

Generalized LL parsing for context-free constrained path search problem

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ABSTRACT

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1. INTRODUCTION

Graph data model and graph data bases are very popular in many different areas such as bioinformatic, semantic web, social networks etc. Extraction of paths satisfying specific constraints may be useful for graph structured data investigation and for relations between data items detection. Path querying with constraints formulated in terms of formal grammars is a specific problem named formal language constrained path problem [3] and research in this area is still actual [8].

Classical parsing techniques can be used to solve formal language constrained path problem thus we can use “graph parsing” and it may be required not only in graph data base querying but also in other different areas: formal verification, and string-embedded language processing, for example.

The most solution in DB area use such parsing algorithms as CYK or Earley. In string-embedded languages analysis (RN)GLR is used. It has better time complexity.

Complexity is $O(n^3)$ in worst case and linear for unambiguous grammars, that better than complexity of CYK and Earley which used as base in other solutions (for example [5], [16]). This fact allow to demonstrate better performance on linear subgraphs and unambiguous grammars. Also it is not necessary to transform input grammar to CNF which required for CYK which allow to avoid grammar size decreasing. It is important because real performance of parsing algorithm is sensitive to grammar size.

Graph parsing can be also used in string-embedded languages processing. Regular approximation for value set of string variable can be represented as directed graph of related finite automata. In order to check correctness or safety (sql injections)... all generated strings (all paths from start states to final states) are correct w.r.t some context-free grammar.

For example grammar of one of SQL dialects. GLR-based for string-embedded SQL checking [2, 4]. Solution based on RNGLR [11] for relaxed parsing of string-embedded languages [20] which allow to find all path between two specified vertices.

Despite of the fact that there is set of path querying solutions [16, 5, ?], query result exploration still a challenge [6]. Complex query debugging also is a problem. To solve these problems structural representation of query result can be useful, and classical parsing techniques allow to construct such representation: derivation tree contains full information about parsed sentence structure in terms of specified grammar.

In this paper, we propose graph parsing technique which allow to construct structural representation of query result with relation to grammar query or derivation of result.

So, we propose algorithm based top-down parsing algorithm. LL is more natural and so on.

2. PRELIMINARIES

In this work we are focused on parsing algorithm, and not on the data representation, and we assume that full input graph can be located in RAM memory by the optimal for our algorithm way.

Also we need to introduce some definitions.

- Context-free grammar $G = (N, \Sigma, P, S)$ where N is a set of nonterminal symbols, Σ is a set of terminal symbols, $S \in N$ is a start nonterminal, and P is a productions set.
- $\mathcal{L}(G)$ is a language specified by grammar G .
- Directed graph $M = (V, E, L)$ where V — vertices set, $L \subseteq \Sigma$ — edge labels set, $E \subseteq V \times L \times V$. We assume that there are no parallel edges with equal labels: for every $e_1 = (v_1, l_1, v_2) \in E, e_2 = (u_1, l_2, u_2) \in E$ if $v_1 = u_1$ and $v_2 = u_2$ then $l_1 \neq l_2$.
- $tag : E \rightarrow L$ is a helper function for edge's tag calculation.

$$tag(e = (v_1, l, v_2), e \in E) = l$$

- $\oplus : L^+ \times L^+ \rightarrow L^+$ is a concatenation operation.
- Path p in graph M .

$$p = (v_0, l_0, v_1), (v_1, l_1, v_2), \dots, (v_{n-1}, l_{n-1}, v_n) \\ = e_0, e_1, \dots, e_{n-1}$$

where $v_i \in V, e_i \in E, e_i = (v_i, l_i, v_{i+1}), l_i \in L, |p| = n, n \geq 1$.

- Set of paths $P = \{p : p \text{ path in } M\}$ where M is a directed graph.
- $\Omega : P \rightarrow L^+$ is a helper function for string produced by path calculation.

$$\Omega(p = e_0, e_1, \dots, e_{n-1}, p \in P) = \text{tag}(e_0) \oplus \dots \oplus \text{tag}(e_{n-1}).$$

As a result we can define that context-free language constrained path querying means that we get query as grammar G and result of this query is a set of paths

$$P = \{p | \Omega(p) \in \mathcal{L}(G)\}.$$

For some graphs and some queries P can be infinite set, and it can not be explicitly represented. In order to solve this problem, in this paper, we will construct not explicit representation of P but compact data structure which store all elements of P in finite space and allow to extract any of them. In this point our solution is slightly similar to subgraph querying proposed in article [16], but we are also construct derivation forest for result subgraph.

