

# Parser-Combinators for Context-Free Path Querying

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## ABSTRACT

A transparent integration of a domain-specific language for specification of context-free path queries (CFPQs) into a general-purpose programming language as well as static checking of errors in queries may greatly simplify the development of applications utilizing CFPQs. Such techniques as LINQ and ORM can be used for the integration, but they have issues with flexibility: query decomposition and reusing of subqueries are a challenge. Adaptation of parser combinators technique for paths querying may solve these problems. Conventional parser combinators process linear input and only the Trails library is known to apply this technique for path querying. Trails suffers the common parser combinators issue: it does not support left-recursive grammars and also experiences problems in cycles handling. We demonstrate that it is possible to create general parser combinators for CFPQ which support arbitrary context-free grammars and arbitrary input graphs. We implement a library of such parser combinators and show that it is applicable for realistic tasks.

## CCS CONCEPTS

• **Information systems** → **Graph-based database models**; **Query languages for non-relational engines**; • **Software and its engineering** → **Functional languages**; • **Theory of computation** → **Grammars and context-free languages**;

## KEYWORDS

Graph Databases, Language-Constrained Path Problem, Context-Free Path Querying, Parser Combinators, Generalized LL, GLL, Neo4J, Scala

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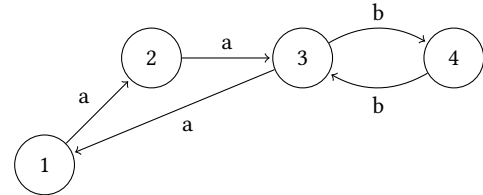
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## 1 INTRODUCTION

One useful type of graph queries is language-constrained path queries [2] which mean that constraints are formulated by using formal languages formalisms such as grammars. For example, suppose that one have a graph presented in fig. 2 and want to find all paths which have a form  $a^n b^n, n > 0$ . It is possible to specify this constraint in terms of context-free grammar  $G$ , which is presented in fig 1.

$$\begin{aligned} S &\rightarrow a S b \\ S &\rightarrow a b \end{aligned}$$

**Figure 1: Context-free grammar  $G$  for the language  $L = \{a^n b^n | n > 0\}$**



**Figure 2: An example of input graph**

There are several languages for graph traversing/querying which support constraints formulated in terms of regular languages. For example SPARQL [24], Cypher<sup>1</sup>, and Gremlin [29]. In this work, we are focused on context-free path queries (CFPQs) which use context-free languages for constraints specification and are used in bioinformatics [33], static code analysis [3, 23, 26, 36, 40], and RDF processing [39]. There are a lot of problem-specific solutions and theoretical research on CFPQs [1, 7–9, 20, 28, 33, 37]. Among them, cSPARQL [39] is a single known graph query language to support CF constraints. Generic solution for the integration of CFPQs into general-purpose languages is not discussed enough.

When one develops a data-centric application, one wants to use a general purpose programming language and have a transparent and native access to data sources. String-embedded DSLs is one

<sup>1</sup>Cypher language web page: <https://neo4j.com/developer/cypher-query-language/>. Access date: 16.01.2018

way to do it. It utilizes a driver to execute a query written as a string and to return a possibly untyped result. This approach has serious drawbacks. First of all, a DSL may require additional knowledge from a developer. Moreover, a string-embedded language itself is a source of possible errors and vulnerabilities, static detection of which is very difficult [4]. In trying to solve these issues, such special techniques as Object Relationship Mapping (ORM) or Language Integrated Query (LINQ) [5, 15, 19] were created. Unfortunately, they still experience difficulties with flexibility: for example with the query decomposition and the reusing of subqueries. In this paper, we propose a transparent and natural integration of CFPQs into a general-purpose language.

Note that CFPQs is applicable not only for graph data base querying but also for static code analysis (with name *context-free language reachability framework* or *IFDS framework*). CFPQ and context-free language reachability (CFL-reachability) is a different names of one thing: the first used mostly in database community and the second one in static code analysis. In 1995 Thomas Reps shows that the wide range of static code analysis problems can be formulated in terms of CFL-reachability in graph [26, 27]. This framework is widely used for solving different problems [6, 10, 23, 34, 36, 40] and in domain specific languages, like the Flix [17]. For software development it is more more convinient way to have an generic integrated framework (library) for general-purpose programming language to avoid integration problems. Our solution may be use as a core of such framework because provide generic (problem and domain independent) mechanism for CFPQs evaluation.

