$\hat{y} = g(\vec{x})$ $y = g(\bar{x}) + e = \hat{y} + e = \hat{y} + (y - \hat{y})$

The algorithm $^{ extstyle A}$ produces g. Since g is fully specified by theta, the algorithm selects / estimates / optimizes / fits a theta. Let's create an algorithm. A bad algorithm will have high estimation y 0 0 1 0 e Let's define an overall error function / objective function called "misclassification error" (ME)

$$ME = \frac{1}{n} \sum_{i=1}^{n} \mathbb{1}_{g(\mathbb{R}_{i})} \neq y_{i} = \frac{1}{n} \sum_{i=1}^{n} |e_{i}|$$
or accuracy (ACC) as
$$ACC = \frac{1}{n} \sum_{i=1}^{n} \mathbb{1}_{g(\mathbb{R}_{i})} = y_{i} = 1 - ME$$

A produces

$$ACC = \frac{1}{n} \sum_{i=1}^{n} \mathbb{1}_{\{i\}} \mathbb{1}_{\{i\}} = 1 - A_i E$$
 goal of the algorithm is to minimize ME (or maximize ACC). To do so, we check every possible $\mathcal{O} = \bigcirc$ and keep track of the ME(theta) and then return the model with the lowest ME.

How to define parameter space? It must be finite because we need to check (i.e. compute ME) each element. Gabriel says grid up [300, 850] e.g. {351, 352, ..., 849, 850}. That's fine, but it's more convenient to only check the unique values of x.

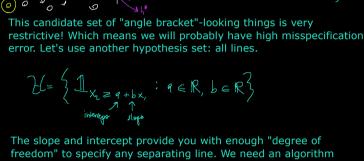
A produce
$$g(x) = 1_{x \ge argmin} \{ \frac{1}{n}, \frac{1}{2}, \frac{1}{2} \}$$

Let's make a loan model with two continuous x's i.e. x_1, x_2 (p=2)

 $\begin{cases} x_1 & \text{of } 1 \\ \text{of } 1 \end{cases}$

A two dimensional threshold model extending what we have before has candidate set:

 $\mathcal{U} = \left\{ 1_{x_1 \geq \theta_1} 1_{x_1 \neq \theta_2} : \begin{bmatrix} \theta_1 \\ \theta_2 \end{bmatrix} \in \mathbb{Q} \right\}$



to find g i.e. to specify a and b. This is a hard problem so we

21 = { 1 wo + v, x, + w, x, = 0 : wo ∈ R, v, ∈ R, wz ∈ R}

We will first reparameterize the hypothesis space to be:

will study it with different conditions.

data record:

weight of the first feature, weight of second feature intercept term "bias In order to fit this model, we "add" a dummy value of 1 to each

$$\vec{X} = \begin{bmatrix} 750 & 59000 \end{bmatrix}$$
 $\vec{X} = \begin{bmatrix} 1 & 750 & 558000 \end{bmatrix}$
So we append the $\vec{1}$, the n-dim column vector to X, the matrix of features in \vec{D} .

 $\overrightarrow{w}_{k} := \underset{\overrightarrow{w} \in \mathbb{R}^{3}}{\operatorname{argin}} \left\{ \begin{array}{c} \sum_{i=1}^{n} \mathbb{1}_{\overrightarrow{w}_{i} \neq 0} = y_{i} \end{array} \right\} = \underset{i=1}{\operatorname{argin}}$

We have a problem here. There is no analytic solution since the indicator function is non-differentiable.

We only need 2 parameters (a,b) but here we have three (w_0, w_1, w_2) and hence we are "over-parameterized" meaning we have infinite solutions seen here:

Step 2: Compute $\hat{y_i} = 1_{\vec{w}^{co}} \cdot \vec{x}_i \ge 0$ Step 3: For j = 0, 1, ..., p set $W_o^{t=1} = W_o^{t=0} + (y_i - \hat{y}_i)$

Step 1: Initialize $\overrightarrow{w}^{t=0} = \overrightarrow{\mathbb{Q}}_{p+1}$ or to a random vector value.

Step 4: Repeat steps 2 and 3 for
$$i = 1, ..., n$$
 (all the observations). Step 5: Repeat steps 2,3 and 4 until ME = 0 i.e. all e_i's = 0 or until a prespecified (large) number of iterations. Note: t is the iteration number. It starts at 0. t = 1 is first iteration... The perception is proved to converged for linearly separable datasets but for non-linearly separable datasets, anything can

 $W_{l}^{t=1} = W_{i}^{t=0} + (y_{i} - \hat{y}_{i})(X_{i,l})$

activation function (in our case the Heaviside indicator function)

all possible solutions which vary based on starting values