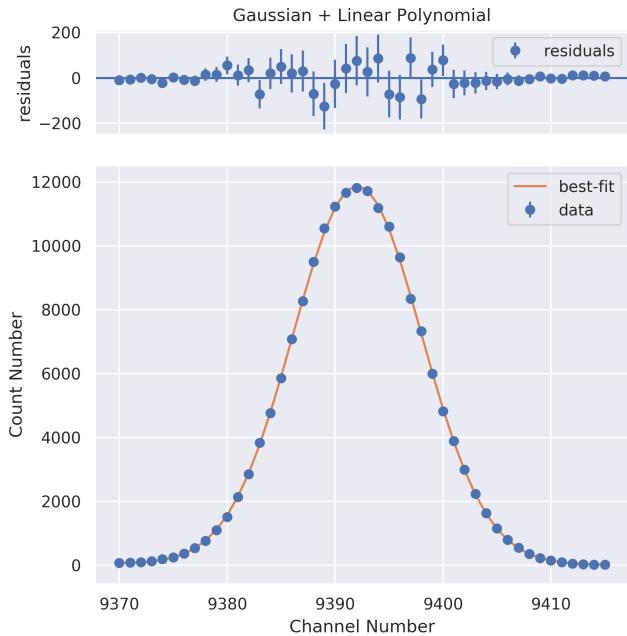


(a) Full peak with fit

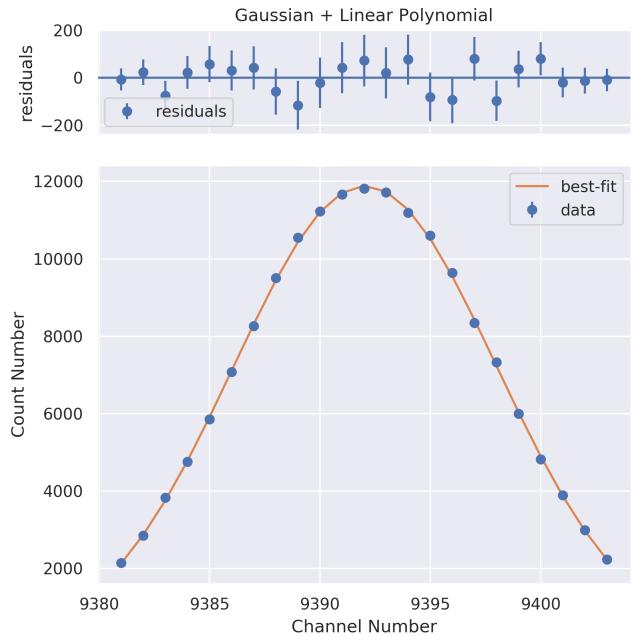


(b) Zoomed in peak with fit

Figure 24: Fit of full & zoomed in peak of ^{60}Co 1173 keV peak



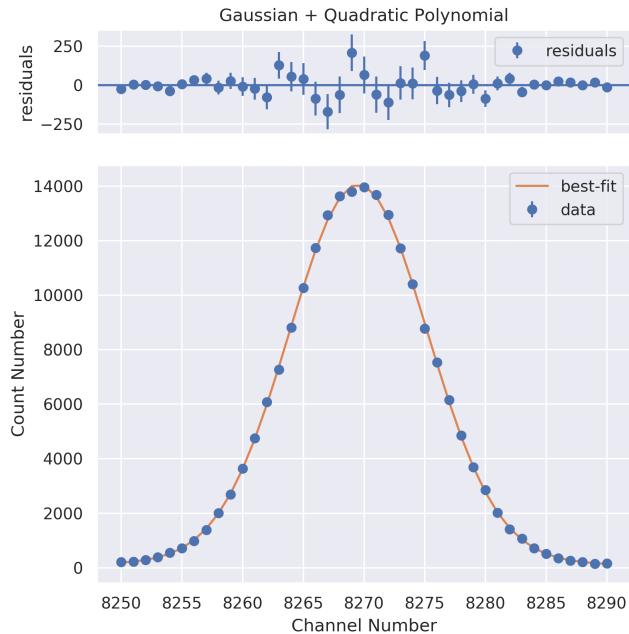
(a) Full peak with fit



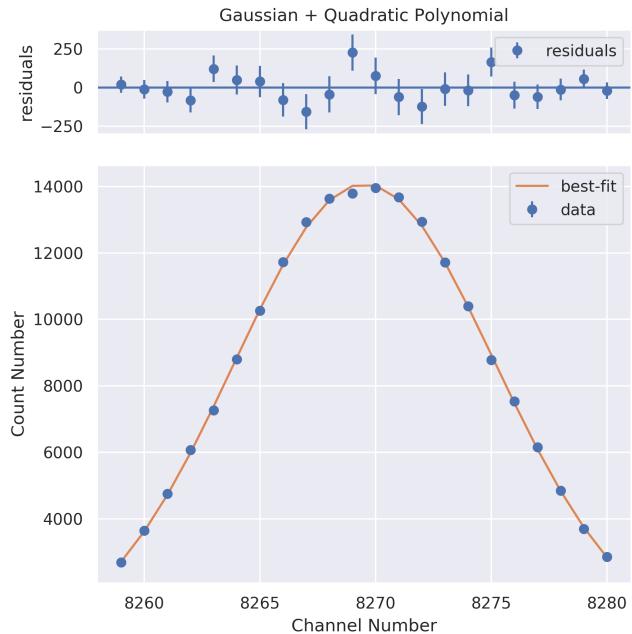
(b) Zoomed in peak with fit

Figure 25: Fit of full & zoomed in peak of ^{60}Co 1332 keV peak

1.2.3 Quadratic + Gaussian Fit

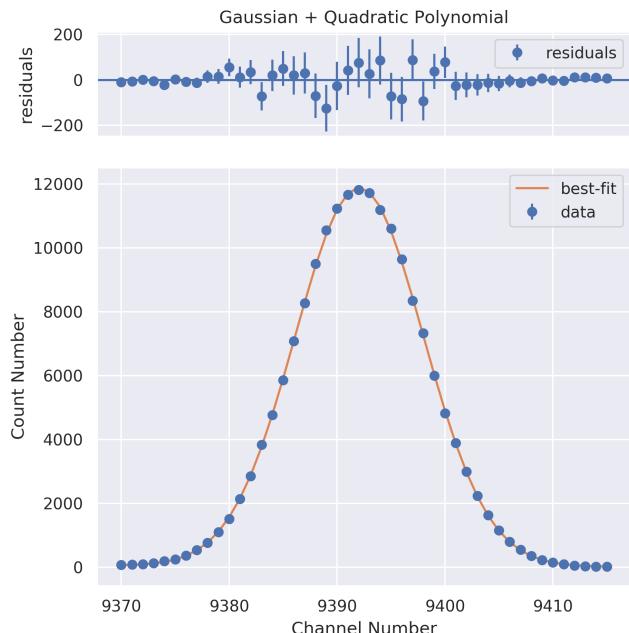


(a) Full peak with fit

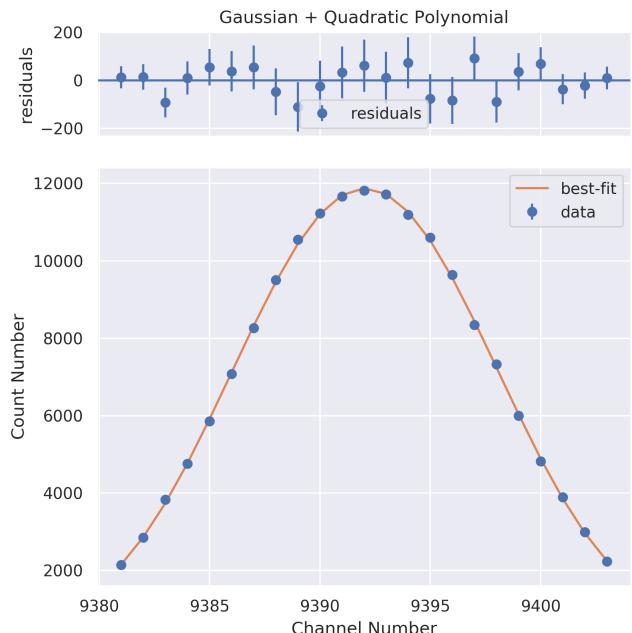


(b) Zoomed in peak with fit

Figure 26: Fit of full & zoomed in peak of ^{60}Co 1173 keV peak



(a) Full peak with fit

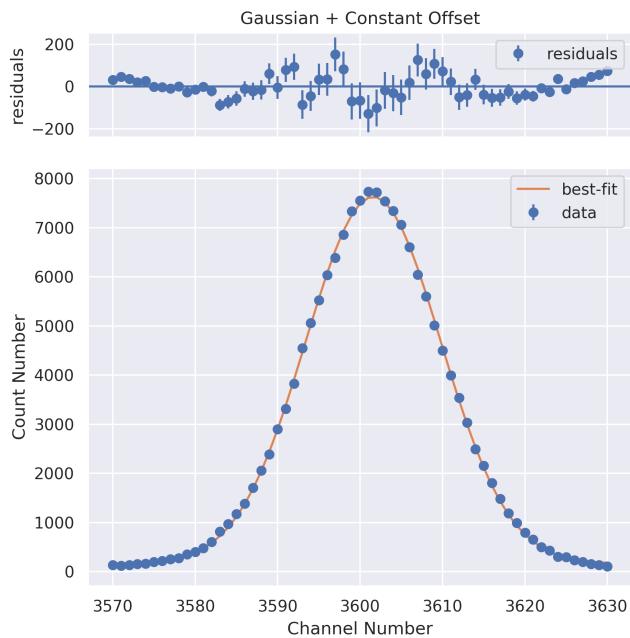


(b) Zoomed in peak with fit

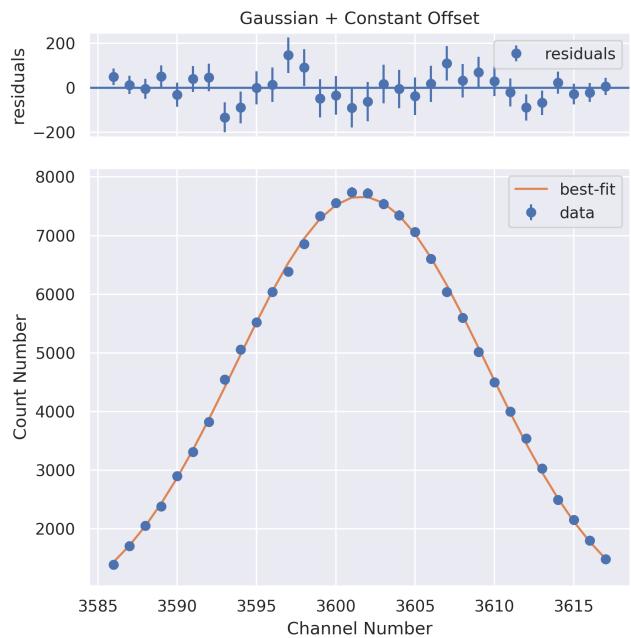
Figure 27: Fit of full & zoomed in peak of ^{60}Co 1332 keV peak

