

Name:

Date:

1. Find the GCD(825, 315) and LCM(825, 315) using prime factorization.

$$825 = 3 \cdot 5^2 \cdot 11^1 = 3 \cdot 5^2 \cdot 7^0 \cdot 11^1$$

$$315 = 3^2 \cdot 5^1 \cdot 7^1 \cdot 11^0 = 3^2 \cdot 5^1 \cdot 7^1 \cdot 11^0$$

$$\text{GCD}(825, 315) = 3^{\min(1, 2)} \cdot 5^{\min(2, 1)} \cdot 7^{\min(0, 1)} \cdot 11^{\min(1, 0)}$$

$$= 3^1 \cdot 5^1 \cdot 7^0 \cdot 11^0 = 15$$

$$\text{LCM}(825, 315) = 3^{\max(1, 2)} \cdot 5^{\max(2, 1)} \cdot 7^{\max(0, 1)} \cdot 11^{\max(1, 0)}$$

$$= 3^2 \cdot 5^2 \cdot 7^1 \cdot 11^1 = 17325$$

$$\text{LCM}(825, 315) \cdot \text{GCD}(825, 315) = (17325)(15) = 259875$$

$$(825)(315) = 259875$$