Parsing Techniques for Contex-Free Path Querying

Semyon Grigorev

s.v.grigoriev@spbu.ru Semen.Grigorev@jetbrains.com

JetBrains Research, Programming Languages and Tools Lab Saint Petersburg University

April 05, 2019

Formal language constrained path querying

- Finite directed edge-laballed graph $\mathcal{G} = (V, E, L)$
- The path is a world over L:

$$\omega(p) = \omega(v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \dots \xrightarrow{l_{n-1}} v_n) = l_0 \cdot l_1 \cdot \dots \cdot l_{n-1}$$

• The language \mathcal{L} (over L)

Formal language constrained path querying

- Finite directed edge-laballed graph G = (V, E, L)
- The path is a world over L:

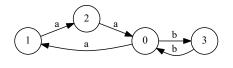
$$\omega(p) = \omega(v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \dots \xrightarrow{l_{n-1}} v_n) = l_0 \cdot l_1 \cdot \dots \cdot l_{n-1}$$

- The language \mathcal{L} (over L)
- Reachability problem: $Q = \{(v_i, v_j) \mid \exists p = v_i \dots v_j, \omega(p) \in \mathcal{L}\}$
- Path querying problem: $Q = \{p \mid \omega(p) \in \mathcal{L}\}$
 - ▶ Single path, all paths, shortest path . . .

Context-Free path querying

- ullet is a context-free language
- $G_{\mathcal{L}} = (N, \Sigma, R, S)$
- Reachability problem: $Q = \{(v_i, v_j) \mid \exists p = v_i \dots v_j, S \xrightarrow[G_i]{*} \omega(p)\}$
- Path querying problem: $Q = \{p \mid \omega(p) \in \mathcal{L}\}$

Example of CFPQ



Input graph

 $0: S \rightarrow a S b$ $1: S \rightarrow Middle$

2: $Middle \rightarrow ab$

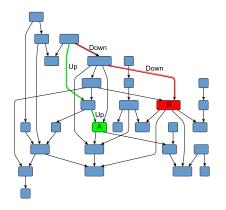
Query: language $\{a^nb^n \mid n > 0\}$

Paths: $2 \xrightarrow{a} 0 \xrightarrow{b} 3$ $1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{b} 3 \xrightarrow{b} 0$ $p_1 = 0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3$ $p_2 = 0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3 \xrightarrow{b} 0$...

Applications

- Graph data bases querying Yann ...
- Static code analysis Reps CFL reachability
- . . .

Graph data bases querying

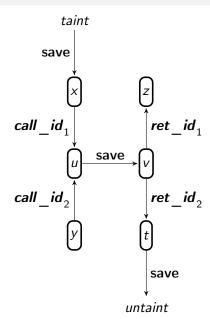


Navigation through a graph

- Are nodes A and B on the same level of hierarchy?
- Is there a path of form Upⁿ Downⁿ?
- Find all paths of form
 Upⁿ Downⁿ which start from the node A

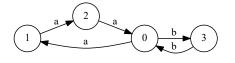
Static code analysis

```
int id(int u)
 v = u;
  return v;
int main()
 //taint
  int x;
  int z, y;
 //untaint
  int t;
  z = id(x);
  t = id(y);
```



Parsing algorithms for CFPQ

- Structural representation of results
- Number of algorithms with different properties
- Number of theoretical results



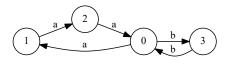
Input graph

 $0: S \rightarrow a S b$

 $1: \ S \rightarrow \textit{Middle}$

2: $Middle \rightarrow a b$

Grammar

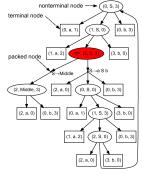


Input graph

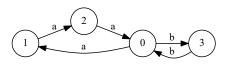
 $0: S \to a S b$

1: $S \rightarrow Middle$ 2: $Middle \rightarrow ab$

Grammar



Query result (SPPF)



