Extended Context-Free Grammars Parsing with Generalized LL

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Abstract. Parsing plays an important role in static program analysis: during this step a structural representation of code is created upon which further analysis is performed. Parser generator tools, being provided with syntax specification, automate parser development. Language documentation often acts as such specification. Documentation usually takes form of ambiguous grammar in Extended Backus-Naur Form which most parser generators fail to process. Automatic grammar transformation generally leads to parsing performance decrease. Some approaches support EBNF grammars natively, but they all fail to handle ambiguous grammars. On the other hand, Generalized LL parsing algorithm admits arbitrary context-free grammars and achieves good performance, but cannot handle EBNF grammars. The main contribution of this paper is a modification of GLL algorithm which can process grammars in a form which is closely related to EBNF (Extended Context-Free Grammar). We also show that the modification improves parsing performance as compared to grammar transformation based approach.

Keywords: Parsing, Generalized Parsing, Extended Context-Free Grammar, GLL, SPPF, EBNF, ECFG, RRPG, Recursive Automata

1 Introduction

Static program analysis is usually performed over a structural representation of code and parsing is a classical way to get such representation. Parser generators are often used to automata parser creation: these tools allow to derive parser from grammar. It decreases amount of efforts required for syntax analyzer creation and maintenance.

Extended Backus-Naur Form [21] is a syntax of expressing context-free grammars. In addition to the Backus-Naur Form syntax it uses the following constructions: alternation |, option [...], repetition $\{$... $\}$, and grouping (...).

This form is widely used for grammar specification in technical documentation because it allows to make description of language syntax more expressive and compact. Thus, it is necessary to have a parser generator which supports grammar in EBNF because documentation is one of main source of information for parsers developers. Note, that EBNF is a standardized notation for *extended* context-free grammars which can be defined as follows.

Definition 1 An extended context-free grammar (ECFG) [10] is a tuple (N, Σ, P, S) , where N and Σ are finite sets of nonterminals and terminals, $S \in N$ is the start symbol, and P (the productions) is a map from N to regular expressions over alphabet $N \cup \Sigma$.

ECFG is widely used as input format for parser generators, but classical parsing algorithms requires CFG, and as a result, parser generators requires conversion to CFG. It is possible to transform ECFG to CFG [9], but this transformation leads to grammar size increase and change in grammar structure: new nonterminals addition is required during transformation. As a result, parsing performs not in terms of user defined grammar. This fact leads to the following problem: parser build structural representation not with respect to the original grammar but with respect to transformed. As a result, derivation tree may differ from expected.

In order to provide ability to process grammar in ECFG there is a wide range of parsing techniques and algorithms [2, 3, 5, 8–10, 12, 13]. Detailed overview of results and problems in ECFG processing area is provided in the article "Towards a Taxonomy for ECFG and RRPG Parsing" [10]. We only note that most of algorithms are based on classical LL [8, 2, 4] and LR [13, 12, 3] techniques, and they can handle only appropriate subclasses of ECFG. As a result, parsing techniques for ECFG is actual problem, and there is no solution for handling arbitrary and ambiguous ECFGs.

The LL-based parsing algorithms is more intuitive than LR-based and can provide better error diagnostic. Thus, LL(1) is most practical algorithm, but it is not powerful enough: LL(k) for any k is not enough to process some languages because there are LR, but not LL languages. Also left and hidden left recursion in grammars is a problem for LL-based parsers. Moreover handling of arbitrary ambiguous grammars is a also problem for LL-based tools. All these facts restrict class of grammars which can be handled, which make parser creation difficult. In order to solve these problems generalized LL (GLL) [16] was proposed [16]. This algorithm handles arbitrary context free grammar, even unambiguous and (hidden)left-recursive. Worst-case time and space complexity of GLL is cubic in terms of input size and for LL(1) grammars it demonstrates linear time and space complexity.

In order to improve performance of GLL algorithm, modification for left factorized grammars processing was introduced in [18]. Factorization means that there are no two productions for one nonterminal with equal prefixes (look at fig 1 for example). Shown, that factorization can reduce memory usage and increase performance which achieved by reusing common parts of rules for one nonterminal. Purposed idea can be used for processing grammars in EBNF with exception of same effects.