3. MOTIVATING EXAMPLE

In this article we are discuss context-free constrained path querying. One of well-known not regular but context-free language is an language

$$\mathcal{L} = \{A^n B^n; n \geq 1\} = \{AB; AAB B; AAABBB; \dots\}$$

. This language is a subset of balanced brackets language and in practice may be used for description many different relations: n -th generation in parent-child, any open should be closed in correct order, etc..

As a motivation of context-free constraints importance let we introduce the next example. Let we have graph $M = (\{0; 1; 2; 3\}, E, \{A; B\})$ presented in figure 1 where labels represent next relations:

each time when it opened it should be closed in future.

Suppose for each $n \geq 1$ we want to find all n -th generation friends with a common ancestor. In the other worlds, we want to find all paths p , such that $\Omega(p) \in \{AB; AAB B; AAABBB; \dots\}$ or $\Omega(p) = A^n B^n$ where $n \geq 1$. This constraint can not be specified with regular language as far as $L = \{A^n B^n; n \geq 1\}$ is not regular but context free. Required language can be specified by grammar G_1 presented in picture 2 where $N = \{s; middle\}$, $\Sigma = \{A; B\}$, and $S = s$.

Result is infinite for this query, and we can not... Also we want to know, who is common ancestor. Further we show how to solve it.

4. ALGORITHM FOR GRAPH PARSING

We propose a context-free language constrained path problem solution which allow to find all paths satisfied specified arbitrary context-free grammar and to construct implicit representation of result. Finite representation of result set with structure related to specified grammar may be useful not only for results understanding and processing but also for query debugging especially for complex queries.

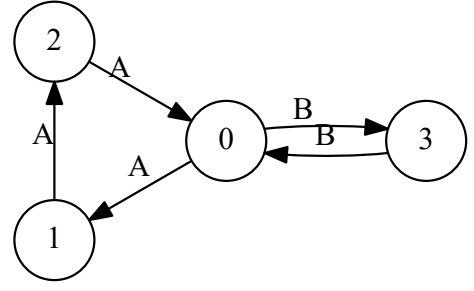


Figure 1: Input graph M

0: $s = L s R$
 1: $s = \text{middle}$
 2: $\text{middle} = L R$

Figure 2: Grammar G_1 for language $L = \{L^n R^n; n \geq 1\}$

Our solution is based on generalized LL (GLL) [12, 1] parsing algorithm which allow to process ambiguous context-free grammars.

4.1 Generalized LL Parsing Algorithm

Generalized LL (GLL) is generalized top-down parsing algorithm which handle all context-free grammars (including left recursive) with worst-case cubic time complexity and linear for LL grammars. GLL is native for grammar, can be simple created blah-blah-blah.

GLL use descriptors for parsing states specification. Each descriptor contains full specification of process state enough to start parsing from state stored.

Descriptor is a quadruple (L, s, j, a) where L is a line label, s is a stack, j is a position in the input, and a is a node of derivation tree.

allows to restore parsing

Graph structured stack (GSS) [18] for multiple stack combining to prevent duplication. In GLL each GSS node is pair of position in input and grammar slot. Grammar slot is a !!!

4.2 Shared packed parse forest

Shared Packed Parse Forest (SPPF) [10] is a special data structure for derivation forest compact representation which allow to reuse common nodes and subtrees. As a result multiple derivation trees, which can be produced in case of ambiguous grammar, can be compressed in one SPPF with optimal reusing of common parts. Binarized form of SPPF proposed in [15] and it allow to achieve worst-case cubic space complexity. GLL can use SPPF [13] for results representation achieve cubic space complexity with binarised version.

Let we present an example of SPPF for ambiguous grammar G_0 (pic 3).

0: $s = \text{NUM}$
 1: $s = \text{LBR } s \text{ RBR}$
 2: $s = s s$

Figure 3: Grammar G_0

Here N is token for number, L and R are tokens for '(' and

' respectively.

