

Arbitrary CFPQ to Dyck language constrained querying

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This reduction is inspired by construction which is described in [?].

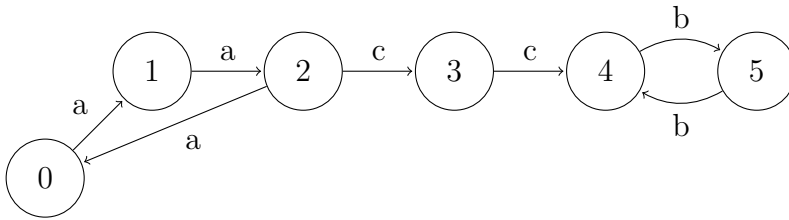
Let we have a context-free grammar $\mathcal{G} = (\Sigma, N, P, S)$ in BNF where Σ is a terminal alphabet, N is a nonterminal alphabet, P is a set of productions, $S \in N$ is a start nonterminal. Also we have a directed labeled graph $G = (V, E, L)$ where $E \subseteq V \times L \times V$ and $L \subseteq \Sigma$.

We should construct new input graph G' and new grammar \mathcal{G}' such that \mathcal{G}' specifies a Dyck language and there is a simple mapping from $\text{CFPQ}(\mathcal{G}', G')$ to $\text{CFPQ}(\mathcal{G}, G)$. Step-by-step example with description is provided below.

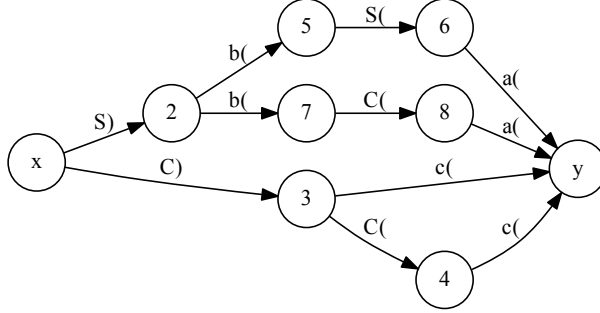
Let the input grammar is

$$\begin{aligned} S &\rightarrow a S b \mid a C b \\ C &\rightarrow c \mid C c \end{aligned}$$

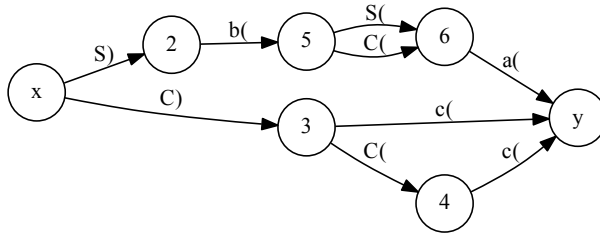
Let the input graph is



1. Let $\Sigma_0 = \{t_(), t_() | t \in \Sigma\}$.
2. Let $N_0 = \{N_(), N_() | N \in N\}$.
3. Let $M_G = (V_G, E_G, L_G)$ is a directed labeled graph, where $L_G \subseteq (\Sigma_0 \cup N_0)$. This graph is created by the same way as described in [?] but it is not required that grammar should be in CNF. Let $x \in V_G$ and $y \in V_G$ is “start” and “final” vertices respectively. This graph may be treated as finite automaton, so it can be minimized and we can compute an ε -closure is input grammar contains ε productions. The graph M_G for our example:



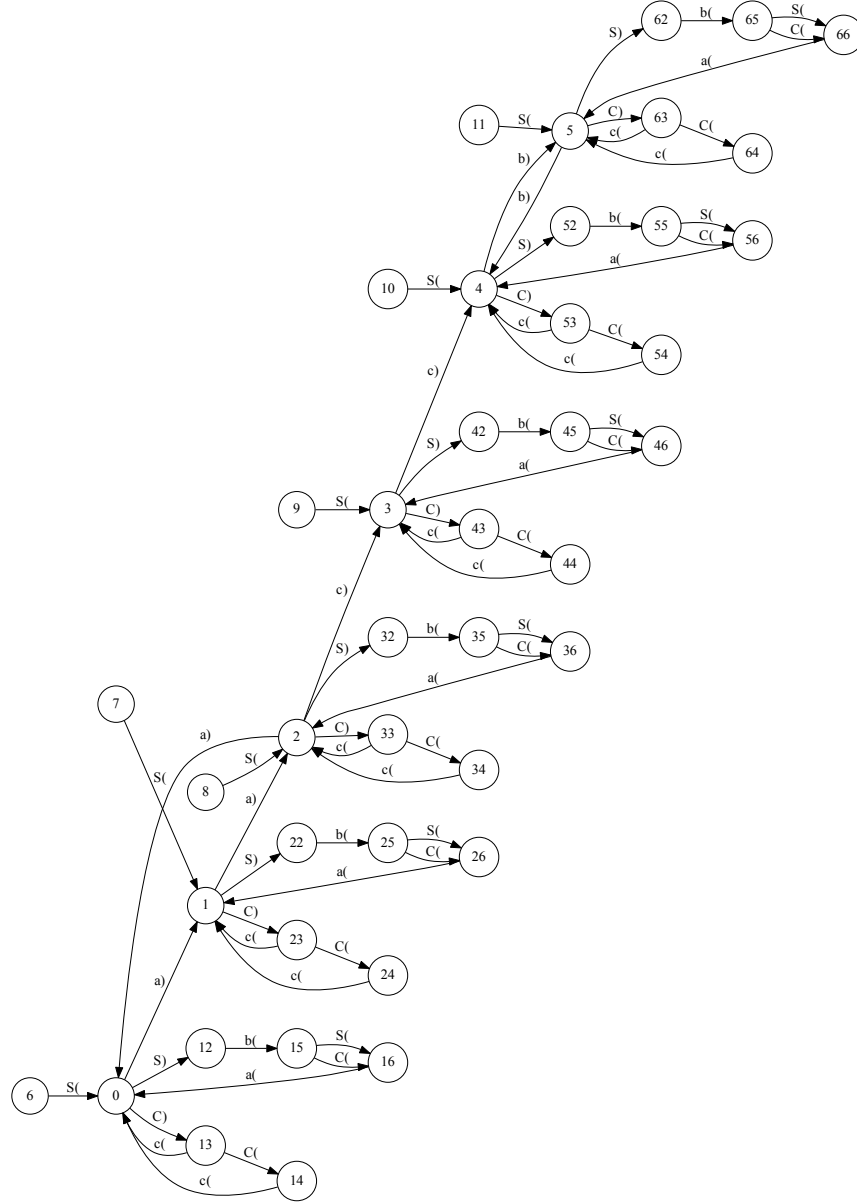
The minimized version:



4. For each $v \in V$ create M_G^v : unique instance of M_G .
5. New graph G' is a graph G where each label t replaced with t^i and some additional edges are created:

- For each $v \in V$ add an edge (v', S_ζ, v) .
- For each $v \in V$ and respective $M_{\mathcal{G}}^v$:
 - reattach all edges outgoing from x^v (“start” of $M_{\mathcal{G}}^v$) to v ;
 - reattach all edges incoming to y^v (“final” of $M_{\mathcal{G}}^v$) to v .

New input graph is ready:



6. New grammar $\mathcal{G}' = (\Sigma', N', P', S')$ where $\Sigma' = \Sigma_0 \cup N_0$, $N' = \{S'\}$, $P' = \{S' \rightarrow b_{\langle} S' b_{\rangle}; S' \rightarrow b_{\langle} b_{\rangle} \mid b_{\langle}, b_{\rangle} \in \Sigma'\} \cup \{S' \rightarrow S' S'\}$ is a set of productions, $S' \in N'$ is a start nonterminal.

Now, if $\text{CFPQ}(\mathcal{G}', G')$ contains pair (u'_0, v') such that $e = (u'_0, S_1, u'_1) \in E'$ — an extension edge (step 5, first subitem), then $(u'_1, v') \in \text{CFPQ}(\mathcal{G}, G)$. In our example we can find the next path: $7 \xrightarrow{S_1} 1 \xrightarrow{S_1} 22 \xrightarrow{b_1} 25 \xrightarrow{C_1} 26 \xrightarrow{a_1} 1 \xrightarrow{a_1} 2 \xrightarrow{C_1} 33 \xrightarrow{C_1} 34 \xrightarrow{c_1} 2 \xrightarrow{c_1} 3 \xrightarrow{C_1} 43 \xrightarrow{c_1} 3 \xrightarrow{c_1} 4 \xrightarrow{b_1} 5$. Edge $7 \xrightarrow{S_1} 1$ is an extension, so $(1,5)$ should be in $\text{CFPQ}(\mathcal{G}, G)$ and it is true.

References

- [1] Krishnendu Chatterjee, Bhavya Choudhary, and Andreas Pavlogiannis. 2017. *Optimal Dyck reachability for data-dependence and alias analysis*. Proc. ACM Program. Lang. 2, POPL, Article 30 (December 2017), 30 pages. DOI: <https://doi.org/10.1145/3158118>