1.3 Sodium-22

1.3.1 Gaussian Fit Only

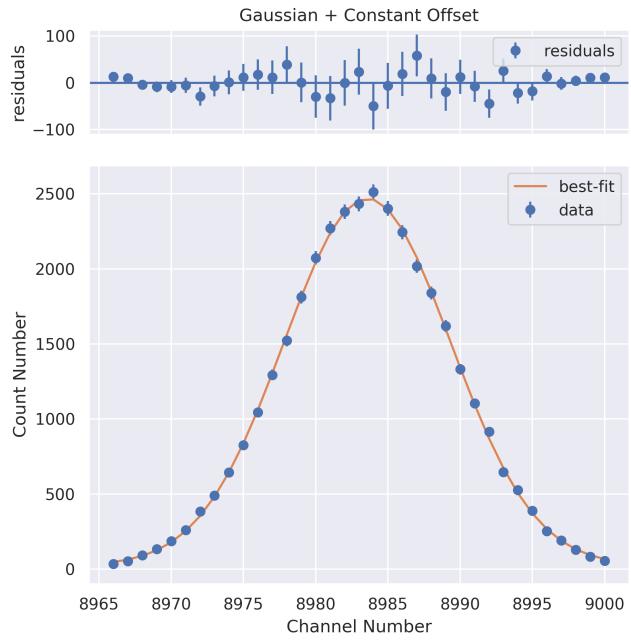


(a) Full peak with fit

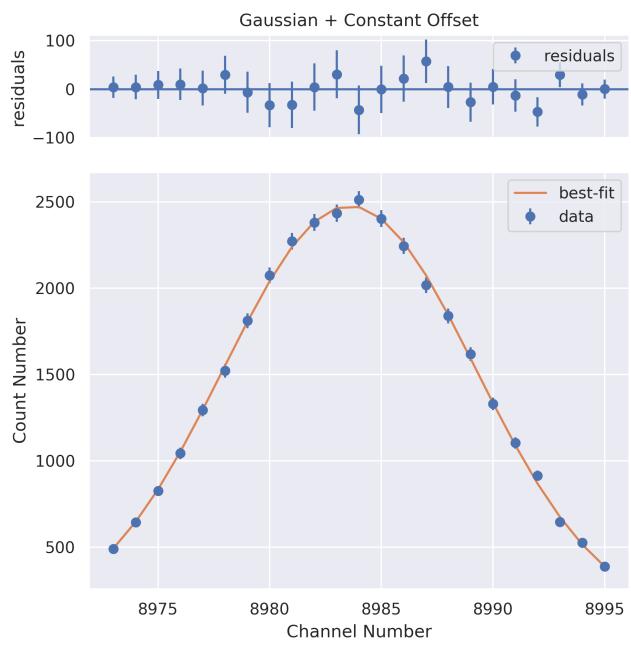


(b) Zoomed in peak with fit

Figure 28: Fit of full & zoomed in peak of ^{22}Na 511 keV peak



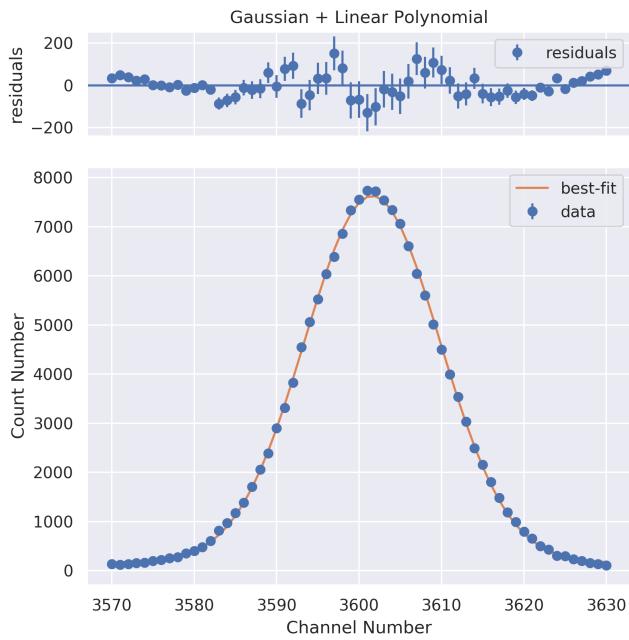
(a) Full peak with fit



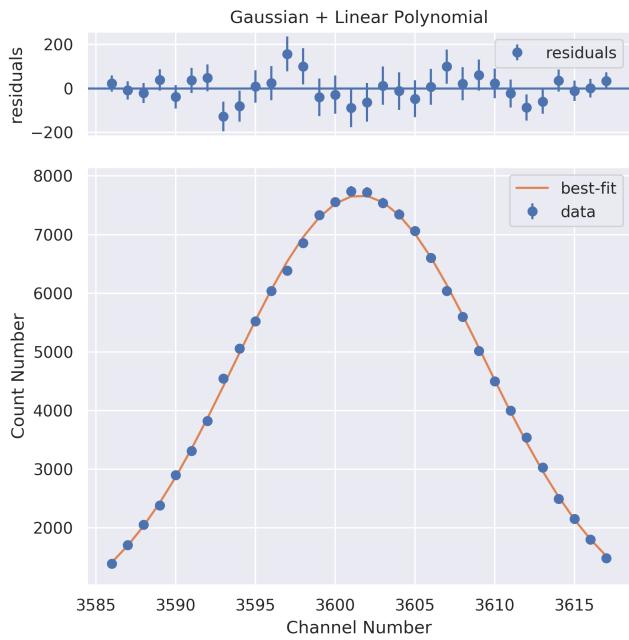
(b) Zoomed in peak with fit

Figure 29: Fit of full & zoomed in peak of ^{22}Na 1274 keV peak

1.3.2 Linear + Gaussian Fit

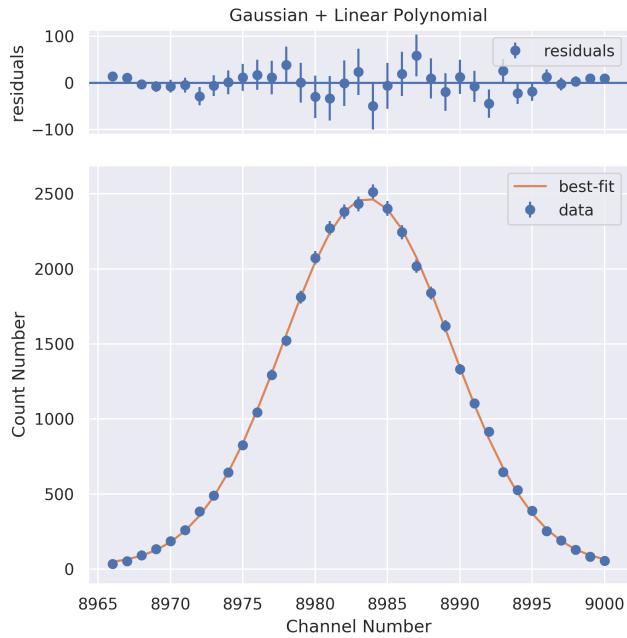


(a) Full peak with fit

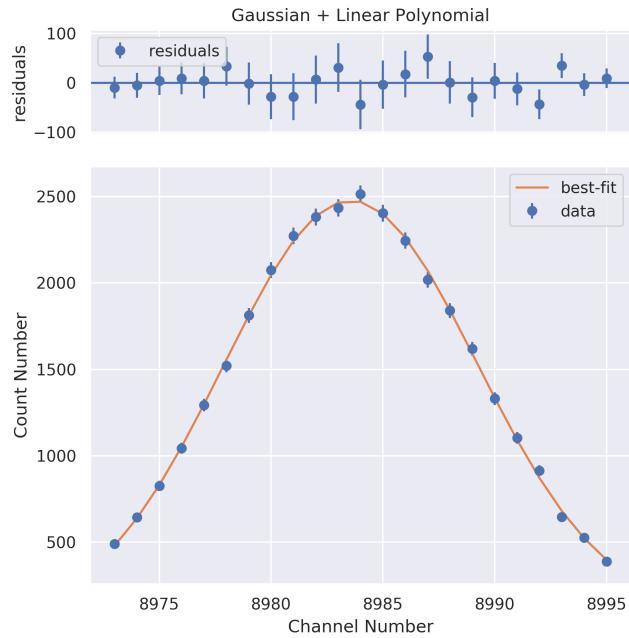


(b) Zoomed in peak with fit

Figure 30: Fit of full & zoomed in peak of ^{60}Na 511 keV peak



(a) Full peak with fit



(b) Zoomed in peak with fit

Figure 31: Fit of full & zoomed in peak of ^{22}Na 1274 keV peak

1.3.3 Quadratic + Gaussian Fit

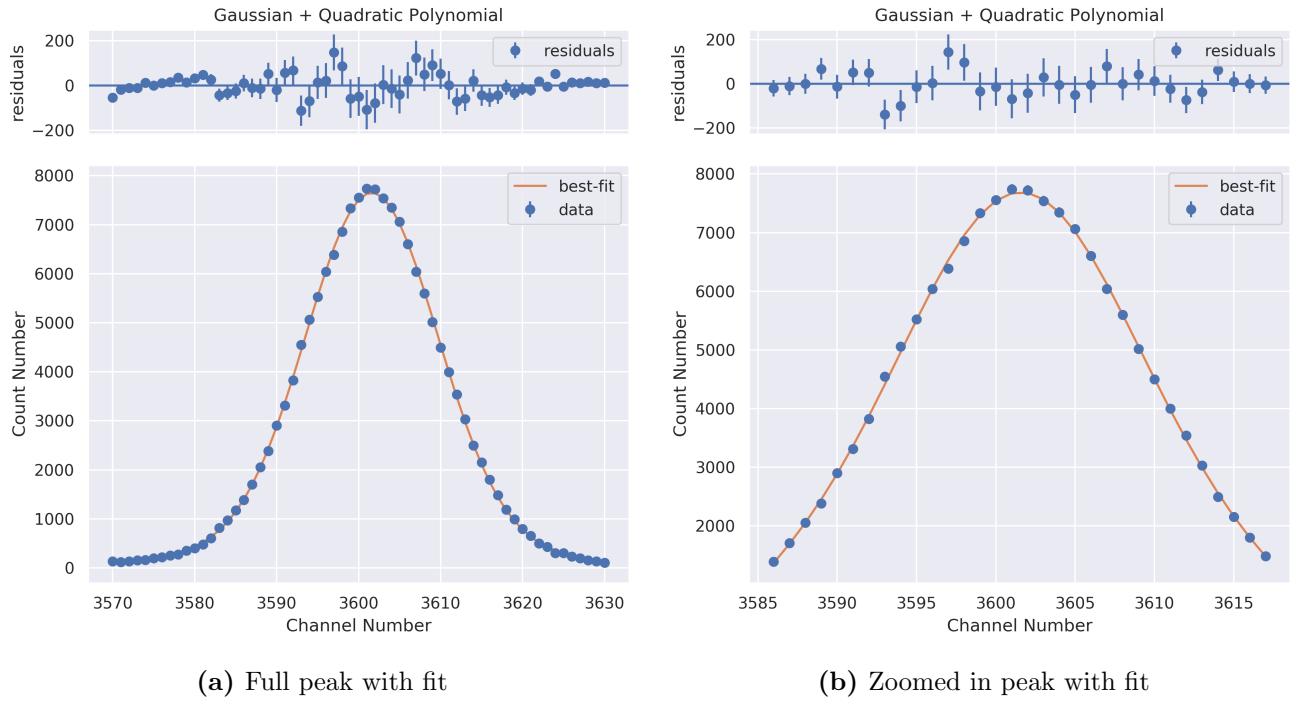


Figure 32: Fit of full & zoomed in peak of ^{60}Na 511 keV peak

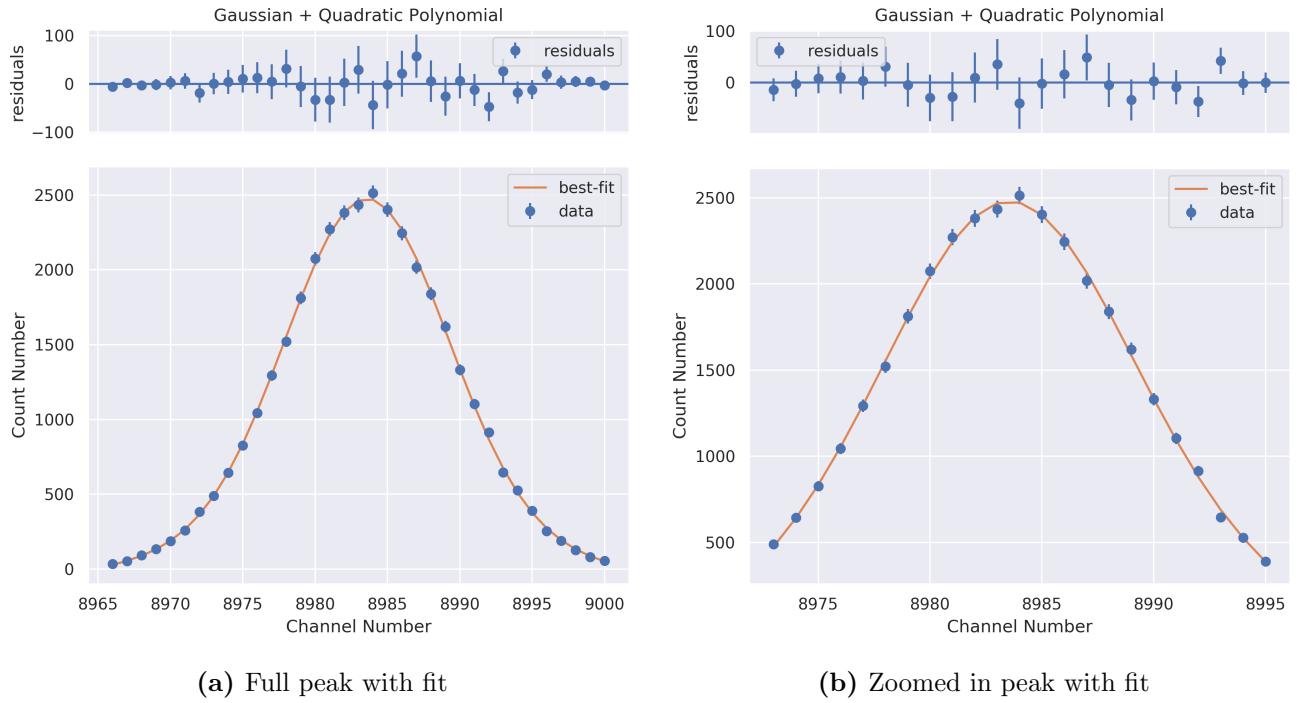


Figure 33: Fit of full & zoomed in peak of ^{22}Na 1274 keV peak

2 Fit Comparisons

2.1 Barium-133

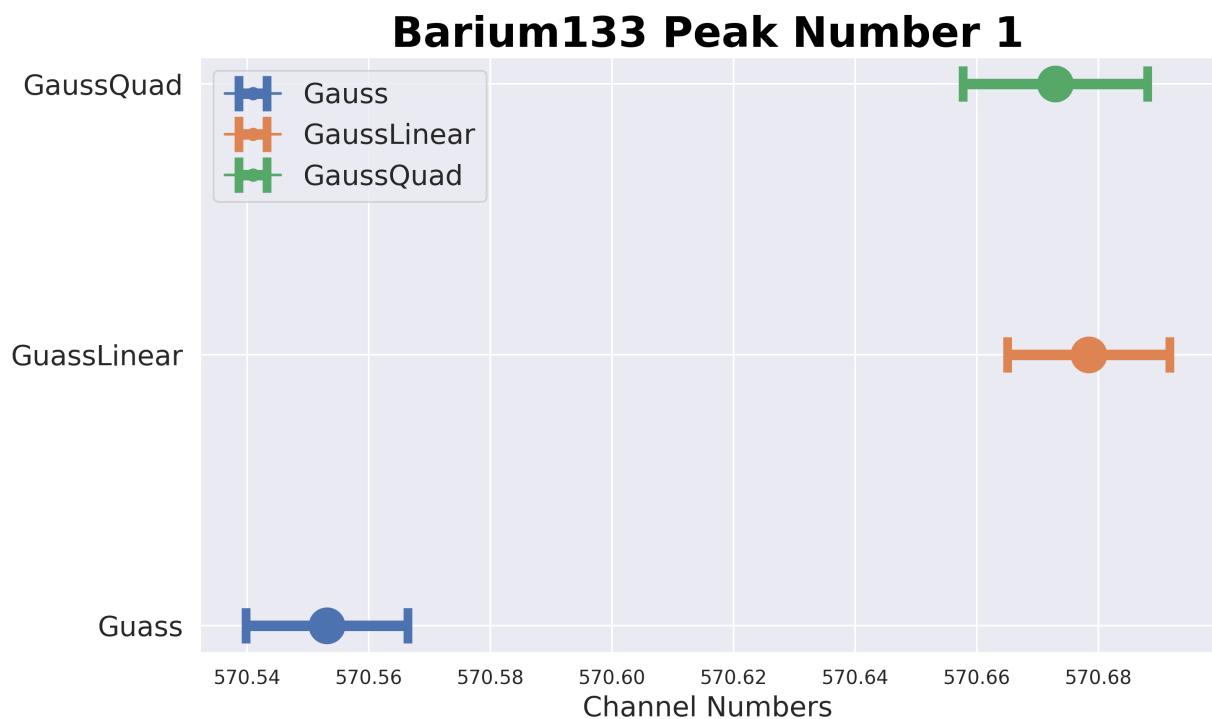


Figure 34: Fit comparisons for ^{133}Ba 81 keV peak

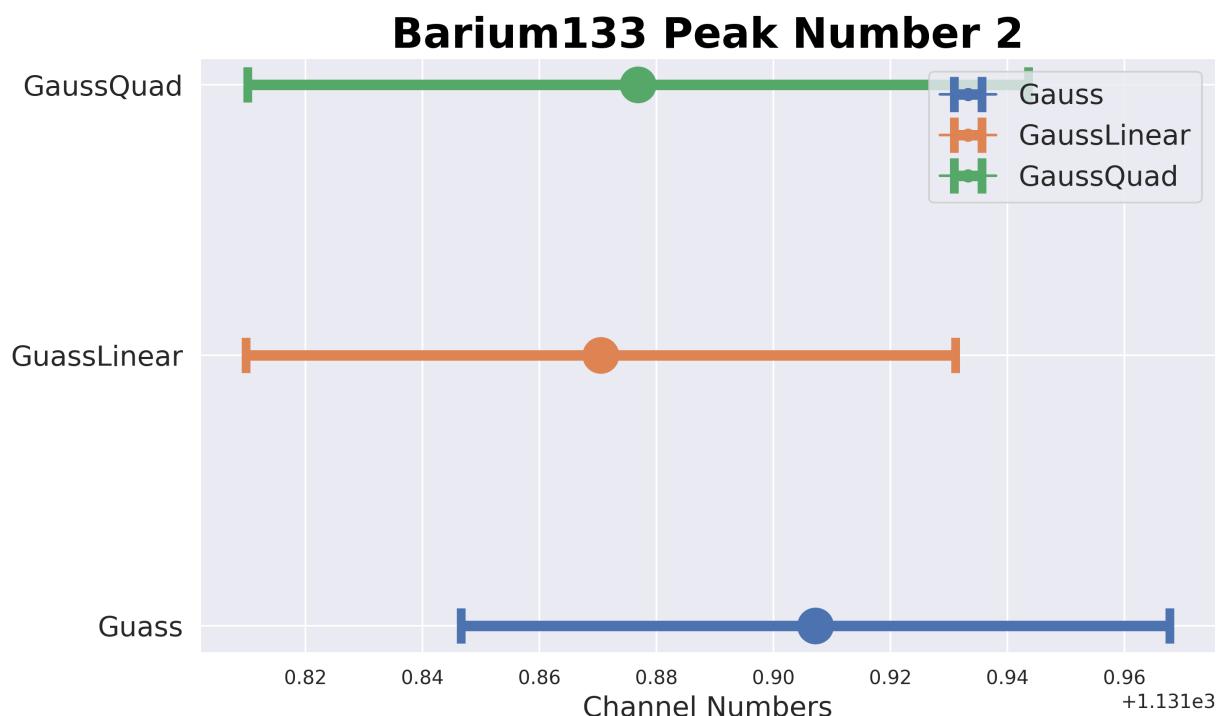


Figure 35: Fit comparisons for ^{133}Ba 161 keV peak

Barium133 Peak Number 3

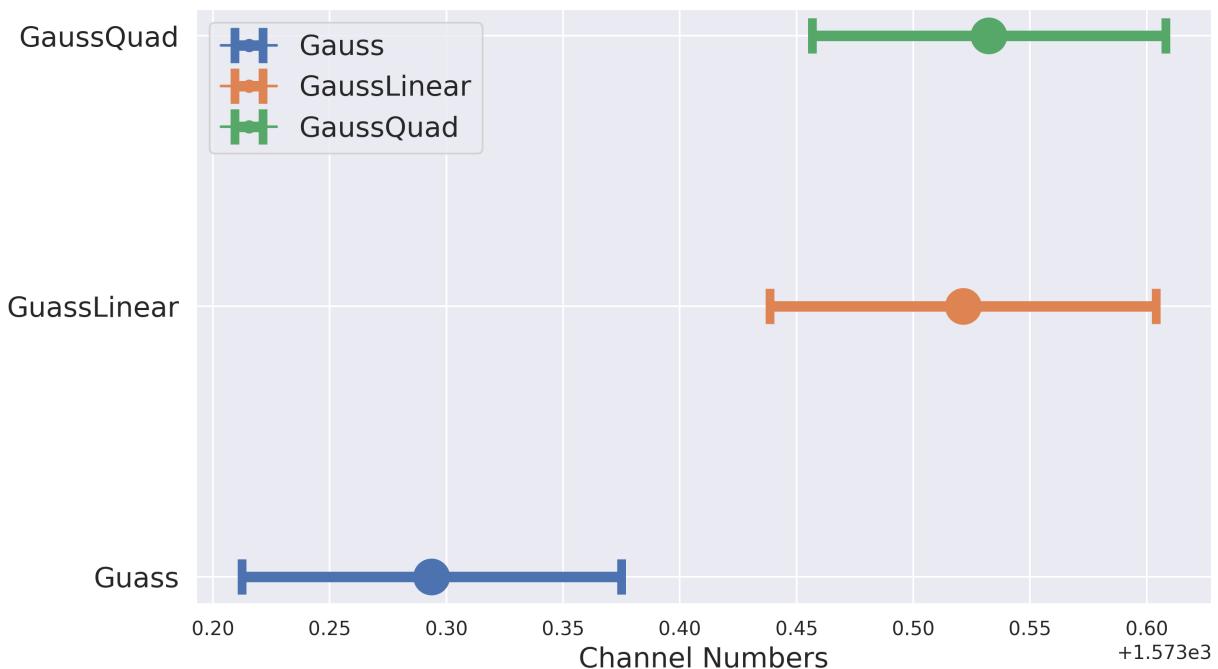


Figure 36: Fit comparisons for ^{133}Ba 223 keV peak

Barium133 Peak Number 4

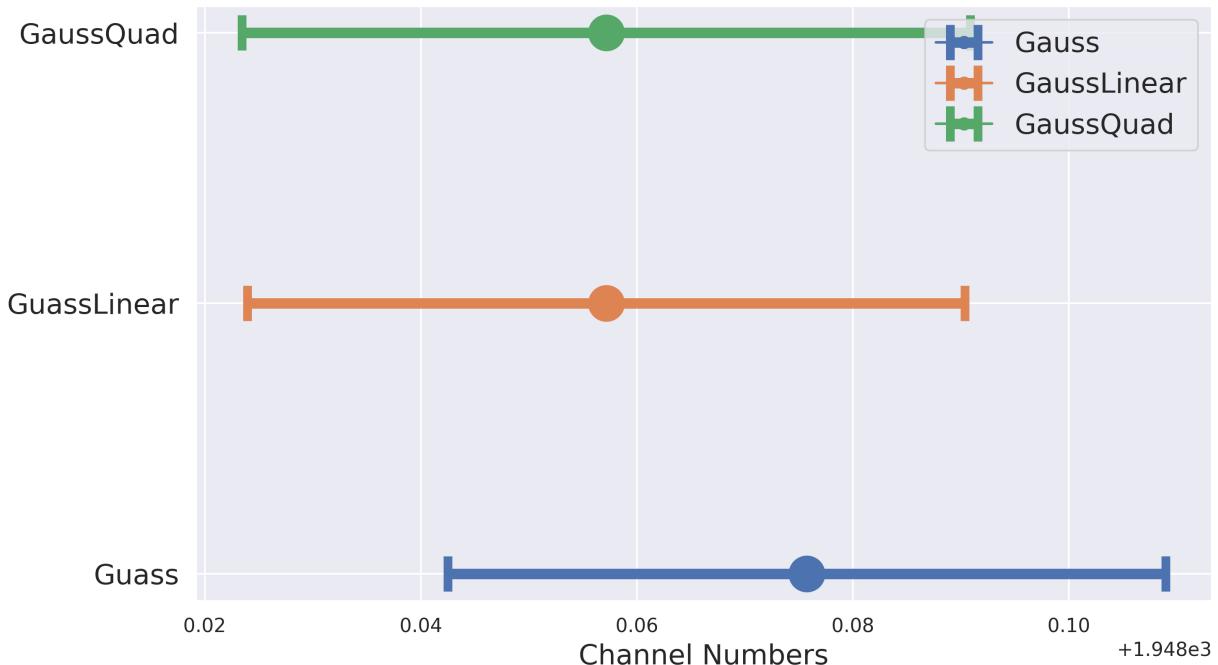


Figure 37: Fit comparisons for ^{133}Ba 276 keV peak

Barium133 Peak Number 5

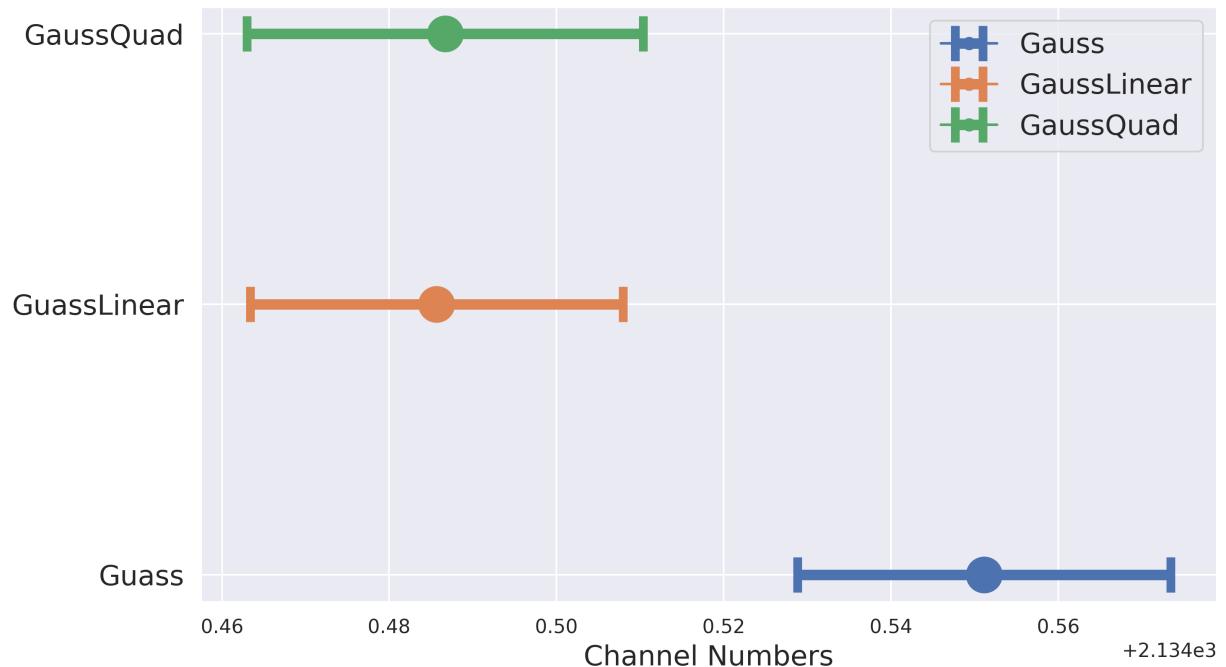


Figure 38: Fit comparisons for ^{133}Ba 303 keV peak

Barium133 Peak Number 6

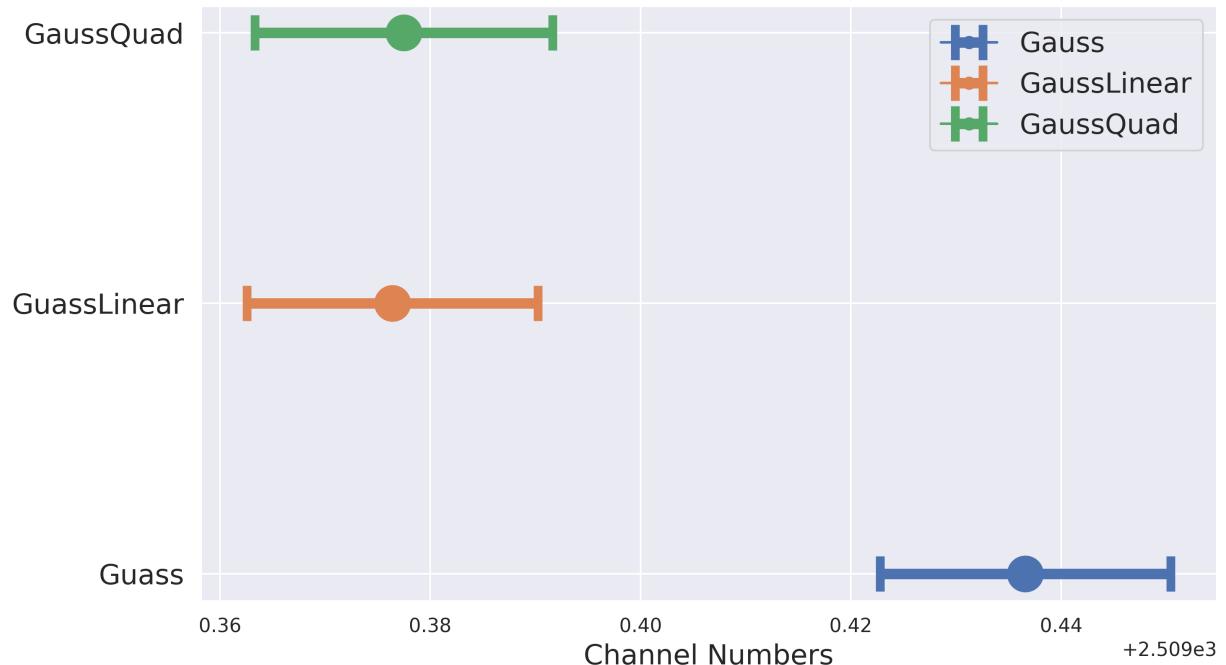


Figure 39: Fit comparisons for ^{133}Ba 356 keV peak

Barium133 Peak Number 7

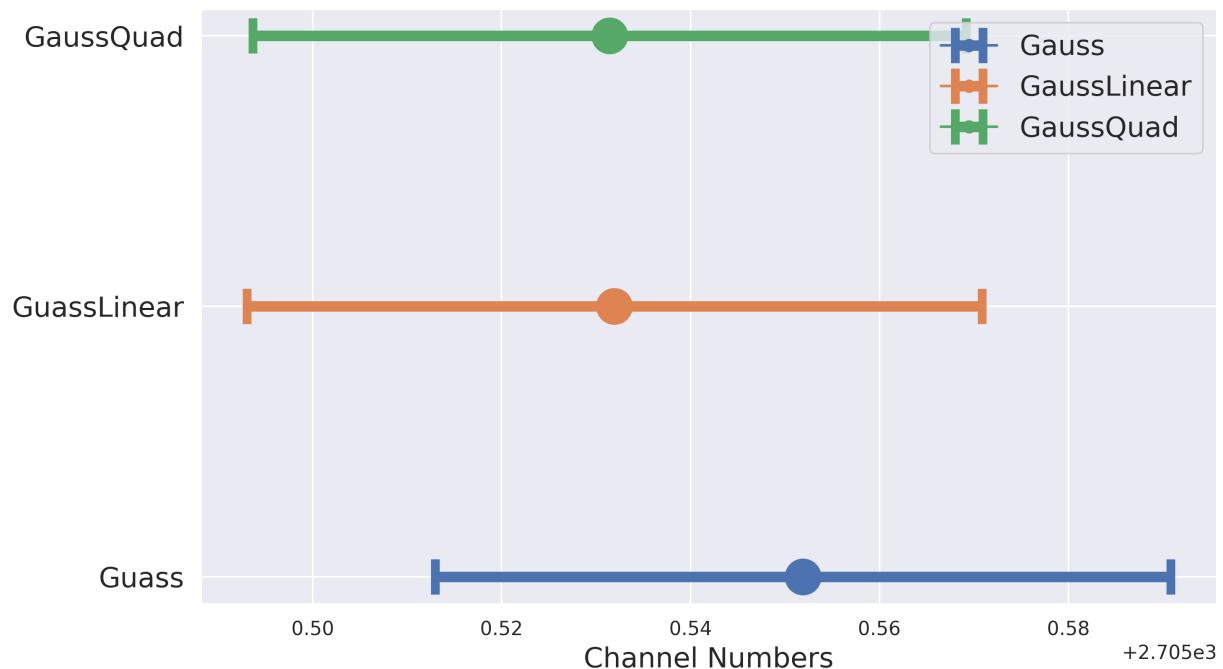


Figure 40: Fit comparisons for ^{133}Ba 384 keV peak

2.2 Cobalt-60

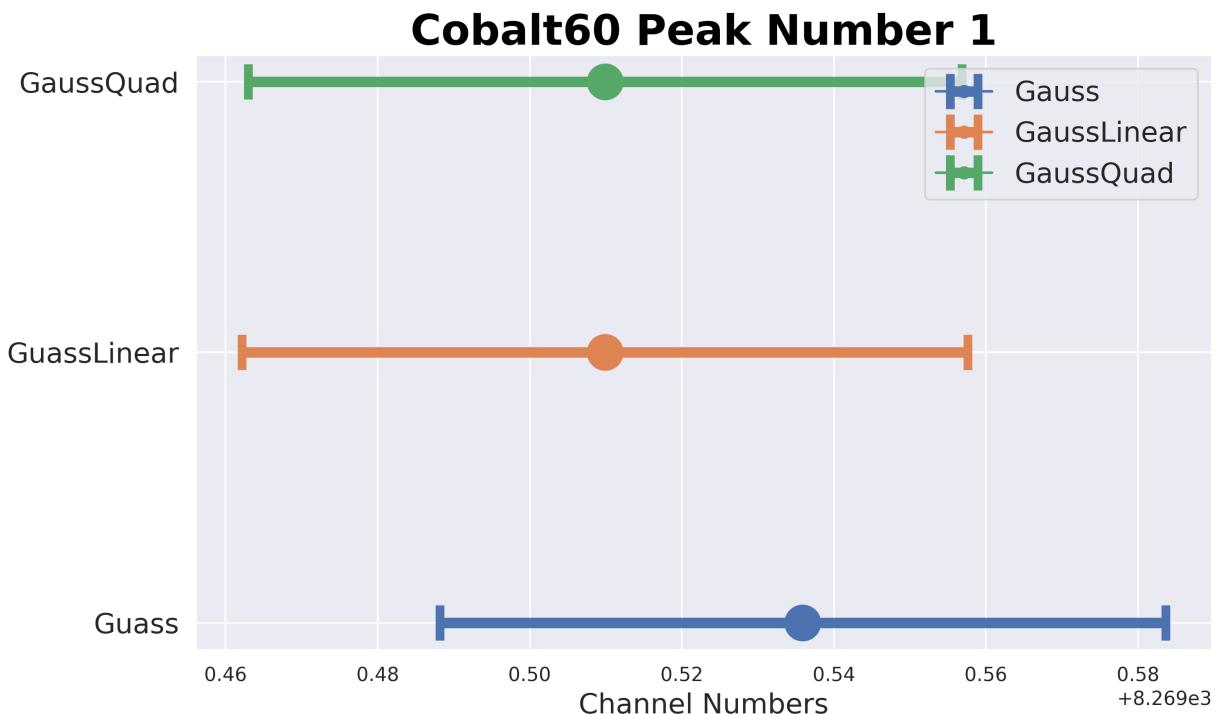


Figure 41: Fit comparisons for ${}^{60}\text{Co}$ 1173 keV peak

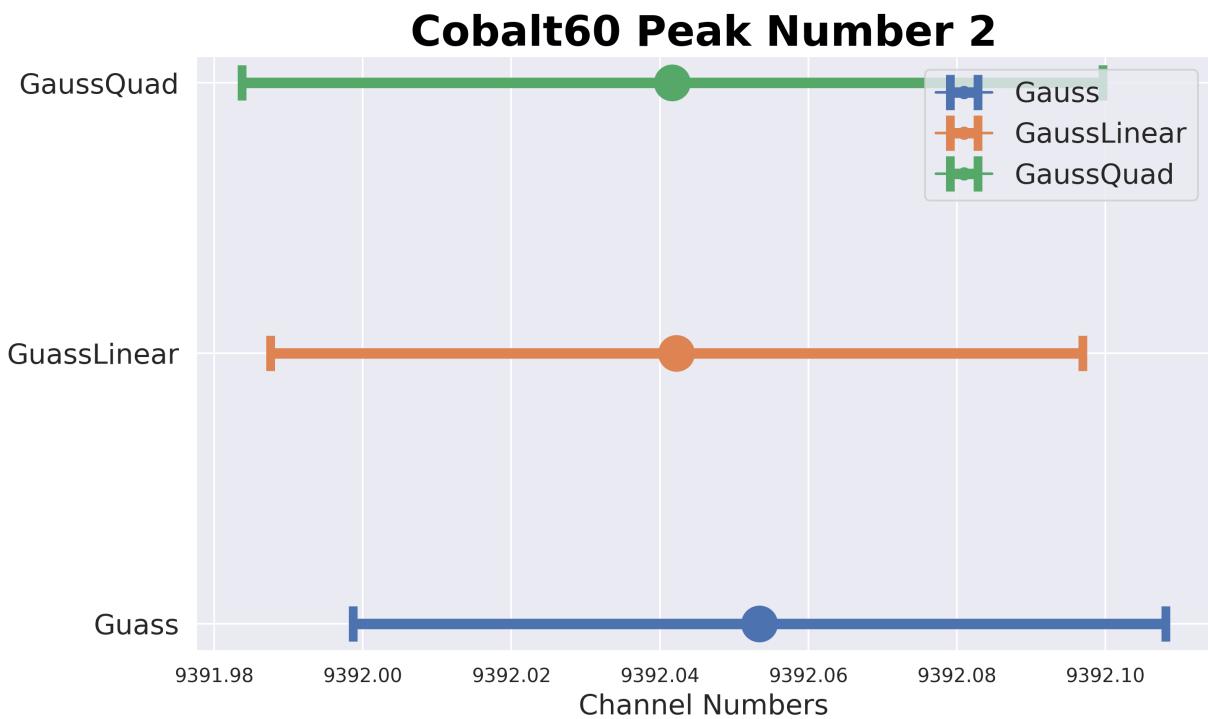


Figure 42: Fit comparisons for ${}^{60}\text{Co}$ 1332 keV peak

2.3 Sodium-22

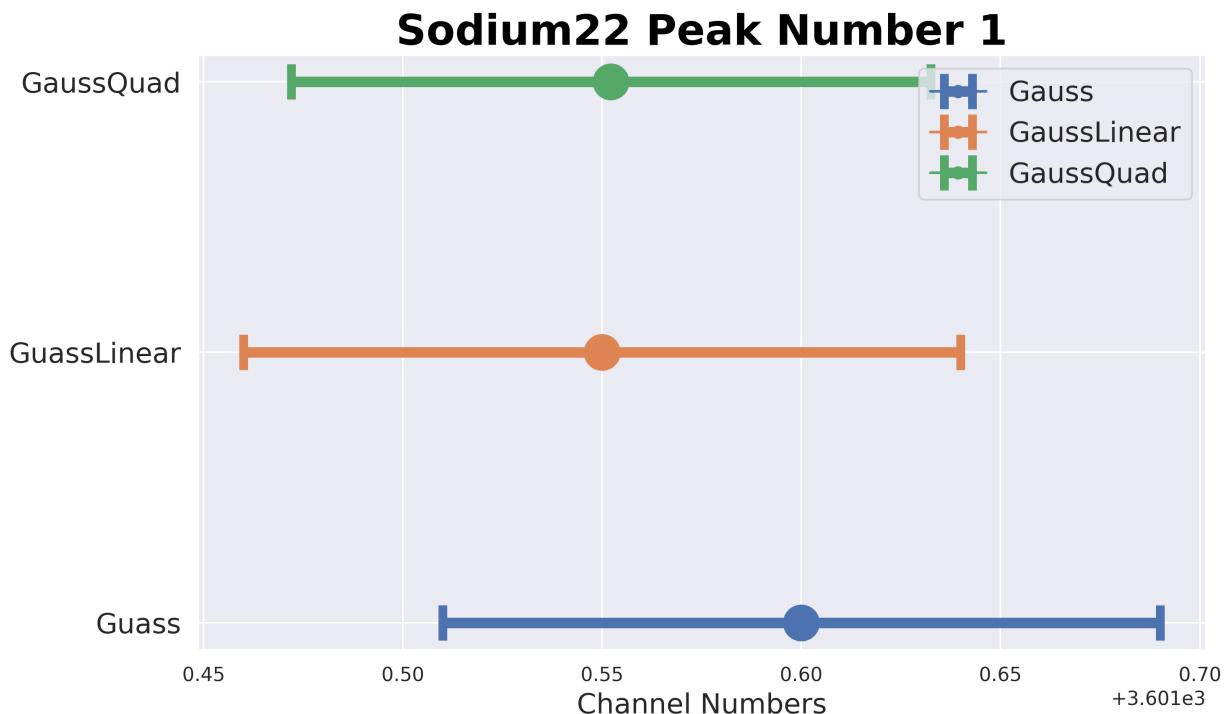


