

GRADES-NDA 2020



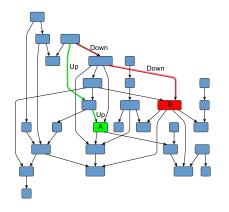
Context-Free Path Querying with Single-Path Semantics by Matrix Multiplication

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Context-Free Path Querying



Navigation through a graph

- Are nodes A and B on the same level of hierarchy?
- Is there a path of form Upⁿ Downⁿ?
- Find all paths of form
 Upⁿ Downⁿ which start from the node A

- $\mathbb{G} = (\Sigma, N, P)$ context-free grammar in normal form
 - ▶ $A \rightarrow BC$, where $A, B, C \in N$
 - ▶ $A \rightarrow x$, where $A \in N, x \in \Sigma \cup \{\varepsilon\}$
 - $L(\mathbb{G}, A) = \{ \omega \mid A \Rightarrow^* \omega \}$

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 - $v \stackrel{l}{\rightarrow} u \in E$
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 - $L \subset \Sigma$
- $\omega(\pi) = \omega(v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \cdots \xrightarrow{l_{n-2}} v_{n-1} \xrightarrow{l_{n-1}} v_n) = l_0 l_1 \cdots l_{n-1}$

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- $R_A = \{(n, m) \mid \exists n\pi m, \text{ such that } \omega(\pi) \in L(\mathbb{G}, A)\}$

Matrix-Based Algorithm: Relational Query Semantics

Algorithm Context-free path querying algorithm

1: function EVALCFPQ($D = (V, E, L), G = (\Sigma, N, P)$)
2: $n \leftarrow |V|$ 3: $T \leftarrow \{T^{A_i} \mid A_i \in N, T^{A_i} \text{ is a matrix } n \times n, T^{A_i}_{k,l} \leftarrow \text{false}\}$ 4: for all $(i, x, j) \in E, A_k \mid A_k \rightarrow x \in P \text{ do } T^{A_k}_{i,j} \leftarrow \text{true}$ 5: for all $A_k \mid A_k \rightarrow \varepsilon \in P \text{ do}$ 6: for all $i \in \{0, \dots, n-1\}$ do $T^{A_k}_{i,i} \leftarrow \text{true}$ 7: while any matrix in T is changing do
8: for $A_i \rightarrow A_i A_k \in P \text{ do } T^{A_i} \leftarrow T^{A_i} + (T^{A_j} \times T^{A_k})$

Rustam Azimov (JetBrains Research)

return T

9:

Context-Free Path Querying: Single-Path Query Semantics

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Context-Free Path Querying: Single-Path Query Semantics

- $R_A = \{(n, m) \mid \exists n\pi m$, such that $\omega(\pi) \in L(\mathbb{G}, A)\}$ answers for the relational query semantics
- For all $A \in N$, for all $(n, m) \in R_A$ also return some such path $n\pi m$
 - usually the shortest path is returned
 - returned path can be used as a proof of existence

Research Questions

- Can we extend the matrix-based CFPQ algorithm to single-path query semantics?
- What the cost of such extension?
- Can we achieve high performance of CFPQ integrated with existing graph database?
- Does using GPGPU still improve performance over CPU versions?

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$$PI_1 \otimes PI_2 = (PI_1.left, PI_2.right, PI_1.right, max(PI_1.height, PI_2.height) + 1,$$

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$$PI_1 \oplus PI_2 = egin{cases} PI_1, & \text{if } PI_1.height \leq PI_2.height \\ PI_2, & \text{otherwise} \end{cases}$$

Matrix-Based Algorithm: Single-Path Query Semantics

Algorithm CFPQ algorithm w.r.t. single-path query semantics

- 1: function EVALCFPQ($D = (V, E), G = (N, \Sigma, P)$)
- 2: $n \leftarrow |V|$
- 3: $T \leftarrow \{T^{A_i} \mid A_i \in \mathbb{N}, T^{A_i} \text{ is a matrix } n \times n, T^{A_i}_{k,l} \leftarrow \bot \}$
- 4: for all $(i, x, j) \in E$, $A_k \mid A_k \rightarrow x \in P$ do $T_{i,j}^{A_k} \leftarrow (i, j, i, 1, 1)$
- 5: for $A_k \mid A_k \to \varepsilon \in P$ do $T_{i,i}^{A_k} \leftarrow (i, i, i, 1, 0)$
 - 6: while any matrix in T is changing do
- 7: for $A_i \rightarrow A_j A_k \in P$ do $T^{A_i} \leftarrow T^{A_i} + (T^{A_j} \odot T^{A_k})$
- 8: **return** *T*

