

# The Composition of Dense Neural Networks and Formal Grammars for Secondary Structure Analysis

Polina Lunina, **Semyon Grigorev**

JetBrains Research, Programming Languages and Tools Lab  
Saint Petersburg University

February 24, 2019

# Long Sequences Analysis

CACATGGAGAGTTTGA . . . CTGGATCACCTCCTTT  
~1500 symbols

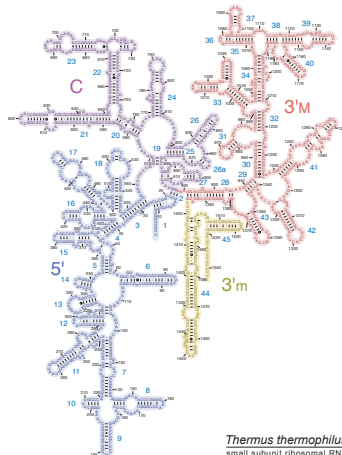
- Classification

# Long Sequences Analysis

CACATGGAGAGTTTGA...CTGGATCACCTCCTTT

~1500 symbols

- Classification
  - ▶ Secondary structure handling

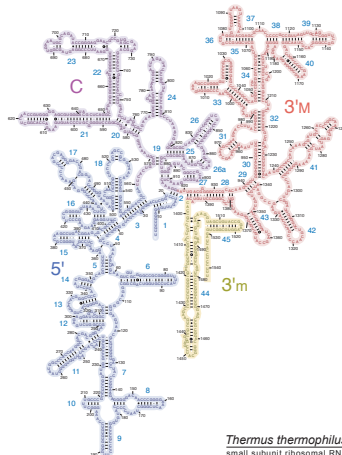


# Long Sequences Analysis

CACATGGAGAGTTTGA . . . CTGGATCACCTCCTTT

~1500 symbols

- Classification
  - ▶ Secondary structure handling
- Metagenomic assembly processing
  - ▶ Filter out chimeric sequences
  - ▶ Secondary structure handling



# Proposed Solution: Parsing + Artificial Neural Network

- Use parsing to extract features, not to model secondary structure
  - ▶ As compared to the classical way of probabilistic CF grammars utilization

# Proposed Solution: Parsing + Artificial Neural Network

- Use parsing to extract features, not to model secondary structure
  - ▶ As compared to the classical way of probabilistic CF grammars utilization
- Formal grammars as secondary structure description
- Parsing as features extraction
- Artificial neural network as probabilistic model for features processing

# Solution Structure

## Grammar

Fixed formal grammar (not necessarily context-free) describes features of secondary structure and can be tuned to increase the quality of result.

## Sequences

Each sequence is treated as a text in  $\{A, C, G, T\}$  alphabet.

## Result of classification

## Parser

Parser extracts features of the given sequence secondary structure. Implementation of parsing algorithm is based on matrix multiplications (Valiant, Okhotin) and utilizes GPGPU.

## Neural Network

Dense neural network with more than 10 dense layers. Aggressive dropout and batch normalization for learning process stabilization. Typical building block:

Dropout (75%)	input: 1024 output: 1024
------------------	-----------------------------

Dense	input: 1024 output: 1024
-------	-----------------------------

BatchNormalization	input: 1024 output: 1024
--------------------	-----------------------------

Activation (relu)	input: 1024 output: 1024
----------------------	-----------------------------

## Matrices

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Parsing result is (0-1) matrix  $M$  which represents secondary structure features for sequence  $\omega$ :

$$M[i, j] = 1 \iff s1 \xrightarrow{*} \omega[i, j], \text{ and } 0 \text{ otherwise.}$$

## Vectors

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\downarrow$$
$$[0, 1, 0, 1, 0, 1, 0, 0, 1, 0]$$

$$\downarrow$$
$$[84, 128]$$

Line-by-line compressed matrix representation: sequence of 8 cells (bits) is compressed into a byte. Bottom left triangle of the matrix is always empty, so can be ignored.

# Solution Structure

## Grammar

Fixed formal grammar (not necessarily context-free) describes features of secondary structure and can be tuned to increase the quality of result.

## Sequences

Each sequence is treated as a text in  $\{A, C, G, T\}$  alphabet.

## Result of classification

## Parser

Parser extracts features of the given sequence secondary structure. Implementation of parsing algorithm is based on matrix multiplications (Valiant, Okhotin) and utilizes GPGPU.

## Neural Network

Dense neural network with more than 10 dense layers. Aggressive dropout and batch normalization for learning process stabilization. Typical building block:

Dropout (75%)	input: 1024
	output: 1024

Dense	input: 1024
	output: 1024

BatchNormalization	input: 1024
	output: 1024

Activation (relu)	input: 1024
	output: 1024

## Matrices

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Parsing result is (0-1) matrix  $M$  which represents secondary structure features for sequence  $\omega$ :

$$M[i, j] = 1 \iff s1 \xrightarrow{*} \omega[i, j], \text{ and } 0 \text{ otherwise.}$$

## Vectors

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\downarrow$$
$$[0, 1, 0, 1, 0, 1, 0, 0, 1, 0]$$

$$\downarrow$$
$$[84, 128]$$

Line-by-line compressed matrix representation: sequence of 8 cells (bits) is compressed into a byte. Bottom left triangle of the matrix is always empty, so can be ignored.



