# FinancePy .171

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2 CONTENTS

# **Chapter 1**

# **Introduction to FinancePy**

# **FinancePy**

FinancePy is a library of native Python functions which covers the following functionality:

- Valuation and risk models for a wide range of equity, FX, interest rate and credit derivatives.
- Portfolio asset allocation using Markovitz and other methods.

As the library is written entirely in Python, the user has the ability to examine the underlying code and its logic.

The target audience for this library is intended to include:

- Students wishing to learn derivative pricing and Python.
- Professors wishing to teach derivative pricing and Python.
- Traders wishing to price or risk-manage a derivative.
- Quantitative analysts seeking to price or reverse engineer a price.
- Risk managers wishing to replicate and understand a price.
- Portfolio managers wishing to check prices or calculate risk measures
- Fund managers wanting to value a portfolio or examine a trading strategy
- Structurers or financial engineers seeking to examine the pricing of a derivative structure.

Users are expected to have a good, but not advanced, understanding of Python.

Up until now my main focus has been on financial derivatives. In general my approach has been:

- 1. To make the code as simple as possible so that those with a basic Python fluency can understand and check the code.
- 2. To keep all the code in Python so users can look through the code to the lowest level.
- 3. To offset the performance impact of (2) by leveraging Numba to make the code as fast as possible without resorting to Cython.

- 4. To make the design product-based rather than model-based so someone wanting to price a specific exotic option can easily find that without having to worry too much about the model just use the default unless they want to.
- 5. To make the library as complete as possible so a user can find all their required finance-related functionality in one place. This is better for the user as they only have to learn one interface.
- 6. To avoid complex designs I am OK with some code duplication, at least temporarily.
- 7. To have good documentation and easy-to-follow examples.
- 8. To make it easy for interested parties to contribute.

In many cases the valuations should be close to if not identical to those produced by financial systems such as Bloomberg. However for some products, larger value differences may arise due to differences in date generation and interpolation schemes. Over time I hope to reduce the size of such differences.

IF YOU HAVE ANY EXAMPLES YOU WOULD LIKE ME TO REPLICATE, SEND ME SCREENSHOTS OF ALL THE UNDERLYING DATA AND MODEL DETAILS

## The Library Design

The underlying Python library is split into a number of major modules:

- Finutils These are utility functions used to assist you with modelling a security. These include dates (FinDate), calendars, schedule generation, some finance-related mathematics functions and some helper functions.
- Market These are modules that capture the market information used to value a security. These include interest rate and credit curves, volatility surfaces and prices.
- Models These are the low-level models used to value derivative securities ranging from Black-Scholes to complex stochastic volatility models.
- Products These are the actual securities and range from Government bonds to Bermudan swaptions.

Any price is the result of a PRODUCT + MODEL + MARKET. The interface to each product has a value() function that will take a model and market to produce a price.

There are also two other folders which are currently fairly empty: They are:

- Portfolio This will be where portfolio allocation will go,
- Risk This is for portfolio risk analysis

# How to Use the Library

FinancePy can be installed using pip (see instructions below). I have provided a range of template Jupyter notebooks under the github repository called FinancePy-Examples. The link is as follows:

https://github.com/domokane/FinancePy-Examples

A pdf description of functions can be found at the same repository.

# Help Needed

The current version of the code is a beta. If you have any questions or issues then please send them to me. Contact me via the github page.

#### **Author**

My name is Dr. Dominic O'Kane. I teach Finance at the EDHEC Business School in Nice, France. I have 12 years of industry experience and 10 years of academic experience.

#### Installation

FinancePy can be installed from pip using the command: pip install financepy To upgrade an existing installation type: pip install –upgrade financepy

### **Dependencies**

FinancePy depends on Numpy, Numba and Scipy.

### Changelog

See the changelog for a detailed history of changes

#### **Contributions**

Contributions are very welcome. There are a number of requirements:

- You should use CamelCase i.e. variables of the form optionPrice
- Comments are required for every class and function and they should be clear
- At least one test case must be provided for every function
- Follow the style of the code as currently written. This may change over time but please use the current style as your guide.

#### License

MIT

# Chapter 2

# financepy.finutils

### 2.1 Introduction

This is a collection of modules used across a wide range of FinancePy functions. Examples include date generation, special mathematical functions and useful helper functions for performing some repeated action.

- FinDate is a class for handling dates in a financial setting. Special functions are included for computing IMM dates and CDS dates and moving dates forward by tenors.
- FinCalendar is a class for determining which dates are not business dates in a specific region or country.
- FinDayCount is a class for determining accrued interest in bonds and also accrual factors in ISDA swap-like contracts.
- FinError is a class which handles errors in the calculations done within FinancePy
- FinFrequency takes in a frequency type and then returns the number of payments per year
- FinGlobalVariables holds the value of constants used across the whole of FinancePy
- FinHelperFunctions is a set of helpful functions that can be used in a number of places
- FinMath is a set of mathematical functions specific to finance which have been optimised for speed using Numba
- FinSobol is the implementation of Sobol quasi-random number generator. It has been speeded up using Numba.
- FinRateConverter converts rates for one compounding frequency to rates for a different frequency
- FinSchedule generates a sequence of cashflow payment dates in accordance with financial market standards
- FinStatistics calculates a number of statistical variables such as mean, standard deviation and variance
- FinTestCases is the code that underlies the test case framework used across FinancePy

## 2.2 FinCalendar

## Enumerated Type: FinBusDayAdjustTypes

This enumerated type has the following values:

- NONE
- FOLLOWING
- MODIFIED\_FOLLOWING
- PRECEDING
- MODIFIED\_PRECEDING

# Enumerated Type: FinCalendarTypes

This enumerated type has the following values:

- TARGET
- US
- UK
- WEEKEND
- JAPAN
- NONE

## Enumerated Type: FinDateGenRuleTypes

This enumerated type has the following values:

- FORWARD
- BACKWARD

# Class: FinCalendar(object)

Class to manage designation of payment dates as holidays according to a regional or country-specific calendar convention specified by the user.

### **FinCalendar**

Create a calendar based on a specified calendar type.

```
def FinCalendar(calendarType: FinCalendarTypes):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
calendarType	FinCalendarTypes	-	-

## adjust

Adjust a payment date if it falls on a holiday according to the specified business day convention.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	FinDate	-	-
busDayConventionType	FinBusDayAdjustTypes	-	-

# isBusinessDay

Determines if a date is a business day according to the specified calendar. If it is it returns True, otherwise False.

```
def isBusinessDay(dt: FinDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	FinDate	-	-

# getHolidayList

generates a list of holidays in a specific year for the specified calendar. Useful for diagnostics.

```
def getHolidayList(year: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
year	float	-	-

# easterMonday

Get the day in a given year that is Easter Monday. This is not easy to compute so we rely on a pre-calculated array.

```
def easterMonday(year: float):
```

Argument Name	Type	Description	Default Value
year	float	-	-

## 2.3 FinDate

# Class: FinDate()

A date class to manage dates that is simple to use and includes a number of useful date functions used frequently in Finance.

### **FinDate**

Create a date given a day of month, month and year. The arguments must be in the order of day (of month), month number and then the year. The year must be a 4-digit number greater than or equal to 1900.

```
def FinDate(d: int, # Day number in month with values from 1 to 31
    m: int, # Month number where January = 1, ..., December = 12
    y: int): # Year number which must be between 1900 and 2100
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
d	int	Day number in month with values from 1 to 31	-
m	int	Month number where January = 1,, December = 12	-
у	int	Year number which must be between 1900 and 2100	-

#### refresh

Update internal representation of date as number of days since the 1st Jan 1900. This is same as Excel convention.

```
def refresh():
```

The function arguments are described in the following table.

### isWeekend

returns True if the date falls on a weekend.

```
def isWeekend():
```

The function arguments are described in the following table.

# addDays

Returns a new date that is numDays after the FinDate.

```
def addDays(numDays: int):
```

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numDays	int	-	-

# addWorkDays

Returns a new date that is numDays working days after FinDate.

```
def addWorkDays(numDays: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
numDays	int	-	-

### addMonths

Returns a new date that is mm months after the FinDate. If mm is an integer or float you get back a single date. If mm is a vector you get back a vector of dates.

```
def addMonths(mm: int):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
mm	int	-	-

### addYears

Returns a new date that is yy years after the FinDate. If yy is an integer or float you get back a single date. If yy is a list you get back a vector of dates.

```
def addYears(yy: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
уу	int	-	-

### nextCDSDate

Returns a CDS date that is mm months after the FinDate. If no argument is supplied then the next CDS date after today is returned.

```
def nextCDSDate(mm: int = 0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
mm	int	-	0

# third We dnesday Of Month

For a specific month and year this returns the day number of the 3rd Wednesday by scanning through dates in the third week.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
m	int	Month number	-
У	int	Year number	-

#### nextIMMDate

This function returns the next IMM date after the current date This is a 3rd Wednesday of Jun, March, Sep or December

```
def nextIMMDate():
```

The function arguments are described in the following table.

### addTenor

Return the date following the FinDate by a period given by the tenor which is a string consisting of a number and a letter, the letter being d, w, m, y for day, week, month or year. This is case independent. For example 10Y means 10 years while 120m also means 10 years.

```
def addTenor(tenor: str):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
tenor	str	-	-

### date

Returns a datetime of the date

```
def date():
```

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### print

prints formatted string of the date.

```
def print():
```

The function arguments are described in the following table.

# $\ daily Working Day Schedule$

Returns a list of working dates between startDate and endDate. This function should be replaced by dateRange once addTenor allows for working days.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
self	-	-	-
startDate	FinDate	-	-
endDate	FinDate	-	-

### datediff

Calculate the number of days between two Findates.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
d1	FinDate	-	-
d2	FinDate	-	-

### **fromDatetime**

Construct a FinDate from a datetime as this is often needed if we receive inputs from other Python objects such as Pandas dataframes.

```
def fromDatetime(dt: FinDate):
```

<b>Argument Name</b>	Type	Description	Default Value
dt	FinDate	-	-

# dateRange

Returns a list of dates between startDate (inclusive) and endDate (inclusive). The tenor represents the distance between two consecutive dates and is set to daily by default.

Argument Name	Type	Description	<b>Default Value</b>
startDate	FinDate	-	-
endDate	FinDate	-	-
tenor	str	-	"1D"

2.4. FINDAYCOUNT 15

# 2.4 FinDayCount

# Enumerated Type: FinDayCountTypes

This enumerated type has the following values:

- THIRTY\_E\_360\_ISDA
- THIRTY\_E\_360\_PLUS\_ISDA
- ACT\_ACT\_ISDA
- ACT\_ACT\_ICMA
- ACT\_365\_ISDA
- THIRTY\_360
- THIRTY\_360\_BOND
- THIRTY\_E\_360
- ACT\_360
- ACT\_365\_FIXED
- ACT\_365\_LEAP

### Class: FinDayCount(object)

Calculate the fractional day count between two dates according to a specified day count convention.

# **FinDayCount**

Create Day Count convention by passing in the Day Count Type.

```
def FinDayCount(dccType: FinDayCountTypes):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
dccType	FinDayCountTypes	-	-

# yearFrac

Calculate the year fraction between dates dt1 and dt2 using the specified day count convention.

Argument Name	Type	Description	Default Value
dt1	FinDate	-	-
dt2	FinDate	-	-
dt3	FinDate	-	None

# 2.5 FinError

# Class: FinError(Exception)

Simple error class specific to FinPy. Need to decide how to handle FinancePy errors. Work in progress.

### **FinError**

Create FinError object by passing a message string.

```
def FinError(message: str):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
message	str	-	-

# print

print("FinError:", self.\_message)

```
def print():
```

The function arguments are described in the following table.

### func\_name

```
def func_name():
```

The function arguments are described in the following table.

# isNotEqual

if abs(x - y); tol:

```
def isNotEqual(x, y, tol=1e-6):
```

Argument Name	Type	Description	Default Value
X	-	-	-
У	-	-	-
tol	-	-	1e-6

2.6. FINFREQUENCY

# 2.6 FinFrequency

# Enumerated Type: FinFrequencyTypes

This enumerated type has the following values:

- CONTINUOUS
- SIMPLE
- ANNUAL
- SEMI\_ANNUAL
- QUARTERLY
- MONTHLY

# **FinFrequency**

This is a function that takes in a Frequency Type and returns an integer for the number of times a year a payment occurs.

```
def FinFrequency(frequencyType):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
frequencyType	-	-	-

### zeroToDf

Convert a zero with a specified compounding frequency to a discount factor.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
r	float	-	-
t	(float	-	-
np.ndarray)	-	-	-
frequencyType	FinFrequencyTypes	-	-

### dfToZero

Convert a discount factor to a zero rate with a specific compounding frequency.

Argument Name	Type	Description	<b>Default Value</b>
df	float	-	-
t	float	-	-
frequencyType	FinFrequencyTypes	-	-

# 2.7 FinGlobalVariables

# 2.8 FinHelperFunctions

# pv01Times

Calculate a bond style pv01 by calculating remaining coupon times for a bond with t years to maturity and a coupon frequency of f. The order of the list is reverse time order - it starts with the last coupon date and ends with the first coupon date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	float	-	-
f	float	-	-

### **timesFromDates**

If a single date is passed in then return the year from valuation date but if a whole vector of dates is passed in then convert to a vector of times from the valuation date. The output is always a numpy vector of times which has only one element if the input is only one date.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
dt	FinDate	-	-
valuationDate	FinDate	-	-
dayCountType	FinDayCountTypes	-	ACT_ACT_ISDA

### **checkVectorDifferences**

Compare two vectors elementwise to see if they are more different than tolerance.

Argument Name	Type	Description	Default Value
X	np.ndarray	-	-
y	np.ndarray	-	-
tol	float	-	1e-6

## checkDate

Check that input d is a FinDate.

```
def checkDate(d: FinDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
d	FinDate	-	-

## dump

Get a list of all of the attributes of a class (not built in ones)

```
def dump(obj):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
obj	-	-	-

# printTree

Function that prints a binomial or trinonial tree to screen for the purpose of debugging.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
array	np.ndarray	-	-
depth	int	-	None

# inputTime

Validates a time input in relation to a curve. If it is a float then it returns a float as long as it is positive. If it is a FinDate then it converts it to a float. If it is a Numpy array then it returns the array as long as it is all positive.

Argument Name	Type	Description	Default Value
dt	FinDate	-	-
curve	-	-	-

### listdiff

Calculate a vector of differences between two equal sized vectors.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	np.ndarray	-	-
b	np.ndarray	-	-

# dotproduct

Fast calculation of dot product using Numba.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
xVector	np.ndarray	-	-
yVector	np.ndarray	-	-

# frange

fast range function that takes start value, stop value and step.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
start	int	-	-
stop	int	-	-
step	int	-	-

# normaliseWeights

Normalise a vector of weights so that they sum up to 1.0.

```
def normaliseWeights(wtVector: np.ndarray):
```

Argument Name	Type	Description	Default Value
wtVector	np.ndarray	-	-

# labelToString

Format label/value pairs for a unified formatting.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
label	str	-	-
value	float	-	-
separator	str	-	"\n"
listFormat	bool	-	False

# tableToString

Format a 2D array into a table-like string.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
header	str	-	-
valueTable	-	-	-
floatPrecision	-	-	"10.7f"

# to Usable Type

Convert a type such that it can be used with 'isinstance'

```
def toUsableType(t):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-

# checkArgumentTypes

Check that all values passed into a function are of the same type as the function annotations. If a value has not been annotated, it will not be checked.

```
def checkArgumentTypes(func, values):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
func	-	-	-
values	-	-	-

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## 2.9 FinMath

# accruedInterpolator

Fast calulation of accrued interest using an Actual/Actual type of convention. This does not calculate according to other conventions.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
tset	float	Settlement time in years	-
couponTimes	np.ndarray	-	-
couponAmounts	np.ndarray	-	-

# isLeapYear

Test whether year y is a leap year - if so return True, else False

```
def isLeapYear(y: int):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
y	int	-	-

### scale

Scale all of the elements of an array by the same amount factor.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-
factor	float	-	-

# testMonotonicity

Check that an array of doubles is monotonic and strictly increasing.

```
def testMonotonicity(x: np.ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-

# testRange

Check that all of the values of an array fall between a lower and upper bound.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	np.ndarray	-	-
lower	float	-	-
upper	float	-	-

### maximum

Determine the array in which each element is the maximum of the corresponding element in two equally length arrays a and b.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
a	np.ndarray	-	-
b	np.ndarray	-	-

#### maxaxis

Perform a search for the vector of maximum values over an axis of a 2D Numpy Array

```
def maxaxis(s: np.ndarray):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	np.ndarray	-	-

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### minaxis

Perform a search for the vector of minimum values over an axis of a 2D Numpy Array

```
def minaxis(s: np.ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
S	np.ndarray	-	-

#### covar

Calculate the Covariance of two arrays of numbers. TODO: check that this works well for Numpy Arrays and add NUMBA function signature to code. Do test of timings against Numpy.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
a	np.ndarray	-	-
b	np.ndarray	-	-

# pairGCD

Determine the Greatest Common Divisor of two integers using Euclid's algorithm. TODO - compare this with math.gcd(a,b) for speed. Also examine to see if I should not be declaring inputs as integers for NUMBA.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
v1	float	-	-
v2	float	-	-

### nprime

Calculate the first derivative of the Cumulative Normal CDF which is simply the PDF of the Normal Distribution

```
def nprime(x: float):
```

<b>Argument Name</b>	Type	Description	Default Value
X	float	-	-

### heaviside

Calculate the Heaviside function for x

```
def heaviside(x: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	float	-	-

# frange

Calculate a range of values from start in steps of size step. Ends as soon as the value equals or exceeds stop.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
start	int	-	-
stop	int	-	-
step	int	-	-

# normpdf

Calculate the probability density function for a Gaussian (Normal) function at value x

```
def normpdf(x: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	float	-	-

## normcdf\_fast

Fast Normal CDF function based on XXX

```
def normcdf_fast(x: float):
```

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The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	float	-	-

# normcdf\_integrate

Calculation of Normal Distribution CDF by simple integration which can become exact in the limit of the number of steps tending towards infinity. This function is used for checking as it is slow since the number of integration steps is currently hardcoded to 10,000.

```
def normcdf_integrate(x: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	float	-	-

### normcdf\_slow

Calculation of Normal Distribution CDF accurate to 1d-15. This method is faster than integration but slower than other approximations. Reference: J.L. Schonfelder, Math Comp 32(1978), pp 1232-1240.

```
def normcdf_slow(z: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
Z	float	-	-

### normcdf

This is the Normal CDF function which forks to one of three of the implemented approximations. This is based on the choice of the fast flag variable. A value of 1 is the fast routine, 2 is the slow and 3 is the even slower integration scheme.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	float	-	-
fastFlag	int	-	-

### N

This is the shortcut to the default Normal CDF function and currently is hardcoded to the fastest of the implemented routines. This is the most widely used way to access the Normal CDF.

```
def N(x: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
X	float	-	-

## phi3

Bivariate Normal CDF function to upper limits b1 and b2 which uses integration to perform the innermost integral. This may need further refinement to ensure it is optimal as the current range of integration is from -7 and the integration steps are dx = 0.001. This may be excessive.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
b1	float	-	-
b2	float	-	-
b3	float	-	-
r12	float	-	-
r13	float	-	-
r23	float	-	-

### norminvcdf

This algorithm computes the inverse Normal CDF and is based on the algorithm found at (http:#home.online.no/pjacklam/notes/invnorm/) which is by John Herrero (3-Jan-03)

```
def norminvcdf(p):
```

Argument Name	Type	Description	<b>Default Value</b>
p	-	-	-

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### $\mathbf{M}$

return phi2(a, b, c)

```
def M(a, b, c):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
С	-	-	-

# phi2

Drezner and Wesolowsky implementation of bi-variate normal

```
def phi2(h1, hk, r):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
h1	-	-	-
hk	-	-	-
r	-	-	-

## corrMatrixGenerator

Utility function to generate a full rank  $n \times n$  correlation matrix with a flat correlation structure and value rho.

```
def corrMatrixGenerator(rho, n):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
rho	-	-	-
n	-	-	-

# 2.10 FinOptionTypes

# Enumerated Type: FinOptionTypes

This enumerated type has the following values:

- EUROPEAN\_CALL
- EUROPEAN\_PUT
- AMERICAN\_CALL
- AMERICAN\_PUT
- DIGITAL\_CALL
- DIGITAL\_PUT
- ASIAN\_CALL
- ASIAN\_PUT
- COMPOUND\_CALL
- COMPOUND\_PUT

## Enumerated Type: FinLiborSwaptionTypes

This enumerated type has the following values:

- PAYER
- RECEIVER

## Enumerated Type: FinOptionExerciseTypes

This enumerated type has the following values:

- EUROPEAN
- BERMUDAN
- AMERICAN

## 2.11 FinRateConverter

# Class: FinRateConverter(object)

Convert rates between different compounding conventions. This is not used.

## **FinRateConverter**

Set the base rate frequency for the converter. This is not used so will be depracated next version.

def FinRateConverter(frequency):

Argument Name	Type	Description	Default Value
frequency	-	-	-

## 2.12 FinSchedule

### Class: FinSchedule(object)

A Schedule is a vector of dates generated according to ISDA standard rules which starts on the next date after the start date and runs up to an end date. Dates are adjusted to a provided calendar. The zeroth element is the previous coupon date (PCD) and the first element is the Next Coupon Date (NCD).

#### **FinSchedule**

Create FinSchedule object which calculates a sequence of dates in line with market convention for fixed income products.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
startDate	FinDate	-	-
endDate	FinDate	-	-
frequencyType	FinFrequencyTypes	-	ANNUAL
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

#### flows

Returns a list of the schedule of FinDates.

```
def flows():
```

The function arguments are described in the following table.

#### generate

Generate schedule of dates according to specified date generation rules and also adjust these dates for holidays according to the specified business day convention and the specified calendar.

```
def generate():
```

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## generate\_alternative

This adjusts each date BEFORE generating the next date. Generate schedule of dates according to specified date generation rules and also adjust these dates for holidays according to the business day convention and the specified calendar.

```
def generate_alternative():
```

The function arguments are described in the following table.