It is necessary to find an appropriate technique for integration of context-free language specification into general-purpose programming languages. One natural way to specify a language is to specify its formal grammar which can be done by using a special DSL based, for example, on EBNF-like notation [35]. The classical alternative way is parser combinators [11] which provide all required features, including transparent integration, compile-time checks of correctness, high-level techniques for generalization.

An idea to use combinators for graph traversing has already been proposed in [14], but the solution presented provides only approximated handling of cycles in the input graph and does not support left-recursive grammars. Authors pointed out that the idea described is very similar to the classical parser combinators, but the language class supported or restrictions are not discussed. This point is very important, because conventional combinators implement top-down parsing and cannot handle left-recursive and ambiguous grammars.

In [12], authors demonstrate a set of parser combinators which can handle arbitrary context-free grammars by using ideas of Generalized LL [30] (GLL). Meerkat<sup>2</sup> parser combinators library is based on [12] and provides result of parsing in a compact form as Shared Packed Parse Forest [25] (SPPF). It is showed that SPPF is a suitable finite structural representation of a CFPQ query result, even if the set of paths is infinite [7], which can be used for paths extraction, queries debugging and processing of result.

In this paper, we show how to compose these ideas and present the parser combinators for CFPQ which can handle arbitrary

context-free grammars and provide a structural representation of the result. We make the following contributions in this paper.

- (1) We show that it is possible to create parser combinators for context-free path querying which work on both arbitrary context-free grammars and arbitrary graphs and provide a finite structural representation of the query result.
- (2) We provide the implementation of the parser combinators library in Scala. This library provides an integration to Neo4j<sup>3</sup> graph database. The source code is available on GitHub: <https://github.com/YaccConstructor/Meerkat>.
- (3) We perform an evaluation on realistic data. Also, we compare the performance of our library with another GLL-based CFPQ tool and with the Trails library. We conclude that our solution is expressive and performant enough to be applied to the real-world problems.

This paper is organized as follows. In section!!! we !!!! and in section !!! sdfsd Then in section !!! we present a set of examples Evaluation Finally in section !!! we discuss possible directions of further research.

## 2 CONTEX-FREE PATH QUERYING PROBLEM

In this section we intrduce context-free path querying problem (or context-free reachability problem) formal description.

First of all we introduce necessary definitions.

- Context-free grammar is a quadruple  $G = (N, \Sigma, P, S)$ , where  $N$  is a set of nonterminal symbols,  $\Sigma$  is a set of terminal symbols,  $S \in N$  is a start nonterminal, and  $P$  is a set of productions.
- $\mathcal{L}(G)$  denotes a language specified by the grammar  $G$ , and is a set of terminal strings derived from the start nonterminal of  $G$ :  $L(G) = \{\omega | S \Rightarrow_G^* \omega\}$ .
- Directed graph is a triple  $M = (V, E, L)$ , where  $V$  is a set of vertices,  $L \subseteq \Sigma$  is a set of labels, and a set of edges  $E \subseteq V \times L \times V$ . We assume that there are no parallel edges with equal labels: for every  $e_1 = (v_1, l_1, v_2) \in E, e_2 = (u_1, l_2, u_2) \in E$  if  $v_1 = u_1$  and  $v_2 = u_2$  then  $l_1 \neq l_2$ .
- $tag : E \rightarrow L$  is a helper function which returns a tag of a given edge.

$$tag(e = (v_1, l, v_2), e \in E) = l$$

- $\oplus : L^+ \times L^+ \rightarrow L^+$  denotes a tag concatenation operation.
- $\Omega$  is a helper function which constructs a string produced by the given path. For every  $p$  path in  $M$

$$\Omega(p = e_0, e_1, \dots, e_{n-1}) = tag(e_0) \oplus \dots \oplus tag(e_{n-1}).$$