# Solution Structure

## Grammar

Fixed formal grammar (not necessarily context-free) describes features of secondary structure and can be tuned to increase the quality of result.

## Sequences

Each sequence is treated as a text in  $\{A, C, G, T\}$  alphabet.

## Result of classification

## Parser

Parser extracts features of the given sequence secondary structure. Implementation of parsing algorithm is based on matrix multiplications (Valiant, Okhotin) and utilizes GPGPU.

## Neural Network

Dense neural network with more than 10 dense layers. Aggressive dropout and batch normalization for learning process stabilization. Typical building block:

Dropout (75%)	input: 1024 output: 1024
------------------	-----------------------------

Dense	input: 1024 output: 1024
-------	-----------------------------

BatchNormalization	input: 1024 output: 1024
--------------------	-----------------------------

Activation (relu)	input: 1024 output: 1024
----------------------	-----------------------------

## Matrices

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Parsing result is (0-1) matrix  $M$  which represents secondary structure features for sequence  $\omega$ :

$$M[i, j] = 1 \iff s1 \xrightarrow{*} \omega[i, j], \text{ and } 0 \text{ otherwise.}$$

## Vectors

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\downarrow$$
$$[0, 1, 0, 1, 0, 1, 0, 0, 1, 0]$$

$$\downarrow$$
$$[84, 128]$$

Line-by-line compressed matrix representation: sequence of 8 cells (bits) is compressed into a byte. Bottom left triangle of the matrix is always empty, so can be ignored.

# Solution Structure

## Grammar

Fixed formal grammar (not necessarily context-free) describes features of secondary structure and can be tuned to increase the quality of result.

## Sequences

Each sequence is treated as a text in  $\{A, C, G, T\}$  alphabet.

## Result of classification

## Parser

Parser extracts features of the given sequence secondary structure. Implementation of parsing algorithm is based on matrix multiplications (Valiant, Okhotin) and utilizes GPGPU.

## Neural Network

Dense neural network with more than 10 dense layers. Aggressive dropout and batch normalization for learning process stabilization. Typical building block:

Dropout (75%)	input: 1024
	output: 1024

Dense	input: 1024
	output: 1024

BatchNormalization	input: 1024
	output: 1024

Activation (relu)	input: 1024
	output: 1024

## Matrices

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Parsing result is (0-1) matrix  $M$  which represents secondary structure features for sequence  $\omega$ :

$$M[i, j] = 1 \iff s1 \xrightarrow{*} \omega[i, j], \text{ and } 0 \text{ otherwise.}$$

## Vectors

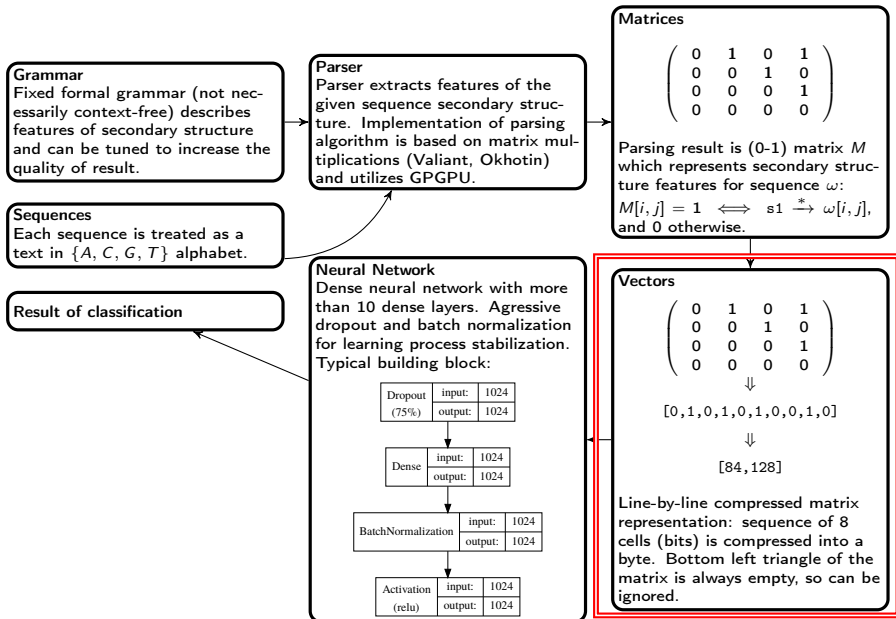
$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$\downarrow$   
[0,1,0,1,0,1,0,0,1,0]

$\downarrow$   
[84,128]

Line-by-line compressed matrix representation: sequence of 8 cells (bits) is compressed into a byte. Bottom left triangle of the matrix is always empty, so can be ignored.