## print

Print out the details of the schedule and the actual dates. This can be used for providing transparency on schedule calculations.

```
def print():
```

# 2.13 FinSobol

## get Gaussian Sobol

Sobol Gaussian quasi random points generator based on graycode order. The generated points follow a normal distribution.

```
def getGaussianSobol(numPoints, dimension):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numPoints	-	-	-
dimension	-	-	-

## getUniformSobol

Sobol uniform quasi random points generator based on graycode order.

```
def getUniformSobol(numPoints, dimension):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
numPoints	-	-	-
dimension	-	-	-

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## 2.14 FinStatistics

#### mean

Calculate the arithmetic mean of a vector of numbers x.

```
def mean(x: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	float	-	-

## stdev

Calculate the standard deviation of a vector of numbers x.

```
def stdev(x: ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
X	ndarray	-	-

#### stderr

Calculate the standard error estimate of a vector of numbers x.

```
def stderr(x: ndarray):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	ndarray	-	-

#### var

Calculate the variance of a vector of numbers x.

```
def var(x: ndarray):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	ndarray	-	-

#### moment

Calculate the m-th moment of a vector of numbers x.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
X	ndarray	-	-
m	int	-	-

## correlation

Calculate the correlation between two series x1 and x2.

Argument Name	Type	Description	<b>Default Value</b>
x1	ndarray	-	-
x2	ndarray	-	-

# **Chapter 3**

# financepy.market.curves

## 3.1 Introduction

#### **Curves**

#### **Overview**

These modules create a family of curve types related to the term structures of interest rates. There are two basic types of curve:

- 1. Best fit yield curves fitting to bond prices which are used for interpolation. A range of curve shapes from polynomials to B-Splines is available.
- 2. Discount curves that can be used to present value a future cash flow. These differ from best fits curves in that they exactly refit the prices of bonds or CDS. The different discount curves are created by calibrating to different instruments. They also differ in terms of the term structure shapes they can have. Different shapes have different impacts in terms of locality on risk management performed using these different curves. There is often a trade-off between smoothness and locality.

#### **Best Fit Bond Curves**

The first category are FinBondYieldCurves.

#### **FinBondYieldCurve**

This module describes a curve that is fitted to bond yields calculated from bond market prices supplied by the user. The curve is not guaranteed to fit all of the bond prices exactly and a least squares approach is used. A number of fitting forms are provided which consist of

- Polynomial
- Nelson-Siegel
- Nelson-Siegal-Svensson
- · Cubic B-Splines

This fitted curve cannot be used for pricing as yields assume a flat term structure. It can be used for fitting and interpolating yields off a nicely constructed yield curve interpolation curve.

#### FinCurveFitMethod

This module sets out a range of curve forms that can be fitted to the bond yields. These includes a number of parametric curves that can be used to fit yield curves. These include:

- Polynomials of any degree
- Nelson-Siegel functional form.
- Nelson-Siegel-Svensson functional form.
- B-Splines

#### **Discount Curves**

These are curves which supply a discount factor that can be used to present-value future payments.

#### FinDiscountCurve

This is a curve made from a Numpy array of times and discount factor values that represents a discount curve. It also requires a specific interpolation scheme. A function is also provided to return a survival probability so that this class can also be used to handle term structures of survival probabilities. Other curves inherit from this in order to share common functionality.

#### FinDiscountCurveFlat

This is a class that takes in a single flat rate.

#### FinDiscountCurveNS

Implementation of the Nelson-Siegel curve parametrisation.

#### FinDiscountCurveNSS

Implementation of the Nelson-Siegel-Svensson curve parametrisation.

#### FinDiscountCurveZeros

This is a discount curve that is made from a vector of times and zero rates.

#### **FinInterpolate**

This module contains the interpolation function used throughout the discount curves when a discount factor needs to be interpolated. There are three interpolation methods:

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1. PIECEWISE LINEAR - This assumes that a discount factor at a time between two other known discount factors is obtained by linear interpolation. This approach does not guarantee any smoothness but is local. It does not guarantee positive forwards (assuming positive zero rates).

- 2. PIECEWISE LOG LINEAR This assumes that the log of the discount factor is interpolated linearly. The log of a discount factor to time T is T x R(T) where R(T) is the zero rate. So this is not linear interpolation of R(T) but of T x R(T).
- 3. FLAT FORWARDS This interpolation assumes that the forward rate is constant between discount factor points. It is not smooth but is highly local and also ensures positive forward rates if the zero rates are positive.

## 3.2 FinDiscountCurve

## Class: FinDiscountCurve()

This is a base discount curve which has an internal representation of a vector of times and discount factors and an interpolation scheme for interpolating between these fixed points.

#### **FinDiscountCurve**

Create the discount curve from a vector of times and discount factors with an anchor date and specify an interpolation scheme. As we are explicitly linking dates and discount factors, we do not need to specify any compounding convention or day count calculation since discount factors are pure prices. We do however need to specify a convention for interpolating the discount factors in time.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	FinDate	-	-
dfDates	list	-	-
dfValues	np.ndarray	-	-
interpMethod	-	-	FLAT_FORWARDS

#### zeroRate

Calculation of zero rates with specified frequency. This function can return a vector of zero rates given a vector of times so must use Numpy functions. Default frequency is a continuously compounded rate.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	(list	-	-
FinDate)	-	-	-
frequencyType	FinFrequencyTypes	-	CONTINUOUS

### parRate

Calculate the par rate to maturity date. This is the rate paid by a bond that has a price of par today. For a par swap rate, use the swap rate function that takes in the swap details.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	FinDate	-	-
frequencyType	-	-	ANNUAL

# swapRate

Calculate the breakeven swap rate for an interest rate swap that starts on the settlement date (which may be forward starting) with a specified frequency and day count convention. Have omitted calendar and other input choices for the moment so default values being used.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	FinDate	-	-
settlementDate	FinDate	-	-
maturityDate	FinDate	-	-
fixedFrequencyType	FinFrequencyTypes	-	-
fixedDayCountType	FinDayCountTypes	-	-

#### df

Function to calculate a discount factor from a date or a vector of dates.

```
def df(dt: (list, FinDate)):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
dt	(list	-	-
FinDate)	-	-	-

#### **survProb**

return self.df(dt)

```
def survProb(dt: FinDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	FinDate	-	-

#### fwd

Calculate the continuously compounded forward rate at the forward FinDate provided. This is done by perturbing the time by a small amount and measuring the change in the log of the discount factor divided by the time increment dt.

```
def fwd(dt: FinDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	FinDate	-	-

#### bump

Calculate the continuous forward rate at the forward date.

```
def bump(bumpSize: float):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
bumpSize	float	-	-

#### **fwdRate**

Calculate the forward rate between two foreward dates according to the specified day count convention.

Argument Name	Type	Description	<b>Default Value</b>
startDate	(list	-	-
FinDate)	-	-	-
endDate	(list	-	-
FinDate)	-	-	-
dayCountType	FinDayCountTypes	-	ACT_360

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# print

Simple print function for backward compatibility.

def print():

#### 3.3 FinDiscountCurveFlat

### Class: FinDiscountCurveFlat(FinDiscountCurve)

A very simple discount curve based on a single zero rate with its own specified compounding method. Hence the curve is assumed to be flat. It is used for quick and dirty analysis and when limited information is available. It inherits several methods from FinDiscountCurve.

#### **FinDiscountCurveFlat**

Create a discount curve which is flat. This is very useful for quick testing and simply requires a curve date and a rate and also a frequency. As we have entered a rate, a corresponding day count convention must be used to specify how time periods are to be measured. As the curve is flat, no interpolation scheme is required.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	FinDate	-	-
flatRate	float	-	-
frequencyType	FinFrequencyTypes	-	CONTINUOUS
dayCountType	FinDayCountTypes	-	ACT_ACT_ISDA

#### bump

Creates a new FinDiscountCurveFlat object with the entire curve bumped up by the bumpsize. All other parameters are preserved.

```
def bump(bumpSize: float):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
bumpSize	float	-	-

#### print

Simple print function for backward compatibility.

```
def print():
```

## 3.4 FinDiscountCurveNS

## Class: FinDiscountCurveNS(FinDiscountCurve)

Implementation of Nelson-Siegel parametrisation of a discount curve. The internal rate is a continuously compounded rate but you can calculate alternative frequencies by providing a corresponding compounding frequency. The class inherits methods from FinDiscountCurve.

## **FinDiscountCurveNS**

Creation of a FinDiscountCurveNS object. Parameters are provided individually for beta0, beta1, beta2 and tau. The zero rates produced by this parametrisation have an implicit compounding convention that defaults to continuous but which can be overridden.

The function arguments are described in the following table.

Type	Description	Default Value
FinDate	-	-
float	-	-
FinFrequencyTypes	-	CONTINUOUS
	FinDate float float float float float	FinDate - float - float - float - float -

#### print

Simple print function for backward compatibility.

```
def print():
```

## 3.5 FinDiscountCurveNSS

## Class: FinDiscountCurveNSS(FinDiscountCurve)

Implementation of Nelson-Siegel-Svensson parametrisation of the zero rate curve. The zero rate is assumed to be continuously compounded. This can be changed when calling for zero rates. The class inherits lots of methods from FinDiscountCurve.

#### **FinDiscountCurveNSS**

Create a FinDiscountCurveNSS object by passing in curve valuation date plus the 4 different beta values and the 2 tau values. The zero rates produced by this parametrisation have an implicit compounding convention that defaults to continuous but can be overriden.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	FinDate	-	-
beta0	float	-	-
beta1	float	-	-
beta2	float	-	-
beta3	float	-	-
tau1	float	-	-
tau2	float	-	-
frequencyType	FinFrequencyTypes	-	CONTINUOUS

## print

Simple print function for backward compatibility.

```
def print():
```

# 3.6 FinDiscountCurvePoly

## Class: FinDiscountCurvePoly(FinDiscountCurve)

Zero Rate Curve of a specified frequency parametrised using a cubic polynomial. The zero rate is assumed to be continuously compounded but this can be amended by providing a frequency when extracting zero rates. The class inherits all of the methods from FinDiscountCurve.

## **FinDiscountCurvePoly**

Create zero rate curve parametrised using a cubic curve from coefficients and specifying a compounding frequency type.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	FinDate	-	-
coefficients	(list	-	-
np.ndarray)	-	-	-
frequencyType	FinFrequencyTypes	-	CONTINUOUS

## print

Simple print function for backward compatibility.

```
def print():
```

## 3.7 FinDiscountCurvePWF

## Class: FinDiscountCurvePWF(FinDiscountCurve)

Curve is made up of a series of zero rates sections with each having a piecewise flat zero rate. The default compounding assumption is continuous. The class inherits methods from FinDiscountCurve.

#### **FinDiscountCurvePWF**

Creates a discount curve using a vector of times and zero rates that assumes that the zero rates are piecewise flat.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	FinDate	-	-
zeroDates	list	-	-
zeroRates	(list	-	-
np.ndarray)	-	-	-
frequencyType	FinFrequencyTypes	-	CONTINUOUS

## print

Simple print function for backward compatibility.

```
def print():
```

## 3.8 FinDiscountCurvePWL

## Class: FinDiscountCurvePWL(FinDiscountCurve)

Curve is made up of a series of sections assumed to each have a piece-wise linear zero rate. The zero rate has a specified frequency which defaults to continuous. This curve inherits all of the extra methods from FinDiscountCurve.

## **FinDiscountCurvePWL**

Curve is defined by a vector of increasing times and zero rates.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	FinDate	-	-
zeroDates	list	-	-
zeroRates	(list	-	-
np.ndarray)	-	-	-
frequencyType	FinFrequencyTypes	-	CONTINUOUS

## print

Simple print function for backward compatibility.

```
def print():
```

## 3.9 FinDiscountCurveZeros

## Class: FinDiscountCurveZeros(FinDiscountCurve)

This is a curve calculated from a set of dates and zero rates. As we have rates as inputs, we need to specify the corresponding compounding frequency. Also to go from rates and dates to discount factors we need to compute the year fraction correctly and for this we require a day count convention. Finally, we need to interpolate the zero rate for the times between the zero rates given and for this we must specify an interpolation convention. The class inherits methods from FinDiscountCurve.

#### **FinDiscountCurveZeros**

Create the discount curve from a vector of dates and zero rates factors. The first date is the curve anchor. Then a vector of zero dates and then another same-length vector of rates. The rate is to the corresponding date. We must specify the compounding frequency of the zero rates and also a day count convention for calculating times which we must do to calculate discount factors. Finally we specify the interpolation scheme.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	FinDate	-	-
zeroDates	list	-	-
zeroRates	(list	-	-
np.ndarray)	-	-	-
frequencyType	FinFrequencyTypes	-	ANNUAL
dayCountType	FinDayCountTypes	-	ACT_ACT_ISDA
interpMethod	FinInterpMethods	-	FLAT_FORWARDS

## bump

Calculate the continuous forward rate at the forward date.

```
def bump(bumpSize):
```

Argument Name	Type	Description	<b>Default Value</b>
bumpSize	-	-	-

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# print

Simple print function for backward compatibility.

def print():

# 3.10 FinInterpolate

# Enumerated Type: FinInterpMethods

This enumerated type has the following values:

- LINEAR\_ZERO\_RATES
- FLAT\_FORWARDS
- LINEAR\_FORWARDS

### interpolate

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
X	-	-	-
times	-	-	-
dfs	-	-	-
method	-	-	-

## uinterpolate

Return the interpolated value of y given x and a vector of x and y. The values of x must be monotonic and increasing. The different schemes for interpolation are linear in y (as a function of x), linear in log(y) and piecewise flat in the continuously compounded forward y rate.

```
def uinterpolate(t, times, dfs, method):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	-	-	-
times	-	-	-
dfs	-	-	-
method	-	-	-

## vinterpolate

Return the interpolated values of y given x and a vector of x and y. The values of x must be monotonic and increasing. The different schemes for interpolation are linear in y (as a function of x), linear in log(y) and piecewise flat in the continuously compounded forward y rate.

Argument Name	Type	Description	<b>Default Value</b>
xValues	-	-	-
xvector	-	-	-
dfs	-	-	-
method	-	-	-

# **Chapter 4**

# financepy.market.volatility

#### 4.1 Introduction

## **Market Volatility**

#### **Overview**

These modules create a family of curve types related to the market volatility. There are three types of class:

- 1. Term structures of volatility i.e. volatility as a function of option expiry date.
- 2. Volatility curves which are smile/skews so store volatility as a function of option strike.
- 3. Volatility surfaces which hold volatility as a function of option expiry date AND option strike.

The classes are as follows:

## **FinEquityVolCurve**

Equity volatility as a function of option strike. This is usually a skew shape.

#### FinFXVolSurface

FX volatility as a function of option expiry and strike. This class constructs the surface from the ATM volatility and 25 delta strangles and risk reversals and does so for multiple expiry dates.

## FinLiborCapFloorVol

Libor cap/floor volatility as a function of option expiry (cap/floor start date). Takes in cap (flat) volatility and boostraps the caplet volatility. This is assumed to be piecewise flat.

## FinLiborCapFloorVolFn

Parametric function for storing the cap and caplet volatilities based on form proposed by Rebonato.

## 4.2 FinEquityVolCurve

## Class: FinEquityVolCurve()

Class to manage a smile or skew in volatility at a single maturity horizon. It fits the volatility using a polynomial. Includes analytics to extract the implied pdf of the underlying at maturity.

## **FinEquityVolCurve**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
curveDate	-	-	-
expiryDate	-	-	-
strikes	-	-	-
volatilities	-	-	-
polynomial	-	-	3

## volatility

Return the volatility for a strike using a given polynomial interpolation.

```
def volatility(strike):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
strike	-	-	-

#### calculatePDF

calculate the probability density function of the underlying using the volatility smile or skew curve following the approach set out in Breedon and Litzenberger.

```
def calculatePDF():
```

## 4.3 FinFXVolSurface

Class: FinFXVolSurface()

#### **FinFXVolSurface**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	-	-
currencyPair	-	-	-
notionalCurrency	-	-	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
tenors	-	-	-
atmVols	-	-	-
mktStrangle25DeltaVols	-	-	-
riskReversal25DeltaVols	-	-	-
atmMethod	-	-	FWD_DELTA_NEUTRAL
deltaMethod	-	-	SPOT_DELTA

#### volFunction

Return the volatility for a strike using a given polynomial interpolation following Section 3.9 of Iain Clark book.

```
def volFunction(K, tenorIndex):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
tenorIndex	-	-	-

#### buildVolSurface

PLEASE ADD A FUNCTION DESCRIPTION

```
def buildVolSurface():
```

The function arguments are described in the following table.

#### solveForSmileStrike

Solve for the strike that sets the delta of the option equal to the target value of delta allowing the volatility to be a function of the strike

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
vanillaOption	-	-	-
deltaTarget	-	-	-
tenorIndex	-	-	-

#### checkCalibration

PLEASE ADD A FUNCTION DESCRIPTION

```
def checkCalibration():
```

The function arguments are described in the following table.

## plotVolCurves

PLEASE ADD A FUNCTION DESCRIPTION

```
def plotVolCurves():
```

The function arguments are described in the following table.

## obj

Return a function that is minimised when the ATM, MS and RR vols have been best fitted using the parametric volatility curve respresented by cvec

```
def obj(cvec, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
cvec	-	-	-
*args	-	-	-

# deltaFit

```
def deltaFit(K, *args):
```

Argument Name	Type	Description	Default Value
K	-	-	-
*args	-	-	-

## 4.4 FinLiborCapVolCurve

## Class: FinLiborCapVolCurve()

Class to manage a term structure of cap (flat) volatilities and to do the conversion to caplet (spot) volatilities. This does not manage a strike dependency, only a term structure. The cap and caplet volatilies are keyed off the cap and caplet maturity dates. However this volatility only applies to the evolution of the Libor rate out to the caplet start dates. Note also that this class also handles floor vols.

## **FinLiborCapVolCurve**

Create a cap/floor volatility curve given a curve date, a list of cap maturity dates and a vector of cap volatilities. To avoid confusion first date of the capDates must be equal to the curve date and first cap volatility for this date must equal zero. The internal times are calculated according to the provided day count convention. Note cap and floor volatilities are the same for the same strike and tenor, I just refer to cap volatilities in the code for code simplicity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
curveDate	-	Valuation date for cap volatility	-
capMaturityDates	-	curve date + maturity dates for caps	-
capSigmas	-	Flat cap volatility for cap maturity dates	-
dayCountType	-	-	-

## generateCapletVols

Bootstrap caplet volatilities from cap volatilities using similar notation to Hull's book (page 32.11). The first volatility in the vector of caplet vols is zero.

```
def generateCapletVols():
```

The function arguments are described in the following table.

## capletVol

```
def capletVol(dt):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
dt	-	-	-

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# capVol

Return the cap flat volatility for a specific cap maturity date for the last caplet/floorlet in the cap/floor. The volatility interpolation is piecewise flat.

```
def capVol(dt):
```

Argument Name	Type	Description	Default Value
dt	-	-	-

# 4.5 FinLiborCapVolCurveFn

## Class: FinLiborCapVolCurveFn()

Class to manage a term structure of caplet volatilities using the parametric form suggested by Rebonato (1999).

# Fin Libor Cap Vol Curve Fn

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
curveDate	-	-	-
a	-	-	-
b	-	-	-
С	-	-	-
d	-	-	-

## capFloorletVol

Return the caplet volatility.

```
def capFloorletVol(dt):
```

Argument Name	Type	Description	Default Value
dt	-	-	-

# **Chapter 5**

# financepy.products.equity

# 5.1 Introduction

This folder covers a range of equity derivative products. These range from simple Vanilla-style options to more complex payoffs and path-dependent options.

## 5.2 FinEquityAsianOption

## Class: FinEquityAsianOption(FinEquityOption)

Class for an Equity Asian Option. This is an option with a final payoff linked to the average stock price. The valuation is done for both an arith- metic and geometric average.

## **FinEquityAsianOption**

Creat FinEquityAsian option.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
startAveragingDate	FinDate	-	-
expiryDate	FinDate	-	-
strikePrice	float	-	-
optionType	FinOptionTypes	-	-
numberOfObservations	int	-	0

#### value

Calculate the value of an Asian option using one of the specified models.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
valuationMethod	-	-	-
accruedAverage	-	-	None

#### valueGeometric

This option valuation is based on paper by Kemna and Vorst 1990. It calculates the Geometric Asian option price which is a lower bound on the Arithmetic option price. This should not be used as a valuation model for the Arithmetic Average option but can be used as a control variate for other approaches.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
accruedAverage	-	-	-

#### valueCurran

Valuation of an Asian option using the result by Vorst.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
accruedAverage	-	-	-

#### valueTurnbullWakeman

Asian option valuation based on paper by Turnbull and Wakeman 1991 which uses the edgeworth expansion to find the first two moments of the arithmetic average.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
accruedAverage	-	-	-

### valueMC

Monte Carlo valuation of the Asian Average option.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
numPaths	-	-	-
seed	-	-	-
accruedAverage	-	-	-

#### valueMC\_fast

Monte Carlo valuation of the Asian Average option.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	Yield	-
model	-	Model	-
numPaths	-	Numpaths integer	-
seed	-	-	-
accruedAverage	-	-	-

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# $valueMC\_fast\_CV$

Monte Carlo valuation of the Asian Average option using a control variate method.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
numPaths	-	-	-
seed	-	-	-
accruedAverage	-	-	-

# 5.3 FinEquityBarrierOption

### Enumerated Type: FinEquityBarrierTypes

This enumerated type has the following values:

- DOWN\_AND\_OUT\_CALL
- DOWN\_AND\_IN\_CALL
- UP\_AND\_OUT\_CALL
- UP\_AND\_IN\_CALL
- UP\_AND\_OUT\_PUT
- UP\_AND\_IN\_PUT
- DOWN\_AND\_OUT\_PUT
- DOWN\_AND\_IN\_PUT

### Class: FinEquityBarrierOption(FinEquityOption)

Class to hold details of an Equity Barrier Option. It also calculates the option price using Black Scholes for 8 different variants on the Barrier structure in enum FinEquityBarrierTypes.