To summarize, it is possible to simplify language description required for parser generation in case a parser generator is based on generalized algorithm which can handle grammars in ECFG. Generalized parsing algorithms can handle arbitrary grammars and these demonstrate good performance. In this work we present modified generalized LL parsing algorithm which handles arbitrary ECFGs without transformations. We show that changes of basic algorithm are very native for GLL nature. Also we demonstrate that proposed modifications allow to get parsing performance and memory usage improvement.

2 ECFG Handling with Generalized LL Algorithm

In order to provide arbitrary context-free grammars handling, generalized parsing algorithms were purposed. Generalized LL algorithm (GLL) [16] inherits properties of classical LL algorithms: it is more intuitive and allows to perform better syntax error diagnostic then generalized LR algorithms. Also, our experience shows that GLR-based solutions is more complex rather GLL-based, which is in good agreement with the observation in [10] that LR-based ECFG parsers are very complex. Thus, we choose GLL as a base for our solution. In this section GLL-style parser for arbitrary ECFG processing presented.

2.1 Generalized LL Parsing Algorithm

An idea of the GLL algorithm based on descriptors, it allows to handle all possible derivations. Descriptor is a four-element tuple (L,i,T,S) that can uniquely define state of parsing process. L is a grammar slot — pointer to position in grammar of the form $(S \to \alpha \cdot \beta)$, i — position in input, T — already built SPPF root, S — current Graph Structured Stack (GSS) [?] node.

In initial state we have descriptors that describe start positions in grammar and input, dummy tree node and bottom of GSS. On each step algorithm processes first descriptor in queue and makes actions depending on the grammar and input. If there are any ambiguity algorithm will queue descriptor for all cases to handle them all.

There are table based approach [14] which allows to generate only tables for given grammar instead of full parser code. The idea is similar to one in original article and main function uses same tree construction and stack processing functions. Pseudo code can be found in appendix A. Note that we do not include the check for first/follow sets in this paper.

2.2 Factorization

In order to improve performance of GLL Elizabeth Scott and Adrian Johnstone offered support of left-factorized grammars in this parsing algorithm [18].

The basic algorithm creates and queues new descriptors depending on current parse state that we get from dequeued descriptor. In case descriptor has been already created it does not add it to queue. For this purpose we have a set of all created descriptors. Thus reducing a number of possible descriptors decreases the parse time and required memory.

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Grammar factorization decreases the number of grammar slots, which leads to decreasing of total descriptor number. Consider example of grammar and its factorized version the from paper [18] on fig. 1.

```
S ::= a \ a \ B \ c \ d
\begin{vmatrix} a \ a \ c \ d \\ | \ a \ a \ c \ e \\ | \ a \ a \end{vmatrix} S ::= a \ a \ (B \ c \ d \ | \ c \ (d \ | \ e) \ | \ \varepsilon)
(a) \ \text{Production} \ P_0
(a) \ \text{Production} \ P_0
```

Fig. 1. Example of factorization

Production P_0 transform to P'_0 during factorization. Second is much compact and contains much less possible slots, so parser creates less descriptors. It gives significant performance improvement on some grammars.

This idea can also be evolved to full ECFG support. Let us show how to do it.

2.3 Recursive automata

In order to use ideas of grammar factorization for handling ECFGs with GLL we propose to use recursive automata (RA) [19] for ECFG representation. We use the following definition of RA.

Definition 2 Recursive automaton(RA) R is a tuple $(\Sigma, Q, S, F, \delta)$, where Σ is a set of terminals, Q — set of states of R, $S \in Q$ — start state, $F \in Q$ — set of final states, $\delta: Q \times (\Sigma \cup Q) \to Q$ — transition function.

The only difference between RA and FSA is that in RA transition can be labeled either by terminal (Σ) or by state (Q). Further in this paper we will call transitions by elements from Q as nonterminal transitions and by terminal as terminal transitions.

Right parts of ECFG are regular expressions over alphabet of terminals and nonterminals. Thus for each right-hand side of grammar productions we can build a finite state automaton using Thompson's method [20]. To transform the set of produced automata we need to eliminate ε -transitions and replace transitions by nonterminals with transitions labeled by start states of corresponding to nonterminal FSA. An example of constructed recursive automaton for grammar Γ_0 (fig. 2a) is given on fig. 2b, state 0 is start state.