# Solution Structure



# Solution Structure

## Grammar

Fixed formal grammar (not necessarily context-free) describes features of secondary structure and can be tuned to increase the quality of result.

## Sequences

Each sequence is treated as a text in  $\{A, C, G, T\}$  alphabet.

## Result of classification

## Parser

Parser extracts features of the given sequence secondary structure. Implementation of parsing algorithm is based on matrix multiplications (Valiant, Okhotin) and utilizes GPGPU.

## Neural Network

Dense neural network with more than 10 dense layers. Aggressive dropout and batch normalization for learning process stabilization. Typical building block:

Dropout (75%)	input: 1024 output: 1024
------------------	-----------------------------

Dense	input: 1024 output: 1024
-------	-----------------------------

BatchNormalization	input: 1024 output: 1024
--------------------	-----------------------------

Activation (relu)	input: 1024 output: 1024
----------------------	-----------------------------

## Matrices

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Parsing result is (0-1) matrix  $M$  which represents secondary structure features for sequence  $\omega$ :

$M[i, j] = 1 \iff s1 \xrightarrow{*} \omega[i, j]$ ,  
and 0 otherwise.

## Vectors

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$\downarrow$   
[0,1,0,1,0,1,0,0,1,0]

$\downarrow$   
[84,128]

Line-by-line compressed matrix representation: sequence of 8 cells (bits) is compressed into a byte. Bottom left triangle of the matrix is always empty, so can be ignored.

# Solution Structure

## Grammar

Fixed formal grammar (not necessarily context-free) describes features of secondary structure and can be tuned to increase the quality of result.

## Sequences

Each sequence is treated as a text in  $\{A, C, G, T\}$  alphabet.

## Result of classification

## Parser

Parser extracts features of the given sequence secondary structure. Implementation of parsing algorithm is based on matrix multiplications (Valiant, Okhotin) and utilizes GPGPU.

## Neural Network

Dense neural network with more than 10 dense layers. Aggressive dropout and batch normalization for learning process stabilization. Typical building block:

Dropout (75%)	input: 1024
	output: 1024

Dense	input: 1024
	output: 1024

BatchNormalization	input: 1024
	output: 1024

Activation (relu)	input: 1024
	output: 1024

## Matrices

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

Parsing result is (0-1) matrix  $M$  which represents secondary structure features for sequence  $\omega$ :

$$M[i, j] = 1 \iff s1 \xrightarrow{*} \omega[i, j], \text{ and } 0 \text{ otherwise.}$$

## Vectors

$$\begin{pmatrix} 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\downarrow$$
$$[0, 1, 0, 1, 0, 1, 0, 0, 1, 0]$$

$$\downarrow$$
$$[84, 128]$$

Line-by-line compressed matrix representation: sequence of 8 cells (bits) is compressed into a byte. Bottom left triangle of the matrix is always empty, so can be ignored.

# Grammar

```
s1: stem<s0>
any_str: any_smb*[2..10]
any_smb: A | T | C | G
stem1<s>:          \\ stem of height exactly 1
            A s T | T s A | C s G | G s C
stem3<s>:          \\ stem of height exactly 3
            stem1< stem1< stem1<s> > >
stem<s>:           \\ stem of height 3 or more
            A stem<s> T
            | T stem<s> A
            | C stem<s> G
            | G stem<s> C
            | stem3<s>
s0: any_str | any_str stem<s0> s0
```

# Grammar

```
s1: stem<s0>
```

```
any_str: any_smb*[2..10]
```

```
any_smb: A | T | C | G
```

```
stem1<s>:                \\ stem of height exactly 1  
    A s T | T s A | C s G | G s C
```

```
stem3<s>:                \\ stem of height exactly 3  
    stem1< stem1< stem1<s> > >
```

```
stem<s>:                \\ stem of height 3 or more  
    A stem<s> T  
    | T stem<s> A  
    | C stem<s> G  
    | G stem<s> C  
    | stem3<s>
```

```
s0: any_str | any_str stem<s0> s0
```

# Grammar

```
s1: stem<s0>
```

```
any_str: any_smb*[2..10]
```

```
any_smb: A | T | C | G
```

```
stem1<s>:                \\ stem of height exactly 1  
    A s T | T s A | C s G | G s C
```

```
stem3<s>:                \\ stem of height exactly 3  
    stem1< stem1< stem1<s> > >
```

```
stem<s>:                \\ stem of height 3 or more  
    A stem<s> T  
    | T stem<s> A  
    | C stem<s> G  
    | G stem<s> C  
    | stem3<s>
```

```
s0: any_str | any_str stem<s0> s0
```