# **FinEquityBarrierOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
strikePrice	float	-	-
optionType	FinEquityBarrierTypes	-	-
barrierLevel	float	-	-
numObservationsPerYear	int	-	-
notional	float	-	1.0

#### value

Thisprices the formulae option using thegiven the paper by Clewlow, Strickland December 1994 Llanos and which can be found at https://warwick.ac.uk/fac/soc/wbs/subjects/finance/research/wpaperseries/1994/94-54.pdf

<b>Argument Name</b>	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

### valueMC

### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
processType	-	-	-
modelParams	-	-	-
numAnnSteps	-	-	252
numPaths	-	-	10000
seed	-	-	4242

# 5.4 FinEquityBasketOption

### Class: FinEquityBasketOption(FinEquityOption)

class FinEquityBasketOption(FinEquityOption):

### FinEquityBasketOption

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
strikePrice	float	-	-
optionType	FinOptionTypes	-	-
numAssets	int	-	-

#### validate

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
stockPrices	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

#### value

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

### valueMC

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-
numPaths	-	-	10000
seed	-	-	4242

# 5.5 FinEquityBinomialTree

### Enumerated Type: FinEquityTreePayoffTypes

This enumerated type has the following values:

- FWD\_CONTRACT
- VANILLA\_OPTION
- DIGITAL\_OPTION
- POWER\_CONTRACT
- POWER\_OPTION
- LOG\_CONTRACT
- LOG\_OPTION

### Enumerated Type: FinEquityTreeExerciseTypes

This enumerated type has the following values:

- EUROPEAN
- AMERICAN

### Class: FinEquityBinomialTree()

class FinEquityBinomialTree():

### **FinEquityBinomialTree**

pass

```
def FinEquityBinomialTree():
```

The function arguments are described in the following table.

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
numSteps	-	-	-
valueDate	-	-	-
payoff	-	-	-
expiryDate	-	-	-
payoffType	-	-	-
exerciseType	-	-	-
payoffParams	-	-	-

### validatePayoff

PLEASE ADD A FUNCTION DESCRIPTION

```
def validatePayoff(payoffType, payoffParams):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
payoffType	-	-	-
payoffParams	-	-	-

# payoffValue

PLEASE ADD A FUNCTION DESCRIPTION

```
def payoffValue(s, payoffType, payoffParams):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
S	-	-	-
payoffType	-	_	-
payoffParams	-	-	-

### valueOnce

```
timeToExpiry,
payoffType,
exerciseType,
payoffParams):
```

Argument Name	Type	Description	<b>Default Value</b>
stockPrice	-	-	-
r	-	-	-
dividendYield	-	-	-
volatility	-	-	-
numSteps	-	-	-
timeToExpiry	-	-	-
payoffType	-	-	-
exerciseType	-	-	-
payoffParams	-	-	-

# 5.6 FinEquityCompoundOption

### Class: FinEquityCompoundOption(FinEquityOption)

class FinEquityCompoundOption(FinEquityOption):

# Fin Equity Compound Option

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiryDate1	FinDate	-	-
expiryDate2	FinDate	-	-
strikePrice1	float	-	-
strikePrice2	float	-	-
optionType1	FinOptionTypes	-	-
optionType2	FinOptionTypes	-	-

#### value

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### valueTree

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
numSteps	-	-	200

# implied Stock Price

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
	Type	Type         Description           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -

f

```
def f(s0, *args):
```

Argument Name	Type	Description	<b>Default Value</b>
s0	-	-	-
*args	-	-	-

### valueOnce

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
stockPrice	-	-	-
riskFreeRate	-	-	-
dividendYield	-	-	-
volatility	-	-	-
t1	-	-	-
t2	-	-	-
optionType1	-	-	-
optionType2	-	-	-
k1	-	-	-
k2	-	-	-
numSteps	-	-	-

# 5.7 FinEquityDigitalOption

### Class: FinEquityDigitalOption(FinEquityOption)

class FinEquityDigitalOption(FinEquityOption):

### **FinEquityDigitalOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
strikePrice	float	-	-
optionType	FinOptionTypes	-	-

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### valueMC

numPaths=10000, seed=4242):

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
numPaths	-	-	10000
seed	-	-	4242

# 5.8 FinEquityFixedLookbackOption

### Enumerated Type: FinEquityFixedLookbackOptionTypes

This enumerated type has the following values:

- FIXED\_CALL
- FIXED\_PUT

### Class: FinEquityFixedLookbackOption(FinEquityOption)

class FinEquityFixedLookbackOption(FinEquityOption):

### Fin Equity Fixed Look back Option

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
optionType	FinEquityFixedLookbackOptionTypes	-	-
optionStrike	float	-	-

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
stockMinMax	-	-	-

### valueMC

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def valueMC(valueDate,
    stockPrice,
    discountCurve,
    dividendYield,
    volatility,
    stockMinMax,
    numPaths=10000,
    numStepsPerYear=252,
    seed=4242):
```

<b>Argument Name</b>	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
stockMinMax	-	-	-
numPaths	-	-	10000
numStepsPerYear	-	-	252
seed	-	-	4242

# 5.9 FinEquityFloatLookbackOption

### Enumerated Type: FinEquityFloatLookbackOptionTypes

This enumerated type has the following values:

- FLOATING\_CALL
- FLOATING\_PUT

### Class: FinEquityFloatLookbackOption(FinEquityOption)

 $class\ Fin Equity Float Look back Option (Fin Equity Option):$ 

### FinEquityFloatLookbackOption

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
optionType	FinEquityFloatLookbackOptionTypes	-	-

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
stockMinMax	-	-	-

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### valueMC

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
stockMinMax	-	-	-
numPaths	-	-	10000
numStepsPerYear	-	-	252
seed	-	-	4242

# 5.10 FinEquityModelTypes

Class: FinEquityModel(object)

### **FinEquityModel**

 $self.\_parentType = None$ 

```
def FinEquityModel():
```

The function arguments are described in the following table.

### Class: FinEquityModelBlackScholes(FinEquityModel)

class FinEquityModelBlackScholes(FinEquityModel):

### FinEquityModelBlackScholes

self.\_parentType = FinEquityModel

```
def FinEquityModelBlackScholes(volatility, numStepsPerYear=100, useTree=False):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
numStepsPerYear	-	-	100
useTree	-	-	False

# Class: FinEquityModelHeston(FinEquityModel)

class FinEquityModelHeston(FinEquityModel):

# FinEquityModelHeston

self.\_parentType = FinEquityModel

```
def FinEquityModelHeston(volatility, meanReversion):
```

Argument Name	Type	Description	Default Value
volatility	-	-	-
meanReversion	-	-	-

# 5.11 FinEquityOption

### Enumerated Type: FinEquityOptionTypes

This enumerated type has the following values:

- EUROPEAN\_CALL
- EUROPEAN\_PUT
- AMERICAN\_CALL
- AMERICAN\_PUT
- DIGITAL\_CALL
- DIGITAL\_PUT
- ASIAN\_CALL
- ASIAN\_PUT
- COMPOUND\_CALL
- COMPOUND\_PUT

### Enumerated Type: FinEquityOptionModelTypes

This enumerated type has the following values:

- BLACKSCHOLES
- ANOTHER

### Class: FinEquityOption(object)

class FinEquityOption(object):

#### delta

v = self.value(

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### gamma

v = self.delta(

```
def gamma(valueDate,
    stockPrice,
    discountCurve,
    dividendYield,
    model):
```

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### vega

v = self.value(

```
def vega(valueDate,
    stockPrice,
    discountCurve,
    dividendYield,
    model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### theta

v = self.value(

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Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

### rho

### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

# 5.12 FinEquityRainbowOption

### Enumerated Type: FinEquityRainbowOptionTypes

This enumerated type has the following values:

- CALL\_ON\_MAXIMUM
- PUT\_ON\_MAXIMUM
- CALL\_ON\_MINIMUM
- PUT\_ON\_MINIMUM
- CALL\_ON\_NTH
- PUT\_ON\_NTH

### Class: FinEquityRainbowOption(FinEquityOption)

class FinEquityRainbowOption(FinEquityOption):

### FinEquityRainbowOption

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiryDate	FinDate	-	-
payoffType	FinEquityRainbowOptionTypes	-	-
payoffParams	List[float]	-	-
numAssets	int	-	-

#### validate

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
stockPrices	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

# validate Payoff

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def validatePayoff(payoffType, payoffParams, numAssets):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
payoffType	-	-	-
payoffParams	-	-	-
numAssets	-	-	-

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
expiryDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

#### valueMC

Argument Name	Type	Description	Default Value
valueDate	-	-	-
expiryDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-
numPaths	-	-	10000
seed	-	-	4242

# payoffValue

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def payoffValue(s, payoffTypeValue, payoffParams):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
payoffTypeValue	-	-	-
payoffParams	-	-	-

### valueMCFast

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-
numAssets	-	-	-
payoffType	-	-	-
payoffParams	-	-	-
numPaths	-	-	10000
seed	-	-	4242

# 5.13 FinEquityVanillaOption

### Class: FinEquityVanillaOption(FinEquityOption)

class FinEquityVanillaOption(FinEquityOption):

### **FinEquityVanillaOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiryDate	FinDate	-	-
strikePrice	float	-	-
optionType	FinOptionTypes	-	-
numOptions	float	-	1.0

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### xdelta

```
dividendYield,
model):
```

<b>Argument Name</b>	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

### xgamma

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### **xvega**

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

### xtheta

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

### **impliedVolatility**

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
price	-	-	-

#### valueMC

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-
numPaths	-	-	10000
seed	-	-	4242

### value\_MC\_OLD

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
terminalS	-	-	-
seed	-	-	4242

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def f(volatility, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
volatility	-	-	-
*args	-	-	-

### fvega

```
def fvega(volatility, *args):
```

Argument Name	Type	Description	Default Value
volatility	-	-	-
*args	-	-	-

# 5.14 FinEquityVarianceSwap

### Class: FinEquityVarianceSwap(object)

### **FinEquityVarianceSwap**

Create variance swap contract.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
startDate	FinDate	-	-
maturityDateOrTenor	FinDate or str	-	-
strikeVariance	float	-	-
notional	float	-	ONE_MILLION
payStrikeFlag	bool	-	True

#### value

Calculate the value of the variance swap based on the realised volatility to the valuation date, the forward looking implied volatility to the maturity date using the libor discount curve.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
realisedVar	-	-	-
fairStrikeVar	-	-	-
liborCurve	-	-	-

# fairStrikeApprox

This is an approximation of the fair strike variance by Demeterfi et al. (1999) which assumes that sigma(K) = sigma(F) - b(K-F)/F where F is the forward stock price and sigma(F) is the ATM forward vol.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
fwdStockPrice	-	-	-
strikes	-	-	-
volatilities	-	-	-

### fairStrike

Calculate the implied variance according to the volatility surface using a static replication methodology with a specially weighted portfolio of put and call options across a range of strikes using the approximate method set out by Demeterfi et al. 1999.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
stockPrice	-	-	-
dividendYield	-	-	-
volatilityCurve	-	-	-
numCallOptions	-	-	-
numPutOptions	-	-	-
strikeSpacing	-	-	-
discountCurve	-	-	-
useForward	-	-	True

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def f(x): return (2.0/tmat)*((x-sstar)/sstar-log(x/sstar))
```

Argument Name	Type	Description	<b>Default Value</b>
x return (2.0/tmat)*((x-sstar)/sstar-log(x/sstar))	-	-	-

### realised Variance

Calculate the realised variance according to market standard calculations which can either use log or percentage returns.

```
def realisedVariance(closePrices, useLogs=True):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
closePrices	-	-	-
useLogs	-	-	True

# print

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def print():
```

# **Chapter 6**

# financepy.products.credit

#### 6.1 Introduction

This folder contains a set of credit-related assets ranging from CDS to CDS options, to CDS indices, CDS index options and then to CDS tranches. They are as follows:

- FinCDS is a credit default swap contract. It includes schedule generation, contract valuation and risk-management functionality.
- FinCDSBasket is a credit default basket such as a first-to-default basket. The class includes valuation according to the Gaussian copula.
- FinCDSIndexOption is an option on an index of CDS such as CDX or iTraxx. A full valuation model
  is included.
- FinCDSOption is an option on a single CDS. The strike is expressed in spread terms and the option is European style. It is different from an option on a CDS index option. A suitable pricing model is provided which adjusts for the risk that the reference credit defaults before the option expiry date.
- FinCDSTranche is a synthetic CDO tranche. This is a financial derivative which takes a loss if the total loss on the portfolio exceeds a lower threshold K1 and which is wiped out if it exceeds a higher threshold K2. The value depends on the default correlation between the assets in the portfolio of credits. This also includes a valuation model based on the Gaussian copula model.

#### **FinCDSCurve**

This is a curve that has been calibrated to fit the market term structure of CDS contracts given a recovery rate assumption and a FinLiborCurve discount curve. It also contains a LiborCurve object for discounting. It has methods for fitting the curve and also for extracting survival probabilities.

#### 6.2 FinCDS

### Class: FinCDS(object)

A class which manages a Credit Default Swap. It performs schedule generation and the valuation and risk management of CDS.

#### **FinCDS**

Create a CDS from the step-in date, maturity date and coupon

```
def FinCDS(stepInDate: FinDate, # FinDate is when protection starts (usually T+1)
    maturityDateOrTenor: Union[FinDate, str], # FinDate or a FinTenor
    runningCoupon: float, # Annualised coupon on premium leg
    notional: float = ONE_MILLION,
    longProtection: bool = True,
    frequencyType: FinFrequencyTypes = FinFrequencyTypes.QUARTERLY,
    dayCountType: FinDayCountTypes = FinDayCountTypes.ACT_360,
    calendarType: FinDayCountTypes = FinCalendarTypes.WEEKEND,
    busDayAdjustType: FinBusDayAdjustTypes = FinBusDayAdjustTypes.FOLLOWING,
    dateGenRuleType: FinDateGenRuleTypes = FinDateGenRuleTypes.BACKWARD):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
stepInDate	FinDate	FinDate is when protection starts (usually T+1)	-
maturityDateOrTenor	FinDate or str	FinDate or a FinTenor	-
runningCoupon	float	Annualised coupon on premium leg	-
notional	float	-	ONE_MILLION
longProtection	bool	-	True
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	ACT_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

#### value

Valuation of a CDS contract on a specific valuation date given an issuer curve and a contract recovery rate.

6.2. FINCDS 105

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
pv01Method	-	-	0
prot_method	-	-	0
numStepsPerYear	-	-	25

#### creditDV01

Calculation of the change in the value of the CDS contract for a one basis point change in the level of the CDS curve.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
pv01Method	-	-	0
prot_method	-	-	0
numStepsPerYear	-	-	25

### interestDV01

Calculation of the interest DV01 based on a simple bump of the discount factors and reconstruction of the CDS curve.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
pv01Method	-	-	0
prot_method	-	-	0
numStepsPerYear	-	-	25

### cashSettlementAmount

Value of the contract on the settlement date including accrued interest.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
settlementDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
pv01Method	-	-	0
prot_method	-	-	0
numStepsPerYear	-	-	25

### cleanPrice

Value of the CDS contract excluding accrued interest.

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Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
pv01Method	-	-	0
prot_method	-	-	0
numStepsPerYear	-	-	52

### riskyPV01\_OLD

RiskyPV01 of the contract using the OLD method.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
pv01Method	-	-	0

### accruedDays

Number of days between the previous coupon and the currrent step in date.

```
def accruedDays():
```

The function arguments are described in the following table.

#### accruedInterest

Calculate the amount of accrued interest that has accrued from the previous coupon date (PCD) to the stepInDate of the CDS contract.

```
def accruedInterest():
```

The function arguments are described in the following table.

# protectionLegPV

Calculates the protection leg PV of the CDS by calling into the fast NUMBA code that has been defined above.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
numStepsPerYear	-	-	25
protMethod	-	-	0

### riskyPV01

The riskyPV01 is the present value of a risky one dollar paid on the premium leg of a CDS contract.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
issuerCurve	-	-	-
pv01Method	-	-	0

# premiumLegPV

Value of the premium leg of a CDS.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
pv01Method	-	-	0

# parSpread

Breakeven CDS coupon that would make the value of the CDS contract equal to zero.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
issuerCurve	-	-	-
contractRecovery	-	-	standardRecovery
numStepsPerYear	-	-	25
pv01Method	-	-	0
protMethod	-	-	0

## valueFastApprox

Implementation of fast valuation of the CDS contract using an accurate approximation that avoids curve building.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
flatContinuousInterestRate	-	-	-
flatCDSCurveSpread	-	-	-
curveRecovery	-	-	standardRecovery
contractRecovery	-	-	standardRecovery

### printFlows

PLEASE ADD A FUNCTION DESCRIPTION

```
def printFlows(issuerCurve):
```

Argument Name	Type	Description	<b>Default Value</b>
issuerCurve	-	-	-

### print

Simple print function for backward compatibility.

```
def print():
```

The function arguments are described in the following table.

# riskyPV01\_NUMBA

Fast calculation of the risky PV01 of a CDS using NUMBA. The output is a numpy array of the full and clean risky PV01.

Argument Name	Type	Description	Default Value
teff	-	-	-
accrualFactorPCDToNow	-	-	-
paymentTimes	-	-	-
yearFracs	-	-	-
npLiborTimes	-	-	-
npLiborValues	-	-	-
npSurvTimes	-	-	-
npSurvValues	-	-	-
pv01Method	-	-	-

6.3. FINCDSBASKET

### 6.3 FinCDSBasket

Class: FinCDSBasket(object)

#### **FinCDSBasket**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
stepInDate	FinDate	-	-
maturityDate	FinDate	-	-
notional	float	-	ONE_MILLION
coupon	float	-	0.0
longProtection	bool	-	True
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	ACT_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

# $valueLegs\_MC$

Value the legs of the default basket using Monte Carlo. The default times are an input so this valuation is not model dependent.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
nToDefault	-	-	-
defaultTimes	-	-	-
issuerCurves	-	-	-
liborCurve	-	-	-

#### valueGaussian\_MC

Value the default basket using a Gaussian copula model. This depends on the issuer curves and correlation matrix.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
nToDefault	-	-	-
issuerCurves	-	-	-
correlationMatrix	-	-	-
liborCurve	-	-	-
numTrials	-	-	-
seed	-	-	-

### valueStudentT\_MC

Value the default basket using the Student-T copula.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
nToDefault	-	-	-
issuerCurves	-	-	-
correlationMatrix	-	-	-
degreesOfFreedom	-	-	-
liborCurve	-	-	-
numTrials	-	-	-
seed	-	-	-

### value1FGaussian\_Homo

Value default basket using 1 factor Gaussian copula and analytical approach which is only exact when all recovery rates are the same.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
nToDefault	-	-	-
issuerCurves	-	-	-
betaVector	-	-	-
liborCurve	-	-	-
numPoints	-	-	50

### 6.4 FinCDSCurve

### Class: FinCDSCurve()

Generate a survival probability curve implied by the value of CDS contracts given a Libor curve and an assumed recovery rate. A scheme for the interpolation of the survival probabilities is also required.

#### **FinCDSCurve**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
curveDate	-	-	-
cdsContracts	-	-	-
liborCurve	-	-	-
recoveryRate	-	-	0.40
useCache	-	-	False
interpolationMethod	-	-	FLAT_FORWARDS

#### survProb

Extract the survival probability to date dt. This function supports vectorisation.

```
def survProb(dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
dt	-	-	-

### df

Extract the discount factor from the underlying Libor curve. This function supports vectorisation.

```
def df(dt):
```

Argument Name	Type	Description	Default Value
dt	-	-	-

6.4. FINCDSCURVE

#### fwd

Calculate the instantaneous forward rate at the forward date dt using the numerical derivative.

```
def fwd(dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-

#### **fwdRate**

Calculate the forward rate according between dates date1 and date2 according to the specified day count convention.

```
def fwdRate(date1, date2, dayCountType):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
date1	-	-	-
date2	-	-	-
dayCountType	-	-	-

#### zeroRate

Calculate the zero rate to date dt in the chosen compounding frequency where -1 is continuous is the default.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-
frequencyType	-	-	CONTINUOUS

### print

Simple print function for backward compatibility.

```
def print():
```

### uniformToDefaultTime

Fast mapping of a uniform random variable to a default time given a survival probability curve.

```
def uniformToDefaultTime(u, t, v):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
u	-	-	-
t	-	-	-
V	-	-	-

f

Function that returns zero when the survival probability that gives a zero value of the CDS has been determined.

```
def f(q, *args):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
q	-	-	-
*args	-	-	-

# 6.5 FinCDSIndexOption

### Class: FinCDSIndexOption(object)

Class to manage the pricing and risk management of an option to enter into a CDS index. Different pricing algorithms are presented.

### **FinCDSIndexOption**

Initialisation of the class object. Note that a large number of the

The function arguments are described in the following table.

Type	Description	Default Value
FinDate	-	-
FinDate	-	-
float	-	-
float	-	-
float	-	ONE_MILLION
bool	-	True
FinFrequencyTypes	-	QUARTERLY
FinDayCountTypes	-	ACT_360
FinCalendarTypes	-	WEEKEND
FinBusDayAdjustTypes	-	FOLLOWING
FinDateGenRuleTypes	-	BACKWARD
	FinDate FinDate float float float bool FinFrequencyTypes FinDayCountTypes FinCalendarTypes FinBusDayAdjustTypes	FinDate - FinDate - float - float - float - float - float - FinFrequencyTypes - FinDayCountTypes - FinCalendarTypes - FinBusDayAdjustTypes -

# value Adjusted Black

This approach uses two adjustments to Black's option pricing model to value an option on a CDS index.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
indexCurve	-	-	-
indexRecovery	-	-	-
liborCurve	-	-	-
sigma	-	-	-

### valueAnderson

This function values a CDS index option following approach by Anderson (2006). This ensures that a no-arbitrage relationship between the consituent CDS contract and the CDS index is enforced. It models the forward spread as a log-normally distributed quantity and uses the credit triangle to compute the forward RPV01.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
issuerCurves	-	-	-
indexRecovery	-	-	-
sigma	-	-	-

### 6.6 FinCDSIndexPortfolio

### Class: FinCDSIndexPortfolio()

This class manages the calculations associated with an equally weighted portfolio of CDS contracts with the same maturity date.