Figure 43: Fit comparisons for ^{22}Na 511 keV peak

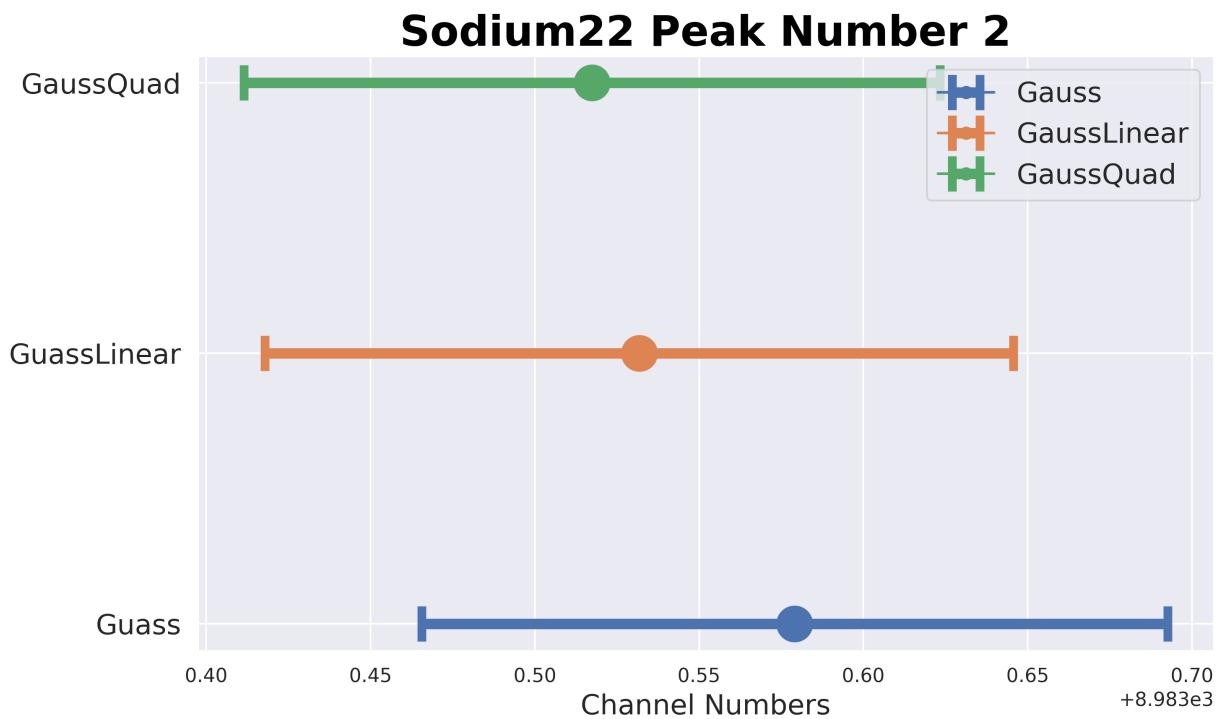


Figure 44: Fit comparisons for ^{22}Na 1274 keV peak

3 Python Code

3.1 GaussianFit.py

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 import seaborn as sns
4 sns.set()
5 import scipy.optimize as sciopt
6 import scipy.stats as scistats
7 from lmfit import Model, Parameters
8 import pandas as pd
9
10 def ChiSqFunc(Measured,Fitted,Errors):
11     ChiSquared = 0
12     for i in range(len(Measured)):
13         ChiSquared += ((Measured[i] - Fitted[i])**2.0) / ((Errors[i])**2.0)
14     ReducedChiSq = ChiSquared/(len(Measured)-2)
15     ProbChiSq = (1.0 - scistats.chi2.cdf(ChiSquared,len(Measured)-2) ) * 100.0
16     return ChiSquared, ReducedChiSq, ProbChiSq
17
18 def Gauss(x,A,mean,sigma,a):
19     return (A/(np.sqrt(2*np.pi) * sigma )) *np.exp(-((x-mean)**2.0)/(2.0*(sigma**2.0)))
20     ↵ + a
21
22 def GaussLinear(x,A,mean,sigma,a,b):
23     return (A/(np.sqrt(2*np.pi) * sigma ))*np.exp(-((x-mean)**2.0)/(2.0*(sigma**2.0)))
24     ↵ + a + b*x
25
26 def GaussQuad(x,A,mean,sigma,a,b,c):
27     return (A/(np.sqrt(2*np.pi) * sigma ))*np.exp(-((x-mean)**2.0)/(2.0*(sigma**2.0)))
28     ↵ + a + b*x + c*x**2.0
29
30 def ChToEnergy(Ch,a,b,c):
31     Energy = np.sqrt( ( (Ch - c + (b**2.0 / (4*a))) )/a ) - (b / (2*a))
32     return Energy
33
34 SetSigma = 2
35
36 BariumList = [ [[550,585,570,81],[1125,1140,1132,161],[1565,1582,1574,223],[1935,1960,
37     ↵ ,1948,276],[2118,2150,2135,303],[2493,2526,2509,356],[2688,2723,2705,384]] , []
38     ↵ ]
39 SodiumList = [ [ [3570,3630,3600,511] , [8966,9000,8984,1274] ] , [] ]
40 CobaltList = [ [ [8250,8290,8270,1173] , [9370,9415,9392,1332] ] , [] ]
41
42 SourceList = ["Barium133-24HrRun_006_eh_1","Sodium22-24HrData_002_eh_1","Cobalt60-24H
43     ↵ rData_004_eh_1"]
44
45 PlotResolution = 300
46
47 PeakNo = int(1)
48
49 datadict = {'Element':[],'Fit type':[], 'Peak number':[], 'Peak type':[], 'Energy
50     ↵ (keV)':[], 'Resolution':[], 'Min of range':[], 'Max of range':[], 'Mean':[],
51     ↵ 'A':[], 'Sigma':[], 'Error on mean':[], 'a':[], 'b':[], 'c':[], 'chisq':[],
