Context-Free Path Querying Can be Fast if Cooked Properly

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ABSTRACT

Recently proposed matrix multiplication based algorithm for context-free path querying (CFPQ) offloads the most performance-critical parts onto boolean matrices multiplication. Thus, it is possible to achieve high performance of CFPQ by means of modern parallel hardware and software. In this paper, we provide results of empirical performance comparison of different implementations of this algorithm on both real-world data and synthetic data for the worst cases.

KEYWORDS

Context-free path querying, transitive closure, graph databases, linear algebra, context-free grammar, GPGPU, CUDA, boolean matrix, matrix multiplication

1 INTRODUCTION

Formal language constrained path querying, or formal language constrained path problem [?], is a graph analysis problem when formal languages are used as a constraints for navigational path queryes. Namely, in this approach concatenation of the labels along the path is treated as a word, and a specification of the language which should contain specific words is a constraint. While regular path querying (RPQ) is actively used in many different graph query languages and graph analysis engines, more expressive one, contxt-free path querying (CFPQ) [?] at the start stage and activly developed. Context-free constraints allow one to express such important class of queryes as *same generation quey* [?] which can not be expressed in terms of regular constraints.

Several algorithms for CFPQ based on such parsing techniques as (G)LL, (G)LR, and CYK are proposed recently [? ? ? ? ? ? ? ? ?]. But recent research by Jochem Kuijpers et.al. [?] shows that existing solutions are not applicable for real-world graph analysis because running time and memory consumption are poor. At the same time, Nikita Mishin et.al in [?] shows that matrix-based CFPQ algorithm can demonstrate good performance on real-world data. Matrix-based algorithm is proposed by Rustam Azimov [?] and offloads the most critical computations onto boolean matrices multiplication. As a result, it is easy to implement, and allows one to utilize modern massive-parallel hardware for CFPQ. But only algorithm performance without integration with graph storage is provided in the paper while J. Kuijpers provides evaluation of algorithms which are integrated with Neo4j[1] graph database. Also, in [?] matrix-based algorithm is evaluated in simple single-thread Java implementation, while N. Mishin shows that the most efficient implementation should utilizes high-performance matrix multiplication libraries which are highly parallel, or even utilize GPGPU. Thus, evaluation of matrix-based algorithm which is integrated with graph storage and implemented in appropriate way is required.

In this work we show that CFPQ in relational semantics (according Hellings [?]) can be fast enough to be applicable to real-world graph analysis. We use RedisGraph[2] [?] garph data base as a storage. This data base use adjacency matrices as arepresenataion of graph and GraphBLAS [?] for matrices manipualtion. These facts allow us to integrate matrix-based CFPQ algorithm to RedisGraph with minimal effort. We make the following contributions in this paper.

(1) We provide a number of implementations of the matrix multiplication based CFPQ algorithm which uses RedisGraph as a graph storage. The first implementation is CPU-based and utilize SuteSparse [?] implemenation of GraphBLAS API for matrices manipulation. The second implementation is GPGPU-based and include both existing implementation from [?] and our own CUSP[3]-based implenetation. The source code is available on GitHub: https://github.com/YaccConstructor/RedisGraph.
(2) We extend the dataset !!!
(3) We provide evaluation which shows that !!!.

2 MATRIX-BASED ALGORITHM FOR CFPQ

Matrix-based algorithm for CFPQ was proposed by Rustam Azimov [?]. This algorithm can be expressed in terms of operations over matrices boolean (see listing 1), and it is a sufficient advantage for implementation.

Here $D = (V, E)$ is the input graph and $G = (N, \Sigma, P)$ is the input grammar. For each matrix T^{A_i}, $T^{A_i}[i, j] = \texttt{true} \iff \exists \pi = v_i \dots v_j$—path in D, such that $A_i \overset{*}{\underset{G}{\Rightarrow}} \omega(\pi)$, where $\omega(\pi)$ is a word formed by the labels along the path π. Thus, this algorithm solves reachability problem, or, according to Hellings [?], processes CFPQs by using relational query semantics.

The performance-critical part of the algorithm is matrix boolean multiplication. Note, that we can apply the next optimization: we can skip update if the matrices T_{N_j} and T_{N_k} have not been changed at the previous iteration. Also, it is important for applications that real-world data is almost sparse, so it should be better solution to use linraries which manipulates with sparse matrices.