Decrease of the quantity of the automaton states decreases number of GLL descriptors, as it was with factorization. Thus to increase performance of parsing we can minimize the number of states in produced automatons.

First, RA should be converted to deterministic RA using the algorithm for FSA described in [1]. Then John Hopcroft's algorithm [11] can be applied to

RA to minimize the number of states. An example for grammar G_0 is shown on fig. 2c.

Later, in order to build SPPF, we will need not only start state number, but nonterminal names. For this purpose we define function $\Delta: Q \to N$ where N is nonterminal name.

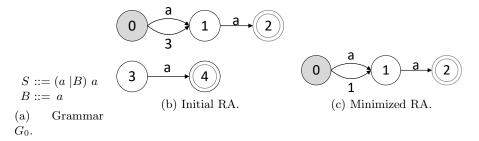


Fig. 2. Example of automatons.

2.4 Input processing

An GLL idea is to move through grammar and input simultaneously, creating multiple descriptors for the case of ambiguity.

Just as we can move through grammar slots we can move through states of automaton. Grammar slot in descriptor changes to state in RA. The problem is that in automaton we have nondeterministic choice because there can be many transitions to other states. Consider such significant cases:

- there are transition by current input terminal to final state
- there are transition by current input terminal to state that is not final
- there are nonterminal transition

All of them should be handled and this leads to nondeterminism. For the last case we just can call create function for each state. But for the terminal cases we need to add descriptor that describes next position to queue without checking it's existence in descriptor elimination set. Thus we use descriptors queue to handle nondeterminism in states, while original algorithm uses it to handle ambiguity in grammars.

Function add queues descriptor if it was not already created.

```
function CREATE(S_{call}, S_{next}, u, i, w)

A \leftarrow \Delta(S_{call})
```

```
if (\exists GSS node labeled (A,i)) then v \leftarrow GSS node labeled (A,i) if (there is no GSS edge from v to u labeled (S_{next},w)) then add a GSS edge from v to u labeled (S_{next},w) for ((v,z) \in \mathcal{P}) do (y,N) \leftarrow \mathbf{getNodes}(S_{next},u.nonterm,w,z) if N \neq \$ then (-,-,h) \leftarrow N \mathbf{pop}(u,h,N) (-,-,h) \leftarrow y \mathbf{add}(S_{next},u,h,y) else v \leftarrow \mathbf{new} GSS node labeled (A,i) create a GSS edge from v to u labeled (S_{next},w) \mathbf{add}(S_{call},v,i,\$) return v
```

Function **create** is called when we meet nonterminal transition. It performs necessary operations with GSS and checks if there are already built SPPF for current input position and nonterminal.

```
\begin{aligned} & \textbf{function} \ \text{POP}(u,i,z) \\ & \textbf{if} \ ((u,z) \notin \mathcal{P}) \ \textbf{then} \\ & \mathcal{P}.add(u,z) \\ & \textbf{for all} \ \text{GSS edges} \ (u,S,w,v) \ \textbf{do} \\ & (y,N) \leftarrow \textbf{getNodes}(S,v.nonterm,w,z) \\ & \textbf{if} \ N \neq \$ \ \textbf{then} \\ & \textbf{pop}(v,i,N) \\ & \textbf{if} \ y \neq \$ \ \textbf{then} \\ & \textbf{add}(S,v,i,y) \end{aligned}
```

Pop function is called when we reach final state. It queues descriptors for all outgoing edges from current GSS node.

```
function PARSE R.add(StartState, newGSSnode(StartNonterminal, 0), 0, \$) while R \neq \emptyset do (C_S, C_U, C_i, C_N) \leftarrow R.Get() C_R \leftarrow \$ if (C_N = \$)\&(C_S \text{ is pop state}) then eps \leftarrow \mathbf{getNodeT}(\varepsilon, C_i) (\_, N) \leftarrow \mathbf{getNodes}(C_S, C_U.nonterm, \$, eps) \mathbf{pop}(C_U, C_i, N) for each transition(C_S, label, S_{next}) do \mathbf{switch} \ label \ \mathbf{do} \mathbf{case} \ Terminal(x) \ \text{where} \ (x = input[i]) R \leftarrow \mathbf{getNodeT}(x, C_i) (y, N) \leftarrow \mathbf{getNodes}(S_{next}, C_U.nonterm, C_N, R)
```

```
\begin{aligned} & \textbf{if } N \neq \$ \textbf{ then} \\ & \textbf{pop}(C_U, i+1, N) \\ & R.add(S_{next}, C_U, i+1, y) \\ & \textbf{case } Nonterminal(S_{call}) \\ & \textbf{create}(S_{call}, S_{next}, C_U, C_i, C_N) \end{aligned}
```