### **FinCDSIndexPortfolio**

Create FinCDSIndexPortfolio object. Note that all of the inputs have a default value which reflects the CDS market standard.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	ACT_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

#### intrinsicRPV01

Calculation of the risky PV01 of the CDS porfolio by taking the average of the risky PV01s of each contract.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

# intrinsic Protection Leg PV

Calculation of intrinsic protection leg value of the CDS porfolio by taking the average sum the protection legs of each contract.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

### intrinsicSpread

Calculation of the intrinsic spread of the CDS portfolio as the one which would make the value of the protection legs equal to the value of the premium legs if all premium legs paid the same spread.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

# average Spread

Calculates the average par CDS spread of the CDS portfolio.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

### totalSpread

Calculates the total CDS spread of the CDS portfolio by summing over all of the issuers and adding the spread with no weights.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

### minSpread

Calculates the minimum par CDS spread across all of the issuers in the CDS portfolio.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

### maxSpread

Calculates the maximum par CDS spread across all of the issuers in the CDS portfolio.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
stepInDate	-	-	-
maturityDate	-	-	-
issuerCurves	-	-	-

### spreadAdjustIntrinsic

Adjust individual CDS curves to reprice CDS index prices. This approach uses an iterative scheme but is slow as it has to use a CDS curve bootstrap required when each trial spread adjustment is made

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurves	-	-	-
indexCoupons	-	-	-
indexUpfronts	-	-	-
indexMaturityDates	-	-	-
indexRecoveryRate	-	-	-
tolerance	-	-	1e-6

# hazardRateAdjustIntrinsic

Adjust individual CDS curves to reprice CDS index prices. This approach adjusts the hazard rates and so avoids the slowish CDS curve bootstrap required when a spread adjustment is made.

<b>Argument Name</b>	Type	Description	Default Value
valuationDate	-	-	-
issuerCurves	-	-	-
indexCoupons	-	-	-
indexUpfronts	-	-	-
indexMaturityDates	-	-	-
indexRecoveryRate	-	-	-
tolerance	-	-	1e-6
maxIterations	-	-	100

# 6.7 FinCDSOption

### Class: FinCDSOption()

Class to manage the pricing and risk-management of an option on a single-name CDS. This is a contract in which the option buyer pays for an option to either buy or sell protection on the underlying CDS at a fixed spread agreed today and to be exercised in the future on a specified expiry date. The option may or may not cancel if there is a credit event before option expiry. This needs to be specified.

### **FinCDSOption**

Create a FinCDSOption object with the option expiry date, the maturity date of the underlying CDS, the option strike coupon, notional, whether the option knocks out or not in the event of a credit event before expiry and the payment details of the underlying CDS.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiryDate	FinDate	-	-
maturityDate	FinDate	-	-
strikeCoupon	float	-	-
notional	float	-	ONE_MILLION
longProtection	bool	-	True
knockoutFlag	bool	-	True
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	ACT_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

#### value

Value the CDS option using Black's model with an adjustment for any Front End Protection. TODO - Should the CDS be created in the init method?

```
def value(valuationDate,
```

6.7. FINCDSOPTION 125

```
issuerCurve,
volatility):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
volatility	-	-	-

### **impliedVolatility**

Calculate the implied CDS option volatility from a price.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
issuerCurve	-	-	-
optionValue	-	-	-

### fvol

Root searching function in the calculation of the CDS implied volatility.

```
def fvol(volatility, *args):
```

Argument Name	Type	Description	<b>Default Value</b>
volatility	-	-	-
*args	-	-	-

### 6.8 FinCDSTranche

### Enumerated Type: FinLossDistributionBuilder

This enumerated type has the following values:

- RECURSION
- ADJUSTED\_BINOMIAL
- GAUSSIAN
- LHP

### Class: FinCDSTranche(object)

class FinCDSTranche(object):

#### **FinCDSTranche**

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
stepInDate	FinDate	-	-
maturityDate	FinDate	-	-
k1	float	-	-
k2	float	-	-
notional	float	-	ONE_MILLION
coupon	float	-	0.0
longProtection	bool	-	True
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	ACT_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

6.8. FINCDSTRANCHE

### valueBC

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def valueBC(valuationDate,
    issuerCurves,
    upfront,
    coupon,
    corr1,
    corr2,
    numPoints=50,
    model=FinLossDistributionBuilder.RECURSION):
```

<b>Argument Name</b>	Type	Description	Default Value
valuationDate	-	-	-
issuerCurves	-	-	-
upfront	-	-	-
coupon	-	-	-
corr1	-	-	-
corr2	-	-	-
numPoints	-	-	50
model	-	-	RECURSION

# **Chapter 7**

# financepy.products.bonds

### 7.1 Introduction

This folder contains a suite of bond-related functionality across a set of files and classes. They are as follows:

- FinAnnuity is a stream of cashflows that is generated and can be priced.
- FinBond is a basic fixed coupon bond with all of the associated duration and convexity measures. It
  also includes some common spread measures such as the asset swap spread and the option adjusted
  spread.
- FinBondCallable is a bond that has an embedded call and put option. A number of rate models pricing functions have been included to allow such bonds to be priced and risk-managed.
- FinBondFuture is a bond future that has functionality around determination of the conversion factor and calculation of the invoice price and determination of the cheapest to deliver.
- FinBondMarket is a database of country-specific bond market conventions that can be referenced. These include settlement days and accrued interest conventions.
- FinBondOption is a bond option class that includes a number of valuation models for pricing both European and American style bond options. Models for European options include a Lognormal Price, Hull-White (HW) and Black-Karasinski (BK). The HW valuation is fast as it uses Jamshidians decomposition trick. American options can also be priced using a HW and BK trinomial tree. The details are abstracted away making it easy to use.
- FinConvertibleBond enables the pricing and risk-management of convertible bonds. The model is a binomial tree implementation of Black-Scholes which allows for discrete dividends, embedded puts and calls, and a delayed start of the conversion option.
- FinFloatingNote enables the pricing and risk-management of a bond with floating rate coupons. Discount margin calculations are provided.
- FinMortgage generates the periodic cashflows for an interest-only and a repayment mortgage.

#### **Conventions**

- All interest rates are expressed as a fraction of 1. So 3
- All notionals of bond positions are given in terms of a notional amount.
- All bond prices are based on a notional of 100.0.
- The face of a derivatives position is the size of the underlying position.

#### **Bond Curves**

These modules create a family of curve types related to the term structures of interest rates. There are two basic types of curve:

- 1. Best fit yield curves fitting to bond prices which are used for interpolation. A range of curve shapes from polynomials to B-Splines is available.
- 2. Discount curves that can be used to present value a future cash flow. These differ from best fits curves in that they exactly refit the prices of bonds or CDS. The different discount curves are created by calibrating to different instruments. They also differ in terms of the term structure shapes they can have. Different shapes have different impacts in terms of locality on risk management performed using these different curves. There is often a trade-off between smoothness and locality.

#### **FinBondYieldCurve**

This module describes a curve that is fitted to bond yields calculated from bond market prices supplied by the user. The curve is not guaranteed to fit all of the bond prices exactly and a least squares approach is used. A number of fitting forms are provided which consist of

- Polynomial
- Nelson-Siegel
- Nelson-Siegal-Svensson
- Cubic B-Splines

This fitted curve cannot be used for pricing as yields assume a flat term structure. It can be used for fitting and interpolating yields off a nicely constructed yield curve interpolation curve.

#### FinCurveFitMethod

This module sets out a range of curve forms that can be fitted to the bond yields. These includes a number of parametric curves that can be used to fit yield curves. These include:

- · Polynomials of any degree
- Nelson-Siegel functional form.
- Nelson-Siegel-Svensson functional form.
- B-Splines

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#### 7.2 FinBond

### Enumerated Type: FinYieldConventions

This enumerated type has the following values:

- UK\_DMO
- US\_STREET
- US\_TREASURY

### Class: FinBond(object)

Class for fixed coupon bonds and performing related analytics. These are bullet bonds which means they have regular coupon payments of a known size that are paid on known dates plus a payment of par at maturity.

#### **FinBond**

Create FinBond object by providing Maturity Date, Frequency, coupon and the accrual convention type.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maturityDate	FinDate	-	-
coupon	float	-	-
frequencyType	FinFrequencyTypes	-	-
accrualType	FinDayCountTypes	-	-
face	float	-	100.0

#### **fullPriceFromYield**

Calculate the full price of bond from its yield to maturity. This function is vectorised with respect to the yield input.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
у у	-	-	-
convention	-	-	UK_DMO

### principal

Calculate the principal value of the bond based on the face amount from its discount margin and making assumptions about the future Libor rates.

The function arguments are described in the following table.

<b>Argument Name</b>	Type Description		<b>Default Value</b>
settlementDate	-	-	-
У	-	-	-
convention	-	-	-

#### dollarDuration

Calculate the risk or dP/dy of the bond by bumping.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
ytm	-	-	-
convention	-	-	UK_DMO

### macauleyDuration

Calculate the Macauley duration of the bond on a settlement date given its yield to maturity.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
ytm	-	-	-
convention	-	-	UK_DMO

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### modifiedDuration

Calculate the modified duration of the bondon a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
ytm	-	-	-
convention	-	-	UK_DMO

### convexityFromYield

Calculate the bond convexity from the yield to maturity. This function is vectorised with respect to the yield input.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
ytm	-	-	-
convention	-	-	UK_DMO

#### cleanPriceFromYield

Calculate the bond clean price from the yield to maturity. This function is vectorised with respect to the yield input.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
ytm	-	-	-
convention	-	-	UK_DMO

#### cleanValueFromDiscountCurve

Calculate the clean bond value using some discount curve to present-value the bond's cashflows back to the curve anchor date and not to the settlement date.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
discountCurve	-	-	-

# value Bond Using Discount Curve

Calculate the bond \*value\* using some discount curve to PV the bond's cashflows to the curve anchor date. The anchor of the discount curve should be on the valuation date and so be 0-3 days before the settlement of the bond. This is not the same as the full price which is only the correct price on the settlement date of the bond which may be in the future.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
discountCurve	-	-	-
verbose	-	-	False

#### currentYield

Calculate the current yield of the bond which is the coupon divided by the clean price (not the full price)

```
def currentYield(cleanPrice):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
cleanPrice	-	-	-

# yieldToMaturity

Calculate the bond's yield to maturity by solving the price yield relationship using a one-dimensional root solver.

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
cleanPrice	-	-	-
convention	-	-	US_TREASURY

#### calcAccruedInterest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date.

```
def calcAccruedInterest(settlementDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-

### assetSwapSpread

Calculate the par asset swap spread of the bond. The discount curve is a Libor curve that is passed in. This function is vectorised with respect to the clean price.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
cleanPrice	-	-	-
discountCurve	-	-	-
swapFloatDayCountConventionType	-	-	ACT_360
swapFloatFrequencyType	-	-	SEMI_ANNUAL
swapFloatCalendarType	-	-	WEEKEND
swapFloatBusDayAdjustRuleType	-	-	FOLLOWING
swapFloatDateGenRuleType	-	-	BACKWARD

#### **fullPriceFromOAS**

Calculate the full price of the bond from its OAS given the bond settlement date, a discount curve and the oas as a number.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
discountCurve	-	-	-
oas	-	-	-

### optionAdjustedSpread

Return OAS for bullet bond given settlement date, clean bond price and the discount relative to which the spread is to be computed.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
cleanPrice	-	-	-
discountCurve	-	-	-

### printFlows

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
def printFlows(settlementDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-

# priceFromSurvivalCurve

Calculate discounted present value of flows assuming default model. This has not been completed.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
discountCurve	-	-	-
survivalCurve	-	-	-
recoveryRate	-	-	-

# print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
def print():
```

# 7.3 FinBondAnnuity

# Class: FinBondAnnuity(object)

An annuity is a vector of dates and flows generated according to ISDA standard rules which starts on the next date after the start date (effective date) and runs up to an end date with no principal repayment. Dates are then adjusted according to a specified calendar.

### **FinBondAnnuity**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maturityDate	FinDate	-	-
coupon	float	-	-
frequencyType	FinFrequencyTypes	-	-
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD
dayCountConventionType	FinDayCountTypes	-	ACT_360
face	float	-	100.0

#### cleanPriceFromDiscountCurve

Calculate the bond price using some discount curve to present-value the bond's cashflows.

```
def cleanPriceFromDiscountCurve(settlementDate, discountCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
discountCurve	-	-	-

#### **fullPriceFromDiscountCurve**

Calculate the bond price using some discount curve to present-value the bond's cashflows.

7.3. FINBONDANNUITY

```
def fullPriceFromDiscountCurve(settlementDate, discountCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
discountCurve	-	-	-

### calculateFlowDatesPayments

PLEASE ADD A FUNCTION DESCRIPTION

```
def calculateFlowDatesPayments(settlementDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-

### printFlows

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
def printFlows(settlementDate):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-

### print

Simple print function for backward compatibility.

```
def print():
```

#### 7.4 FinBondConvertible

#### Class: FinBondConvertible(object)

Class for convertible bonds. These bonds embed rights to call and put the bond in return for equity. Until then they are bullet bonds which means they have regular coupon payments of a known size that are paid on known dates plus a payment of par at maturity. As the options are price based, the decision to convert to equity depends on the stock price, the credit quality of the issuer and the level of interest rates.

#### **FinBondConvertible**

Create FinBond object by providing Maturity Date, Frequency, coupon and the accrual convention type.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maturityDate	FinDate	bond maturity date	-
coupon	float	annual coupon	-
frequencyType	FinFrequencyTypes	coupon frequency type	-
startConvertDate	FinDate	conversion starts on this date	-
conversionRatio	float	num shares per face of notional	-
callDates	List[FinDate]	list of call dates	-
callPrices	List[float]	list of call prices	-
putDates	List[FinDate]	list of put dates	-
putPrices	List[float]	list of put prices	-
accrualType	FinDayCountTypes	day count type for accrued	-
face	float	face amount	100.0

#### value

A binomial tree valuation model for a convertible bond that captures the embedded equity option due to the existence of a conversion option which can be invoked after a specific date. The model allows the user to enter a schedule of dividend payment dates but the size of the payments must be in yield terms i.e. a known percentage of currently unknown future stock price is paid. Not a fixed amount. A fixed yield. Following this payment the stock is assumed to drop by the size of the dividend payment. The model also captures the stock dependent credit risk of the cash flows in which the bond price can default at any time with a hazard rate

implied by the credit spread and an associated recovery rate. This is the model proposed by Hull (OFODS 6th edition, page 522). The model captures both the issuer's call schedule which is assumed to apply on a list of dates provided by the user, along with a call price. It also captures the embedded owner's put schedule of prices.

The function arguments are described in the following table.

-
-
-
-
-
-
-
0.40
100

### accruedDays

Calculate number days from previous coupon date to settlement.

```
def accruedDays(settlementDate):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-

#### currentYield

Calculate the current yield of the bond which is the coupon divided by the clean price (not the full price)

```
def currentYield(cleanPrice):
```

Argument Name	Type	Description	Default Value
cleanPrice	-	-	-

# print

Simple print function for backward compatibility.

```
def print():
```

The function arguments are described in the following table.

# printTree

n1, n2 = array.shape

```
def printTree(array):
```

Argument Name	Type	Description	Default Value
array	-	-	-

### 7.5 FinBondEmbeddedOption

### Enumerated Type: FinBondModelTypes

This enumerated type has the following values:

- BLACK
- HO\_LEE
- HULL\_WHITE
- BLACK\_KARASINSKI

#### Enumerated Type: FinBondOptionTypes

This enumerated type has the following values:

- EUROPEAN\_CALL
- EUROPEAN\_PUT
- AMERICAN\_CALL
- AMERICAN\_PUT

### Class: FinBondEmbeddedOption(object)

#### FinBondEmbeddedOption

Create a FinBondEmbeddedOption object with a maturity date, coupon and all of the bond inputs.

Argument Name	Type	Description	<b>Default Value</b>
maturityDate	FinDate	FinDate	-
coupon	float	Annualised coupon - $0.03 = 3.00\%$	-
frequencyType	FinFrequencyTypes	-	-
accrualType	FinDayCountTypes	-	-
callDates	List[FinDate]	-	-
callPrices	List[float]	-	-
putDates	List[FinDate]	-	-
putPrices	List[float]	-	-
face	float	-	100.0

### value

Value the bond that settles on the specified date that can have both embedded call and put options. This is done using the specified model and a discount curve.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
discountCurve	-	-	-
model	-	-	-

### print

print(self)

```
def print():
```

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#### 7.6 FinBondFRN

### Class: FinBondFRN(object)

Class for managing floating rate notes that pay a floating index plus a quoted margin.

#### **FinBondFRN**

Create FinFloatingRateNote object given its maturity date, its quoted margin, coupon frequency, accrual type. Face is the size of the position and par is the notional on which price is quoted.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maturityDate	FinDate	-	-
quotedMargin	float	-	-
frequencyType	FinFrequencyTypes	-	-
accrualType	FinDayCountTypes	-	-
face	float	-	100.0

# fullPriceFromDiscountMargin

Calculate the full price of the bond from its discount margin and making assumptions about the future Libor rates.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

### principal

Calculate the clean trade price of the bond based on the face amount from its discount margin and making assumptions about the future Libor rates.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

#### dollarRateDuration

Calculate the risk or dP/dy of the bond by bumping.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

#### dollarCreditDuration

Calculate the risk or dP/dy of the bond by bumping.

7.6. FINBONDFRN

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

# macauleyRateDuration

Calculate the Macauley duration of the FRN on a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

#### modifiedRateDuration

Calculate the modified duration of the bondon a settlement date given its yield to maturity.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

### modifiedCreditDuration

Calculate the modified duration of the bondon a settlement date given its yield to maturity.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

### convexity From Discount Margin

Calculate the bond convexity from the discount margin using a numerical bump of size 1 basis point and taking second differences.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

# clean Price From Discount Margin

Calculate the bond clean price from the yield.

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The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
dm	-	-	-

#### **fullPriceFromDiscountCurve**

Calculate the bond price using some discount curve to present-value the bond's cashflows. THIS IS NOT COMPLETE.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
indexCurve	-	-	-
discountCurve	-	-	-

# discount Margin

Calculate the bond's yield to maturity by solving the price yield relationship using a one-dimensional root solver.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
resetLibor	-	-	-
currentLibor	-	-	-
futureLibor	-	-	-
cleanPrice	-	-	-

#### calcAccruedInterest

Calculate the amount of coupon that has accrued between the previous coupon date and the settlement date.

```
def calcAccruedInterest(settlementDate, resetLibor):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-
resetLibor	-	-	-

### printFlows

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
def printFlows(settlementDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	-	-	-

### print

Simple print function for backward compatibility.

```
def print():
```

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### 7.7 FinBondFuture

#### Class: FinBondFuture(object)

Class for managing futures contracts on government bonds that follows CME conventions and related analytics.

#### **FinBondFuture**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
tickerName	str	-	-
firstDeliveryDate	FinDate	-	-
lastDeliveryDate	FinDate	-	-
contractSize	int	-	-
coupon	float	-	-

#### conversionFactor

Determine the conversion factor for a specific bond using CME convention. To do this we need to know the contract standard coupon and must round the bond maturity (starting its life on the first delivery date) to the nearest 3 month multiple and then calculate the bond clean price.

```
def conversionFactor(bond):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
bond	-	-	-

# principalInvoicePrice

Argument Name	Type	Description	<b>Default Value</b>
bond	-	-	-
futuresPrice	-	-	-

#### totalInvoiceAmount

'The total invoice amount paid to take delivery of bond.'

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	-	-	-
bond	-	-	-
futuresPrice	-	-	-

### cheapestToDeliver

Determination of CTD as deliverable bond with lowest cost to buy versus what is received when the bond is delivered.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
bonds	-	-	-
bondCleanPrices	-	-	-
futuresPrice	-	-	-

### deliveryGainLoss

Determination of what is received when the bond is delivered.

Argument Name	Type	Description	Default Value
bond	-	-	-
bondCleanPrice	-	-	-
futuresPrice	-	-	-

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# print

Simple print function for backward compatibility.

def print():

#### 7.8 FinBondMarket

### Enumerated Type: FinBondMarkets

This enumerated type has the following values:

- AUSTRIA
- BELGIUM
- CYPRUS
- ESTONIA
- FINLAND
- FRANCE
- GERMANY
- GREECE
- IRELAND
- ITALY
- LATVIA
- LITHUANIA
- LUXEMBOURG
- MALTA
- NETHERLANDS
- PORTUGAL
- SLOVAKIA
- SLOVENIA
- SPAIN
- ESM
- EFSF
- BULGARIA
- CROATIA
- CZECH\_REPUBLIC
- DENMARK
- HUNGARY
- POLAND
- ROMANIA
- SWEDEN
- JAPAN
- SWITZERLAND
- UNITED\_KINGDOM
- UNITED\_STATES

### ${\bf get Treasury Bond Market Conventions}$

Returns the day count convention for accrued interest, the frequency and the number of days from trade date to settlement date. This is for Treasury markets. And for secondary bond markets.

def getTreasuryBondMarketConventions(country):

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Argument Name	Type	Description	Default Value
country	-	-	-

### 7.9 FinBondMortgage

### Enumerated Type: FinBondMortgageTypes

This enumerated type has the following values:

- REPAYMENT
- INTEREST\_ONLY

### Class: FinBondMortgage(object)

A mortgage is a vector of dates and flows generated in order to repay a fixed amount given a known interest rate. Payments are all the same amount but with a varying mixture of interest and repayment of principal.

### **FinBondMortgage**

Create the mortgage using start and end dates and principal.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
startDate	FinDate	-	-
endDate	FinDate	-	-
principal	float	-	-
frequencyType	FinFrequencyTypes	-	MONTHLY
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD
dayCountConventionType	FinDayCountTypes	-	ACT_360

# repaymentAmount

Determine monthly repayment amount based on current zero rate.