Let we parse the sentence " $()()()$ ". There are two different leftmost derivations of this sentence in grammar G_0 (\rightarrow^n denote an application of production with number n):

1. $s \xrightarrow{2} ss \xrightarrow{2} sss \xrightarrow{1} LsRss \xrightarrow{0} LNRss \xrightarrow{1} LNRLsRs \xrightarrow{1} LNRLsRs \xrightarrow{0} LNRLNRs \xrightarrow{1} LNRLNRsR \xrightarrow{0} LNRLNRsR$
2. $s \xrightarrow{2} ss \xrightarrow{1} LsRs \xrightarrow{0} LNRs \xrightarrow{2} LNRss \xrightarrow{1} LNRLsRs \xrightarrow{1} LNRLsRs \xrightarrow{0} LNRLNRs \xrightarrow{1} LNRLNRsR \xrightarrow{0} LNRLNRsR$

As far as there are two different derivations, SPPF should contain two different trees and it is presented in figure 4: result SPPF (fig. 4a) and trees for derivation 1 (fig. 4b) and derivation 2 (fig. 4c) respectively.

Binarised SPPF can be represented as a graph where each node has one of four types:

- terminal node with label (i, T, j) ;
- nonterminal node with label (i, N, j) ;
- intermediate node with label (t, i, j) where t is a grammar slot;
- packed node with label $(N : \gamma, k)$;

, and one of nodes can be marked as 'root' — node for start nonterminal.

Further in our examples we will remove redundant intermediate and packed nodes from SPPF to simplify it and decrease size of structure.

4.3 GLL-based graph parsing

In order to adapt GLL for graph parsing we need only use graph vertices as position in input. As far as we work with context-free languages it is not important how this descriptor was created, and so descriptors management and other basic mechanisms of original algorithm can be reused "as is". We can merge it if they are equal.

We implement some optimizations: [1]

We also use binarised SPPF for result representation which allow to simplify query debugging and result exploration. In our case more than one root may be specified. For example, look at picture!!!! We

$\mathbb{P} : G, M, StartVset, FinalVSet \rightarrow SPPF$ In details, main function input is graph M , set of start vertices $V_s \subseteq V$, set of final vertices $V_f \subseteq V$, grammar G_1 . Output is Shared Packed Parse Forest (SPPF) [10] — finite data structure which contains all derivation trees for all paths in M , $\Omega(p) \in L(G_1)$ and allows to reconstruct any of paths implicitly. As far as we can specify sets of start and final vertices, our solution can find all paths in graph, all paths from specified vertex, all paths between specified vertices. Also SPPF represents a structure of paths in terms of derivation which allow to get more useful information about result. Binarized SPPF is at most cubic in terms of result size. Any path can be extracted in the linear time.

4.4 Complexity

Time complexity estimation in terms of input graph and grammar size is pretty similar to estimation of GLL complexity provided in [13].

LEMMA 1. For any descriptor (L, u, i, w) either $w = \$$ or w has extension (j, i) where u has index j .

PROOF. Proof of this lemma is the same as provided for original GLL in [13] because main function used for descriptor creation are the same as original one. \square

THEOREM 1. The GSS generated by GLL-based graph parsing algorithm for grammar G on input graph $M = (V, E, L)$ has at most $O(|V|)$ vertices and $O(|V|^2)$ edges.

PROOF. Proof the same as the proof of Theorem 2 from [13].

\square

THEOREM 2. The SPPF generated by GLL-based graph parsing algorithm on input graph $M = (V, E, L)$ has at most $O(|V|^3 + |E|)$ vertices and edges.

PROOF. Let we estimate number of nodes of each type.

- Terminal nodes. Each of them has label of form (T, v_0, v_1) , and such label can be created only if there is such $e \in E$ that $e = (v_0, T, v_1)$. Note, that there are no duplicate edges. Hence there are at most $|E|$ terminal nodes.
- ε nodes labeled with (ε, v, v) , hence there are at most $|E|$ of these.
- Nonterminal nodes have label of form (N, v_0, v_1) , so there are at most $O(|V|^2)$ of these.
- Intermediate nodes have label of form (t, v_0, v_1) , where t is grammar slot, so there are at most $O(|V|^2)$ of these.
- Packed nodes are children of intermediate or nonterminal nodes and have label of form (t, v) where t is a grammar slot $N : \alpha \cdot \beta$. There are at most $O(|V|^2)$ parents for packed nodes and each of them can have at most $O(|V|)$ children.