# Grammar

s1: stem<s0>

any\_str: any\_smb\*[2..10]

any\_smb: A | T | C | G

stem1<s>:                   \\ stem of height exactly 1  
          A s T | T s A | C s G | G s C

stem3<s>:                   \\ stem of height exactly 3  
          stem1< stem1< stem1<s> > >

stem<s>:                   \\ stem of height 3 or more  
          A stem<s> T  
          | T stem<s> A  
          | C stem<s> G  
          | G stem<s> C  
          | stem3<s>

s0: any\_str | any\_str stem<s0> s0

# Grammar

```
s1: stem<s0>
any_str: any_smb*[2..10]
any_smb: A | T | C | G
stem1<s>:          \\ stem of height exactly 1
             A s T | T s A | C s G | G s C
stem3<s>:          \\ stem of height exactly 3
             stem1< stem1< stem1<s> > >
stem<s>:          \\ stem of height 3 or more
             A stem<s> T
             | T stem<s> A
             | C stem<s> G
             | G stem<s> C
             | stem3<s>
s0: any_str | any_str stem<s0> s0
```

# Grammar

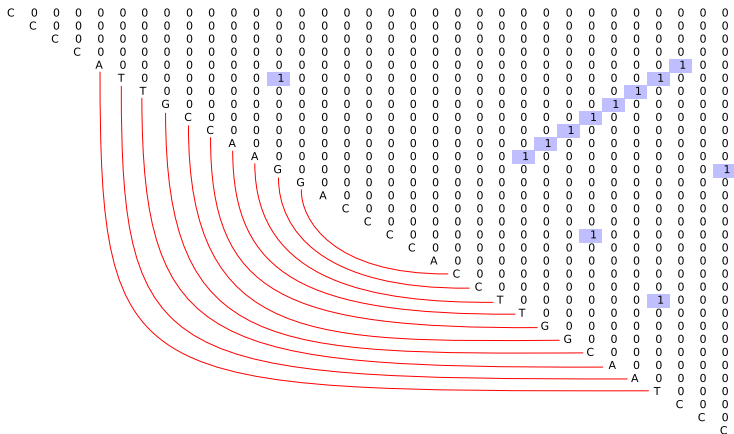
```
s1: stem<s0>
any_str: any_smb*[2..10]
any_smb: A | T | C | G
stem1<s>:          \\ stem of height exactly 1
            A s T | T s A | C s G | G s C
stem3<s>:          \\ stem of height exactly 3
            stem1< stem1< stem1<s> > >
stem<s>:          \\ stem of height 3 or more
            A stem<s> T
            | T stem<s> A
            | C stem<s> G
            | G stem<s> C
            | stem3<s>
s0: any_str | any_str stem<s0> s0
```

# Grammar

```
s1: stem<s0>
any_str: any_smb*[2..10]
any_smb: A | T | C | G
stem1<s>:          \\ stem of height exactly 1
             A s T | T s A | C s G | G s C
stem3<s>:          \\ stem of height exactly 3
             stem1< stem1< stem1<s> > >
stem<s>:           \\ stem of height 3 or more
             A stem<s> T
             | T stem<s> A
             | C stem<s> G
             | G stem<s> C
             | stem3<s>
s0: any_str | any_str stem<s0> s0
```