52     ↵ 'Reduced chisq':[], 'Probchisq':[]}
53
54 # Fit parameters
```

```

46  a = 2.63977565e-06
47  b = 7.04767648
48  c = -1.91414134e-01
49
50 for source in SourceList:
51     if source == "Barium133-24HrRun_006_eh_1":
52         ElementList = BariumList
53         Element = "Barium133"
54     elif source == "Sodium22-24HrData_002_eh_1":
55         ElementList = SodiumList
56         Element = "Sodium22"
57     else:
58         ElementList = CobaltList
59         Element = "Cobalt60"
60
61 for item in ElementList:
62     for peak in item:
63         #! Initialises the source and ranges for run
64
65     if item == ElementList[0]:
66         PeakType = "Full"
67     else:
68         PeakType = "Zoom"
69
70     df = pd.read_csv(source + ".dat", sep = r"\s+", names = ['channel
    ↪   number', 'count number'])
71
72     df['count errors'] = np.sqrt(df['count number'])
73     df['count errors'] = df['count errors'].replace(0,1)
74
75     MinValue = peak[0]
76     MaxValue = peak[1]
77     MeanValue = peak[2]
78     PeakEnergy = peak[3]
79
80     data = df[(MinValue<=df['channel number']) & (df['channel number']<=MaxValue)]
81     #?plt.plot(data['channel number'],data['count number'])
82     #?plt.show()
83     #-----]
    ↪ -----
84     #! Gaussian + Offset model only
85
86     GaussModel = Model(Gauss)
87     Params = Parameters()
88
89     Params.add('A',value=max(data['count number']),vary=True,min=0)
90     Params.add('mean',value=MeanValue,vary=True)
91     Params.add('sigma',value=1,vary=True)
92     Params.add('a',value=1,vary=True)
93
94     FitResult = GaussModel.fit(data['count number'],params=Params,x=data['channel
    ↪   number'])
95     TempList = [ FitResult.best_values['mean'] - SetSigma
    ↪   *FitResult.best_values['sigma'] , FitResult.best_values['mean'] + SetSigma
    ↪   *FitResult.best_values['sigma'] , FitResult.best_values['mean'] ,
    ↪   PeakEnergy ]
96     if item == ElementList[0]:

```

```

97     ElementList[1].append(TempList)
98
99 #print(FitResult.best_values)
100 FitResult.plot(yerr=data['count errors'], xlabel='Channel Number', ylabel='Count
101   Number', title='Gaussian + Constant Offset')
