

§ 8.1 Problems: 5, 6, ~~7~~, 9, 10, 11, ~~12~~, 13, 14, 27, ~~28~~, 29, 33 (34, 44, 45) ^{Bonus} I will do these.

§ 8.2 Problems: 5, 6, 12, ~~15~~, ~~18~~, 19, 20, 23, 25, 26, 30, ~~32~~, 33, ~~41~~

Please grade the circled problems for $\frac{1}{2}$ point each. The rest may have $\frac{1}{4}$ point without grading.

$$\text{total} = \underbrace{(2.5 + 1.5)}_{\S 8.1} + \underbrace{(2.5 + 2)}_{\S 8.2} = 8.5.$$

In § 8.1, problems # 34, 44, & 45 were bonus problems. I

I can take care of those. Thanks. Hamid

§ 8.1: #7) There is no Euler cycle because vertices b and d have odd degrees, $\delta(b) = \delta(d) = 5$.

#12) $V = \{v_1, v_2, v_3, v_4, v_5\}$, $E = \{e_1, e_2, e_3, e_4, e_5, e_6, e_7, e_8\}$

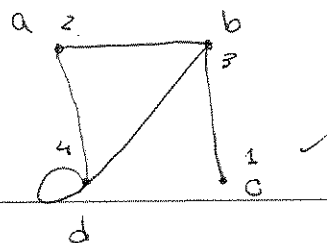
There are no parallel edges. There are no loops.

There are no isolated vertices. G is simple, e_1 is incident on v_2 & v_4 .

#28)	Path	length
	c, a, b, e, d	23 ← optimal path.
	c, e, b, a, d	26
	c, b, a, e, d	24
	d, a, b, e, c	26

§ 8.2

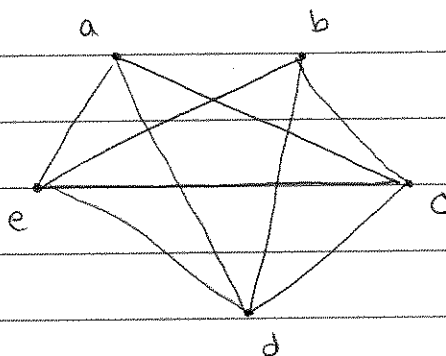
#15) 4 vertices having degrees 1, 2, 3, 4



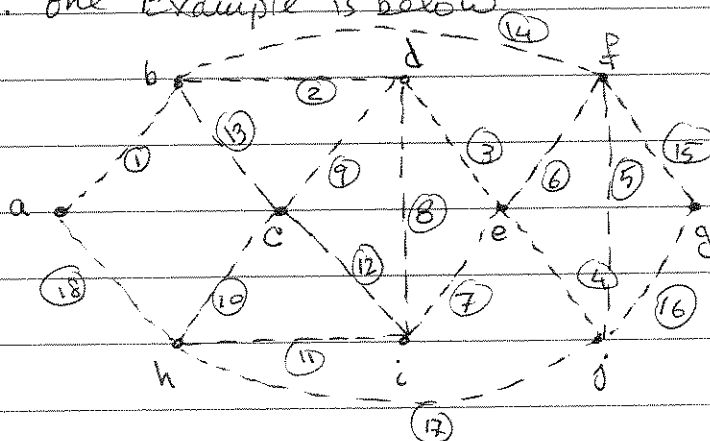
#18) simple graph, 5 vertices having degrees 2, 2, 4, 4, 4.
no such graph can exist.

Suppose the vertices are $V = \{a, b, c, d, e\}$ where $\delta(a) = \delta(b) = 2$ and $\delta(c) = \delta(d) = \delta(e) = 4$.

Since $\delta(c) = 4$, c is adjacent on a, b, d , and e . Similarly, d is adjacent on a, b, c , and e . Finally, e is adjacent to a, b, c , and d . This forces the vertices a and b having degrees 3.

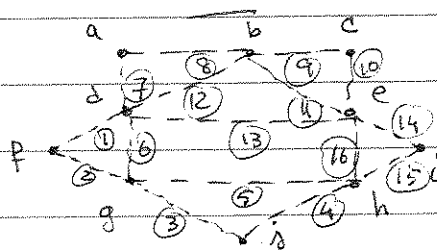


32) The graph has an Euler cycle since all vertices have even degrees. one Example is below



$c, b, d, e, j, f, e, i, d, c, h, i, c, b, f, g, j, h, a$

#41)



$d, f, g, j, h, g, d, a, b, c, e, h, d, e, i, h, e$