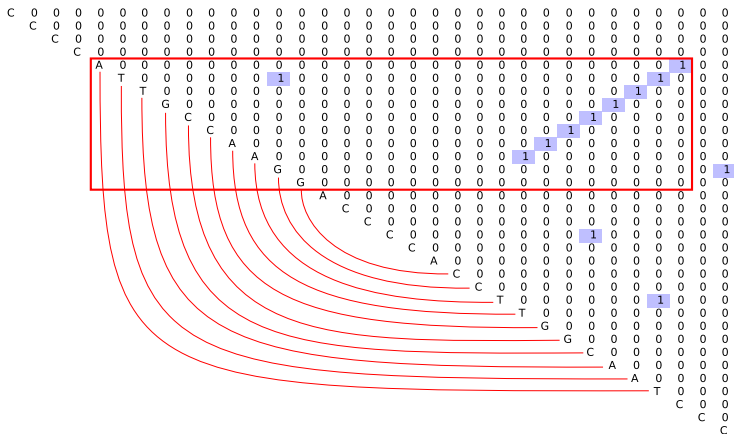
# Example 1: Stem

CCCCATTGCCAAGGACCCACCTTGGCAATCCC



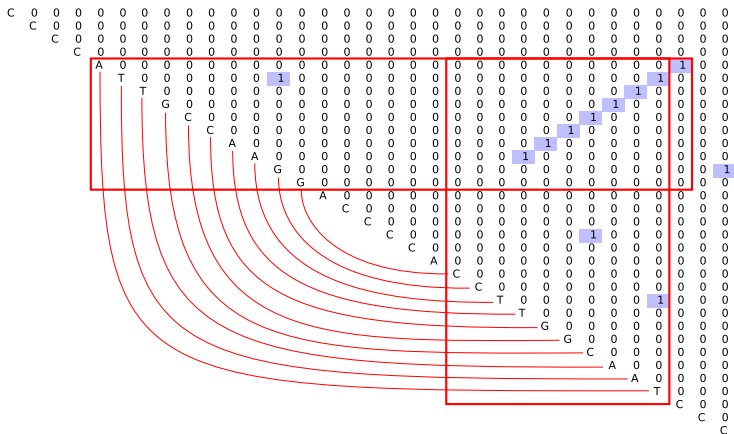
# Example 1: Stem

CCCCATTGCCAAGGACCCACCTTGGCAATCCC



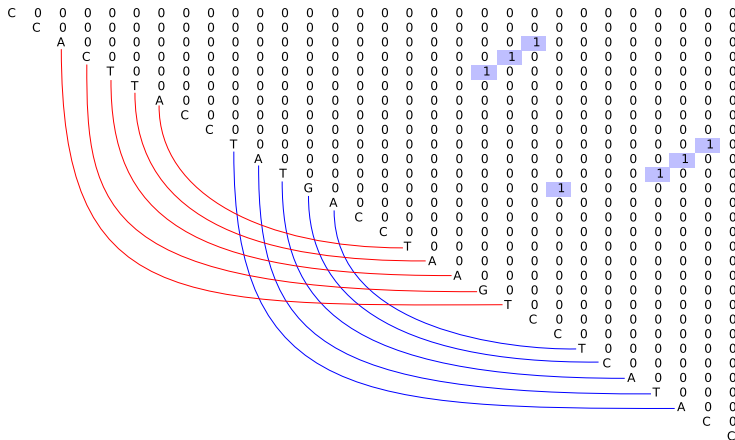
# Example 1: Stem

CCCCATTGCCAAGGACCCACCTTGGCAATCCC



## Example 2: Pseudoknot

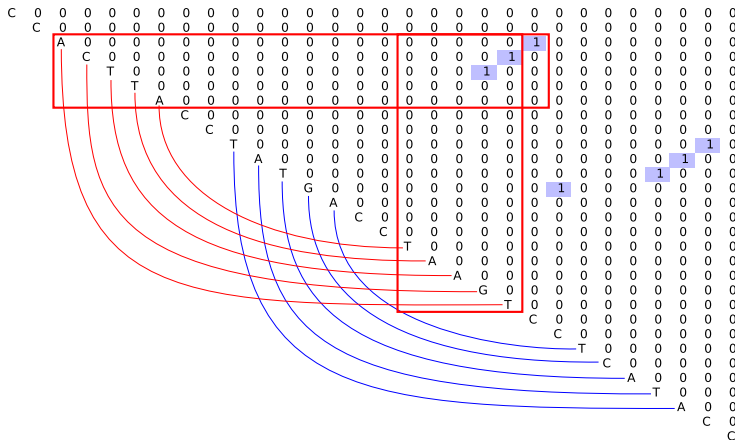
CCACTTACCTATGACCTAAGTCCTCATACC





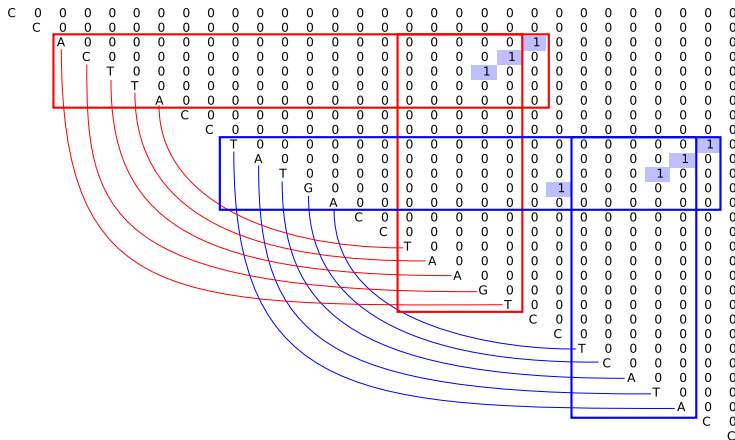
## Example 2: Pseudoknot

CCACTTACCTATGACCTAAGTCCTCATACC