Using these definitions, we define the context-free language constrained path querying as, given a query in form of grammar  $G$ , to construct the set of paths

$$Q(M, G) = \{p | p \text{ is path in } M, \Omega(p) \in \mathcal{L}(G)\}.$$

Reachability problem is a pretty similar and may be formulated as follows:

$$Q(M, G) = \{(v_0, v_n) | \exists p \text{ is path in } M, p = v_0 \xrightarrow{l_0} \dots \xrightarrow{l_{n-1}} v_n, \Omega(p) \in \mathcal{L}(G)\}$$

<sup>2</sup>Meerkat project repository: <https://github.com/meerkat-parser/Meerkat>. Access date: 16.01.2018

<sup>3</sup>Neo4j graph database site: <https://neo4j.com/>. Access date: 16.01.2018

Note that  $Q(M, G)$  can be an infinite set, hence it cannot be represented explicitly. In order to solve this problem, we construct compact data structure representation which stores all elements of  $Q(M, G)$  in finite space and from which one can extract any of them.

The main idea of our solution is that language may be specified in terms of parser combinators. Further we describe some details of parsing techniques which is necessary to provide generic parser combinators based solution for CFPQs evaluation.

### 3 GENERALIZED PARSER COMBINATORS

In [14] showed that combinators techniques is applicable for graph traversing, but well-known problem of combinator with left recursion is not solved. But this problem was solved in classical parser-combinators [12] and implemented in Meerkat library. Meerkat library is a general parser combinators library implemented in Scala programming language; by using memoization, continuation-passing style and the ideas of Johnson [13], it supports arbitrary (left-recursive and ambiguous) context-free specifications. This library implements classical set of combinators, supports action code specification, and provide `syn` macro for custom handling of recursive nonterminal description. Meerkat creates compressed representation of parse forest (SPPF) which is useful for CFPQs results representation [7]. Time and space complexity of this solution are cubic in worst case.

An example Meerkat specification of grammar 1 is presented in 3.

```
val S = syn("a" ~ S.? ~ "b")
```

**Figure 3: Meerkat specification of grammar 1**

In [7] showed that generalized LL parsing algorithm [30] can be generalized to CFPQs processing and this generalization produces efficient solution which can provide structured representation of query result. As the Meerkat library is closely related to the Generalized LL algorithm and since GLL can be generalized for context-free path querying, it is also possible to adapt Meerkat library for graph querying. It can be done by providing a function for retrieving the symbols which follow the specified position and utilizing it in the basic set of combinators. Details described below.

#### 3.1 SPPF

Structural representation. Derivation tree. Forest for unambiguous grammars. For graph too. Shared Packed Parse Forest (SPPF) [25] structure, description, usability for CFPQ.

Binarized Shared Packed Parse Forest (SPPF) [32] compresses derivation trees optimally reusing common nodes and subtrees. Version of GLL which utilizes this structure for parsing forest representation achieves worst-case cubic space complexity [31].

Binarized SPPF can be represented as a graph in which each node has one of four types described below. We denote the start and the end positions of substring as  $i$  and  $j$  respectively, and we call tuple  $(i, j)$  an *extension* of a node.

- **Terminal node** with label  $(i, T, j)$ .

- **Nonterminal node** with label  $(i, N, j)$ . This node denotes that there is at least one derivation for substring  $\alpha = \omega[i..j-1]$  such that  $N \Rightarrow_G^* \alpha, \alpha = \omega[i..j-1]$ . All derivation trees for the given substring and nonterminal can be extracted from SPPF by left-to-right top-down graph traversal started from respective node.
- **Intermediate node**: a special kind of node used for binarization of SPPF. These nodes are labeled with  $(i, t, j)$ , where  $t$  is a grammar slot.
- **Packed node** with label  $(N \rightarrow \alpha, k)$ . Subgraph with “root” in such node is one possible derivation from nonterminal  $N$  in case when the parent is a nonterminal node labeled with  $(\nrightarrow (i, N, j))$ .

An example of SPPF is presented in figure ??.