102
103
104 #?plt.plot(data['channel number'],data['count number'])
105 plt.tight_layout()
106 plt.savefig(f'Plots/{Element}/Gauss/Gauss_{PeakNo}_{PeakType}.png',
107   format='png', dpi=PlotResolution)
108 plt.close('all')
109 #plt.show()
110
111 CountMax1 = FitResult.best_values['A'] / ( FitResult.best_values['sigma'] *
112   np.sqrt(2 * np.pi) ) + FitResult.best_values['a']
113 ErrorOnMean1 = FitResult.best_values['sigma'] / np.sqrt(CountMax1)
114
115 datadict['Element'].append(Element)
116 datadict['Fit type'].append('Gauss')
117 datadict['Energy (keV)'].append(PeakEnergy)
118 FWHM_Energy = 2 * np.sqrt(2*np.log(2)) *
119   ChToEnergy(FitResult.best_values['sigma'],a,b,c)
120 datadict['Resolution'].append( FWHM_Energy / PeakEnergy )
121 #datadict['Resolution'].append( ( 2 *
122   np.sqrt(2*np.log(2))*FitResult.best_values['sigma'] - b ) / a ) /
123   PeakEnergy )
124 datadict['Peak number'].append(PeakNo)
125 datadict['Peak type'].append(PeakType)
126 datadict['Min of range'].append(MinValue)
127 datadict['Max of range'].append(MaxValue)
128 datadict['Mean'].append(FitResult.best_values['mean'])
129 datadict['A'].append(FitResult.best_values['A'])
130 datadict['Sigma'].append(FitResult.best_values['sigma'])
131 datadict['Error on mean'].append(1)
132 datadict['a'].append(FitResult.best_values['a'])
133 datadict['b'].append(0)
134 datadict['c'].append(0)
135 datadict['chisq'].append(thingy[0])
136 datadict['Reduced chisq'].append(thingy[1])
137 datadict['Probchisq'].append(thingy[2])
138
139 #-----]
140
141 GaussModel2 = Model(GaussLinear)
142 Params2 = Parameters()
143
144 Params2.add('A', value=max(data['count number']), vary=True, min=0)
145 Params2.add('mean', value=MeanValue, vary=True)
146 Params2.add('sigma', value=1, vary=True)
147 Params2.add('a', value=1, vary=True)
148 Params2.add('b', value=1, vary=True)

```

```

146
147 FitResult2 = GaussModel2.fit(data['count
148   ↪  number'],params=Params2,x=data['channel number'])
149 #TempList2 = [ FitResult2.best_values['mean'] - SetSigma
150   ↪  *FitResult2.best_values['sigma'] , FitResult2.best_values['mean'] +
151   ↪  SetSigma *FitResult2.best_values['sigma'] , FitResult2.best_values['mean']