The main function **parse** handles queued descriptor and checks all transitions from current state to be appropriate for current input terminal, or calls create function when meets nonterminal transitions.

2.5 Parse forest construction

Result of the parsing process is structural representation of input — tree, or parse forest for the case of many derivation variants.

First, we should define derivation tree for recursive automatons: it is an ordered tree whose root labeled with start state, leaf nodes are labeled with a terminals or ε and interior nodes are labeled with nonterminals A and have a sequence of children that corresponds to transition labels of path in automaton that starts from the state $\Delta(A)$. More formal definition provided below.

Definition 3 Derivation tree of sentence α for the recursive automaton $R = (\Sigma, Q, S, F, \delta)$:

- Ordered rooted tree. Root labeled with $\Delta(S)$
- Leaves are terminals $\in \Sigma$
- Nodes are nonterminals $\in \Delta(Q)$
- Node with label $N_i \in \Delta(q_i)$ has children $l_0 \dots l_n(l_i \in \Sigma \cup \Delta(Q))$ iff exists path $q_i \xrightarrow{l_0} \dots \xrightarrow{l_n} q_m$, $q_m \in F$.

RA is ambiguous if there exist string that have more than one derivation trees. We work with arbitrary grammars, thus our RA can be ambiguous and we can define Shared Packed parse Forest (SPPF) [15] that can represent all possible derivation trees. It is similar to SPPF for grammars described in [17]. SPPF contains symbol nodes, packed nodes and intermediate nodes.

Packed nodes are of the form (S,k), where S is a state of automaton. Symbol nodes have labels (X,i,j) where $X\in \mathcal{L}\cup \Delta(Q)\cup \varepsilon$. Intermediate nodes have labels (S,i,j), where S is a state of automaton. i is position in input before leftmost leaf terminal, j—position after rightmost leaf.

Packed node necessarily has right child — symbol node, and optional left child — symbol or intermediate node. Nonterminal and intermediate nodes may have several packed children. Terminal symbol nodes are leaves.

Use of intermediate and packed nodes leads to binarization of SPPF and thus the space complexity is $O(n^3)$.

Let us to describe functions which required for SPPF construction. The function $\mathbf{getNodeT}(x,i)$, which create terminal nodes, reused without modification from basic algorithm. To manipulate other nodes we define function $\mathbf{getNodes}$

which can construct two nodes: intermediate and nonterminal (at least one of them, at most both). It uses modified function **getNodeP** that takes additional argument: state or nonterminal name. Symbol in returned SPPF node will be this argument's value.

```
function GETNODES(S, A, w, z)
    if (S \text{ is pop state}) then
        x \leftarrow \mathbf{getNodeP}(S, A, w, z)
    else
        x \leftarrow \$
    if (w = \$)& not (z is nonterminal node and it's extents are equal) then
    else
        y \leftarrow \mathbf{getNodeP}(S, S, w, z)
    return (y, x)
function GETNODEP(S, L, w, z)
    (\underline{\phantom{a}}, k, i) \leftarrow z
    if (w \neq \$) then
        (\_,j,k) \leftarrow w
        y \leftarrow \text{find or create SPPF node labelled } (L, j, i)
        if (\nexists child of y labelled (S,k)) then
             y' \leftarrow \mathbf{new} \ packedNode(S, k)
             y'.addLeftChild(w)
             y'.addRightChild(z)
             y.addChild(y')
    else
        y \leftarrow \text{find or create SPPF node labelled } (L, k, i)
        if (\nexists child of y labelled (S, k)) then
             y' \leftarrow \mathbf{new} \ packedNode(S, k)
             y'.addRightChild(z)
             y.addChild(y\prime)
    return y
```

3 Evaluation(under construction)

We have implemented parser generator for suggested algorithm, and in this section we show SPPF example and performance comparison with the parser built on factorized grammar.