As we can see, CFPQ can be naturally reduced to linead algebra. Linear algebra for graph problems is an actively developed area. One of the most important result is a GraphBLAS

[1]Neo4j graph databaes web page: https://neo4j.com/. Access date: 12.11.2019.

[2]RedisGraph is a graph data base which is based on Property Graph Model. Project web page: https://oss.redislabs.com/redisgraph/. Access data: 12.11.2019.
[3]CUSP is an open source library for sparse matrix multiplication on GPGPU. Project site: https://cusplibrary.github.io/. Access date: 12.11.2019.

Listing 1 Context-free path quering algorithm

function CONTEXTFREEPATHQUERYING(D, G)
  $n \leftarrow$ the number of nodes in D
  $E \leftarrow$ the directed edge-relation from D
  $P \leftarrow$ the set of production rules in G
  $N \leftarrow$ the set of nonterminals in G
  $T \leftarrow \{T^{A_i} \mid A_i \in N, T^{A_i}$ is a matrix $n \times n$ in which each element is `false`$\}$
  for all $(i, x, j) \in E$ **do** ▷ Matrix initialization
    $B \leftarrow \{B_i \mid B_i \rightarrow x \in P\}$
    for $B_i \in B$ **do**
      $T^{B_i}_{i,j} \leftarrow$ `true`
  while any matrix in T is changing **do** ▷ Transitive closure calculation
    for $A_i \rightarrow A_j A_k \in P$ **do**
      $T^{A_i} \leftarrow T^{A_i} + (T^{A_j} \times T^{A_k})$
  return T

API which provides a way to operate over matrices and vectors over user-defined semirings. In this paper we use SuteSparse implementation of GraphBLAS and boolena semiring. All our implementations are based on the optimized version of the algorithm.

3 IMPLEMENTATION

Previous works show [? ?] that existing linear algebra libraries utilization is a right way to get high-performance CFPQ implementation in minimal effort. But non of these works do not provide evaluation with data storage, only pure time of algorithm execution was mesured.

We provide a number of implementations of matrix-based CFPQ algorithm. All of them a based on RedisGraph — we use RedisGraph as a storage and implement CFPQ as an extension by using provided mechanism. Note thet currenly we do not provide full integration with querying mechanism: one can not use Cypher, which uses in RedisGraph as a query language. Instead, in current omplementation query provided explicetely as an file with grammar in Chomsky normal form [?]. So, we can evaluate querying algorithms, but we should improve integration to make our solution applicable.

CPU-based implementation. Details on CPU implemenattion

GPGPU-based implementation. Details on GPGPU implemenattion

4 DATASET DESCRIPTION

In our evaluation we use combined dataset which contains the following parts.

- CFPQ_Data dataset which provided in[4] [?] and contains both syntethic and real-world graphs and queryes. Real-world data includes RDFs, syntatic cases include theoretical worst-case and random graphs.
- Dataset which provided in [?]. We integrate both Geospecies and Synthetic data sets into CFPQ_Data and use it in our evaluation.
- New bigger RDFs, such as *go-hierarchy* or *enzime* — parts of UniProt database[5]. In [?] was shown that matrix-based algorithm is performad enough to handle bigger RDFs than used in initial data sets, such as [?]. So, we add a number of big RDFs to CFPQ_Data and use them in our evaluation.

The variants of the *same generation query* [?] is used in almost all cases because it is an important example of real-world queries that are context-free but not regular. So, variations of the same generation query is used in out evaluaton. All queryes are added to the CFPQ_Data data set.

5 EVALUATION AND DISCUSSION

We evaluate all the described implementations on all the datasets and the queries presented. We compare our implementations with [?] and [?]. We measure full time of query execution, so all overhead on data preparing is incuded. Thus we can estimate applicability of matrix-based algrithm for real-world solutions.

For evaluation, we use a PC with Ubuntu 18.04 installed. It has Intel core !!! CPU, DDR4 32 Gb RAM, and Geforce !!! GPGPU with 8Gb RAM.

The results of the evaluation are summarized in the tables below. Time is measured in seconds unless specified otherwise. Note that for all implementations except our own we provide results form related paper. The cell is left blank if the time limit is exceeded, if there is not enough memory to allocate the data, or information is not available.