As a result there are at most $O(|V|^3 + |E|)$ nodes in SPPF.

The packed nodes have at most two children so there are at most $O(|V|^3 + |E|)$ edges with source in packed node. Nonterminal and intermediate nodes have at most $O(|V|)$ children and all of them are packed nodes. Thus there are at most $O(|V|^3)$ edges with source in nonterminal or intermediate nodes. As a result there are at most $O(|V|^3 + |E|)$ edges in SPPF.

\square

THEOREM 3. The space complexity of GLL-based graph parsing algorithm for graph $M = (V, E, L)$ is at most $O(|V|^3 + |E|)$.

PROOF. From theorems 1 and 2 we have that space required for main data structures is at most $O(|V|^3 + |E|)$.

\square

THEOREM 4. The runtime complexity of GLL-based graph parsing algorithm for graph $M = (V, E, L)$ is at most

$$O\left(|V|^3 * \max_{v \in V}(\deg^+(v))\right).$$



Figure 4: SPPF for sentence "(1)(2)(3)" and grammar G_0

PROOF. From Lemma 1 we get that there are at most $O(|V|^2)$ descriptors. Complexity of all functions are the same as in proof of **Theorem 4** from [13] except *processing* function where we should process not one next input token, but all outgoing edges. Thus for each descriptor we should examine at most

$$\max_{v \in V} (deg^+(v))$$

edges where $deg^+(v)$ is outdegree of vertex v .

So, worst-case complexity of proposed algorithm is

$$O\left(V^3 * \max_{v \in V} (deg^+(v))\right).$$

□

From theorem (4) we can get estimations for linear input and for LL grammars: for any $v \in V$ $deg^+(v) \leq 1$, so $\max_{v \in V} (deg^+(v)) = 1$ and we get $O(|V|^3)$. For LL grammars and linear input complexity should be $O(|V|)$ for the same reason as for original GLL.

As discussed in [7] achieving of theoretical complexity required special datastructures which can be irrational for practice implementation and it is necessary to find balance between performance, software complexity, and hardware resources. As a result in practice we can get slightly worse performance than theoretical estimation.

Note that result SPPF contains only paths matched specified query, so result SPPF size is $O(|V'|^3 + |E'|)$ where $M' = (V', E', L')$ is a subgraph of input graph M which contains only matched paths. Also note that each specific path can be explored with linear SPPF traversal.

4.5 Example

Let we introduce the next example. Grammar G_1 is a query and we want to find all paths in graph M (presented in picture 1) matched this query. Result SPPF for this input is presented in picture 5. Note that presented version does not contain obsolete nodes.

We use next markers for nodes which similar to original SPPF but have some additional information in order to relation with graph.

- Node with rectangle shape labeled with (v_0, T, v_1) is terminal node. Each terminal node corresponds with edge in the input graph: for each node with label (v_0, T, v_1) there is $e \in E : e = (v_0, T, v_1)$. Duplication of terminal nodes is only for figure simplification.
- Node with oval shape labeled with (v_0, nt, v_1) is non-terminal node. This node denote that there is at least one path p from vertex v_0 to vertex v_1 in input graph M such that $nt \Rightarrow_G^* \Omega(p)$. All paths matched this condition can be extracted from SPPF by left-to-right top-down graph traversal started from respective node.
- Filled node with oval shape labeled with $(< | > (v_0, nt, v_1))$ is nonterminal node denote that there are more then one path p from v_0 to v_1 such that $nt \Rightarrow_G^* \Omega(p)$.
- Node with dot shape is used for representation of derivation variants. Subgraph with root in one such node is one variant of derivation. Parent of such nodes is always node with label $(\diamond (v_0, nt, v_1))$.
- v_0 and v_1 are left and right extensions of node respectively.

As an example of derivation structure usage we can find 'middle' of any path in example above simply by finding corresponded nonterminal *middle* in SPPF. So we can found that there is only one common ancestor for all results, and it is vertex with $id = 0$.

Extensions stored in nodes allow to check whether path from u to v exists, and extract it. To extract specified path we need only travers SPPF, and it can be done in linear time (in terms of SPPF size).