3.1 SPPF example

For the SPPF example we have taken ECFG grammar G_1 (fig. 3). It contains constructions (option and repetition) that should be converted with use of extra

nonterminals to build regular GLL parser. Our generator constructs recursive automaton R_1 (fig. 4a) and parser for it.

For input aabk this parser builds SPPF showed on fig. 4b.

$$S ::= (a^* \ b? \ k) \mid M$$

$$M ::= \quad a \ a \ b \ k$$

Fig. 3. Grammar G_1 .

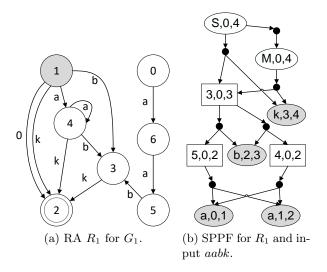
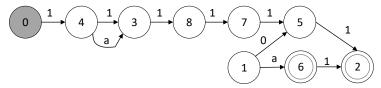


Fig. 4. Example of SPPF.

3.2 Performance measure

We have compared our parsers built on factorized grammars and on minimized recursive automatons. Grammar $G_2(\text{fig. 5a})$ was used for the tests, it has long tails in alternatives which is not unified with factorization. FSA built for this grammar presented on fig. 5b.



(b) RA for grammar G_2 .

Fig. 5. Grammar G_2 and RA for it.

Explanation of slots difference: for BNF, for factorized, for ECFG Description of input. Short info about PC.

	Time, s	Descriptors	GSS Edges	GSS Nodes	SPPF Nodes
Factorized grammar	81.814	7940	6974	80	111127244
Minimized RA	54.637	5830	4234	80	74292078

Table 1. Experiments results for input a^{40} .

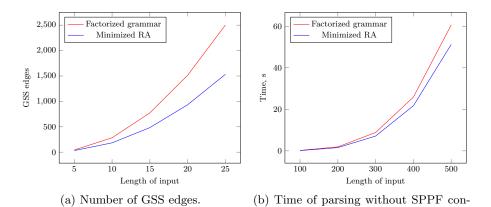


Fig. 6. Experiments results(1).

struction.

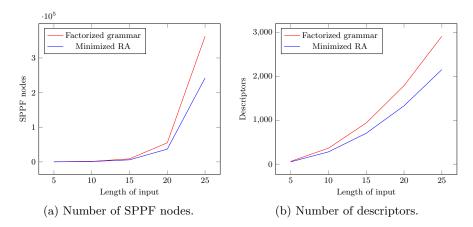


Fig. 7. Experiments results(2).

Fig. 6 and fig. 7 show experiments results. In general minimized RA version works 33% faster, uses 27% less descriptors, 29% less GSS edges and 33% less SPPF nodes.

We also use this automaton approach in metagenomic assemblies parsing and it gives visible performance increase.

A bit more discussion on evaluation.

Examples of SPPF.

May be some nontrivial cases: s -; a^* a^* and so on

4 Conclusion and Future Work

Described algorithm and parser generator based on it implemented in F# as part of the YaccConstructor project. Source code available here: https://github.com/YaccConstructor/YaccConstructor.

As we show in evaluation, proposed modification not only increase performance, but also decrease memory usage. It is critical for big input processing. For example, Anastasia Ragozina in her master's thesis [14] shows that GLL can be used for graph parsing. In some areas graphs can be really huge: metagenomic assemblies in bioinfomatics, social graphs. We hope that proposed modification can improve performance not only in case of classical parsing, but in graph parsing too. We perform some tests that shows performance increasing in metagenomic analysis, but full integration with graph parsing and formal description is required.

One of way to specify any useful manipulations on derivation tree (or semantic of language) is an attributed grammars, but it is not supported in the algorithm which presented in this article. There is number of works on subclasses of attributed ECFGs (for example [2]), however still no solution for arbitrary ECFGs. Thus, arbitrary attributed ECFGs and semantic calculation support is a future work.