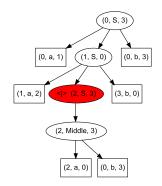
 $0: S \rightarrow a S b$ $1: S \rightarrow Middle$

2 : $Middle \rightarrow a b$ Grammar

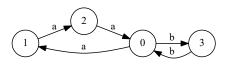
Input graph

nonterminal node -- (0, s, 3) terminal node (1, S, 0) (0, b, 3) (3, b, 0) packed node TS→aSb S→Middle (2, a, 0) (0, S, 0) (2, Middle, 3) (0, a, 1) (1, S, 3) (3, b, 0) (0, b, 3) (2, S, 0) (0, b, 3) (1, a, 2) (2, a, 0)

Query result (SPPF)



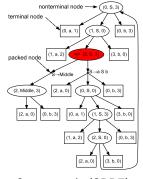
Tree for p_1



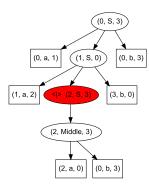
 $0: S \rightarrow a S b$ $1: S \rightarrow Middle$

2 : $Middle \rightarrow a b$ Grammar

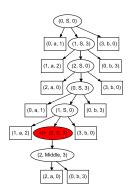
Input graph



Query result (SPPF)



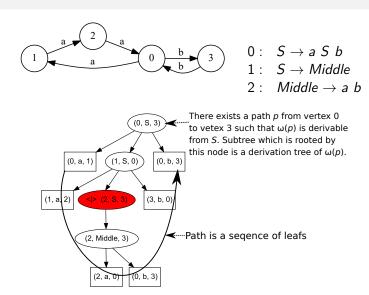
Tree for p_1



Tree for p_2

9/27

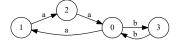
Paths extraction



Path: $0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3$

Bar-Hillel theorem

Context-free languages are closed under intersection with regular languages



Regular language

 $0: S \rightarrow a S b$

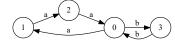
 $1: \ S \to \textit{Middle}$

 $2: \quad \textit{Middle} \rightarrow \textit{a} \; \textit{b}$

Context-free language

Bar-Hillel theorem

Context-free languages are closed under intersection with regular languages

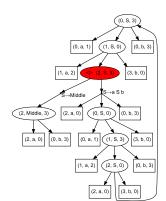


 $0: S \rightarrow a S b$ $1: S \rightarrow Middle$

1: $S \rightarrow Middle$ 2: $Middle \rightarrow ab$

Regular language

Context-free language



Bar-Hillel theorem

Context-free languages are closed under intersection with regular languages



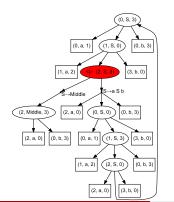
 $0: S \rightarrow a S b$

 $1: S \rightarrow \textit{Middle}$

 $2: Middle \rightarrow ab$

Regular language

Context-free language



$$(0, S, 3) \rightarrow (0, a, 1) (1, S, 0) (0, b, 3)$$

$$(1, S, 0) \rightarrow (1, a, 2) (2, S, 3) (3, b, 0)$$

$$(2, S, 3) \rightarrow (2, a, 0) (0, S, 0) (0, b, 3)$$

$$(2, S, 3) \rightarrow (2, Middle, 3)$$

$$(0, S, 0) \rightarrow (0, a, 1) (1, S, 3) (3, b, 0)$$

$$(1, S, 3) \rightarrow (1, a, 2) (2, S, 0) (0, b, 3)$$

$$(2, S, 0) \rightarrow (2, a, 0) (0, S, 3) (3, b, 0)$$

$$(0, Middle, 3) \rightarrow (2, a, 0) (0, b, 3)$$

Our experiments

- Generalized LR for CFPQ
 - Based on Right Nulled Generalized LR: Scott E., Johnstone A. "Right Nulled GLR Parsers"
 - Ekaterina Verbitskaia, Semyon Grigorev, and Dmitry Avdyukhin.
 "Relaxed Parsing of Regular Approximations of String-Embedded Languages" 2015