```
def repaymentAmount(zeroRate):
```

<b>Argument Name</b>	Type	Description	Default Value
zeroRate	-	-	-

### generateFlows

Generate the bond flow amounts.

```
def generateFlows(zeroRate, mortgageType):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
zeroRate	-	-	-
mortgageType	-	-	-

### printLeg

print("START DATE:", self.\_startDate)

```
def printLeg():
```

The function arguments are described in the following table.

# print

Simple print function for backward compatibility.

```
def print():
```

# 7.10 FinBondOption

#### Enumerated Type: FinBondModelTypes

This enumerated type has the following values:

- BLACK
- HO\_LEE
- HULL\_WHITE
- BLACK\_KARASINSKI

#### Enumerated Type: FinBondOptionTypes

This enumerated type has the following values:

- EUROPEAN\_CALL
- EUROPEAN\_PUT
- AMERICAN\_CALL
- AMERICAN\_PUT

#### Class: FinBondOption()

#### **FinBondOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
bond	FinBond	-	-
expiryDate	FinDate	-	-
strikePrice	float	-	-
face	float	-	-
optionType	FinBondOptionTypes	-	-

#### value

Value a bond option (option on a bond) using the specified model which include Hull-White Tree, Black-Karasinski Tree.

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The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
discountCurve	-	-	-
model	-	-	-

# print

Simple print function for backward compatibility.

```
def print():
```

#### 7.11 FinBondYieldCurve

### Class: FinBondYieldCurve()

Class to do fitting of the yield curve and to enable interpolation of yields. Because yields assume a flat term structure for each bond, this class does not allow discounting to be done and so does not inherit from FinDiscountCurve. It should only be used for visualisation and simple interpolation but not for full term-structure-consistent pricing.

#### **FinBondYieldCurve**

Fit the curve to a set of bond yields using the type of curve specified. Bounds can be provided if you wish to enforce lower and upper limits on the respective model parameters.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	FinDate	-	-
bonds	-	-	-
ylds	-	-	-
curveFit	-	-	-

### interpolated Yield

PLEASE ADD A FUNCTION DESCRIPTION

```
def interpolatedYield(maturityDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
maturityDate	-	-	-

#### plot

Display yield curve.

```
def plot(title):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
title	-	-	-

# print

Simple print function for backward compatibility.

def print():

#### 7.12 FinBondYieldCurveModel

Class: FinCurveFitMethod()

class FinCurveFitMethod():

Class: FinCurveFitPolynomial()

class FinCurveFitPolynomial():

### **FinCurveFitPolynomial**

self.\_parentType = FinCurveFitMethod

```
def FinCurveFitPolynomial(power=3):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
power	-	-	3

### print

Simple print function for backward compatibility.

```
def print():
```

The function arguments are described in the following table.

# Class: FinCurveFitNelsonSiegel()

class FinCurveFitNelsonSiegel():

### FinCurveFitNelsonSiegel

Fairly permissive bounds. Only tau1 is 1-100

```
def FinCurveFitNelsonSiegel(tau=None, bounds=[(-1, -1, -1, 0.5), (1, 1, 1, 100)]):
```

Argument Name	Type	Description	Default Value
tau	-	-	None
bounds	-	-	[(-1, -1, -1, 0.5), (1, 1, 1, 100)]

#### print

Simple print function for backward compatibility.

```
def print():
```

The function arguments are described in the following table.

#### Class: FinCurveFitNelsonSiegelSvensson()

class FinCurveFitNelsonSiegelSvensson():

#### FinCurveFitNelsonSiegelSvensson

Create object to store calibration and functional form of NSS parametric fit.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value	
tau1	-	-	None	
tau2	-	-	None	
bounds	-	-	[(0, -1, -1, -1, 0, 1), (1, 1, 1, 1, 10, 100)]	

#### print

Simple print function for backward compatibility.

```
def print():
```

The function arguments are described in the following table.

### Class: FinCurveFitBSpline()

class FinCurveFitBSpline():

### **FinCurveFitBSpline**

self.\_parentType = FinCurveFitMethod

```
def FinCurveFitBSpline(power=3, knots=[1, 3, 5, 10]):
```

Argument Name	Type	Description	<b>Default Value</b>
power	-	-	3
knots	-	-	[1, 3, 5, 10]

# print

Simple print function for backward compatibility.

```
def print():
```

#### 7.13 FinBondZeroCurve

### Class: FinBondZeroCurve(FinDiscountCurve)

#### **FinBondZeroCurve**

Fit a discount curve to a set of bond yields using the type of curve specified.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
bonds	-	-	-
cleanPrices	-	-	-
interpMethod	-	-	FLAT_FORWARDS

#### zeroRate

Calculate the zero rate to maturity date.

```
def zeroRate(dt, frequencyType=FinFrequencyTypes.CONTINUOUS):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
dt	-	-	-
frequencyType	-	-	CONTINUOUS

#### df

t = inputTime(dt, self)

```
def df(dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-

#### **survProb**

t = inputTime(dt, self)

```
def survProb(dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
dt	-	-	-

#### fwd

Calculate the continuous forward rate at the forward date.

```
def fwd(dt):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
dt	-	-	-

#### **fwdRate**

Calculate the forward rate according to the specified day count convention.

```
def fwdRate(date1, date2, dayCountType):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
date1	-	-	-
date2	-	-	-
dayCountType	-	-	-

#### plot

Display yield curve.

```
def plot(title):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
title	-	-	-

#### print

Simple print function for backward compatibility.

def print():

# **Chapter 8**

# financepy.products.libor

#### 8.1 Introduction

#### **Libor Products**

This folder contains a set of Libor-related products. More recently with the demise of Libor these are known as Ibor products. It includes:

#### FinInterestRateFuture

This is a class to handle interest rate futures contracts. This is an exchange-traded contract to receive or pay Libor on a specified future date. It can be used to build the Liboir term structure.

#### **FinLiborCapFloor**

This is a contract to buy a sequence of calls or puts on Libor over a period at a strike agreed today.

### **FinLiborDeposit**

This is the basic Libor instrument in which a party borrows an amount for a specified term and rate unsecured.

#### **FinLiborFRA**

This is a class to manage Forward Rate Agreements (FRAs) in which one party agrees to lock in a forward Libor rate.

### FinLiborSwap

This is a contract to exchange fixed rate coupons for floating Libor rates. This class has functionality to value the swap contract and to calculate its risk.

### **FinLiborSwaption**

This is a contract to buy or sell an option to enter into a swap to either pay or receive a fixed swap rate at a specific future expiry date. The model includes code that prices a payer or receiver swaption with the

following models: - Black's Model - Shifted Black Model - SABR - Shifted SABR - Hull-White Tree Model - Black-Karasinski Tree Model - Black-Derman-Toy Tree Model

#### FinLiborBermudanSwaption

This is a contract to buy or sell an option to enter into a swap to either pay or receive a fixed swap rate at a specific future expiry date on specific coupon dates starting on a designated expiry date. The model includes code that prices a payer or receiver swaption with the following models: - Hull-White Tree Model - Black-Karasinski Tree Model - Black-Derman-Toy Tree Model

It is also possible to price this using a Libor Market Model. However for the moment this must be done directly via the Monte-Carlo implementation of the LMM found in FinModelRatesLMM.

#### **FinOIS**

This is a contract to exchange the daily compounded Overnight index swap rate for a fixed rate agreed at contract initiation.

#### **FinLiborCurve**

This is a discount curve that is extracted by bootstrapping a set of Libor deposits, Libor FRAs and Libor swap prices. The internal representation of the curve are discount factors on each of the deposit, FRA and swap maturity dates. Between these dates, discount factors are interpolated according to a specified scheme - see below.

### 8.2 FinLiborBermudanSwaption

### Class: FinLiborBermudanSwaption(object)

This is the class for the Bermudan-style swaption, an option to enter into a swap (payer or receiver of the fixed coupon), that starts in the future and with a fixed maturity, at a swap rate fixed today. This swaption can be exercised on any of the fixed coupon payment dates after the first exercise date.

#### **FinLiborBermudanSwaption**

Create a Bermudan swaption contract. This is an option to enter into a payer or receiver swap at a fixed coupon on all of the fixed # leg coupon dates until the exercise date inclusive.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
settlementDate	FinDate	-	-
exerciseDate	FinDate	-	-
maturityDate	FinDate	-	-
swaptionType	FinLiborSwaptionTypes	-	-
exerciseType	FinOptionExerciseTypes	-	-
fixedCoupon	float	-	-
fixedFrequencyType	FinFrequencyTypes	-	-
fixedDayCountType	FinDayCountTypes	-	-
notional	-	-	ONE_MILLION
floatFrequencyType	-	-	QUARTERLY
floatDayCountType	-	-	THIRTY_360
calendarType	-	-	WEEKEND
busDayAdjustType	-	-	FOLLOWING
dateGenRuleType	-	-	BACKWARD

#### value

Value the Bermudan swaption using the specified model and a discount curve.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
discountCurve	-	-	-
model	-	-	-

# print

print(self)

```
def print():
```

# 8.3 FinLiborCallableSwap

### 8.4 FinLiborCapFloor

#### Enumerated Type: FinLiborCapFloorTypes

This enumerated type has the following values:

- CAP
- FLOOR

#### Enumerated Type: FinLiborCapFloorModelTypes

This enumerated type has the following values:

- BLACK
- SHIFTED\_BLACK
- SABR

#### Class: FinLiborCapFloor()

Class for Caps and Floors. These are contracts which observe a Libor reset L on a future start date and then make a payoff at the end of the Libor period which is Max[L-K,0] for a cap and Max[K-L,0] for a floor. This is then day count adjusted for the Libor period and then scaled by the contract notional to produce a valuation. A number of models can be selected from.

# Fin Libor Cap Floor

Initialise FinLiborCapFloor object.

Argument Name	Type	Description	Default Value
startDate	FinDate	-	-
maturityDateOrTenor	FinDate or str	-	-
optionType	FinLiborCapFloorTypes	-	-
strikeRate	float	-	-
lastFixing	Optional[float]	-	None
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	THIRTY_E_360_ISDA
notional	float	-	ONE_MILLION
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

#### value

Value the cap or floor using the chosen model which specifies the volatility of the Libor rate to the cap start date.

```
def value(valuationDate, liborCurve, model):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
liborCurve	-	-	-
model	-	-	-

# value Caplet Floor Let

Value the caplet or floorlet using a specific model.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
capletStartDate	-	-	-
capletEndDate	-	-	-
liborCurve	-	-	-
model	-	-	-

# printLeg

Prints the cap floor payment amounts.

```
def printLeg():
```

The function arguments are described in the following table.

# print

print(self)

```
def print():
```

# 8.5 FinLiborConventions

# Class: FinLiborConventions()

class FinLiborConventions():

# **FinLiborConventions**

PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
currencyName	str	-	-
indexName	str	-	"LIBOR"

### 8.6 FinLiborCurve

## Class: FinLiborCurve(FinDiscountCurve)

Constructs a discount curve as implied by the prices of Libor deposits, FRAs and IRS. The curve date is the date on which we are performing the valuation based on the information available on the curve date. Typically it is the date on which an amount of 1 paidhasa present value of 1.

This class inherits from FinDiscountCurve so has all of the methods that class has.

### **FinLiborCurve**

Create an instance of a FinLibor curve given a valuation date and a set of libor deposits, libor FRAs and liborSwaps. Some of these may be left None and the algorithm will just use what is provided. An interpolation method has also to be provided.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
name	str	-	-
valuationDate	FinDate	-	-
liborDeposits	list	-	-
liborFRAs	list	-	-
liborSwaps	list	-	-
interpMethod	FinInterpMethods	-	FLAT_FORWARDS

### print

Simple print function for backward compatibility.

```
def print():
```

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# 8.7 FinLiborDeposit

## Class: FinLiborDeposit(object)

A Libor deposit is an agreement to borrow money interbank at the Libor fixing rate starting on the settlement date and repaid on the maturity date with the interest amount calculated according to a day count convention and dates calculated according to a calendar and business day adjustment rule.

## **FinLiborDeposit**

Create a Libor deposit object which takes the settlement date when the amount of notional is borrowed, the deposit rate, the day count convention used to calculate the interest paid and a calendar and a business day adjustment method if dates fall on holidays.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
settlementDate	FinDate	-	-
maturityDateOrTenor	FinDate or str	-	-
depositRate	float	-	-
dayCountType	FinDayCountTypes	-	-
notional	float	-	100.0
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	MODIFIED_FOLLOWING

## maturityDf

Returns the maturity date discount factor that would allow the Libor curve to reprice the contractual market deposit rate. Note that this is a forward discount factor that starts on settlement date.

```
def maturityDf():
```

The function arguments are described in the following table.

#### value

Determine the value of an existing Libor Deposit contract given a valuation date and a Libor curve. This is simply the PV of the future repayment plus interest discounted on the current Libor curve.

```
def value(valuationDate, liborCurve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
liborCurve	-	-	-

# printFlows

Print the date and size of the future repayment.

```
def printFlows(valuationDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-

## print

print(self)

```
def print():
```

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### 8.8 FinLiborFRA

### Class: FinLiborFRA(object)

Class for managing LIBOR forward rate agreements. A forward rate agreement is an agreement to exchange a fixed pre-agreed rate for a floating rate linked to LIBOR that is not known until some specified future fixing date. The FRA payment occurs on or soon after this date on the FRA settlement date. Typically the timing gap is two days.

A FRA is used to hedge a Libor quality loan or lend of some agreed notional amount. This period starts on the settlement date of the FRA and ends on the maturity date of the FRA. For example a 1x4 FRA relates to a Libor starting in 1 month for a loan period ending in 4 months. Hence it links to 3-month Libor rate. The amount received by a payer of fixed rate at settlement is:

```
acc(1,2) * (Libor(1,2) - FRA RATE) / (1 + acc(0,1) \times Libor(0,1))
So the value at time 0 is acc(1,2) * (FWD Libor(1,2) - FRA RATE) \times df(0,2)
```

If the base date of the curve is before the value date then we forward adjust this amount to that value date. For simplicity I have assumed that the fixing date and the settlement date are the same date. This should be amended later.

#### **FinLiborFRA**

Create a Forward Rate Agreeement object.

Argument Name	Type	Description	Default Value
startDate	FinDate	The date the FRA starts to accrue	-
maturityDateOrTenor	FinDate or str	End of the Libor rate period	-
fraRate	float	The fixed contractual FRA rate	-
dayCountType	FinDayCountTypes	For interest period	-
notional	float	-	100.0
payFixedRate	bool	True if the FRA rate is being paid	True
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	MODIFIED_FOLLOWING

### value

Determine mark to market value of a FRA contract based on the market FRA rate. The same curve is used for calculating the forward Libor and for doing discounting on the expected forward payment.

```
def value(valuationDate, liborCurve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
liborCurve	-	-	-

# maturityDf

Determine the maturity date discount factor needed to refit the FRA given the libor curve and the contract FRA rate.

```
def maturityDf(liborCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
liborCurve	-	-	-

# printFlows

Determine the value of the Deposit given a Libor curve.

```
def printFlows(valuationDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-

### print

print(self)

```
def print():
```

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### 8.9 FinLiborFuture

### Class: FinLiborFuture(object)

### **FinLiborFuture**

Create an interest rate futures contract which has the same conventions as those traded on the CME. The current date, the tenor of the future, the number of the future and the accrual convention and the contract size should be provided.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
todayDate	FinDate	-	-
futureNumber	int	The number of the future after todayDate	-
futureTenor	str	'1M', '2M', '3M'	"3M"
accrualType	FinDayCountTypes	-	ACT_360
contractSize	float	-	ONE_MILLION

### toFRA

Convert the futures contract to a FinLiborFRA object so it can be used to boostrap a Libor curve. For this we need to adjust the futures rate using the convexity correction.

```
def toFRA(futuresPrice, convexity):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
futuresPrice	-	-	-
convexity	-	-	-

### **futuresRate**

Calculate implied futures rate from the futures price.

```
def futuresRate(futuresPrice):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
futuresPrice	-	-	-

### **FRARate**

Convert futures price and convexity to a FRA rate using the BBG negative convexity (in percent). This is then divided by 100 before being added to the futures rate.

```
def FRARate(futuresPrice, convexity):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
futuresPrice	-	-	-
convexity	-	-	-

## convexity

Calculation of the convexity adjustment between FRAs and interest rate futures using the Hull-White model as described in technical note in link below: http://www-2.rotman.utoronto.ca/ hull/TechnicalNotes/TechnicalNote1.pdf NOTE THIS DOES NOT APPEAR TO AGREE WITH BLOOMBERG!! INVESTIGATE.

```
def convexity(valuationDate, volatility, meanReversion):
```

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
volatility	-	-	-
meanReversion	-	-	-

### 8.10 FinLiborLMMProducts

## Class: FinLiborLMMProducts()

### **FinLiborLMMProducts**

Create a European-style swaption by defining the exercise date of the swaption, and all of the details of the underlying interest rate swap including the fixed coupon and the details of the fixed and the floating leg payment schedules.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
settlementDate	FinDate	_	-
maturityDate	FinDate	-	-
floatFrequencyType	FinFrequencyTypes	-	QUARTERLY
floatDayCountType	FinDayCountTypes	-	THIRTY_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

#### simulate1F

Run the one-factor simulation of the evolution of the forward Libors to generate and store all of the Libor forward rate paths.

Argument Name	Type	Description	<b>Default Value</b>
discountCurve	-	-	-
volCurve	FinLiborCapVolCurve	-	-
numPaths	int	-	1000
numeraireIndex	int	-	0
useSobol	bool	-	True
seed	int	-	42

### **simulateMF**

Run the simulation to generate and store all of the Libor forward rate paths. This is a multi-factorial version so the user must input a numpy array consisting of a column for each factor and the number of rows must equal the number of grid times on the underlying simulation grid. CHECK THIS.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
discountCurve	-	-	-
numFactors	int	-	-
lambdas	np.ndarray	-	-
numPaths	int	-	10000
numeraireIndex	int	-	0
useSobol	bool	-	True
seed	int	-	42

### simulateNF

Run the simulation to generate and store all of the Libor forward rate paths using a full factor reduction of the fwd-fwd correlation matrix using Cholesky decomposition.

Argument Name	Type	Description	<b>Default Value</b>
discountCurve	-	-	-
volCurve	FinLiborCapVolCurve	-	-
correlationMatrix	np.ndarray	-	-
modelType	FinRateModelLMMModelTypes	-	-
numPaths	int	-	1000
numeraireIndex	int	-	0
useSobol	bool	-	True
seed	int	-	42

## valueSwaption

Value a swaption in the LMM model using simulated paths of the forward curve. This relies on pricing the fixed leg of the swap and assuming that the floating leg will be worth par. As a result we only need simulate Libors with the frequency of the fixed leg.

Argument Name	Type	Description	Default Value
settlementDate	FinDate	-	-
exerciseDate	FinDate	-	-
maturityDate	FinDate	-	-
swaptionType	FinLiborSwaptionTypes	-	-
fixedCoupon	float	-	-
fixedFrequencyType	FinFrequencyTypes	-	-
fixedDayCountType	FinDayCountTypes	-	-
notional	float	-	ONE_MILLION
floatFrequencyType	FinFrequencyTypes	-	QUARTERLY
floatDayCountType	FinDayCountTypes	-	THIRTY_360
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

# valueCapFloor

Value a cap or floor in the LMM.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
settlementDate	FinDate	-	-
maturityDate	FinDate	-	-
capFloorType	FinLiborCapFloorTypes	-	-
capFloorRate	float	-	-
frequencyType	FinFrequencyTypes	-	QUARTERLY
dayCountType	FinDayCountTypes	-	ACT_360
notional	float	-	ONE_MILLION
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

## print

Alternative print method.

```
def print():
```

8.11. FINLIBORSWAP

# 8.11 FinLiborSwap

## Class: FinLiborSwap(object)

## **FinLiborSwap**

Create an interest rate swap contract giving the contract start date, its maturity, fixed coupon, fixed leg frequency, fixed leg day count convention and notional. The floating leg parameters have default values that can be overwritten if needed.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
startDate	FinDate	This is typically T+2 on a new swap	-
maturityDateOrTenor	FinDate or str	-	-
fixedCoupon	float	-	-
fixedFreqType	FinFrequencyTypes	-	-
fixedDayCountType	FinDayCountTypes	-	-
notional	float	-	100.0
floatSpread	float	-	0.0
floatFreqType	FinFrequencyTypes	-	QUARTERLY
floatDayCountType	FinDayCountTypes	-	THIRTY_360
payFixedFlag	bool	-	True
calendarType	FinCalendarTypes	-	WEEKEND
busDayAdjustType	FinBusDayAdjustTypes	-	FOLLOWING
dateGenRuleType	FinDateGenRuleTypes	-	BACKWARD

### value

Value the interest rate swap on a value date given a single Libor discount curve.

```
principal=0.0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
discountCurve	-	-	-
indexCurve	-	-	-
firstFixingRate	-	-	None
principal	-	-	0.0

### **fixedDates**

return a vector of the fixed leg payment dates

```
def fixedDates():
```

The function arguments are described in the following table.

### **floatDates**

return a vector of the fixed leg payment dates

```
def floatDates():
```

The function arguments are described in the following table.

# pv01

Calculate the value of 1 basis point coupon on the fixed leg.

```
def pv01(valuationDate, discountCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
valuationDate	-	-	-
discountCurve	-	-	-

# parCoupon

Calculate the fixed leg coupon that makes the swap worth zero. If the valuation date is before the swap payments start then this is the forward swap rate as it starts in the future. The swap rate is then a forward swap rate and so we use a forward discount factor. If the swap fixed leg has begun then we have a spot starting swap.

8.11. FINLIBORSWAP

```
def parCoupon(valuationDate, discountCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
discountCurve	-	-	-

### fixedLegValue

The swap may have started in the past but we can only value payments that have occurred after the valuation date.