152   ↪  ]
153 #print(FitResult2.best_values)
154 FitResult2.plot(yerr=data['count errors'],xlabel='Channel Number',ylabel='Count
155   ↪  Number',title='Gaussian + Linear Polynomial')
156
157 thingy2 = ChiSqFunc(list(data['count
158   ↪  number']),list(FitResult2.best_fit),list(data['count errors']))
159
160 #?plt.plot(data['channel number'],data['count number'])
161 plt.tight_layout()
162 plt.savefig(f'Plots/{Element}/Linear/Linear_{PeakNo}_{PeakType}.png',
163   ↪  format='png', dpi=PlotResolution)
164 plt.close('all')
165
166 CountMax2 = FitResult2.best_values['A'] / ( FitResult2.best_values['sigma'] *
167   ↪  np.sqrt(2 * np.pi) ) + FitResult2.best_values['a'] +
168   ↪  FitResult2.best_values['b'] * FitResult2.best_values['mean']
169 ErrorOnMean2 = FitResult2.best_values['sigma'] / np.sqrt(CountMax2)
170
171 datadict['Element'].append(Element)
172 datadict['Fit type'].append('Linear')
173 datadict['Energy (keV)'].append(PeakEnergy)
174 FWHM_Energy = 2 * np.sqrt(2*np.log(2)) *
175   ↪  ChToEnergy(FitResult2.best_values['sigma'],a,b,c)
176 datadict['Resolution'].append( FWHM_Energy / PeakEnergy)
177 datadict['Peak number'].append(PeakNo)
178 datadict['Peak type'].append(PeakType)
179 datadict['Min of range'].append(MinValue)
180 datadict['Max of range'].append(MaxValue)
181 datadict['Mean'].append(FitResult2.best_values['mean'])
182 datadict['A'].append(FitResult2.best_values['A'])
183 datadict['Sigma'].append(FitResult2.best_values['sigma'])
184 datadict['Error on mean'].append(1)
185 datadict['a'].append(FitResult2.best_values['a'])
186 datadict['b'].append(FitResult2.best_values['b'])
187 datadict['c'].append(0)
188 datadict['chisq'].append(thingy2[0])
189 datadict['Reduced chisq'].append(thingy2[1])
190 datadict['Probchisq'].append(thingy2[2])
191
192 #-----
193   ↪  -----
194 #! Gaussian + Quadratic model
195
196 GaussModel3 = Model(GaussQuad)
197 Params3 = Parameters()
198
199 Params3.add('A',value=max(data['count number']),vary=True,min=0)
200 Params3.add('mean',value=MeanValue,vary=True)
201 Params3.add('sigma',value=1,vary=True)
202 Params3.add('a',value=1,vary=True)

```