### 4 PARSER COMBINATORS FOR PATH QUERYING

Parser combinators provide a way to specify a language syntax in terms of functions and operations on them. A parser in this framework is usually a function which consumes a prefix of an input and returns either a parsing result or an error if the input is erroneous. Parsers can be composed by using a set of parser combinators to form more complex parsers. A parser combinators library provides with a set of basic combinators (such as sequential application or choice), and there can also be user-defined combinators. Most parser combinators libraries, including the Meerkat library, can only process the linear input — strings or some kind of streams. We extend the Meerkat library to work on the graph input.

Extension is based on some common ideas.

- Intersection of context-free language and regular one is a context-free language and there are different constructive proofs of this fact. Proposed solution is a yet another constructive proof and SPPF is a just user-friendly representation of result context-free grammar.
- Linear input is a simple case of graph: positions are vertices and tokens are edges labels. Each edge is going from position (vertex)  $i$  to position (vertex)  $i + 1$ .
- Parser can move pointer in input from position  $i$  to position  $i + 1$  and create new state when token between  $i$  to position  $i + 1$  matches with required in grammar. In case of graph processing there are more than one ways to go from current vertex  $i$  and it is possible to get more than one new state. Generalized parsing is designed to optimally handle steps which produce multiple new states and can handle help to handle this situation.
- We can treat the fact that token in input matches with required token from grammar as a predicate. This observation may be generalized: we can pass through edge if its label satisfies some predicate. This way we can flexibly handle labels of arbitrary types.
- Vertex may be converted to edge: all incoming edges are converted to incoming into source of new edge, all outgoing are converted to outgoing from target of new edge. This way we can handle vertex and edge labelled graphs as edge labelled.

#### 4.1 The Set of Combinators

First we introduce a small example graph which represent a map and presented in fig. 4. Here we have some cities which can have road between them and this relation is shown in graph as an edge with label *road\_to*. Each city labeled with name and with a country it belongs to.

And let us try to extract some information from this map.

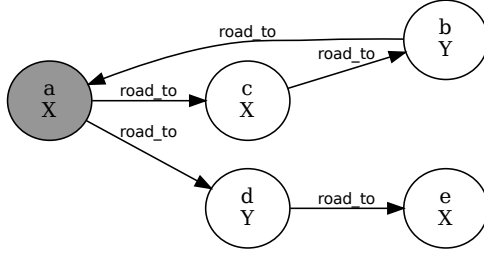


Figure 4: Example Input Graph of Roads

First of all, for creating queries we need to work with edges and vertices. There are two main functions for that:

- $V[L](\text{predicate}: L \Rightarrow \text{Boolean})$  combinator for working with vertices. Accepts a predicate and parses only vertices which satisfies that predicate
- $E[N](\text{predicate}: N \Rightarrow \text{Boolean})$  combinator for working with edges. Accepts a predicate and parses only edges which satisfies that predicate

(Write sth about syn macro

I think it should be in section 2 in Meerkat description)

Suppose that we would like to select cities from our graph which belongs to some country. For that we use function  $V$ :  $V[L]((e: \text{Entity}) \Rightarrow e.\text{country} == \text{"County\_Name"})$ . Here *Entity* is a property container for graph entities: edges and vertices. All properties usings (like  $(e: \text{Entity}).\text{country}$ ) are converted to the corresponding graph entity properties using Scala's Dynamic trait. Also, for the sake of simplicity, we will not explicitly specify *Entity* type for predicates. Now let us build a query which gets all roads from city in country *X* to the city in country *Y*. For that we can use a sequentiallital combinator  $\sim$ . It allows to create queries which sequentially applies two queries one after another. When we have subquery for retrieving a vertex with specific city, let's call it  $\text{city}(\text{name}: \text{String})$  and a subquery  $\text{roadTo}$  for retrieving road edges. Let us finally build a query  $\text{city}(\text{"X"}) \sim \text{roadTo} \sim \text{city}(\text{"Y"})$  which will give us requested set of paths from our graph. The full query with subqueries is shown on fig. 6.