```
def fixedLegValue(valuationDate, discountCurve, principal=0.0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
discountCurve	-	-	-
principal	-	-	0.0

### cashSettledPV01

Calculate the forward value of an annuity of a forward starting swap using a single flat discount rate equal to the swap rate. This is used in the pricing of a cash-settled swaption in the FinLiborSwaption class. This method does not affect the standard valuation methods.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
flatSwapRate	-	-	-
frequencyType	-	-	-

# floatLegValue

Value the floating leg with payments from an index curve and discounting based on a supplied discount curve.

```
firstFixingRate=None,
principal=0.0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	IS THIS THE SETTLEMENT DATE ????	-
discountCurve	-	-	-
indexCurve	-	-	-
firstFixingRate	-	-	None
principal	-	-	0.0

# printFixedLeg

Prints the fixed leg amounts.

```
def printFixedLeg():
```

The function arguments are described in the following table.

# printFloatLeg

Prints the floating leg amounts.

```
def printFloatLeg():
```

The function arguments are described in the following table.

## print

Print a list of the unadjusted coupon payment dates used in analytic calculations for the bond.

```
def print():
```

# 8.12 FinLiborSwaption

## Class: FinLiborSwaption()

This is the class for the European-style swaption, an option to enter into a swap (payer or receiver of the fixed coupon), that starts in the future and with a fixed maturity, at a swap rate fixed today.

## **FinLiborSwaption**

Create a European-style swaption by defining the exercise date of the swaption, and all of the details of the underlying interest rate swap including the fixed coupon and the details of the fixed and the floating leg payment schedules. Bermudan style swaption should be priced using the FinLiborBermudanSwaption class.

Type	Description	Default Value
FinDate	-	-
FinDate	-	-
FinDate	-	-
FinLiborSwaptionTypes	-	-
float	-	-
FinFrequencyTypes	-	-
FinDayCountTypes	-	-
float	-	ONE_MILLION
FinFrequencyTypes	-	QUARTERLY
FinDayCountTypes	-	THIRTY_360
FinCalendarTypes	-	WEEKEND
FinBusDayAdjustTypes	-	FOLLOWING
FinDateGenRuleTypes	-	BACKWARD
	FinDate FinDate FinDate FinDate FinLiborSwaptionTypes float FinFrequencyTypes FinDayCountTypes float FinFrequencyTypes FinFrequencyTypes FinCalendarTypes FinBusDayAdjustTypes	FinDate  FinDate  FinDate  FinDate  FinLiborSwaptionTypes  float  FinFrequencyTypes  FinDayCountTypes  float  FinFrequencyTypes  FinDayCountTypes  FinDayCountTypes

### value

Valuation of a Libor European-style swaption using a choice of models on a specified valuation date. Models include FinModelBlack, FinModelBlackShifted,

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
discountCurve	-	-	-
model	-	-	-

### cashSettledValue

Valuation of a Libor European-style swaption using a cash settled approach which is a market convention that used Black's model and that discounts all of the future payments at a flat swap rate. Note that the Black volatility for this valuation should in general not equal the Black volatility for the standard arbitrage-free valuation.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	FinDate	-	-
discountCurve	-	-	-
swapRate	float	-	-
model	-	-	-

# printSwapFixedLeg

PLEASE ADD A FUNCTION DESCRIPTION

```
def printSwapFixedLeg():
```

The function arguments are described in the following table.

# printSwapFloatLeg

PLEASE ADD A FUNCTION DESCRIPTION

def printSwapFloatLeg():

The function arguments are described in the following table.

# print

Alternative print method.

def print():

### 8.13 FinOIS

### Class: FinOIS(object)

Class for managing overnight index swaps. This is a swap contract in which a fixed payment leg is exchanged for a floating coupon leg. There is no exchange of par.

The contract lasts from a start date to a specified maturity date. The fixed coupon is the OIS fixed rate which is set at contract initiation.

The floating rate is not known until the end of each payment period. It is calculated at the end of the period as it is based on daily observations of the overnight index rate which are compounded according to a specific convention. Hence the OIS floating rate is determined by the history of the OIS rates.

In its simplest form, there is just one fixed rate payment and one floating rate payment at contract maturity. However when the contract becomes longer than one year the floating and fixed payments become periodic.

The value of the contract is the NPV of the two coupon streams. Discounting is done on a supplied OIS curve which is itself implied by the term structure of market OIS rates.

### **FinOIS**

Create OIS object.

Type	Description	Default Value
FinDate	-	-
FinDate	-	-
float	-	-
FinFrequencyTypes	-	-
FinDayCountTypes	-	-
FinFrequencyTypes	-	ANNUAL
FinDayCountTypes	-	ACT_360
bool	-	True
float	-	ONE_MILLION
FinCalendarTypes	-	WEEKEND
FinBusDayAdjustTypes	-	FOLLOWING
FinDateGenRuleTypes	-	BACKWARD
	FinDate FinDate float FinFrequencyTypes FinDayCountTypes FinFrequencyTypes FinDayCountTypes bool float FinCalendarTypes FinBusDayAdjustTypes	FinDate  FinDate  FinDate  float  FinFrequencyTypes  FinDayCountTypes  FinFrequencyTypes  FinDayCountTypes  -  FinCalendarTypes  -  FinBusDayAdjustTypes

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# generatePaymentDates

PLEASE ADD A FUNCTION DESCRIPTION

```
def generatePaymentDates(valueDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-

# generate Fixed Leg Flows

PLEASE ADD A FUNCTION DESCRIPTION

```
def generateFixedLegFlows(valueDate):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-

# generateFloatLegFlows

Generate the payment amounts on floating leg implied by index curve

```
def generateFloatLegFlows(valueDate, indexCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
indexCurve	-	-	-

### rate

Calculate the OIS rate implied rate from the history of fixings.

```
def rate(oisDates, oisFixings):
```

Argument Name	Type	Description	<b>Default Value</b>
oisDates	-	-	-
oisFixings	-	-	-

### value

Value the interest rate swap on a value date given a single Libor discount curve.

```
def value(valueDate, discountCurve):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
discountCurve	-	-	-

# fixed Leg Value

PLEASE ADD A FUNCTION DESCRIPTION

```
def fixedLegValue(valueDate, discountCurve, principal=0.0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
discountCurve	-	-	-
principal	-	-	0.0

## floatLegValue

Value the floating leg with payments from an index curve and discounting based on a supplied discount curve.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
discountCurve	-	-	-
indexCurve	-	-	-
principal	-	-	0.0

### df

Calculate the OIS rate implied discount factor.

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The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
oisRate	-	-	-
startDate	-	-	-
endDate	-	-	-

# printFlows

Print the dates and cash flows on the OIS.

```
def printFlows(valueDate, indexCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
valueDate	-	-	-
indexCurve	-	-	-

## print

print(self)

```
def print():
```

# **Chapter 9**

# financepy.products.fx

## 9.1 Introduction

## **FX Derivatives**

### **Overview**

These modules price and produce the sensitivity measures needed to hedge a range of FX Options and other derivatives with an FX underlying.

### **FX Forwards**

Calculate the price and breakeven forward FX Rate of an FX Forward contract.

## FX Vanilla Option

## **FX** Option

This is a class from which other classes inherit and is used to perform simple perturbatory calculation of option Greeks.

**FX Barrier Options** 

FX Basket Options

FX Digital Options

FX Fixed Lookback Option

FX Float Lookback Option

**FX Rainbow Option** 

FX Variance Swap

# 9.2 FinFXBarrierOption

## Enumerated Type: FinFXBarrierTypes

This enumerated type has the following values:

- DOWN\_AND\_OUT\_CALL
- DOWN\_AND\_IN\_CALL
- UP\_AND\_OUT\_CALL
- UP\_AND\_IN\_CALL
- UP\_AND\_OUT\_PUT
- UP\_AND\_IN\_PUT
- DOWN\_AND\_OUT\_PUT
- DOWN\_AND\_IN\_PUT

## Class: FinFXBarrierOption(FinFXOption)

class FinFXBarrierOption(FinFXOption):

## **FinFXBarrierOption**

Create FX Barrier option product. This is an option that cancels if the FX rate crosses a barrier during the life of the option.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
strikeFXRate	float	ONE UNIT OF FOREIGN IN DOMESTIC CCY	-
currencyPair	str	FORDOM	-
optionType	FinFXBarrierTypes	-	-
barrierLevel	float	-	-
numObservationsPerYear	int	-	-
notional	float	-	-
notionalCurrency	str	-	-

### value

Value FX Barrier Option using Black-Scholes model with closed-form analytical models.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	-	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

# valueMC

Value the FX Barrier Option using Monte Carlo.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
spotFXRate	-	-	-
domInterestRate	-	-	-
processType	-	-	-
modelParams	-	-	-
numAnnSteps	-	-	552
numPaths	-	-	5000
seed	-	-	4242

# 9.3 FinFXBasketOption

### Class: FinFXBasketOption(FinFXOption)

Class to manage FX Basket Option which is an option on a portfolio of FX rates.

## **FinFXBasketOption**

Create FX Basket Option with expiry date, strike price, option type, number of assets and notional.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
strikePrice	float	-	-
optionType	FinOptionTypes	-	-
numAssets	int	-	-
notional	float	-	1.0

### validate

Check that there is an input for each asset in the basket.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
stockPrices	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

#### value

Value an FX Basket Option using Black-Scholes closed-form model which takes into account mean and variance of underlying.

```
discountCurve,
  dividendYields,
  volatilities,
  betas):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

## valueMC

Value the FX Basket Option using Monte Carlo.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrices	-	-	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
volatilities	-	-	-
betas	-	-	-
numPaths	-	-	10000
seed	-	-	4242

# 9.4 FinFXDigitalOption

Class: FinFXDigitalOption()

class FinFXDigitalOption():

### **FinFXDigitalOption**

Create the FX Digital Option object. Inputs include expiry date, strike, currency pair, option type (call or put), notional and the currency of the notional. And adjustment for spot days is enabled. All currency rates must be entered in the price in domestic currency of one unit of foreign. And the currency pair should be in the form FORDOM where FOR is the foreign currency pair currency code and DOM is the same for the domestic currency.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiryDate	FinDate	-	-
strikePrice	float	ONE UNIT OF FOREIGN IN DOMESTIC CC	-
currencyPair	str	FORDOM	-
optionType	FinOptionTypes	-	-
notional	float	-	-
premCurrency	str	-	-

### value

Valuation of a digital option using Black-Scholes model. This allows for 4 cases - first upper barriers that when crossed pay out cash (calls) and lower barriers than when crossed from above cause a cash payout (puts) PLUS the fact that the cash payment can be in domestic or foreign currency.

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Argument Name	Type	Description	Default Value
valueDate	-	-	-
spotFXRate	-	ONE UNIT OF FOREIGN IN DOMESTIC CCY	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

# 9.5 FinFXFixedLookbackOption

## Enumerated Type: FinFXFixedLookbackOptionTypes

This enumerated type has the following values:

- FIXED\_CALL
- FIXED\_PUT

## Class: FinFXFixedLookbackOption()

## FinFXFixedLookbackOption

Create option with expiry date, option type and the option strike

The function arguments are described in the following table.

Argument Name	Туре	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
optionType	FinFXFixedLookbackOptionTypes	-	-
optionStrike	float	-	-

### value

Value FX Fixed Lookback Option using Black Scholes model and analytical formulae.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	_	-
domesticCurve	-	-	-
foreignCurve	-	-	-
volatility	-	-	-
stockMinMax	-	-	-

### valueMC

Value FX Fixed Lookback option using Monte Carlo.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
spotFXRate	-	FORDOM	-
domesticCurve	-	-	-
foreignCurve	-	-	-
volatility	-	-	-
spotFXRateMinMax	-	-	-
numPaths	-	-	10000
numStepsPerYear	-	-	252
seed	-	-	4242

# 9.6 FinFXFloatLookbackOption

## Enumerated Type: FinFloatLookbackOptionTypes

This enumerated type has the following values:

- FLOATING\_CALL
- FLOATING\_PUT

## Class: FinFloatLookbackOption(FinEquityOption)

 $class\ Fin Float Look back Option (Fin Equity Option):$ 

## FinFloatLookbackOption

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
optionType	FinFloatLookbackOptionTypes	-	-

### value

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
stockMinMax	-	-	-

# valueMC

### PLEASE ADD A FUNCTION DESCRIPTION

```
def valueMC(valueDate,
    stockPrice,
    discountCurve,
    dividendYield,
    volatility,
    stockMinMax,
    numPaths=10000,
    numStepsPerYear=252,
    seed=4242):
```

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
volatility	-	-	-
stockMinMax	-	-	-
numPaths	-	-	10000
numStepsPerYear	-	-	252
seed	-	-	4242

### 9.7 FinFXForward

Class: FinFXForward()

#### **FinFXForward**

Creates a FinFXForward which allows the owner to buy the FOR against the DOM currency at the strike-FXRate and to pay it in the notional currency.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
expiryDate	FinDate	-	-
strikeFXRate	float	PRICE OF 1 UNIT OF FOREIGN IN DOM CCY	-
currencyPair	str	FORDOM	-
notional	float	-	-
notionalCurrency	str	must be FOR or DOM	-
spotDays	int	-	0

#### value

Calculate the value of an FX forward contract where the current FX rate is the spotFXRate.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	PRICE OF ONE UNIT OF FOREIGN IN DOMESTIC CCY	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-

#### forward

Calculate the FX Forward rate that makes the value of the FX contract equal to zero.

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Argument Name	Type	Description	Default Value
valueDate	-	-	-
spotFXRate	-	PRICE OF ONE UNIT OF FOREIGN IN DOMESTIC CCY	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-

### 9.8 FinFXMktConventions

### Enumerated Type: FinFXATMMethod

This enumerated type has the following values:

- SPOT
- FWD
- FWD\_DELTA\_NEUTRAL
- FWD\_DELTA\_NEUTRAL\_PREM\_ADJ

### Enumerated Type: FinFXDeltaMethod

This enumerated type has the following values:

- SPOT\_DELTA
- FORWARD\_DELTA
- SPOT\_DELTA\_PREM\_ADJ
- FORWARD\_DELTA\_PREM\_ADJ

### Class: FinFXRate()

class FinFXRate():

#### **FinFXRate**

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
ccy1	-	-	-
ccy2	-	-	-
rate	-	-	-

## 9.9 FinFXModelTypes

Class: FinFXModel(object)

class FinFXModel(object):

#### **FinFXModel**

pass

```
def FinFXModel():
```

The function arguments are described in the following table.

Class: FinFXModelBlackScholes(FinFXModel)

#### **FinFXModelBlackScholes**

Create Black Scholes FX model object which holds volatility.

```
def FinFXModelBlackScholes(volatility):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-

Class: FinFXModelHeston(FinFXModel)

#### **FinFXModelHeston**

Create Heston FX Model which takes in volatility and mean reversion.

```
def FinFXModelHeston(volatility, meanReversion):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
meanReversion	-	-	-

Class: FinFXModelSABR(FinFXModel)

#### **FinFXModelSABR**

Create FX Model SABR which takes alpha, beta, rho, nu and volatility as parameters.

def FinFXModelSABR(alpha, beta, rho, nu, volatility):

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-
volatility	-	-	-

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### 9.10 FinFXOption

Class: FinFXOption(object)

#### delta

Calculate the option delta (FX rate sensitivity) by adding on a small bump and calculating the change in the option price.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### gamma

Calculate the option gamma (delta sensitivity) by adding on a small bump and calculating the change in the option delta.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### vega

Calculate the option vega (volatility sensitivity) by adding on a small bump and calculating the change in the option price.

```
def vega(valueDate, stockPrice, discountCurve, dividendYield, model):
```

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### theta

Calculate the option theta (calendar time sensitivity) by moving forward one day and calculating the change in the option price.

```
def theta(valueDate, stockPrice, discountCurve, dividendYield, model):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

#### rho

Calculate the option rho (interest rate sensitivity) by perturbing the discount curve and revaluing.

```
def rho(valueDate, stockPrice, discountCurve, dividendYield, model):
```

<b>Argument Name</b>	Type	Description	Default Value
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
model	-	-	-

### 9.11 FinFXRainbowOption

### Enumerated Type: FinFXRainbowOptionTypes

This enumerated type has the following values:

- CALL\_ON\_MAXIMUM
- PUT\_ON\_MAXIMUM
- CALL\_ON\_MINIMUM
- PUT\_ON\_MINIMUM
- CALL\_ON\_NTH
- PUT\_ON\_NTH

### Class: FinRainbowOption(FinEquityOption)

class FinRainbowOption(FinEquityOption):

### **FinRainbowOption**

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Туре	Description	Default Value
expiryDate	FinDate	-	-
payoffType	FinFXRainbowOptionTypes	-	-
payoffParams	List[float]	-	-
numAssets	int	-	-

#### validate

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
stockPrices	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

# validate Payoff

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def validatePayoff(payoffType, payoffParams, numAssets):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
payoffType	-	-	-
payoffParams	-	-	-
numAssets	-	-	-

#### value

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
valueDate	-	-	-
expiryDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-

#### valueMC

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
expiryDate	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-
numPaths	-	-	10000
seed	-	-	4242

# payoffValue

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def payoffValue(s, payoffTypeValue, payoffParams):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
S	-	-	-
payoffTypeValue	-	-	-
payoffParams	-	-	-

### valueMCFast

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
t	-	-	-
stockPrices	-	-	-
discountCurve	-	-	-
dividendYields	-	-	-
volatilities	-	-	-
betas	-	-	-
numAssets	-	-	-
payoffType	-	-	-
payoffParams	-	-	-
numPaths	-	-	10000
seed	-	-	4242

### 9.12 FinFXVanillaOption

### Class: FinFXVanillaOption()

This is a class for an FX Option trade. It permits the user to calculate the price of an FX Option trade which can be expressed in a number of ways depending on the investor or hedgers currency. It aslo allows the calculation of the options delta in a number of forms as well as the various Greek risk sensitivies.

### **FinFXVanillaOption**

Create the FX Vanilla Option object. Inputs include expiry date, strike, currency pair, option type (call or put), notional and the currency of the notional. And adjustment for spot days is enabled. All currency rates must be entered in the price in domestic currency of one unit of foreign. And the currency pair should be in the form FORDOM where FOR is the foreign currency pair currency code and DOM is the same for the domestic currency.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
expiryDate	FinDate	-	-
strikeFXRate	float	ONE UNIT OF FOREIGN IN DOMESTIC CCY	-
currencyPair	str	FORDOM	-
optionType	FinOptionTypes	-	-
notional	float	-	-
premCurrency	str	-	-
spotDays	int	-	0

#### value

This function calculates the value of the option using a specified model with the resulting value being in domestic i.e. ccy2 terms. Recall that Domestic = CCY2 and Foreign = CCY1 and FX rate is in price in domestic of one unit of foreign currency.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
spotFXRate	-	ONE UNIT OF FOREIGN IN DOMESTIC CCY	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

### delta\_bump

Calculation of the FX option delta by bumping the spot FX rate by 1 cent of its value. This gives the FX spot delta. For speed we prefer to use the analytical calculation of the derivative given below.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	-	-
ccy1DiscountCurve	-	-	-
ccy2DiscountCurve	-	-	-
model	-	-	-

### delta

Calculation of the FX Option delta. There are several definitions of delta and so we are required to return a dictionary of values. The definitions can be found on Page 44 of Foreign Exchange Option Pricing by Iain Clark, published by Wiley Finance.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	-	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

#### gamma

This function calculates the FX Option Gamma using the spot delta.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valueDate	-	-	-
spotFXRate	-	value of a unit of foreign in domestic currency	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

#### vega

This function calculates the FX Option Vega using the spot delta.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	value of a unit of foreign in domestic currency	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

#### theta

This function calculates the time decay of the FX option.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	value of a unit of foreign in domestic currency	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-

### **impliedVolatility**

This function determines the implied volatility of an FX option given a price and the other option details. It uses a one-dimensional Newton root search algorith to determine the implied volatility.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
stockPrice	-	-	-
discountCurve	-	-	-
dividendYield	-	-	-
price	-	-	-

### valueMC

Calculate the value of an FX Option using Monte Carlo methods. This function can be used to validate the risk measures calculated above or used as the starting code for a model exotic FX product that cannot be priced analytically. This function uses Numpy vectorisation for speed of execution.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
spotFXRate	-	-	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
model	-	-	-
numPaths	-	-	10000
seed	-	-	4242

f

```
def f(volatility, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
volatility	-	-	-
*args	-	-	-

# fvega

```
def fvega(volatility, *args):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
*args	-	-	-

g

```
def g(K, *args):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
*args	-	-	-

# solve For Strike

This function determines the implied strike of an FX option given a delta and the other option details. It uses a one-dimensional Newton root search algorith to determine the strike that matches an input volatility.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
vanillaOption	-	-	-
spotFXRate	-	-	-
domDiscountCurve	-	-	-
forDiscountCurve	-	-	-
delta	-	-	-
deltaType	-	-	-
volatility	-	-	-

### 9.13 FinFXVarianceSwap

### Class: FinFXVarianceSwap(object)

### **FinFXVarianceSwap**

Create variance swap contract.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
startDate	FinDate	-	-
maturityDateOrTenor	[FinDate,str]	-	-
strikeVariance	float	-	-
notional	float	-	ONE_MILLION
payStrikeFlag	bool	-	True

#### value

Calculate the value of the variance swap based on the realised volatility to the valuation date, the forward looking implied volatility to the maturity date using the libor discount curve.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
valuationDate	-	-	-
realisedVar	-	-	-
fairStrikeVar	-	-	-
liborCurve	-	-	-

### fairStrikeApprox

This is an approximation of the fair strike variance by Demeterfi et al. (1999) which assumes that sigma(K) = sigma(F) - b(K-F)/F where F is the forward stock price and sigma(F) is the ATM forward vol.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
fwdStockPrice	-	-	-
strikes	-	-	-
volatilities	-	-	-

#### fairStrike

Calculate the implied variance according to the volatility surface using a static replication methodology with a specially weighted portfolio of put and call options across a range of strikes using the approximate method set out by Demeterfi et al. 1999.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valuationDate	-	-	-
stockPrice	-	-	-
dividendYield	-	-	-
volatilityCurve	-	-	-
numCallOptions	-	-	-
numPutOptions	-	-	-
strikeSpacing	-	-	-
discountCurve	-	-	-
useForward	-	-	True

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def f(x): return (2.0/tmat)*((x-sstar)/sstar-log(x/sstar))
```

Argument Name	Type	Description	<b>Default Value</b>
x return (2.0/tmat)*((x-sstar)/sstar-log(x/sstar))	-	-	-

### realised Variance

Calculate the realised variance according to market standard calculations which can either use log or percentage returns.