Matrix-Based Algorithm: Technical Details

- We can remove *length* or *height* to reduce memory consumption
- The PathIndex operations can be represented as bitwise atomic operations
- We still can use existing high-performance libraries for matrix operations if they support the creation of custom operations

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 - ▶ The path which forms a string with minimal height of derivation tree
 - ► The shortest path
- Linear complexity in the length of the extracted path

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 - ▶ RG_SPARSE_{path} single-path query semantics, operating over PathIndex semiring

Dataset¹

RDF Name	#V	#E			
univ-bench	179	413			
pizza	671	2,604			
wine	733	2,450			
core	1,323	8,684			
pathways	6,238	37,196			
go-hierarchy	45,007	1,960,436			
enzyme	48,815	219,390			
eclass_514en	239,111	1,047,454			
go	272,770	1,068,622			
geospecies	450,609	4,622,922			

¹Queries is based on the context-free grammars for nested parentheses

Evaluation

OS: Ubuntu 18.04

• CPU: Intel core i7 6700 3,4GHz

• RAM: DDR4 64 Gb

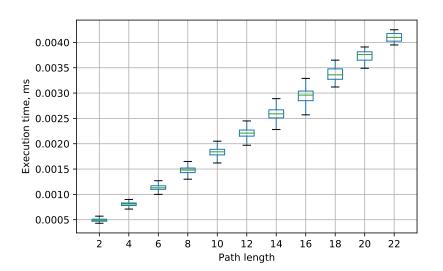
GPGPU: NVIDIA GeForce 1070 (8Gb RAM)

Evaluation: CFPQ²

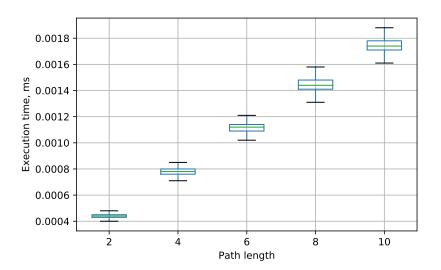
	Relational semantics index					Single path semantics index					
Name	RG_CPU _{rel} RG_		RG_C	G_CUSP _{rel} I		RG_SPARSE _{rel}		RG_CPU _{path}		RG_SPARSE _{path}	
	Time	Mem	Time	Mem	Time	Mem	Time	Mem	Time	Mem	
core	0.004	0.3	0.022	2.0	0.010	0.1	0.002	0.3	0.016	0.1	
eclass 514en	0.067	13.8	0.075	14.0	0.166	16.0	0.195	31.2	0.496	26.0	
enzyme	0.018	5.9	0.021	0.1	0.018	4.0	0.029	8.1	0.043	6.0	
go-hierarchy	0.091	16.3	0.433	650.0	0.108	121.2	0.976	92.0	0.336	125.0	
go	0.604	28.8	0.590	70.0	0.365	30.2	1.286	75.7	0.739	45.4	
pathways	0.011	0.1	0.019	0.1	0.007	0.1	0.021	0.5	0.021	2.0	
univ-bench	0.002	0.3	0.010	0.1	0.005	0.1	0.013	0.3	0.007	0.1	
pizza	0.030	1.8	0.021	4.0	0.006	0.1	0.075	5.5	0.009	0.1	
wine	0.017	3.5	0.032	6.0	0.009	0.1	0.117	7.1	0.015	0.2	
geospecies	7.146	16934.2		_	0.856	5274	15.134	35803.6	1.935	5282	

²Time in seconds and memory is measured in megabytes

Evaluation: Path Extraction Time For go



Evaluation: Path Extraction Time For geospecies



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- The additional running time of the path extraction is small and linear in the length of the path
- The matrix-based algorithm paired with a suitable database is a promising way to make CFPQ applicable for real-world data analysis
- Dataset is published: both graphs and queries
 - ► Link: https://github.com/JetBrains-Research/CFPQ_Data
- Implementations are available on GitHub
 - ► Link: https://github.com/YaccConstructor/RedisGraph

Future Research

• Extend the matrix-based CFPQ algorithm to all-path query semantics

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- Extend the matrix-based CFPQ algorithm to all-path query semantics
- Update the query results dynamically when data changes
- Improve the dataset
 - Include real-world cases from the area of static code analysis
 - ▶ Find new applications that required CFPQ, such as graph segmentation

Acknowledgments

- Special thanks to
 - Gábor Szárnyas for turning our attention to SuiteSparse and GraphBLAS
 - ► George Fletcher for telling us about his research on CFPQ for Neo4j
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- Artyom Khoroshev: arthoroshev@gmail.com
- Dataset: https://github.com/JetBrains-Research/CFPQ_Data
- Algorithm implementations: https://github.com/YaccConstructor/RedisGraph

Thanks!