Yet another question is possibility of unification our results with tree languages: our definition of derivation tree for ECFG is quite similar to unranked tree and SPPF is similar to automata for unranked trees [7]. Theory of tree languages seems more mature than theory of general SPPF manipulations and relations between tree languages and SPPF investigation may get interesting results. For example, relations between tree languages and ECFG discussed here [6] but mainly in context of XML manipulation.

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A GLL pseudocode

```
function ADD(L, u, i, w)
    if (L, u, i, w) \notin U then
        U.add(L, u, i, w)
        R.add(L, u, i, w)
function CREATE(L, u, i, w)
    (X ::= \alpha A \cdot \beta) \leftarrow L
    if (\exists GSS \text{ node labeled } (A, i)) then
        v \leftarrow GSS \text{ node labeled } (A, i)
        if (there is no GSS edge from v to u labeled (L, w)) then
             add a GSS edge from v to u labeled (L, w)
            for ((v,z) \in \mathcal{P}) do
                 y \leftarrow \mathbf{getNodeP}(L, w, z)
                 add(L, u, h, y) where h is the right extent of y
    else
        v \leftarrow \mathbf{new} \text{ GSS node labeled } (A, i)
        create a GSS edge from v to u labeled (L, w)
        for each alternative \alpha_k of A do
            add(\alpha_k, v, i, \$)
    return v
function POP(u, i, z)
    if ((u,z) \notin \mathcal{P}) then
        \mathcal{P}.add(u,z)
        for all GSS edges (u, L, w, v) do
            y \leftarrow \mathbf{getNodeP}(L, w, z)
            add(L, v, i, y)
function GETNODET(x, i)
    if (x = \varepsilon) then
        h \leftarrow i
    else
        h \leftarrow i + 1
    y \leftarrow \text{find or create SPPF node labelled } (x, i, h)
     return y
function GETNODEP(X := \alpha \cdot \beta, w, z)
    if (\alpha is a terminal or a non-nullable nontermial) & (\beta \neq \varepsilon) then
        return z
```

```
else
         if (\beta = \varepsilon) then
              L \leftarrow X
         else
              L \leftarrow (X ::= \alpha \cdot \beta)
          (-,k,i) \leftarrow z
         if (w \neq \$) then
              (-,j,k) \leftarrow w
              y \leftarrow \text{find or create SPPF node labelled } (L, j, i)
              if (\nexists child of y labelled (X := \alpha \cdot \beta, k)) then
                   y' \leftarrow \mathbf{new} \ packedNode(X ::= \alpha \cdot \beta, k)
                   y'.addLeftChild(w)
                   y'.addRightChild(z)
                   y.addChild(y')
         else
              y \leftarrow \text{find or create SPPF node labelled } (L, k, i)
              if (\nexists child of y labelled (X := \alpha \cdot \beta, k)) then
                   y' \leftarrow \mathbf{new} \ packedNode(X ::= \alpha \cdot \beta, k)
                   y'.addRightChild(z)
                   y.addChild(y')
         return y
function DISPATCHER
    if R \neq \emptyset then
         (C_L, C_u, C_i, C_N) \leftarrow R.Get()
         C_R \leftarrow \$
         dispatch \leftarrow false
    else
         stop \leftarrow true
function PROCESSING
    dispatch \leftarrow true
    switch C_L do
         case (X \to \alpha \cdot x\beta) where (x = input[C_i] \parallel x = \varepsilon)
              C_R \leftarrow \mathbf{getNodeT}(x, C_i)
              if x \neq \varepsilon then
                   C_i \leftarrow C_i + 1
              C_L \leftarrow (X \rightarrow \alpha x \cdot \beta)
              C_N \leftarrow \mathbf{getNodeP}(C_L, C_N, C_R)
              dispatch \leftarrow false
         case (X \to \alpha \cdot A\beta) where A is nonterminal
              \mathbf{create}((X \to \alpha A \cdot \beta), C_u, C_i, C_N)
         case (X \to \alpha \cdot)
              \mathbf{pop}(C_u, C_i, C_N)
function Parse
    while not stop do
```

if dispatch then
 dispatcher()
else
 processing()