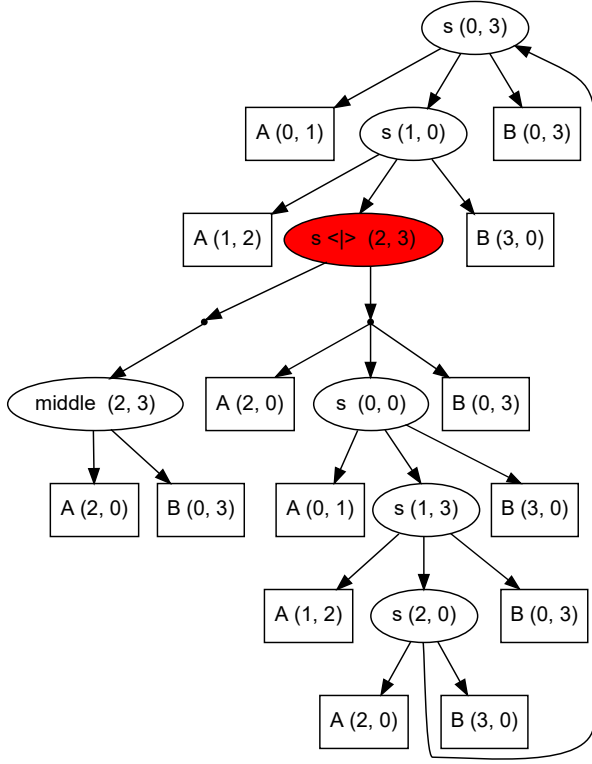


Figure 5: Result SPPF for input graph M (pic. 1) and query G_1 (pic. 2)

Let for example we want to find paths satisfying specified in G_1 constraints from vertex 0. To do this we should find vertices with label $(0, s, _)$ in SPPF. We can see that there are two vertices with required label: $(0, s, 0)$ and $(0, s, 3)$. Next step let us try to extract corresponded paths from SPPF. In our example there is a cycle in SPPF so there are **at least** two different paths:

$$p_0 = \{(0, A, 1); (1, A, 2); (2, A, 0); (0, B, 3); (3, B, 0); (0, B, 3)\}$$

and

$$p_1 = \{(0, A, 1); (1, A, 2); (2, A, 0); (0, A, 1); (1, A, 2); (2, A, 0); (0, B, 3); (3, B, 0); (0, B, 3); (3, B, 0); (0, B, 3); (3, B, 0)\}.$$

Thus SPPF which is constructed by the described algorithm can be useful for query result investigation. But in some cases explicit representation of matched subgraph may be preferred, and required subgraph may be extracted from SPPF trivially by its traversal.

5. EVALUATION

We use two grammars for balanced brackets — ambiguous grammar G_0 3 and unambiguous grammar G_2 6 — in order to investigate performance and grammar ambiguity correlation.

For input we use complete graphs where for each terminal symbol there is an edge between two vertices labeled with it. Note that we use only terminal symbols for edge labels. Task we solve in our experiments is to find all paths from all vertices to all vertices satisfying the specified query. Such

0: $s = L s R s$
1: $s = \text{eps}$

Figure 6: Unambiguous grammar G_2 for balanced brackets

designed input looks hard for querying in terms of required resources because there are correct paths between any two vertices and the result set is infinite.

All tests were performed on a PC with the following characteristics:

- OS Name: Microsoft Windows 10 Pro
- System Type: x64-based PC
- CPU: Intel(R) Core(TM) i7-4790 CPU @ 3.60GHz, 3601 Mhz, 4 Core(s), 4 Logical Processor(s)
- RAM: 32 GB

Performance measurement results are presented in Figure 7. As far as for complete graph $M = (V, E, L)$

$$\max_{v \in V} (\deg^+(v)) = (|V| - 1) * |\Sigma|$$

where Σ is the terminals of the input grammar, we should get time complexity at most $O(|V|^4)$ and space complexity at most $O(|V|^3)$. For time measurement results we have that all two curves can be fitted with a polynomial function of degree 4 to a high level of confidence with R^2 .