## Example 2: Pseudoknot

CCACTTACCTATGACCTAAGTCCTCATACC

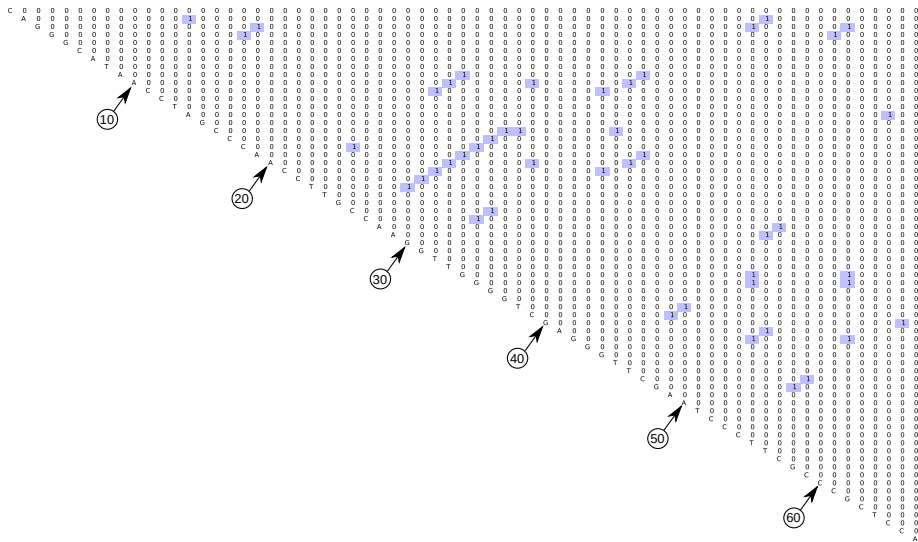


## Example 3: real tRNA

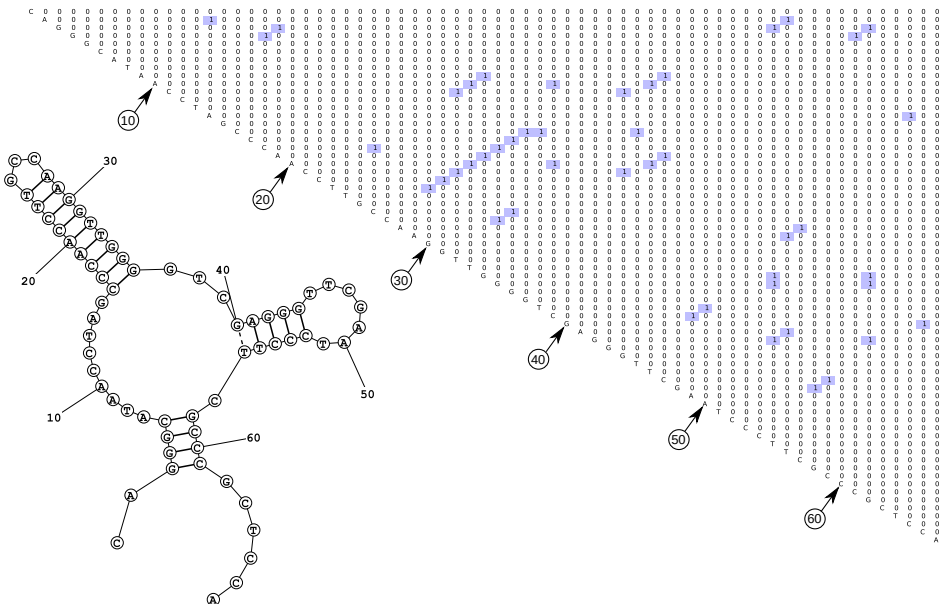
CAGGGCATAACCTAGCCCAACCTTGCCAAGG  
TTGGGGTCGAGGGTTCGAATCCCTTCGCCCCTCCA

- *Novosphingobium aromaticivorans* DSM 12444  
chr.trna57-GlyGCC(268150-268084) Gly (GCC) 67 bp Sc: 22.9, from  
GtRNAdb
- Predicted secondary structures are given by using the Fold Web Server  
with default settings