```

192 Params3.add('b',value=1,vary=True)
193 Params3.add('c',value=1,vary=True)
194
195 FitResult3 = GaussModel3.fit(data['count
196     ↵ number'],params=Params3,x=data['channel number'])
#TempList3 = [ FitResult3.best_values['mean'] - SetSigma
197     ↵ *FitResult3.best_values['sigma'] , FitResult3.best_values['mean'] +
198     ↵ SetSigma *FitResult3.best_values['sigma'] , FitResult3.best_values['mean']
199     ↵ ]
200 #print(FitResult3.best_values)
201 FitResult3.plot(yerr=data['count errors'],xlabel='Channel Number',ylabel='Count
202     ↵ Number',title='Gaussian + Quadratic Polynomial')
203
204 thingy3 = ChiSqFunc(list(data['count
205     ↵ number']),list(FitResult3.best_fit),list(data['count errors']))
#print(thingy3)
206
207 #?plt.plot(data['channel number'],data['count number'])
208 plt.tight_layout()
209 plt.savefig(f'Plots/{Element}/Quad/Quad_{PeakNo}_{PeakType}.png', format='png',
210     ↵ dpi=PlotResolution)
211 plt.close('all')
212
213 CountMax3 = FitResult3.best_values['A'] / ( FitResult3.best_values['sigma'] *
214     ↵ np.sqrt(2 * np.pi) ) + FitResult3.best_values['a'] +
215     ↵ FitResult3.best_values['b'] * FitResult3.best_values['mean'] +
216     ↵ FitResult3.best_values['c'] * (FitResult3.best_values['mean'])** 2.0
217 ErrorOnMean3 = FitResult3.best_values['sigma'] / np.sqrt(CountMax3)
218
219 datadict['Element'].append(Element)
220 datadict['Fit type'].append('Quad')
221 datadict['Energy (keV)'].append(PeakEnergy)
222 FWHM_Energy = 2 * np.sqrt(2*np.log(2)) *
223     ↵ ChToEnergy(FitResult3.best_values['sigma'],a,b,c)
224 datadict['Resolution'].append( FWHM_Energy / PeakEnergy)
225 datadict['Peak number'].append(PeakNo)
226 datadict['Peak type'].append(PeakType)
227 datadict['Min of range'].append(MinValue)
228 datadict['Max of range'].append(MaxValue)
229 datadict['Mean'].append(FitResult3.best_values['mean'])
230 datadict['A'].append(FitResult3.best_values['A'])
231 datadict['Sigma'].append(FitResult3.best_values['sigma'])
232 datadict['Error on mean'].append(1)
233 datadict['a'].append(FitResult3.best_values['a'])
234 datadict['b'].append(FitResult3.best_values['b'])
235 datadict['c'].append(FitResult3.best_values['c'])
236 datadict['chisq'].append(thingy3[0])
datadict['Reduced chisq'].append(thingy3[1])
datadict['Probchisq'].append(thingy3[2])
237
238 Delta12 = np.abs(FitResult3.best_values['mean'] - FitResult2.best_values['mean'])
239 ErrorDelta12 = np.sqrt( ErrorOnMean1**2.0 + ErrorOnMean2**2.0 )
240
241 Delta23 = np.abs(FitResult2.best_values['mean'] -
242     ↵ FitResult3.best_values['mean'])
243 ErrorDelta23 = np.sqrt( ErrorOnMean2**2.0 + ErrorOnMean3**2.0 )

```

```

237
238
239     if PeakType == "Zoom":
240         if abs(ErrorDelta23) > abs(Delta23):
241             print('best fit')
242         else:
243             print('not best fit')
244
245     TitleFont = {'size': '24', 'color': 'black', 'weight': 'bold'}
246     AxTitleFont = {'size': '16'}
247     plt.figure(figsize=(10,6))
248     plt.errorbar(FitResult.best_values['mean'], 1, xerr=ErrorOnMean1, elinewidth=6, c_]
249         ↳ apsize=10,capthick=5,marker='o',markersize=20,label="Gauss")
250     plt.errorbar(FitResult2.best_values['mean'], 1.25, xerr=ErrorOnMean2, elinewidth_]
251         ↳ =6,capsize=10,capthick=5,marker='o',markersize=20,label="GaussLinear")
252     plt.errorbar(FitResult3.best_values['mean'], 1.5, xerr=ErrorOnMean3, elinewidth=_]
253         ↳ 6,capsize=10,capthick=5,marker='o',markersize=20,label="GaussQuad")
254     plt.legend(fontsize=16,markerscale=0.33)
255     plt.title(str(Element) + ' Peak Number ' + str(PeakNo),**TitleFont)
256     plt.xlabel('Channel Numbers',**AxTitleFont)
257     plt.yticks([1,1.25,1.5],['Guass','GuassLinear','GaussQuad'],**AxTitleFont)
258     plt.tight_layout()
259     plt.savefig(f'Plots/{Element}/FitComparison_Peak{PeakNo}.png', format='png',
260         ↳ dpi=PlotResolution)
261     plt.close('all')
262
263     PeakNo +=1
264
265     PeakNo = 1
266
267     Fitdf = pd.DataFrame(datadict)
268     Fitdf.to_csv('Gamma_Peak_Stats_and_Params.csv')

```

3.2 Calibration.py

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 import scipy.optimize as sciopt
4 import seaborn as sns
5 import pandas as pd
6 sns.set()
7 import scipy.stats as scistats
8
9 source = "MysterySource-2HrRun_001_eh_1"
10 df = pd.read_csv(source+ ".dat", sep=r"\s+", names = ['channel number', 'count number'])
11
12 TitleFont = {'size': '25', 'color': 'black', 'weight': 'bold'}
13 AxTitleFont = {'size': '22'}
14
15 def Linear(E,a,b):
16     return E*a + b
17
18 def Quadratic(E,a,b,c):
19     return a*E**2.0 + E*b + c
20
21 def ChiSqFunc(Measured,Fitted,Errors,Params):
22     ChiSquared = 0
23     for i in range(len(Measured)):
24         ChiSquared += ((Measured[i] - Fitted[i])**2.0) / ((Errors[i])**2.0)
25     ReducedChiSq = ChiSquared/(len(Measured)-len(Params))
26     ProbChiSq = (1.0 - scistats.chi2.cdf(ChiSquared,len(Measured)-len(Params))) * *
27         100.0
28     return ChiSquared, ReducedChiSq, ProbChiSq
29
30 FitDF = pd.read_csv('Gamma_Peak_Stats_and_Params.csv', names=['Element', 'Fit type',
31                     'Peak number', 'Peak type', 'Energy (keV)', 'Resolution', 'Min', 'Max', 'Mean',
32                     'A', 'Sigma', 'Error', 'a', 'b', 'chisq', 'Reduced chisq',
33                     'Probchisq'],usecols=list(range(1,18)))
34
35 FitDF['Mean'] = FitDF['Mean'].astype(float)
36 FitDF['Error'] = FitDF['Error'].astype(float)
37
38 FitDF['Energy (keV)'] = FitDF['Energy (keV)'].astype(float)
39
40 plt.plot(FitDF['Energy (keV)'],FitDF['Mean'],'bo')
41
42 plt.show()
43
44 DataBa = FitDF[FitDF['Element'] == 'Barium133']
45 DataCo = FitDF[FitDF['Element'] == 'Cobalt60']
46 DataNa = FitDF[FitDF['Element'] == 'Sodium22']
47
48 ParamsLinear, ErrorsLinear = sciopt.curve_fit(Quadratic,FitDF['Energy
49             (keV)'],FitDF['Mean'])
50 print(ParamsLinear)
51
```

```

52 rough_EC_a = a = ParamsLinear[0]
53 rough_EC_b = b = ParamsLinear[1]
54 rough_EC_c = c = ParamsLinear[2]
55
56
57 Energies = np.sqrt( (FitDF['Mean'] - c + (b**2.0/ (4 * a))/a ) - (b/(2*a)))
58
59 plt.errorbar(DataBa['Energy (keV)'],DataBa['Mean'], fmt='ro',label="Barium-133",
   ↵ markersize=10.5,yerr=DataBa['Error'].values)
60 plt.errorbar(DataCo['Energy (keV)'],DataCo['Mean'],fmt='bo',label="Cobalt-60",
   ↵ markersize=10.5,yerr=DataCo['Error'].values)
61 plt.errorbar(DataNa['Energy (keV)'],DataNa['Mean'],fmt='yo',label="Sodium-22",
   ↵ markersize=10.5,yerr=DataNa['Error'].values)
62
63 plt.plot(Energies,Quadratic(Energies,*ParamsLinear),label='Fit')
64 plt.title('Energy calibration plot with fit',**TitleFont)
65 plt.xlabel('Gamma Energy [keV]',**AxTitleFont)
66 plt.ylabel('Channel Number',**AxTitleFont)
67 plt.legend()
68 plt.show()
69
70
71 plt.errorbar(DataBa['Energy (keV)'],[(DataBa['Mean'].iloc[i] -
   ↵ Quadratic(DataBa['Energy (keV)'].iloc[i],*ParamsLinear)) for i in
   ↵ range(len(DataBa['Energy (keV)']))],fmt='ro',label="Barium-133",
   ↵ markersize=7.5,yerr=DataBa['Error'].values)
72 plt.errorbar(DataCo['Energy (keV)'],[(DataCo['Mean'].iloc[i] -
   ↵ Quadratic(DataCo['Energy (keV)'].iloc[i],*ParamsLinear)) for i in
   ↵ range(len(DataCo['Energy (keV)']))],fmt='bo',label="Cobalt-60",
   ↵ markersize=7.5,yerr=DataCo['Error'].values)
73 plt.errorbar(DataNa['Energy (keV)'],[(DataNa['Mean'].iloc[i] -
   ↵ Quadratic(DataNa['Energy (keV)'].iloc[i],*ParamsLinear)) for i in
   ↵ range(len(DataNa['Energy (keV)']))],fmt='yo',label="Sodium-22",
   ↵ markersize=7.5,yerr=DataNa['Error'].values)
74 plt.title('Energy calibration residual plot',**TitleFont)
75 plt.xlabel('Gamma Energy [keV]',**AxTitleFont)
76 plt.ylabel('Channel Number Residual',**AxTitleFont)
77 plt.legend()
78 plt.show()
79
80
81 ChiStats = ChiSqFunc(list(FitDF['Mean']),list(Quadratic(FitDF['Energy
   ↵ (keV)'],*ParamsLinear)),list(FitDF['Error']),ParamsLinear)
82 print(ChiStats)