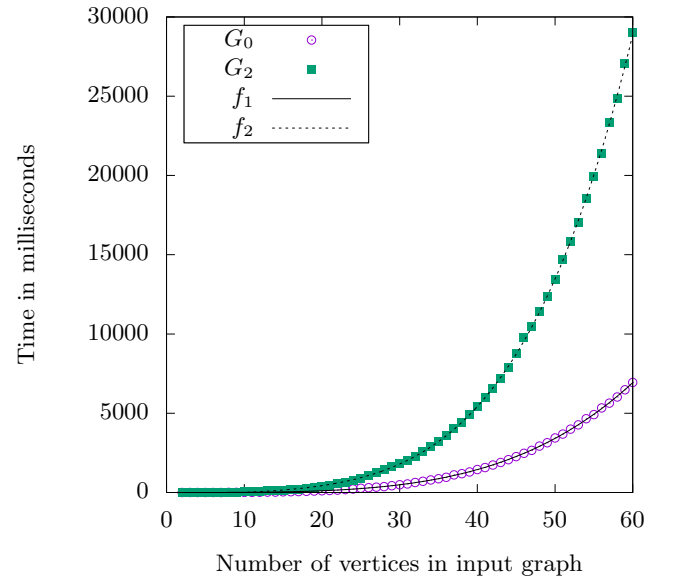


Figure 7: Performance on complete graphs for grammars G_0 and G_2

$$f_1(x) = 0.000495989 * x^4 + 0.001252184 * x^3 + 0.068491746 * x^2 - 0.306749160 * x; R^2 = 0.99996$$

$$f_2(x) = 0.003368883 * x^4 - 0.114919298 * x^3 + 3.161793404 * x^2 - 22.549491142 * x; R^2 = 0.99995$$

Also we present SPPF size in terms of nodes for both G_0 and G_2 grammars 8. As we expected, all two curves are cubic to a high level of confidence with $R^2 = 1$.

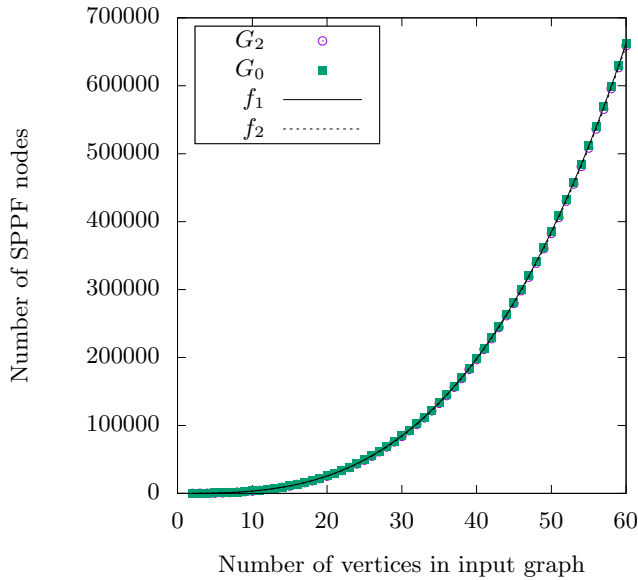


Figure 8: SPPF size on complete graph for grammars G_0 and G_2 on complete graphs

$$f_1(x) = 3.000047 * x^3 + 3.994579 * x^2 + 4.191568 * x; R^2 = 1$$

$$f_2(x) = 3.000050 * x^3 + 2.994338 * x^2 + 4.196472 * x; R^2 = 1$$

6. CONCLUSION AND FUTURE WORK

We propose GLL-based algorithm for context-free path querying which construct finite structural representation of all paths satisfying given constraint. Provided data structure can be useful for result investigation and processing, and query debugging. Presented algorithm implemented in F# [17] and available on GitHub: <https://github.com/YaccConstructor/YaccConstructor>.

In order to estimate practical value of proposed algorithm we should perform evaluation on real dataset and real queries. One of possible application of our algorithm is metagenomical assembly querying, and we are working on this topic.

Also we are working on performance improvement by implementation of recently proposed modifications in original GLL algorithm [14]. One of direction of our research is generalization of grammar factorization proposed in [14] which may be useful for regular query processing.

We are working on utilisation of GPGPU and multicore CPU power for graph parsing problem with Valiant [19] algorithm modification proposed by Alexander Okhotin [9]. One of possible benefit is ability to process more expressive queries because modification proposed by Alexander Okhotin extended to support boolean grammars.

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