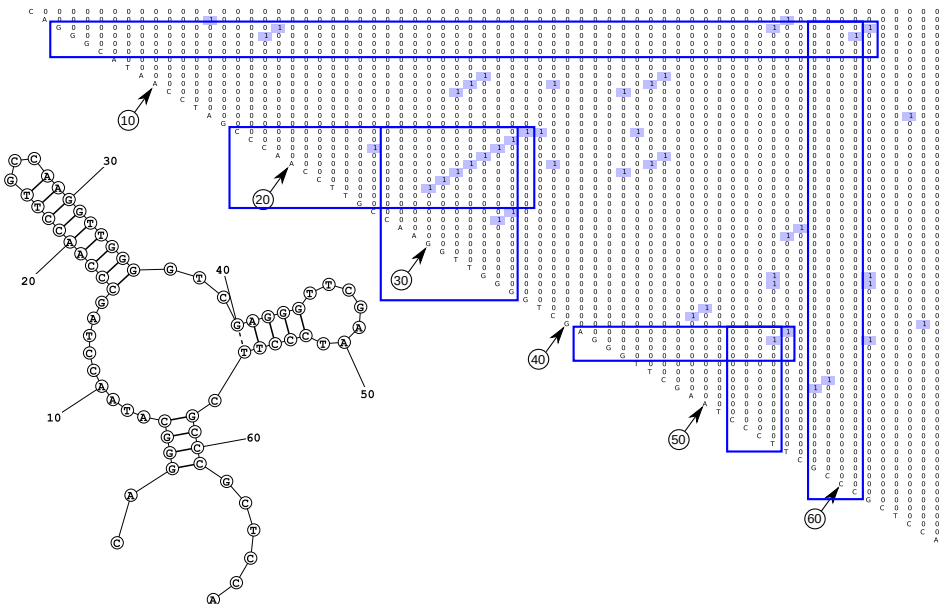
# Example 3: real tRNA



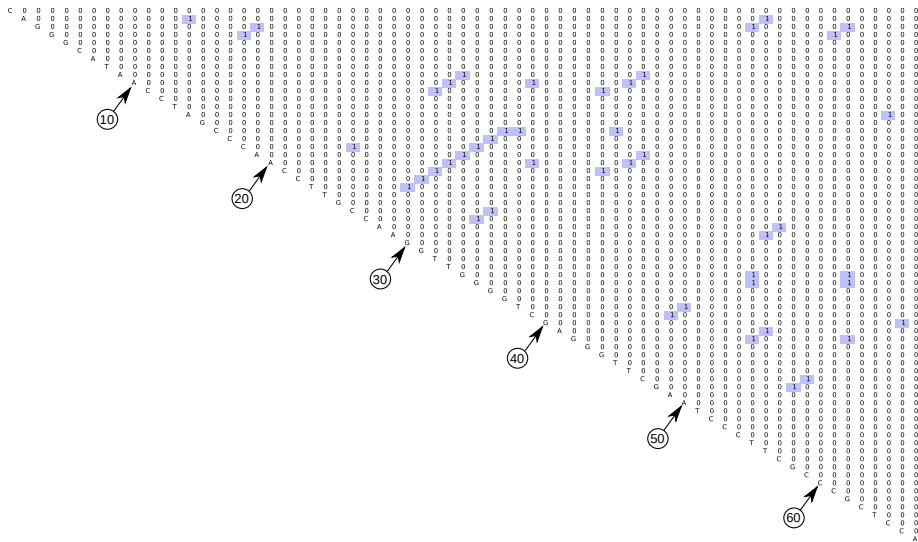
# Example 3: real tRNA



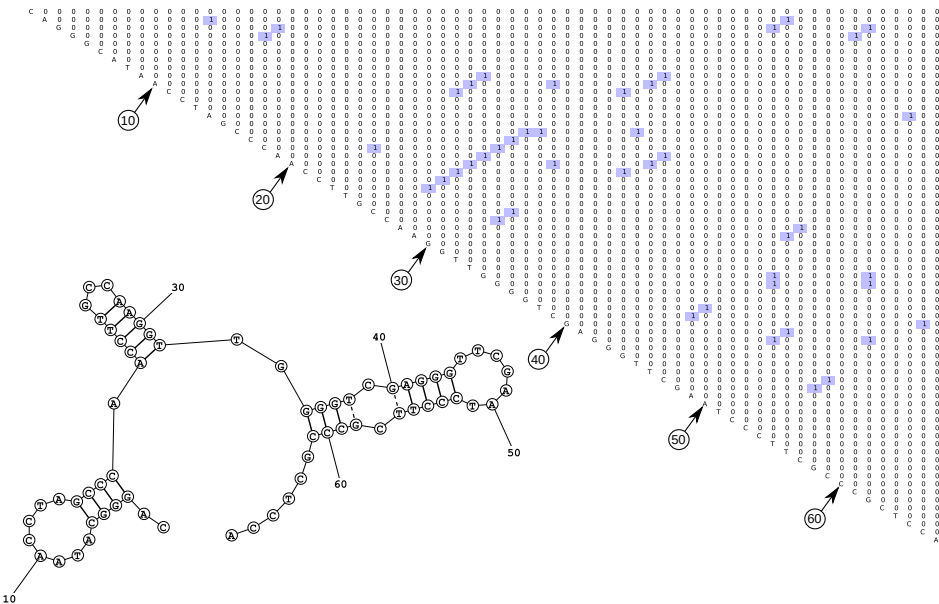
# Example 3: real tRNA



# Example 3: real tRNA

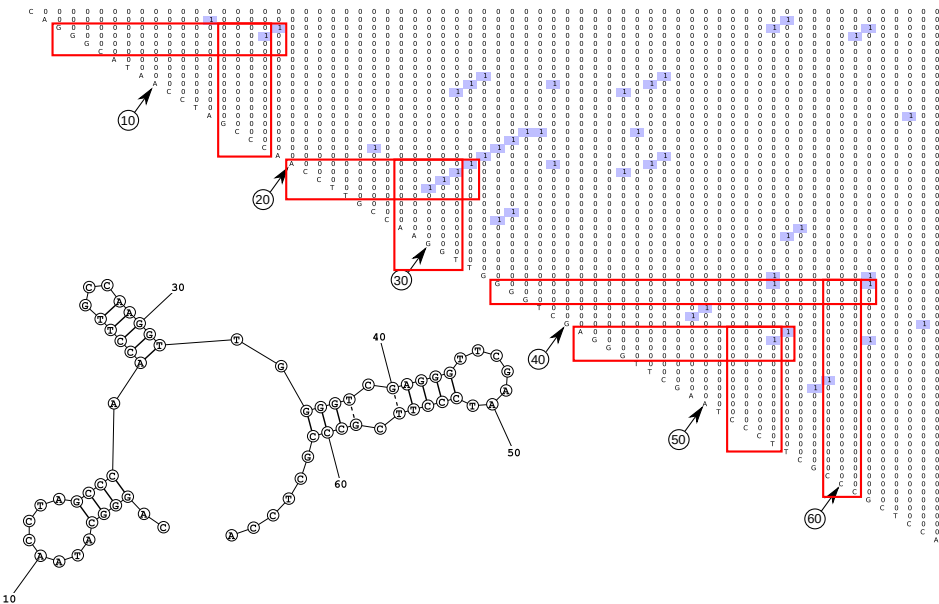


### Example 3: real tRNA

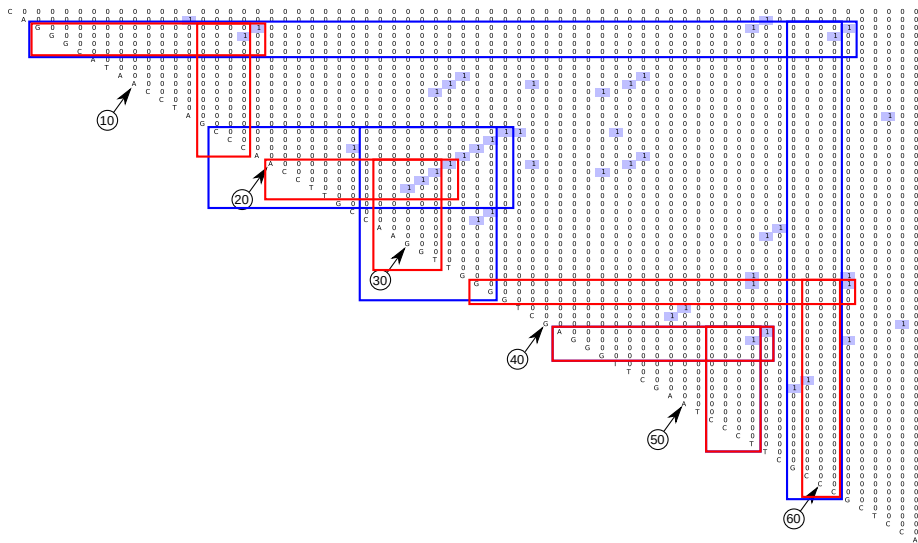




# Example 3: real tRNA



# Example 3: real tRNA



- Dense neural network
  - ▶ About 10 dense layers
  - ▶ ReLU activation function
- Aggressive dropout (up to 90% after each layer) and batch normalization (after each layer) for learning stabilization

# Evaluation: 16s rRNA detection

- Training data
  - ▶ All sequences are 512 symbols in length
  - ▶ Totally up to 310000 sequences
  - ▶ Positive: random subsequences of 16s rRNA sequences from the Green Genes database
  - ▶ Negative: random subsequences of full genes from the NCBI database
- Validation set: up to 81000 sequences
- Accuracy is 90% after training

# Evaluation: tRNA classification

- Training data: 50000 sequences from GtRNADB
- Input data normalization
  - ▶ Set the upper bound of sequence length to 220
  - ▶ First  $k$  symbols of the input are tRNA and the rest  $220 - k$  symbols are filled by the special symbol
- Validation set: 217984 sequences for prokaryotes and 62656 sequences for eukaryotes from tRNADB-CE 3
- Accuracy is 97% after training
  - ▶ 3276 of eukaryotes (5.23% of all eukaryotes in the validation set) are classified as prokaryotes