```

3.3 Subtraction.py

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 import seaborn as sns
4 sns.set()
5 import scipy as sc
6 import pandas as pd
7
8 # If statements that control what the code does!
9 PlotMysterySource = True
10 PlotKnownSources = True
11
12 # Plot controls
13 TitleFont = {'size':'23', 'color':'black', 'weight':'bold'}
14 AxTitleFont = {'size':'20'}
15
16 if PlotMysterySource:
17     BgWithShield = "WeekendBgWithShield_003_eh_1"
18     BgWithShieldDF = pd.read_csv(BgWithShield+ ".dat", sep=r"\s+", names = ['channel
19     ↵ number','count number'])
20
21     MysterySource = "MysterySource-24HrRun_001_eh_1"
22     MysterySourceDF = pd.read_csv(MysterySource+ ".dat", sep=r"\s+", names = ['channel
23     ↵ number','count number'])
24
25     # Normalises the timings of the two runs to 24 hours each
26     BgWithShieldDF['count number2'] = BgWithShieldDF['count number']
27     BgWithShieldDF['count number'] = BgWithShieldDF['count number'] / ( 239068 ) *
28     ↵ 86400
29
30     MysterySourceDF['count number'] = MysterySourceDF['count number'] -
31     ↵ BgWithShieldDF['count number']
32
33     a = 2.63977565e-06
34     b = 7.04767648
35     c = -1.91414134e-01
36
37     MysterySourceDF['Energies'] = np.sqrt( (BgWithShieldDF['channel number'] - c +
38     ↵ (b**2.0/ ( 4 * a ))/a ) - (b/(2*a)))
39     BgWithShieldDF['Energies'] = np.sqrt( (BgWithShieldDF['channel number'] - c +
40     ↵ (b**2.0/ ( 4 * a ))/a ) - (b/(2*a)))
41
42     plt.semilogy(MysterySourceDF['Energies'],MysterySourceDF['count
43     ↵ number'],label="Mystery Source")
44     plt.semilogy(BgWithShieldDF['Energies'],BgWithShieldDF['count
45     ↵ number2'],label="Background With Shield")
46     plt.xlabel('Gamma Energy [keV]',**AxTitleFont)
47     plt.ylabel('Log-10 of count number',**AxTitleFont)
48     plt.title('Mystery Source With Background Subtracted',**TitleFont)
49     plt.xlim(0,2216)
50     plt.ylim(1)
51     plt.legend()
52     plt.show()
53
54 if PlotKnownSources:
```

```

49 BgWithShield = "WeekendBgWithShield_003_eh_1"
50 BgWithShieldDF = pd.read_csv(BgWithShield+ ".dat", sep=r"\s+",names = ['channel
   ↵ number','count number'])
51
52 Sodium = 'Sodium22-24HrData_002_eh_1'
53 SodiumDF = pd.read_csv(Sodium+ ".dat", sep=r"\s+",names = ['channel number','count
   ↵ number'])
54
55 Barium = 'Barium133-24HrRun_006_eh_1'
56 BariumDF = pd.read_csv(Barium+ ".dat", sep=r"\s+",names = ['channel number','count
   ↵ number'])
57
58 Cobalt = 'Cobalt60-24HrData_004_eh_1'
59 CobaltDF = pd.read_csv(Cobalt+ ".dat", sep=r"\s+",names = ['channel number','count
   ↵ number'])
60
61 # Normalises the background to the correct timings
62 BgWithShieldDFCobalt = BgWithShieldDF.copy()
63 BgWithShieldDF['count number'] = BgWithShieldDF['count number'] / ( 239068 ) *
   ↵ 86400
64 BgWithShieldDFCobalt['count number'] = BgWithShieldDF['count number'] / ( 239068 )
   ↵ * (86400/12.0)
65
66 # Subtracts the background from the original data
67 SodiumDF['count number'] = SodiumDF['count number'] - BgWithShieldDF['count number']
68 BariumDF['count number'] = BariumDF['count number'] - BgWithShieldDF['count number']
69 CobaltDF['count number'] = CobaltDF['count number'] - BgWithShieldDFCobalt['count
   ↵ number']
70
71 # Fitting parameters
72 a = 7.01164642
73 b = 8.1697501
74
75 # Converting channel numbers to energies
76 SodiumDF['Energies'] = ( SodiumDF['channel number'] - b )/a
77 BariumDF['Energies'] = ( BariumDF['channel number'] - b )/a
78 CobaltDF['Energies'] = ( CobaltDF['channel number'] - b )/a
79
80
81 # Now plotting the different elements on different log-y plots.
82
83 plt.figure(1)
84 plt.semilogy(SodiumDF['Energies'],SodiumDF['count number'],label="Sodium 22
   ↵ data",color='yellow')
85 TitleFont = {'size':25, 'color':'black', 'weight':'bold'}
86 AxTitleFont = {'size':22}
87 plt.xlabel('Gamma Energy [keV]',**AxTitleFont)
88 plt.ylabel('Log-10 of count number',**AxTitleFont)
89 plt.title('Sodium 22, no background, energies',**TitleFont)
90 plt.xlim(0)
91 plt.ylim(1)
92 plt.legend()
93
94
95 plt.figure(2)
96 plt.semilogy(BariumDF['Energies'],BariumDF['count number'],label="Barium 133
   ↵ data",color='green')

```

```

97     TitleFont = {'size': '25', 'color': 'black', 'weight': 'bold'}
98     AxTitleFont = {'size': '22'}
99     plt.xlabel('Gamma Energy [keV]', **AxTitleFont)
100    plt.ylabel('Log-10 of count number', **AxTitleFont)
101    plt.title('Barium 133, no background, energies', **TitleFont)
102    plt.xlim(0)
103    plt.ylim(1)
104    plt.legend()
105
106
107    plt.figure(3)
108    plt.semilogy(CobaltDF['Energies'], CobaltDF['count number'], label="Cobalt 60
109      ↳ data", color='blue')
110    TitleFont = {'size': '25', 'color': 'black', 'weight': 'bold'}
111    AxTitleFont = {'size': '22'}
112    plt.xlabel('Gamma Energy [keV]', **AxTitleFont)
113    plt.ylabel('Log-10 of count number', **AxTitleFont)
114    plt.title('Cobalt 60, no background, energies', **TitleFont)
115    plt.xlim(0)
116    plt.ylim(1)
117    plt.legend()
118    plt.show()

```

3.4 Resolution.py

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 import scipy.optimize as sciopt
4 import seaborn as sns
5 import pandas as pd
6 sns.set()
7 import scipy.stats as scistats
8
9
10 def ResolutionFit(E,a,b):
11     return a/np.sqrt(E) + b
12
13 FitDF = pd.read_csv('Gamma_Peak_Stats_and_Parms.csv', names=['Element', 'Fit type',
14     ↪ 'Peak number', 'Peak type', 'Energy (keV)', 'Resolution', 'Min', 'Max', 'Mean',
15     ↪ 'A', 'Sigma', 'Error', 'a', 'b', 'chisq', 'Reduced chisq',
16     ↪ 'Probchisq'],usecols=list(range(1,18)))
17
18 FitDF['Energy (keV)'] = FitDF['Energy (keV)'].astype(float)
19 FitDF['Resolution'] = FitDF['Resolution'].astype(float).multiply(100)
20 SodiumDF = FitDF[(FitDF['Energy (keV)'] == 511)]
21 FitDF = FitDF[~(FitDF['Energy (keV)'] == 511)]
22
23
24 DataBa = FitDF[FitDF['Element'] == 'Barium133']
25 DataCo = FitDF[FitDF['Element'] == 'Cobalt60']
26 DataNa = FitDF[FitDF['Element'] == 'Sodium22']
27
28
29 Fit, Errors = sciopt.curve_fit(ResolutionFit,FitDF['Energy
30     ↪ (keV)'],FitDF['Resolution'])
31 print(Fit)
32
33 TitleFont = {'size':20, 'color':'black', 'weight':'bold'}
34 AxTitleFont = {'size':18}
35
36 plt.figure(1)
37 Energies = np.linspace(55,1400,14000)
38 plt.plot(Energies,ResolutionFit(Energies,*Fit),label="Fit")
39
40 plt.errorbar(DataBa['Energy (keV)'],DataBa['Resolution'],fmt="o",color='red',label="Barium-133",
41     ↪ markersize=7,yerr=(7.05/DataBa['Energy
42     ↪ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
43 plt.errorbar(DataCo['Energy (keV)'],DataCo['Resolution'],fmt="o",color='blue',label="Cobalt-60",
44     ↪ markersize=7,yerr=(7.05/DataCo['Energy
45     ↪ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
46 plt.errorbar(DataNa['Energy (keV)'],DataNa['Resolution'],fmt="o",color='yellow',label="Sodium-22",
47     ↪ markersize=7,yerr=(7.05/DataNa['Energy
48     ↪ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
49 plt.errorbar(SodiumDF['Energy (keV)'],SodiumDF['Resolution'],fmt="o",color='yellow',label="",
50     ↪ markersize=7,yerr=(7.05/SodiumDF['Energy
51     ↪ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
52
53 plt.xlabel('Peak Energy [keV]',**AxTitleFont)
54 plt.ylabel('Energy Resolution [%]',**AxTitleFont)
```

```

45 plt.title('Energy Resolution as a Function of Gamma Energy',**TitleFont)
46 plt.legend(fontsize=16,fancybox=True,shadow=False)
47
48 plt.figure(2)
49 plt.errorbar(DataBa['Energy (keV)'],DataBa['Resolution']-ResolutionFit(DataBa['Energy
   ↵ (keV)'],*Fit),fmt="o",color='red',label="Barium-133",markersize=7,yerr=(7.05/Data_
   ↵ Ba['Energy
   ↵ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
50 plt.errorbar(DataCo['Energy (keV)'],DataCo['Resolution']-ResolutionFit(DataCo['Energy
   ↵ (keV)'],*Fit),fmt="o",color='blue',label="Cobalt-60",markersize=7,yerr=(7.05/Data_
   ↵ Co['Energy
   ↵ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
51 plt.errorbar(DataNa['Energy (keV)'],DataNa['Resolution']-ResolutionFit(DataNa['Energy
   ↵ (keV)'],*Fit),fmt="o",color='yellow',label="Sodium-22",markersize=7,yerr=(7.05/Da_
   ↵ taNa['Energy
   ↵ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
52 plt.errorbar(SodiumDF['Energy
   ↵ (keV)'],SodiumDF['Resolution']-ResolutionFit(SodiumDF['Energy (keV)'],*Fit),fmt="_
   ↵ o",color='yellow',label="",markersize=7,yerr=(7.05/SodiumDF['Energy
   ↵ (keV)']),elinewidth=3,capsize=5,capthick=3,marker='o')
53 plt.xlabel('Peak Energy [keV]',**AxTitleFont)
54 plt.ylabel('Energy Resolution Residual [%]',**AxTitleFont)
55 plt.title('Energy Resolution Residuals',**TitleFont)
56 plt.legend(fontsize=16,fancybox=True,shadow=False)
57 plt.show()
58
59 def ChiSqFunc(Measured,Fitted,Errors,Params):
60     ChiSquared = 0
61     for i in range(len(Measured)):
62         ChiSquared += ((Measured[i] - Fitted[i])**2.0) / ((Errors[i])**2.0)
63     ReducedChiSq = ChiSquared/(len(Measured)-len(Params))
64     ProbChiSq = (1.0 - scistats.chi2.cdf(ChiSquared,len(Measured)-len(Params)) ) * *
       ↵ 100.0
65     return ChiSquared, ReducedChiSq, ProbChiSq
66
67
68 MeasuredThungys = list(DataBa['Resolution'])+list(DataCo['Resolution']) +
   ↵ list(DataNa['Resolution'])
69 FittedThingys = list(ResolutionFit(DataBa['Energy (keV)'],*Fit)) +
   ↵ list(ResolutionFit(DataCo['Energy (keV)'],*Fit)) +
   ↵ list(ResolutionFit(DataNa['Energy (keV)'],*Fit))
70 ErrorThingys = list(7.05/DataBa['Energy (keV)']) + list(7.05/DataCo['Energy (keV)']) +
   ↵ + list(7.05/DataBa['Energy (keV)'])
71
72 ChiStats = ChiSqFunc(MeasuredThungys, FittedThingys, ErrorThingys,Fit)
73 print(ChiStats)

```