```
def realisedVariance(closePrices, useLogs=True):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
closePrices	-	-	-
useLogs	-	-	True

# print

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def print():
```

# Chapter 10

# financepy.models

#### 10.1 Introduction

#### **Models**

#### **Overview**

This folder contains a range of models used in the various derivative pricing models implemented in the product folder. These include credit models for valuing portfolio credit products such as CDS Tranches, Monte-Carlo based models of stochastics processes used to value equity, FX and interest rate derivatives, and some generic implementations of models such as a tree-based Hull White model. Because the models are useful across a range of products, it is better to factor them out of the product/asset class categorisation as it avoids any unnecessary duplication.

In addition we seek to make the interface to these models rely only on fast types such as floats and integers and Numpy arrays.

These modules hold all of the models used by FinancePy across asset classes.

The general philosophy is to separate where possible product and models so that these models have as little product knowledge as possible.

Also, Numba is used extensively, resulting in code speedups of between x 10 and x 100.

# **Generic Arbitrage-Free Models**

There are the following arbitrage-free models:

- FinModelBlack is Black's model for pricing forward starting contracts (in the forward measure) assuming the forward is lognormally distributed.
- FinModelBlackShifted is Black's model for pricing forward starting contracts (in the forward measure) assuming the forward plus a shift is lognormally distributed. CHECK
- FinModelBachelier prices options assuming the underlying evolves according to a Gaussian (normal) process.
- FinSABR Model is a stochastic volatility model for forward values with a closed form approximate solution for the implied volatility. It is widely used for pricing European style interest rate options, specifically caps and floors and also swaptions.

• FinSABRShifted Model is a stochastic volatility model for forward value with a closed form approximate solution for the implied volatility. It is widely used for pricing European style interest rate options, specifically caps and floors and also swaptions.

The following asset-specific models have been implemented:

### **Equity Models**

- FinHestonModel
- FinHestonModelProcess
- FinProcessSimulator

#### **Interest Rate Models**

### Equilibrium Rate Models

There are two main short rate models.

- FinCIRRateModel is a short rate model where the randomness component is proportional to the square root of the short rate. This model implementation is not arbitrage-free across the term structure.
- FinVasicekRateModel is a short rate model that assumes mean-reversion and normal volatility. It has a closed form solution for bond prices. It does not have the flexibility to fit a term structure of interest rates. For that you need to use the more flexible Hull-White model.

### Arbitrage Free Rate Models

- FinBlackKaraskinskiRateModel is a short rate model in which the log of the short rate follows a meanreverting normal process. It refits the interest rate term structure. It is implemented as a trinomial tree and allows valuation of European and American-style rate-based options.
- FinHullWhiteRateModel is a short rate model in which the short rate follows a mean-reverting normal process. It fits the interest rate term structure. It is implemented as a trinomial tree and allows valuation of European and American-style rate-based options. It also implements Jamshidian's decomposition of the bond option for European options.

### **Credit Models**

- FinGaussianCopula1FModel is a Gaussian copula one-factor model. This class includes functions that calculate the portfolio loss distribution. This is numerical but deterministic.
- FinGaussianCopulaLHPModel is a Gaussian copula one-factor model in the limit that the number of credits tends to infinity. This is an asymptotic analytical solution.
- FinGaussianCopulaModel is a Gaussian copula model which is multifactor model. It has a Monte-Carlo implementation.
- FinLossDbnBuilder calculates the loss distribution.

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• FinMertonCreditModel is a model of the firm as proposed by Merton (1974).

# **FX Models**

### 10.2 FinGBMProcess

### Class: FinGBMProcess()

class FinGBMProcess():

### getPaths

paths = getPaths(numPaths, numTimeSteps,

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
numPaths	-	-	-
numTimeSteps	-	-	-
t	-	-	-
mu	-	-	-
stockPrice	-	-	-
volatility	-	-	-
seed	-	-	-

# getPathsAssets

PLEASE ADD A FUNCTION DESCRIPTION

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
	Type	Type         Description           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -

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# getPaths

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numPaths	-	-	-
numTimeSteps	-	-	-
t	-	-	-
mu	-	-	-
stockPrice	-	-	-
volatility	-	-	-
seed	-	-	-

# getPathsAssets

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
numAssets	-	-	-
numPaths	-	-	-
numTimeSteps	-	-	-
t	-	-	-
mus	-	-	-
stockPrices	-	-	-
volatilities	-	-	-
betas	-	-	-
seed	-	-	-

# getAssets

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
numAssets	-	-	-
numPaths	-	-	-
t	-	-	-
mus	-	-	-
stockPrices	-	-	-
volatilities	-	-	-
betas	-	-	-
seed	-	-	-

# 10.3 FinMertonCreditModel

### mertonCreditModelValues

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
assetValue	-	-	-
bondFace	-	-	-
timeToMaturity	-	-	-
riskFreeRate	-	-	-
assetGrowthRate	-	-	-
volatility	-	-	-

### 10.4 FinModelBachelier

### Class: FinModelBachelier()

Bacheliers Model which prices call and put options in the forward measure assuming the underlying rate follows a normal process.

#### **FinModelBachelier**

Create FinModel black using parameters.

```
def FinModelBachelier(volatility):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
volatility	-	-	-

#### value

Price a derivative using Bachelier's model which values in the forward measure following a change of measure.

Argument Name	Type	Description	<b>Default Value</b>
forwardRate	-	Forward rate F	-
strikeRate	-	Strike Rate K	-
timeToExpiry	-	Time to Expiry (years)	-
df	-	Discount Factor to expiry date	-
callOrPut	-	Call or put	-

### 10.5 FinModelBlack

### Class: FinModelBlack()

Blacks Model which prices call and put options in the forward measure according to the Black-Scholes equation.

#### **FinModelBlack**

Create FinModel black using parameters.

```
def FinModelBlack(volatility, implementation=0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
volatility	-	-	-
implementation	-	-	0

#### value

Price a derivative using Black's model which values in the forward measure following a change of measure.

Argument Name	Type	Description	<b>Default Value</b>
forwardRate	-	Forward rate F	-
strikeRate	-	Strike Rate K	-
timeToExpiry	-	Time to Expiry (years)	-
df	-	Discount Factor to expiry date	-
callOrPut	-	Call or put	-

### 10.6 FinModelBlackShifted

### Class: FinModelBlackShifted()

Blacks Model which prices call and put options in the forward measure according to the Black-Scholes equation. This model also allows the distribution to be shifted to the negative in order to allow for negative interest rates.

#### **FinModelBlackShifted**

Create FinModel black using parameters.

```
def FinModelBlackShifted(volatility, shift, implementation=0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
volatility	-	-	-
shift	-	-	-
implementation	-	-	0

#### value

Price a derivative using Black's model which values in the forward measure following a change of measure.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
forwardRate	-	Forward rate	-
strikeRate	-	Strike Rate	-
timeToExpiry	-	time to expiry in years	-
df	-	Discount Factor to expiry date	-
callOrPut	-	Call or put	-

### 10.7 FinModelCRRTree

#### crrTreeVal

Value an American option using a Binomial Treee

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
stockPrice	-	-	-
ccInterestRate	-	continuously compounded	-
ccDividendRate	-	continuously compounded	-
volatility	-	Black scholes volatility	-
numStepsPerYear	-	-	-
timeToExpiry	-	-	-
optionType	-	-	-
strikePrice	-	-	-
isEven	-	-	-

### crrTreeValAvg

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
stockPrice	-	-	-
ccInterestRate	-	continuously compounded	-
ccDividendRate	-	continuously compounded	-
volatility	-	Black scholes volatility	-
numStepsPerYear	-	-	-
timeToExpiry	-	-	-
optionType	-	-	-
strikePrice	-	-	-

# 10.8 FinModelGaussianCopula

### defaultTimesGC

Generate a matrix of default times by credit and trial using a Gaussian copula model using a full rank correlation matrix.

Argument Name	Type	Description	<b>Default Value</b>
issuerCurves	-	-	-
correlationMatrix	-	-	-
numTrials	-	-	-
seed	-	-	-

### 10.9 FinModelGaussianCopula1F

#### lossDbnRecursionGCD

Full construction of the loss distribution of a portfolio of credits where losses have been calculate as number of units based on the GCD.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
numCredits	-	-	-
defaultProbs	-	-	-
lossUnits	-	-	-
betaVector	-	-	-
numIntegrationSteps	-	-	-

### homogeneous Basket Loss Dbn

Calculate the loss distribution of a CDS default basket where the portfolio is equally weighted and the losses in the portfolio are homo-geneous i.e. the credits have the same recovery rates.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
survivalProbabilities	-	-	-
recoveryRates	-	-	-
betaVector	-	-	-
numIntegrationSteps	-	-	-

#### **trSurvProbRecursion**

Get the tranche survival probability of a portfolio of credits in the one-factor GC model using a full recursion calculation of the loss distribution and survival probabilities to some time horizon.

```
recoveryRates,

betaVector,

numIntegrationSteps):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
k1	-	-	-
k2	-	-	-
numCredits	-	-	-
survivalProbabilities	-	-	-
recoveryRates	-	-	-
betaVector	-	-	-
numIntegrationSteps	-	-	-

### gaussApproxTrancheLoss

PLEASE ADD A FUNCTION DESCRIPTION

```
def gaussApproxTrancheLoss(k1, k2, mu, sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
mu	-	-	-
sigma	-	-	-

#### trSurvProbGaussian

Get the approximated tranche survival probability of a portfolio of credits in the one-factor GC model using a Gaussian fit of the conditional loss distribution and survival probabilities to some time horizon. Note that the losses in this fit are allowed to be negative.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
numCredits	-	-	-
survivalProbabilities	-	-	-
recoveryRates	-	-	-
betaVector	-	-	-
numIntegrationSteps	-	-	-

### lossDbnHeterogeneousAdjBinomial

Get the portfolio loss distribution using the adjusted binomial approximation to the conditional loss distribution.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
numCredits	-	-	-
defaultProbs	-	-	-
lossRatio	-	-	-
betaVector	-	-	-
numIntegrationSteps	-	-	-

# tr Surv Prob Adj Binomial

Get the approximated tranche survival probability of a portfolio of credits in the one-factor GC model using the adjusted binomial fit of the conditional loss distribution and survival probabilities to some time horizon. This approach is both fast and highly accurate.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
numCredits	-	-	-
survivalProbabilities	-	-	-
recoveryRates	-	-	-
betaVector	-	-	-
numIntegrationSteps	-	-	-

# 10.10 FinModelGaussianCopulaLHP

#### trSurvProbLHP

Get the approximated tranche survival probability of a portfolio of credits in the one-factor GC model using the large portfolio limit which assumes a homogenous portfolio with an infinite number of credits. This approach is very fast but not so as accurate as the adjusted binomial.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k1	-	-	-
k2	-	-	-
numCredits	-	-	-
survivalProbabilities	-	-	-
recoveryRates	-	-	-
beta	-	-	-

### portfolioCDF\_LHP

PLEASE ADD A FUNCTION DESCRIPTION

```
def portfolioCDF_LHP(k, numCredits, qvector, recoveryRates, beta, numPoints):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
k	-	-	-
numCredits	-	-	-
qvector	-	-	-
recoveryRates	-	-	-
beta	-	-	-
numPoints	-	-	-

# expMinLK

PLEASE ADD A FUNCTION DESCRIPTION

```
def expMinLK(k, p, r, n, beta):
```

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
p	-	-	-
r	-	-	-
n	-	-	-
beta	-	-	-

# **LHPDensity**

PLEASE ADD A FUNCTION DESCRIPTION

```
def LHPDensity(k, p, r, beta):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
k	-	-	-
p	-	-	-
r	-	-	-
beta	-	-	-

## LHP Analytical Density Base Corr

PLEASE ADD A FUNCTION DESCRIPTION

```
def LHPAnalyticalDensityBaseCorr(k, p, r, beta, dbeta_dk):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
р	-	-	-
r	-	-	-
beta	-	-	-
dbeta_dk	-	-	-

## LHPAnalyticalDensity

PLEASE ADD A FUNCTION DESCRIPTION

```
def LHPAnalyticalDensity(k, p, r, beta):
```

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
p	-	-	-
r	-	-	-
beta	-	-	-

# **ExpMinLK**

PLEASE ADD A FUNCTION DESCRIPTION

```
def ExpMinLK(k, p, r, n, beta):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k	-	-	-
p	-	-	-
r	-	-	-
n	-	-	-
beta	-	-	-

# probLGreaterThanK

c = normpdf(P)

```
def probLGreaterThanK(K, P, R, beta):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
K	-	-	-
P	-	-	-
R	-	-	-
beta	-	-	-

### 10.11 FinModelHeston

### Enumerated Type: FinHestonNumericalScheme

This enumerated type has the following values:

- EULER
- EULERLOG
- QUADEXP

### Class: FinModelHeston()

class FinModelHeston():

#### **FinModelHeston**

PLEASE ADD A FUNCTION DESCRIPTION

```
def FinModelHeston(v0, kappa, theta, sigma, rho):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
v0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
rho	-	-	-

#### value\_MC

#### PLEASE ADD A FUNCTION DESCRIPTION

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	EULERLOG
	Type	Type Description

### value\_Lewis

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
option	-	-	-
stockPrice	-	-	-
interestRate	-	-	-
dividendYield	-	-	-

### phi

 $k = k_{-}in + 0.5 * 1j$ 

```
def phi(k_in,):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k_in	-	-	-

# phi\_transform

def integrand(k): return 2.0 \* np.real(np.exp(-1j \*

```
def phi_transform(x):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
X	-	-	-

### integrand

```
k * x) * phi(k)) / (k**2 + 1.0 / 4.0)
```

```
def integrand(k): return 2.0 * np.real(np.exp(-1j * \)
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
k return 2.0 * np.real(np.exp(-1j * \	-	-	-

### value\_Lewis\_Rouah

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
option	-	-	-
stockPrice	-	-	-
interestRate	-	-	-
dividendYield	-	-	-

#### f

```
k = k_{-}in + 0.5 * 1j
```

```
def f(k_in):
```

Argument Name	Type	Description	<b>Default Value</b>
k_in	-	-	-

### value\_Weber

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
valueDate	-	-	-
option	-	-	-
stockPrice	-	-	-
interestRate	-	-	-
dividendYield	-	-	-

#### F

defintegrand(u):

```
def F(s, b):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
S	-	-	-
b	-	-	-

## integrand

beta = b - 1j \* rho \* sigma \* u

```
def integrand(u):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
u	-	-	-

### value\_Gatheral

PLEASE ADD A FUNCTION DESCRIPTION

```
stockPrice,
interestRate,
dividendYield):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
valueDate	-	-	-
option	-	-	-
stockPrice	-	-	-
interestRate	-	-	-
dividendYield	-	-	-

### F

defintegrand(u):

```
def F(j):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
j	-	-	-

# integrand

V = sigma \* sigma

```
def integrand(u):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
u	-	-	-

# getPaths

PLEASE ADD A FUNCTION DESCRIPTION

```
dt,
numPaths,
seed,
scheme):
```

Argument Name	Type	Description	Default Value
s0	-	-	-
r	-	-	-
q	-	-	-
v0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
rho	-	-	-
t	-	-	-
dt	-	-	-
numPaths	-	-	-
seed	-	-	-
scheme	-	-	-

### 10.12 FinModelLHPlus

### Class: LHPlusModel()

Large Homogenous Portfolio model with extra asset. Used for approximating full Gaussian copula.

### **LHPlusModel**

PLEASE ADD A FUNCTION DESCRIPTION

```
def LHPlusModel(P, R, H, beta, P0, R0, H0, beta0):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
P	-	-	-
R	-	-	-
Н	-	-	-
beta	-	-	-
P0	-	-	-
R0	-	-	-
Н0	-	-	-
beta0	-	-	-

### probLossGreaterThanK

Returns P(L;K) where L is the portfolio loss given by model.

```
def probLossGreaterThanK(K):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
K	-	-	-

# expMinLKIntegral

PLEASE ADD A FUNCTION DESCRIPTION

```
def expMinLKIntegral(K, dK):
```

Argument Name	Type	Description	Default Value
K	-	-	-
dK	-	-	-

## expMinLK

PLEASE ADD A FUNCTION DESCRIPTION

```
def expMinLK(K):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
K	-	-	-

# expMinLK2

PLEASE ADD A FUNCTION DESCRIPTION

```
def expMinLK2(K):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
K	-	-	-

# tranche Survival Probability

PLEASE ADD A FUNCTION DESCRIPTION

```
def trancheSurvivalProbability(k1, k2):
```

Argument Name	Type	Description	Default Value
k1	-	-	-
k2	-	-	-

### 10.13 FinModelLossDbnBuilder

### indepLossDbnHeterogeneousAdjBinomial

PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numCredits	-	-	-
condProbs	-	-	-
lossRatio	-	-	-

### portfolioGCD

PLEASE ADD A FUNCTION DESCRIPTION

```
def portfolioGCD(actualLosses):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
actualLosses	-	-	-

# indep Loss Dbn Recursion GCD

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	Default Value
numCredits	-	-	-
condDefaultProbs	-	-	-
lossUnits	-	-	-

### 10.14 FinModelRatesBDT

Class: FinModelRatesBDT()

class FinModelRatesBDT():

#### **FinModelRatesBDT**

Constructs the Black-Derman-Toy rate model in the case when the volatility is assumed to be constant. The short rate process simplifies and is given by  $d(\log(r)) = theta(t) * dt + sigma * dW$ . Although

```
def FinModelRatesBDT(sigma, numTimeSteps=100):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
sigma	-	-	-
numTimeSteps	-	-	100

#### **buildTree**

PLEASE ADD A FUNCTION DESCRIPTION

```
def buildTree(treeMat, dfTimes, dfValues):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
treeMat	-	-	-
dfTimes	-	-	-
dfValues	-	-	-

# bondOption

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
strike	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseType	-	-	-

## bermudanSwaption

Swaption that can be exercised on specific dates over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strike	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseType	-	-	-

#### callablePuttableBond\_Tree

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
couponTimes	-	-	-
couponFlows	-	-	-
callTimes	-	-	-
callPrices	-	-	-
putTimes	-	-	-
putPrices	-	-	-
face	-	-	-

# option Exercise Types To Int

PLEASE ADD A FUNCTION DESCRIPTION

```
def optionExerciseTypesToInt(optionExerciseType):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
optionExerciseType	-	-	-

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def f(x0, m, Q, rt, dfEnd, dt, sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
x0	-	-	-
m	-	-	-
Q	-	-	-
rt	-	-	-
dfEnd	-	-	-
dt	-	-	-
sigma	-	-	-

### searchRoot

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def searchRoot(x0, m, Q, rt, dfEnd, dt, sigma):
```

Argument Name	Type	Description	<b>Default Value</b>
x0	-	-	-
m	-	-	-
Q	-	-	-
rt	-	-	-
dfEnd	-	-	-
dt	-	-	-
sigma	-	-	-

# $bermudan Swaption\_Tree\_Fast$

Option to enter into a swap that can be exercised on coupon payment dates after the start of the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseType	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-
_treeTimes	-	-	-
_Q	-	-	-
_rt	-	-	-
_dt	-	-	-

# $american Bond Option\_Tree\_Fast$

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

```
_treeTimes, _Q, _rt, _dt):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseType	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-
_treeTimes	-	-	-
_Q	-	-	-
_rt	-	-	-
_dt	-	-	-

### $callable Puttable Bond\_Tree\_Fast$

Value a bond with embedded put and call options that can be exercised at any time over the specified list of put and call dates. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
couponTimes	-	-	-
couponFlows	-	-	-
callTimes	-	-	-
callPrices	-	-	-
putTimes	-	-	-
putPrices	-	-	-
face	-	-	-
_sigma	-	IS SIGMA USED ?	-
_a	-	IS SIGMA USED ?	-
_Q	-	IS SIGMA USED ?	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_treeTimes	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-

## buildTreeFast

# Unlike the BK and HK Trinomial trees, this Tree is packed into the lower

```
def buildTreeFast(sigma, treeTimes, numTimeSteps, discountFactors):
```

Argument Name	Type	Description	Default Value
sigma	-	-	-
treeTimes	-	-	-
numTimeSteps	-	-	-
discountFactors	-	-	-

### 10.15 FinModelRatesBK

### Class: FinModelRatesBK()

class FinModelRatesBK():

#### **FinModelRatesBK**

Constructs the Black Karasinski rate model. The speed of mean reversion a and volatility are passed in. The short rate process is given by  $d(\log(r)) = (theta(t) - a*log(r))*dt + sigma*dW$ 

```
def FinModelRatesBK(sigma, a, numTimeSteps=100):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
sigma	-	-	-
a	-	-	-
numTimeSteps	-	-	100

#### **buildTree**

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def buildTree(tmat, dfTimes, dfValues):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
tmat	-	-	-
dfTimes	-	-	-
dfValues	-	-	-

### bondOption

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	Default Value
texp	-	-	-
strike	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseType	-	-	-

### bermudanSwaption

Swaption that can be exercised on specific dates over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strike	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseType	-	-	-

#### callablePuttableBond\_Tree

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
couponTimes	-	-	-
couponFlows	-	-	-
callTimes	-	-	-
callPrices	-	-	-
putTimes	-	-	-
putPrices	-	-	-
face	-	-	-

# option Exercise Types To Int

PLEASE ADD A FUNCTION DESCRIPTION

```
def optionExerciseTypesToInt(optionExerciseType):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
optionExerciseType	-	-	-

#### f

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def f(alpha, nm, Q, P, dX, dt, N):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value	
alpha	-	-	-	
nm	-	-	-	
Q	-	-	-	
P	-	-	-	
dX	-	-	-	
dt	-	-	-	
N	-	-	-	

# **fprime**

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def fprime(alpha, nm, Q, P, dX, dt, N):
```

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

#### searchRoot

PLEASE ADD A FUNCTION DESCRIPTION

```
def searchRoot(x0, nm, Q, P, dX, dt, N):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
x0	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

#### searchRootDeriv

PLEASE ADD A FUNCTION DESCRIPTION

```
def searchRootDeriv(x0, nm, Q, P, dX, dt, N):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
x0	-	-	-
nm	-	-	-
Q	-	-	-
P	-	-	-
dX	-	-	-
dt	-	-	-
N	-	-	-

### $bermudan Swaption\_Tree\_Fast$

Option to enter into a swap that can be exercised on coupon payment dates after the start of the exercise period. Due to multiple exercise times we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseTypeInt	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-
_treeTimes	-	-	-
_Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
rt	-	-	-
_dt	-	-	-
_a	-	-	-

# $american Bond Option\_Tree\_Fast$

Option that can be exercised at any time over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseTypeInt	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-
_treeTimes	-	-	-
Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
rt	-	-	-
_dt	-	-	-
_a	-	-	-

### callablePuttableBond\_Tree\_Fast

Value a bond with embedded put and call options that can be exercised at any time over the specified list of put and call dates. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
couponTimes	-	-	-
couponFlows	-	-	-
callTimes	-	-	-
callPrices	-	-	-
putTimes	-	-	-
putPrices	-	-	-
face	-	-	-
_sigma	-	IS SIGMA USED ?	-
_a	-	IS SIGMA USED ?	-
-Q	-	IS SIGMA USED ?	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_treeTimes	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-

## buildTreeFast

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def buildTreeFast(a, sigma, treeTimes, numTimeSteps, discountFactors):
```

Argument Name	Type	Description	Default Value
a	-	-	-
sigma	-	-	-
treeTimes	-	-	-
numTimeSteps	-	-	-
discountFactors	-	-	-

### 10.16 FinModelRatesCIR

# Enumerated Type: FinCIRNumericalScheme

This enumerated type has the following values:

- EULER
- LOGNORMAL
- MILSTEIN
- KAHLJACKEL
- EXACT

### Class: FinModelRatesCIR()

class FinModelRatesCIR():

#### **FinModelRatesCIR**

 $self.\_a = a$ 

```
def FinModelRatesCIR(a, b, sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
sigma	-	-	-

#### meanr

Mean value of a CIR process after time t

```
def meanr(r0, a, b, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
t	-	-	-

#### variancer

Variance of a CIR process after time t

```
def variancer(r0, a, b, sigma, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

#### zeroPrice

Price of a zero coupon bond in CIR model.