  - ▶ 4373 of prokaryotes (2.01% of all prokaryotes in the validation set) are classified as eukaryotes

- Create DNN which does not require input parsing
  - ▶ Create a training set of matrices using parsing
  - ▶ Train the network  $NN_1$  which can handle vectorized matrices
  - ▶ Create network  $NN_2$  by extending  $NN_1$  with a set of layers which convert the sequence to input for  $NN_1$
  - ▶ Train  $NN_2$ , weights of layers from  $NN_1$  are fixed
- Try to use other types of neural networks: bitwise networks, convolutional networks
- Do more evaluation
- Perform comparison with other tools

# Conclusion

- We propose the approach to handle secondary structure of sequences
  - ▶ Parser is only a features extractor
  - ▶ Parsing result contains all possible foldings (w.r.t. grammar) including impossible in practice
  - ▶ Grammar is a parameter: one can add a G-T pair, change minimal height of the stem, etc
  - ▶ It is possible to detect features which are not expressible in the language class in use
  - ▶ It is possible to use more expressive classes of formal languages
    - ★ Conjunctive and boolean grammars
    - ★ Multiple context-free grammars
- This approach can be applied for real data processing

- Semyon Grigorev:
  - ▶ s.v.grigoriev@spbu.ru
  - ▶ Semen.Grigorev@jetbrains.com
- Polina Lunina:
  - ▶ lunina\_polina@mail.ru
- Trained models: <https://github.com/YaccConstructor/YC.Bio>

Thanks!