Our experiments

- Generalized LR for CFPQ
 - Based on Right Nulled Generalized LR: Scott E., Johnstone A. "Right Nulled GLR Parsers"
 - Ekaterina Verbitskaia, Semyon Grigorev, and Dmitry Avdyukhin.
 "Relaxed Parsing of Regular Approximations of String-Embedded Languages" 2015
- Generalized LL for CFPQ (GLL)
 - Based on Generalized LL: Scott E., Johnstone A. "GLL parsing"
 - Semyon Grigorev and Anastasiya Ragozina. "Context-free path querying with structural representation of result." 2017

Query language integration

How to integrate query language into general-purpose programming language?

- Transparency
- Compositionality
- Static error checking

Query language integration

How to integrate query language into general-purpose programming language?

- Transparency
- Compositionality
- Static error checking
- String-embedded languages
- ORMs
- Combinators

Combinators for CFPQ

- Implemented in Scala
- Based on Meerkat parser combinator library: Anastasia Izmaylova, Ali Afroozeh, and Tijs van der Storm. "Practical, general parser combinators" 2016
- Ekaterina Verbitskaia, Ilya Kirillov, Ilya Nozkin, Semyon Grigorev. "Parser Combinators for Context-Free Path Querying" 2019

Supported combinators

Combinator		Description
a ~ b)	sequential parsing: a then b
a b)	choice: a or b

Supported combinators

Combinator	Description
a ~ b	sequential parsing: a then b
a b	choice: a or b
a ?	optional parsing: a or nothing
a *	repetition of zero or more a
a +	repetition of at least one a

Supported combinators

Combinator	Description		
a ~ b	sequential parsing: a then b		
a b	choice: a or b		
a ?	optional parsing: a or nothing		
a *	repetition of zero or more a		
a +	repetition of at least one a		
a ^ f	apply f function to a if a is a token		
a ^^	capture output of a if a is a token		
a & f	apply f function to a if a is a parser		
a &&	capture output of a if a is a parser		

A set of functions for edges and vertices values handling.

```
def LV(labels: String*) =
  V(e => labels.forall(e.hasLabel))
def outLE(label:String) = outE(_.label() == label)
def inLE (label:String) = inE (_.label() == label)
```

Basic example

Is there a path from vertex 0 to vertex 3 which has form $a^n b^n$?

Example of generalization

```
def sameGen(brs) =
  reduceChoice(
    brs.map {case (lbr, rbr) =>
        lbr ~ syn(sameGen(brs).?) ~ rbr})
```

Example of generalization

```
def sameGen(brs) =
  reduceChoice(
    brs.map {case (lbr, rbr) =>
        lbr ~ syn(sameGen(brs).?) ~ rbr})

val query1 = syn(sameGen(List(("a", "b"))))

val query2 = syn(
  sameGen(List((p1, p2),("(",")"))) ~ p3)
```

Example of values handling

```
Actors who played in some film
In Cypher
  MATCH (m: Movie { title : 'Forrest Gump'})
        <-[:ACTS\ IN]-(a:Actor)
  RETURN a.name, a.birthplace;
In Meerkat
  val query =
    syn((
       (LV("Movie")::V( .title == "Forrest_Gump")) \sim
       inLE("ACTS IN") ~
      syn(LV("Actor") ^
             (e \Rightarrow (e.name, e.birthplace)))) \&\&)
  executeQuery(query, input)
```

Limitations

- Overhead for the regular constraints
- Not exactly clear how to compute arbitrary semantics for the paths
 - ▶ Paths can be lazily extracted, but in what order?
 - Is it possible to compute some semantics in case of cycles?