```
def zeroPrice(r0, a, b, sigma, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

#### draw

Draw a next rate from the CIR model in Monte Carlo.

```
def draw(rt, a, b, sigma, dt):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
rt	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
dt	-	-	-

#### ratePath\_MC

Generate a path of CIR rates using a number of numerical schemes.

```
def ratePath_MC(r0, a, b, sigma, t, dt, seed, scheme):
```

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
seed	-	-	-
scheme	-	-	-

# zeroPrice\_MC

```
def zeroPrice_MC(r0, a, b, sigma, t, dt, numPaths, seed, scheme):
```

<b>Argument Name</b>	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
numPaths	-	-	-
seed	-	-	-
scheme	-	-	-

### 10.17 FinModelRatesHL

# Class: FinModelRatesHL()

class FinModelRatesHL():

### **FinModelRatesHL**

Construct Ho-Lee model using single parameter of volatility. The dynamical equation is dr = theta(t) dt + sigma \* dW. Any no-arbitrage fitting is done within functions below.

```
def FinModelRatesHL(sigma):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
sigma	-	-	-

#### zcb

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def zcb(rt1, t1, t2, discountCurve):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
rt1	-	-	-
t1	-	-	-
t2	-	-	-
discountCurve	-	-	-

# optionOnZCB

Price an option on a zero coupon bond using analytical solution of Hull-White model. User provides bond face and option strike and expiry date and maturity date.

```
def optionOnZCB(texp, tmat, strikePrice, face, dfTimes, dfValues):
```

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-
dfTimes	-	-	-
dfValues	-	-	-

### P\_Fast

Forward discount factor as seen at some time t which may be in the future for payment at time T where Rt is the delta-period short rate seen at time t and pt is the discount factor to time t, ptd is the one period discount factor to time t+dt and pT is the discount factor from now until the payment of the 1 dollar of the discount factor.

```
def P_Fast(t, T, Rt, delta, pt, ptd, pT, _sigma):
```

Argument Name	Type	Description	<b>Default Value</b>
t	-	-	-
T	-	-	-
Rt	-	-	-
delta	-	-	-
pt	-	-	-
ptd	-	-	-
pT	-	-	-
_sigma	-	-	-

### 10.18 FinModelRatesHW

### Class: FinModelRatesHW()

class FinModelRatesHW():

#### **FinModelRatesHW**

Constructs the Hull-White rate model. The speed of mean reversion a and volatility are passed in. The short rate process is given by dr = (theta(t) - ar) \* dt + sigma \* dW. The model will switch to use Jamshidian's approach where possible unless the useJamshidian flag is set to false in which case it uses the trinomial Tree.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
sigma	-	-	-
a	-	-	-
numTimeSteps	-	-	100
useJamshidian	-	-	True

## optionOnZCB

Price an option on a zero coupon bond using analytical solution of Hull-White model. User provides bond face and option strike and expiry date and maturity date.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strike	-	-	-
face	-	-	-
dfTimes	-	-	-
dfValues	-	-	-

### europeanBondOption\_Jamshidian

Valuation of a European bond option using the Jamshidian deconstruction of the bond into a strip of zero coupon bonds with the short rate that would make the bond option be at the money forward.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
strike	-	-	-
face	-	-	-
cpnTimes	-	-	-
cpnAmounts	-	-	-
dfTimes	-	-	-
dfValues	-	-	-

### $european Bond Option\_Tree$

Price an option on a coupon-paying bond using tree to generate short rates at the expiry date and then to analytical solution of zero coupon bond in HW model to calculate the corresponding bond price. User provides bond object and option details.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
strikePrice	-	-	-
face	-	-	-
cpnTimes	-	-	-
cpnAmounts	-	-	-

# $option On Zero Coupon Bond\_Tree\\$

Price an option on a zero coupon bond using a HW trinomial tree. The discount curve was already supplied to the tree build.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-

## bermudanSwaption

Swaption that can be exercised on specific dates over the exercise period. Due to non-analytical bond price we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

Type	Description	Default Value
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
		Type         Description           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -           -         -

## $american Bond Option\_Tree$

Value an option on a bond with coupons that can have European or American exercise. Some minor issues to do with handling coupons on the option expiry date need to be solved.

Argument Name	Type	Description	Default Value
texp	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponAmounts	-	-	-
americanExercise	-	-	-

#### $callable Puttable Bond\_Tree$

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
couponTimes	-	-	-
couponAmounts	-	-	-
callTimes	-	-	-
callPrices	-	-	-
putTimes	-	-	-
putPrices	-	-	-
face	-	-	-

### df\_Tree

Discount factor as seen from now to time tmat as long as the time is on the tree grid.

```
def df_Tree(tmat):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
tmat	-	-	-

#### buildTree

Build the trinomial tree.

```
def buildTree(treeMat, dfTimes, dfValues):
```

Argument Name	Type	Description	Default Value
treeMat	-	-	-
dfTimes	-	-	-
dfValues	-	-	-

## option Exercise Types To Int

PLEASE ADD A FUNCTION DESCRIPTION

```
def optionExerciseTypesToInt(optionExerciseType):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
optionExerciseType	-	-	-

#### P\_Fast

Forward discount factor as seen at some time t which may be in the future for payment at time T where Rt is the delta-period short rate seen at time t and pt is the discount factor to time t, ptd is the one period discount factor to time t+dt and pT is the discount factor from now until the payment of the 1 dollar of the discount factor.

```
def P_Fast(t, T, Rt, delta, pt, ptd, pT, _sigma, _a):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
t	-	-	-
T	-	-	-
Rt	-	-	-
delta	-	-	-
pt	-	-	-
ptd	-	-	-
pT	-	-	-
_sigma	-	-	-
_a	-	-	-

#### buildTree Fast

Fast tree construction using Numba.

```
def buildTree_Fast(a, sigma, treeTimes, numTimeSteps, discountFactors):
```

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
a	-	-	-
sigma	-	-	-
treeTimes	-	-	-
numTimeSteps	-	-	-
discountFactors	-	-	-

# $american Bond Option\_Tree\_Fast$

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
texp	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponAmounts	-	-	-
americanExercise	-	-	-
_sigma	-	-	-
_a	-	-	-
Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_treeTimes	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-

# $bermudan Swaption\_Tree\_Fast$

Option to enter into a swap that can be exercised on coupon payment dates after the start of the exercise

period. Due to multiple exercise times we need to extend tree out to bond maturity and take into account cash flows through time.

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
texp	-	-	-
tmat	-	-	-
strikePrice	-	-	-
face	-	-	-
couponTimes	-	-	-
couponFlows	-	-	-
exerciseTypeInt	-	-	-
_dfTimes	-	-	-
_dfValues	-	-	-
_treeTimes	-	-	-
_Q	-	-	-
_pu	-	-	-
_pm	-	-	-
_pd	-	-	-
_rt	-	-	-
_dt	-	-	-
_a	-	-	-

## $callable Puttable Bond\_Tree\_Fast$

Type	Description	<b>Default Value</b>
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	IS SIGMA USED ?	-
-	IS SIGMA USED ?	-
-	IS SIGMA USED ?	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
-	-	-
	Type	

### fwdFullBondPrice

Price a coupon bearing bond on the option expiry date and return the difference from a strike price. This is used in a root search to find the future expiry time short rate that makes the bond price equal to the option strike price. It is a key step in the Jamshidian bond decomposition approach. The strike is a clean price.

```
def fwdFullBondPrice(rt, *args):
```

Argument Name	Type	Description	Default Value
rt	-	-	-
*args	-	-	-

#### 10.19 FinModelRatesLMM

### Enumerated Type: FinRateModelLMMModelTypes

This enumerated type has the following values:

- LMM\_ONE\_FACTOR
- LMM\_HW\_M\_FACTOR
- LMM\_FULL\_N\_FACTOR

#### **LMMPrintForwards**

Helper function to display the simulated Libor rates.

```
def LMMPrintForwards(fwds):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
fwds	-	-	-

## LMMSwaptionVolApprox

Implements Rebonato's approximation for the swap rate volatility to be used when pricing a swaption that expires in period a for a swap maturing at the end of period b taking into account the forward volatility term structure (zetas) and the forward-forward correlation matrix rho..

```
def LMMSwaptionVolApprox(a, b, fwd0, taus, zetas, rho):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
a	-	-	-
b	-	-	-
fwd0	-	-	-
taus	-	-	-
zetas	-	-	-
rho	-	-	-

## LMMSimSwaptionVol

Calculates the swap rate volatility using the forwards generated in the simulation to see how it compares to Rebonatto estimate.

```
def LMMSimSwaptionVol(a, b, fwd0, fwds, taus):
```

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

#### LMMFwdFwdCorrelation

Extract forward forward correlation matrix at some future time index from the simulated forward rates and return the matrix.

```
def LMMFwdFwdCorrelation(numForwards, numPaths, iTime, fwds):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numForwards	-	-	-
numPaths	-	-	-
iTime	-	-	-
fwds	-	-	-

## LMMPriceCapsBlack

Price a strip of capfloorlets using Black's model using the time grid of the LMM model. The prices can be compared with the LMM model prices.

```
def LMMPriceCapsBlack(fwd0, volCaplet, p, K, taus):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
fwd0	-	-	-
volCaplet	-	-	-
p	-	-	-
K	-	-	-
taus	-	-	-

#### **subMatrix**

Returns a submatrix of correlation matrix at later time step in the LMM simulation which is then used to generate correlated Gaussian RVs.

```
def subMatrix(t, N):
```

Argument Name	Type	Description	Default Value
t	-	-	-
N	-	-	-

### **CholeskyNP**

Numba-compliant wrapper around Numpy cholesky function.

```
def CholeskyNP(rho):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
rho	-	-	-

#### LMMSimulateFwdsNF

Full N-Factor Arbitrage-free simulation of forward Libor curves in the spot measure given an initial forward curve, volatility term structure and full rank correlation structure. Cholesky decomposition is used to extract the factor weights. The number of forwards at time 0 is given. The 3D matrix of forward rates by path, time and forward point is returned. WARNING: NEED TO CHECK THAT CORRECT VOLATILITY IS BEING USED (OFF BY ONE BUG NEEDS TO BE RULED OUT)

```
def LMMSimulateFwdsNF(numForwards, numPaths, fwd0, zetas, correl, taus, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
numForwards	-	-	-
numPaths	-	-	-
fwd0	-	-	-
zetas	-	_	-
correl	-	-	-
taus	-	-	-
seed	-	-	-

#### LMMSimulateFwds1F

One factor Arbitrage-free simulation of forward Libor curves in the spot measure following Hull Page 768. Given an initial forward curve, volatility term structure. The 3D matrix of forward rates by path, time and forward point is returned. This function is kept mainly for its simplicity and speed. NB: The Gamma volatility has an initial entry of zero. This differs from Hull's indexing by one and so is why I do not subtract 1 from the index as Hull does in his equation 32.14. The Number of Forwards is the number of points on the initial curve to the trade maturity date. For example a cap that matures in 10 years with quarterly caplets has 40 forwards.

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
numForwards	-	-	-
numPaths	-	-	-
numeraireIndex	-	-	-
fwd0	-	-	-
gammas	-	-	-
taus	-	-	-
useSobol	-	-	-
seed	-	-	-

#### LMMSimulateFwdsMF

Multi-Factor Arbitrage-free simulation of forward Libor curves in the spot measure following Hull Page 768. Given an initial forward curve, volatility factor term structure. The 3D matrix of forward rates by path, time and forward point is returned.

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
numForwards	-	-	-
numFactors	-	-	-
numPaths	-	-	-
numeraireIndex	-	-	-
fwd0	-	-	-
lambdas	-	-	-
taus	-	-	-
useSobol	-	-	-
seed	-	-	-

## LMMCapFlrPricer

Function to price a strip of cap or floorlets in accordance with the simulated forward curve dynamics.

```
def LMMCapFlrPricer(numForwards, numPaths, K, fwd0, fwds, taus, isCap):
```

Argument Name	Type	Description	<b>Default Value</b>
numForwards	-	-	-
numPaths	-	-	-
K	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-
isCap	-	-	-

## **LMMSwapPricer**

Function to reprice a basic swap using the simulated forward Libors.

```
def LMMSwapPricer(cpn, numPeriods, numPaths, fwd0, fwds, taus):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
cpn	-	-	-
numPeriods	-	-	-
numPaths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

### LMMSwaptionPricer

Function to price a European swaption using the simulated forward curves.

```
def LMMSwaptionPricer(strike, a, b, numPaths, fwd0, fwds, taus, isPayer):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
strike	-	-	-
a	-	-	-
b	-	-	-
numPaths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-
isPayer	-	-	-

# LMMR at chet Cap let Pricer

Price a ratchet using the simulated Libor rates.

def LMMRatchetCapletPricer(spread, numPeriods, numPaths, fwd0, fwds, taus):

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
spread	-	-	-
numPeriods	-	-	-
numPaths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

## LMMFlexiCapPricer

Price a flexicap using the simulated Libor rates.

```
def LMMFlexiCapPricer(maxCaplets, K, numPeriods, numPaths, fwd0, fwds, taus):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
maxCaplets	-	-	-
K	-	-	-
numPeriods	-	-	-
numPaths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

## **LMMStickyCapletPricer**

Price a sticky cap using the simulated Libor rates.

```
def LMMStickyCapletPricer(spread, numPeriods, numPaths, fwd0, fwds, taus):
```

Argument Name	Type	Description	<b>Default Value</b>
spread	-	-	-
numPeriods	-	-	-
numPaths	-	-	-
fwd0	-	-	-
fwds	-	-	-
taus	-	-	-

### 10.20 FinModelRatesVasicek

## Class: FinModelRatesVasicek()

class FinModelRatesVasicek():

### **FinModelRatesVasicek**

 $self.\_a = a$ 

```
def FinModelRatesVasicek(a, b, sigma):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
sigma	-	-	-

#### meanr

$$mr = r0 * exp(-a * t) + b * (1 - exp(-a * t))$$

```
def meanr(r0, a, b, t):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
t	-	-	-

#### variancer

$$vr = sigma * sigma * (1.0 - exp(-2.0 * a * t)) / 2.0 / a$$

```
def variancer(a, b, sigma, t):
```

Argument Name	Type	Description	Default Value
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

### zeroPrice

$$B = (1.0 - exp(-a * t)) / a$$

```
def zeroPrice(r0, a, b, sigma, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-

### ratePath\_MC

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def ratePath_MC(r0, a, b, sigma, t, dt, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
seed	-	-	-

### zeroPrice\_MC

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def zeroPrice_MC(r0, a, b, sigma, t, dt, numPaths, seed):
```

Argument Name	Type	Description	<b>Default Value</b>
r0	-	-	-
a	-	-	-
b	-	-	-
sigma	-	-	-
t	-	-	-
dt	-	-	-
numPaths	-	-	-
seed	-	-	-

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### 10.21 FinModelSABR

Class: FinModelSABR()

#### **FinModelSABR**

Create FinModelSABR with model parameters.

```
def FinModelSABR(alpha, beta, rho, nu):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	Default Value
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-

#### blackVol

Black volatility from SABR model using Hagan et al. approx.

```
def blackVol(f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	Default Value
f	-	-	-
k	-	-	-
t	-	-	-

#### value

Price an option using Black's model which values in the forward measure following a change of measure.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
forwardRate	-	Forward rate	-
strikeRate	-	Strike Rate	-
timeToExpiry	-	time to expiry in years	-
df	-	Discount Factor to expiry date	-
callOrPut	-	Call or put	-

## blackVolFromSABR

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def blackVolFromSABR(alpha, beta, rho, nu, f, k, t):
```

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

### 10.22 FinModelSABRShifted

Class: FinModelSABRShifted()

#### **FinModelSABRShifted**

 $self.\_alpha = alpha$ 

```
def FinModelSABRShifted(alpha, beta, rho, nu, shift):
```

The function arguments are described in the following table.

<b>Argument Name</b>	Type	Description	<b>Default Value</b>
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-
shift	-	-	-

#### blackVol

Black volatility from SABR model using Hagan et al. approx.

```
def blackVol(f, k, t):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
f	-	-	-
k	-	-	-
t	-	-	-

#### value

Price an option using Black's model which values in the forward measure following a change of measure.

```
def value(forwardRate,  # Forward rate F
    strikeRate,  # Strike Rate K
    timeToExpiry,  # Time to Expiry (years)
    df,  # Discount Factor to expiry date
    callOrPut):  # Call or put
```

Argument Name	Type	Description	<b>Default Value</b>
forwardRate	-	Forward rate F	-
strikeRate	-	Strike Rate K	-
timeToExpiry	-	Time to Expiry (years)	-
df	-	Discount Factor to expiry date	-
callOrPut	-	Call or put	-

# black Vol From Shifted SABR

#### PLEASE ADD A FUNCTION DESCRIPTION

```
def blackVolFromShiftedSABR(alpha, beta, rho, nu, s, f, k, t):
```

Argument Name	Type	Description	<b>Default Value</b>
alpha	-	-	-
beta	-	-	-
rho	-	-	-
nu	-	-	-
S	-	-	-
f	-	-	-
k	-	-	-
t	-	-	-

# 10.23 FinModelStudentTCopula

# Class: FinModelStudentTCopula()

class FinModelStudentTCopula():

### defaultTimes

PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	Default Value
issuerCurves	-	-	-
correlationMatrix	-	-	-
degreesOfFreedom	-	-	-
numTrials	-	-	-
seed	-	-	-

### 10.24 FinProcessSimulator

### Enumerated Type: FinProcessTypes

This enumerated type has the following values:

- GBM
- CIR
- HESTON
- VASICEK
- CEV
- JUMP\_DIFFUSION

## Enumerated Type: FinHestonNumericalScheme

This enumerated type has the following values:

- EULER
- EULERLOG
- QUADEXP

### Enumerated Type: FinGBMNumericalScheme

This enumerated type has the following values:

- NORMAL
- ANTITHETIC

### Enumerated Type: FinVasicekNumericalScheme

This enumerated type has the following values:

- NORMAL
- ANTITHETIC

## Enumerated Type: FinCIRNumericalScheme

This enumerated type has the following values:

- EULER
- LOGNORMAL
- MILSTEIN
- KAHLJACKEL
- EXACT

## Class: FinProcessSimulator()

class FinProcessSimulator():

### **FinProcessSimulator**

pass

```
def FinProcessSimulator():
```

The function arguments are described in the following table.

# getProcess

#### PLEASE ADD A FUNCTION DESCRIPTION

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
processType	-	-	-
t	-	-	-
modelParams	-	-	-
numAnnSteps	-	-	-
numPaths	-	-	-
seed	-	-	-

## getHestonPaths

#### PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
numPaths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
drift	-	-	-
s0	-	-	-
v0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
rho	-	-	-
scheme	-	-	-
seed	-	-	-

# ${\bf getGBMPaths}\\$

PLEASE ADD A FUNCTION DESCRIPTION

```
def getGBMPaths(numPaths, numAnnSteps, t, mu, stockPrice, sigma, scheme, seed):
```

The function arguments are described in the following table.

Argument Name	Type	Description	<b>Default Value</b>
numPaths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
mu	-	-	-
stockPrice	-	-	-
sigma	-	-	-
scheme	-	-	-
seed	-	-	-

# get Vasice k Paths

PLEASE ADD A FUNCTION DESCRIPTION

Argument Name	Type	Description	<b>Default Value</b>
numPaths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
r0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
scheme	-	-	-
seed	-	-	-

# getCIRPaths

#### PLEASE ADD A FUNCTION DESCRIPTION

<b>Argument Name</b>	Type	Description	Default Value
numPaths	-	-	-
numAnnSteps	-	-	-
t	-	-	-
r0	-	-	-
kappa	-	-	-
theta	-	-	-
sigma	-	-	-
scheme	-	-	-
seed	-	-	-