The results of the first dataset **[RDF]** are presented in table **??**. We can see, that in this case the running time of all our implementations is smaller than of the reference implementation, and all implementations but **[CuSprs]** demonstrate similar performance. It is obvious that performance improvement in comparison with the first implementation is huge and it is necessary to extend the dataset with new RDFs of the significantly bigger size.

Table 2: Evaluation results for the worst case

#V	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
16	0.032	< 1	0.008	0.002	0.027	0.309
32	0.118	0.001	0.034	0.008	0.136	0.441
64	0.476	0.041	0.133	0.032	0.524	0.988
128	2.194	0.226	0.562	0.129	2.751	3.470
256	15.299	1.994	3.088	0.544	11.883	15.317
512	121.287	23.204	13.685	2.499	43.563	102.269
1024	1593.284	528.521	88.064	19.357	217.326	1122.055
2048	-	-	-	325.174	-	-

Results of the theoretical worst case (**[Worst]** datatset) are presented in table 2. This case is really hard to process: even for a graph of 1024 vertices, the query evaluation time is greater than 10 seconds even for the most performant implementation. We can see, that the running time grows too fast with the number of vertices.

[4]CFPQ_Data data set GitHub repository: https://github.com/JetBrains-Research/CFPQ_Data. Access date: 12.11.2019.

[5]Protein sequences data base: https://www.uniprot.org/. RDFs with data are avalable here: ftp://ftp.uniprot.org/pub/databases/uniprot/current_release/rdf. Access date: 12.11.2019

Table 1: RDFs querying results (time in milliseconds)

RDF			Query G_4						Query G_5					
Name	#V	#E	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
atm-prim	291	685	3	2	2	1	5	269	1	< 1	1	< 1	2	267
biomed	341	711	3	5	2	1	5	283	4	< 1	1	< 1	5	280
foaf	256	815	2	9	2	< 1	5	270	1	< 1	1	< 1	2	263
funding	778	1480	4	7	4	1	5	279	2	< 1	3	< 1	4	274
generations	129	351	3	3	2	< 1	5	273	1	< 1	1	< 1	2	263
people_pets	337	834	3	3	3	1	7	284	1	< 1	1	< 1	3	277
pizza	671	2604	6	8	3	1	6	292	2	< 1	2	< 1	5	278
skos	144	323	2	4	2	< 1	5	273	< 1	< 1	1	< 1	2	265
travel	131	397	3	5	2	< 1	6	268	1	< 1	1	< 1	3	271
unv-bnch	179	413	2	4	2	< 1	5	266	1	< 1	1	< 1	3	266
wine	733	2450	7	6	4	1	7	294	1	< 1	3	< 1	3	281

Table 3: Sparse graphs querying results

Graph	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
G5k-0.001	10.352	0.647	0.113	0.041	0.216	5.729
G10k-0.001	37.286	2.395	0.435	0.215	1.331	35.937
G10k-0.01	97.607	1.455	0.273	0.138	0.763	47.525
G10k-0.1	601.182	1.050	0.223	0.114	0.859	395.393
G20k-0.001	150.774	11.025	1.842	1.274	6.180	-
G40k-0.001	-	97.841	11.663	8.393	37.821	-
G80k-0.001	-	1142.959	88.366	65.886	-	-

The next is the **[Sparse]** datatset presented in table **??**. The evaluation shows that sparsity of graphs (value of parameter p) is important both for implementations which use sparse matrices and for implementations which use dense matrices. Note that the behavior of the sparse matrices based implementation is as expected, but for dense matrices we can see, that more sparse graphs are processed faster. Reasons for such behavior demand further investigation. Note that we estimate only the query execution time, so it is hard to compare our results with the results presented in [**?**]. Nevertheless, the running time of our **[GPU_N]** implementation is significantly smaller than the one provided in [**?**].

The last dataset is **[Full]**, and results are shown in table **??**. As we expect, this case is very hard for sparse matrices based implementations: the running time grows too fast. This dataset also demonstrates the impact of the grammar size. Both queries specify the same constraints, but the grammar G_3 in CNF contains 2 times more rules then the grammar G_2, so, the running time for big graphs differs by more than twice.