Boolean Matrix Multiplication for CFPQ

Transitive Closure

- Subset multiplication, $N_1, N_2 \subseteq N$
 - ▶ $N_1 \cdot N_2 = \{A \mid \exists B \in N_1, \exists C \in N_2 \text{ such that } (A \rightarrow BC) \in P\}$
- Subset addition: set-theoretic union.
- Matrix multiplication
 - ▶ Matrix of size $|V| \times |V|$
 - Subsets of N are elements
 - $ightharpoonup c_{i,j} = \bigcup_{k=1}^n a_{i,k} \cdot b_{k,j}$
- Transitive closure
 - $a^{cf} = a^{(1)} \cup a^{(2)} \cup \cdots$
 - $a^{(1)} = a$
 - $a^{(i)} = a^{(i-1)} \cup (a^{(i-1)} \times a^{(i-1)}), i > 2$

The algorithm

Algorithm Context-free recognizer for graphs

- 1: function CONTEXTFREEPATHQUERYING(D, G)
- $n \leftarrow$ the number of nodes in D 2:
- 3: $E \leftarrow$ the directed edge-relation from D
- $P \leftarrow$ the set of production rules in G 4:
- $T \leftarrow$ the matrix $n \times n$ in which each element is \emptyset 5:
- ▶ Matrix initialization for all $(i, x, j) \in E$ do 6:
- $T_{i,i} \leftarrow T_{i,i} \cup \{A \mid (A \rightarrow x) \in P\}$ 7:
- while matrix T is changing do 8:
- $T \leftarrow T \cup (T \times T)$ > Transitive closure T^{cf} calculation 9:
- 10: return T

Boolean Matrix Multiplication for CFPQ

- The matrix for nonterminal is a set of boolean matrices
- Matrices multiplication can be implemented efficiently by using modern harware and high-performance libraries

Performance comparison setup

We use graphs from the classical set of ontologies: skos, foaf, univ-bench, wine, pizza, etc.

Queries are classical variants of the same-generation query

$$\begin{array}{lll} \mathbf{S} \to subClassOf^{-1} \ \mathbf{S} \ subClassOf \\ \mathbf{S} \to type^{-1} \ \mathbf{S} \ type & \mathbf{S} \to subClassOf \\ \mathbf{S} \to subClassOf^{-1} \ subClassOf & \mathbf{B} \to subClassOf^{-1} \ \mathbf{B} \ subClassOf \\ \mathbf{S} \to type^{-1} \ type & \mathbf{B} \to subClassOf^{-1} \ subClassOf \end{array}$$

Query 1

Query 2

Performance comparison results

Nº	#V	#E	Query 1 (ms)			Query 2 (ms)	
			CYK ¹	GLL	GPGPU	GLL	GPGPU
1	144	323	1044	10	12	1	1
2	129	351	6091	19	13	1	0
3	131	397	13971	24	30	1	10
4	179	413	20981	25	15	11	9
5	337	834	82081	89	32	3	6
6	291	685	515285	255	22	66	2
7	341	711	420604	261	20	45	24
8	671	2604	3233587	697	24	29	23
9	733	2450	4075319	819	54	8	6
10	6224	11840	_	1926	82	167	38
11	5864	19600	-	6246	185	46	21
12	5368	20832	_	7014	127	393	40

¹Zhang, et al. "Context-free path queries on RDF graphs."

Performance comparison results

Graph	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
G5k-0.001	10.352	0.647	0.113	0.041	0.216	5.729
G10k-0.001	37.286	2.395	0.435	0.215	1.331	35.937
G10k-0.01	97.607	1.455	0.273	0.138	0.763	47.525
G10k-0.1	601.182	1.050	0.223	0.114	0.859	395.393
G20k-0.001	150.774	11.025	1.842	1.274	6.180	-
G40k-0.001	-	97.841	11.663	8.393	37.821	-
G80k-0.001	-	1142.959	88.366	65.886	-	-

Directions for research

- Develop parallel and distributed algorithms
- Adopt other parsing algorithms
- Utilize other classes of languages for constraints specification
- Investigate incremental queryes evaluation