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Base case:  $m = \text{Obj}(w)$

Prove:  $\text{size } \text{Obj}(w) = \text{size}' \text{Obj}(w) \ 0$

$\text{size } \text{Obj}(w)$

$\vee \text{Obj}(w) \rightarrow 1$

$\Rightarrow 1$

$\text{size}' \text{Obj}(w) \ 0$

$\vee \text{Obj}(w) \rightarrow 1 + \text{acc}$

$\Rightarrow 1 + 0$

$\Rightarrow 1$

Step case: if  $\text{size } m1 = \text{size}' m1 \ 0$  and  $\text{size } m2 = \text{size}' m2 \ 0$ ,  
 $m = \text{Wire}(m1, m2)$

Theorem:  $\text{size}(m) + \text{acc}' = \text{size}' m \ \text{acc}'$

Theorem proof:

Base case:  $m = \text{Obj}(w)$

Prove:  $\text{size } \text{Obj}(w) + \text{acc}' = \text{size}' \text{Obj}(w) \ \text{acc}'$

$\text{size } \text{Obj}(w) + \text{acc}'$

$\vee [\text{Obj}(w) \rightarrow 1] + \text{acc}'$

$\Rightarrow 1 + \text{acc}'$

$\text{size}' \text{Obj}(w) \ \text{acc}'$

$\vee \text{Obj}(w) \rightarrow 1 + \text{acc}'$

$\Rightarrow 1 + \text{acc}'$

Step case: for any  $\text{acc}'$ , if  $\text{size}(m) + \text{acc}' = \text{size}' m \ \text{acc}'$  and  $m1, m2$  satisfy  $m$

Prove:  $\text{size } \text{Wire}(m1, m2) + \text{acc}' = \text{size}' \text{Wire}(m1, m2) \ \text{acc}'$

$\text{size } \text{Wire}(m1, m2) + \text{acc}'$

$\vee [\text{Wire}(m1, m2) \rightarrow \text{size } m1 + \text{size } m2 + 1] + \text{acc}'$

$\Rightarrow \text{size } m1 + \text{size } m2 + 1 + \text{acc}'$

$\text{size}' \text{Wire}(m1, m2) \ \text{acc}'$

$\vee \text{Wire}(m1, m2) \rightarrow \text{size}' m1 \ (\text{size}' m2 \ (1 + \text{acc}'))$

$\Rightarrow \text{size}' m1 \ (\text{size}' m2 \ (1 + \text{acc}'))$  [let  $\text{acc}1 = 1 + \text{acc}'$ ]

$\Rightarrow \text{size}' m1 \ (\text{size}' m2 \ (\text{acc}1))$

$\Rightarrow \text{size}' m1 \ (\text{size } m2 \ \text{acc}1)$  [let  $\text{acc}2 = \text{size } m2 \ \text{acc}1$ ]

$\Rightarrow \text{size}' m1 \ \text{acc}2$

$\Rightarrow \text{size } m1 + \text{acc}2$

$\Rightarrow \text{size } m1 + \text{size } m2 + \text{acc}1$

$\Rightarrow \text{size } m1 + \text{size } m2 + 1 + \text{acc}'$

So if  $\text{acc}' = 0$ , theorem remains satisfied, and  $\text{size}(m) = \text{size}' m \ 0$