Finally, we can conclude that GPGPU utilization for CFPQ can significantly improve performance, but more research on advanced optimization techniques should be done. On the other hand, the high-level implementation (**[GPU_Py]**) is comparable with other GPGPU-based implementations. So, it may be a balance between implementation complexity and performance. Highly optimized existing libraries can be of some use: the implementation based on m4ri is faster than the reference implementation and the other CPU-based implementation. Moreover, it is comparable with some GPGPU-based implementations in some cases. Sparse matrices utilization demands more thorough investigation. The main question is if we can create an efficient implementation for sparse boolean matrices multiplication.

6 CONCLUSION AND FUTURE WORK

We provide an CPU and GPGPU based context-free path querying implementations for RedisGraph and show that CFPQ can be fast enough to analize real-world data. But our implementations are on prototype stage and we should provide full integration of CFPQ to RedisGraph. First of all it is necessary to extend Cupher graph query language, which uses in RedisGraph, to support respective syntax for context-free constraints specification. There is a proposal whish describes such syntax extension[6] and we plan to support proposed sintax in libcypher-parser[7] which uses in RedisGraph.

In current version we use CUSP matrix multiplication library for GPGPU utilization, but it may be better to use GraphBLAST[8] [**?**] — Gunrock[9] [**?**] based implementation of GraphBLAS API for GPGPU. Firs of all, we should evaluate GraphBlast based implementation of CFPQ. Also, we should investigate to implement multi-GPU support for GraphBlast, because it should improve performance of huge real-world data processing.

Our implementations calculate queryes in respect to relational semantics, but in sume cases it is necessary to provide a path which satisfied constraints. As we know, matrix based algorithm for single path or all paths semantix is not prvided yet, and it is a direction for future research.

Another important question for future research is how to update query result dynamically when data changes. Mechanism for result updating allows one to recalculate qury faster and use result as an index for other queryes.

Also, futer improvements of the dataset are requred. For example, it is necessary to include real-world cases from static code analysis [**?**].

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[6]Proposal with path pattern syntax for openCypher: https://github.com/thobe/openCypher/blob/rpq/cip/1.accepted/CIP2017-02-06-Path-Patterns.adoc. It is shown that context-free constraints are expressible in proposrd syntax. Access date: 12.11.2019

[7]Web page of libcypher-parser project: http://cleishm.github.io/libcypher-parser/. Access date: 12.11.2019

[8]GraphBLAST project: https://github.com/gunrock/graphblast. Access date: 12.11.2019.

[9]Gunrock project web page: https://gunrock.github.io/docs/. Access date: 12.11.2019.

Table 4: Free scale graphs querying results

Graph	CPU		m4ri		CUSP		neo4j	
	Time	Mem	Time	Mem	Time	Mem	Time	Mem
G(100,1)	0.007	0.002	0.002	< 1	0.003	0.278	0.023	0.076
G(100,3)	0.040	0.003	0.002	0.001	0.004	0.279	0.105	0.098
G(100,5)	0.480	0.003	0.003	0.001	0.004	0.329	1.636	0.094
G(100,10)	3.741	0.007	0.005	0.001	0.006	0.571	13.071	0.106
G(500,1)	40.309	0.063	0.019	0.003	0.017	1.949	93.676	0.108
G(500,3)	651.343	0.366	0.125	0.038	0.150	99.651	1205.421	0.851
G(500,5)	-	1.932	0.552	0.315	0.840	1029.042	-	4.690
G(500,10)	-	33.236	7.252	5.314	15.521	-	-	70.823
G(2500,1)	40.309	0.063	0.019	0.003	0.017	1.949	93.676	0.108
G(2500,3)	651.343	0.366	0.125	0.038	0.150	99.651	1205.421	0.851
G(2500,5)	-	1.932	0.552	0.315	0.840	1029.042	-	4.690
G(2500,10)	-	360.035	58.751	44.611	129.641	-	-	775.765
G(10000,1)	40.309	0.063	0.019	0.003	0.017	1.949	93.676	0.108
G(10000,3)	651.343	0.366	0.125	0.038	0.150	99.651	1205.421	0.851
G(10000,5)	-	1.932	0.552	0.315	0.840	1029.042	-	4.690
G(10000,10)	-	1292.81	256.579	190.343	641.260	-	-	-

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