Now we would like to get all pair of cities which have a road between them. So we need to transform our query to use semantic actions which is described in 4.3 section. Now let us specify what we want from every our query. From the  $\text{city}$  query we want only city name, so we need to map a result of basic vertex combinator. For that case we have a  $\wedge$  combinator we can write

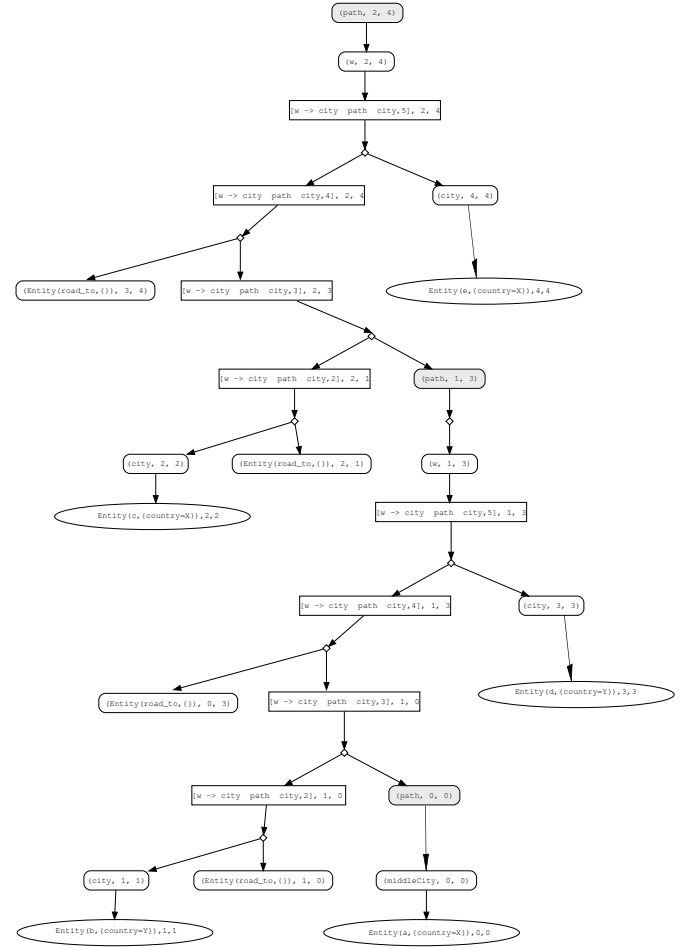


Figure 5: SPPF: result of applying actor/movie query to the graph 4

```
def city(country: String) =
  V(e.country == country)
val roadTo = E(_.value() == "road_to")
val ourPath =
  city("X") ~ roadTo ~ city("Y")
```

Figure 6: Path query

def  $\text{city}(\text{name}: \text{String}) = \text{syn}(V(e.\text{value}() == \text{name}) \wedge (\_.\text{value}))$  to achive that. In ourPath query we need first and second cities to be represented as a pair. For that we have a  $\&$  combinator which will map our sequence to a pair of strings. The final representation is shown on 7. Now when we execute that query we will get a

list which consists of all pairs of city's names which have a road between.

```
def city(country: String) =
  syn(V(e.country() == country) ^ (_.name))
val roadTo = E(_.value() == "road_to")
val ourPath =
  syn(city("X") ~ roadTo ~ city("Y") &
    { case c0 ~ c1 => (c1, c2) })
```

Figure 7: Path query

The whole set of basic combinators our library provides are presented in table 1. It consists of two kind of combinators. The first kind creates new parsers from existing ones, meanwhile the second one allows mapping parsers result. Parsers for matching strings are implicitly generated whenever a string is used within a query.

Combinator	Description
$a \sim b$	sequential parsing: $a$ then $b$
$a \mid b$	choice: $a$ or $b$
$a ?$	optional parsing: $a$ or nothing
$a *$	repetition of zero or more $a$
$a +$	repetition of at least one $a$
$a \wedge f$	apply $f$ function to $a$ if $a$ is a token
$a \wedge \wedge$	capture output of $a$ if $a$ is a token
$a \& f$	apply $f$ function to $a$ if $a$ is a parser
$a \& \&$	capture output of $a$ if $a$ is a parser

Table 1: Meerkat combinators

## 4.2 Generic interface for input

Combinators is a generic way to describe a query and when we have a query we want to execute that query on some graph considering it as an input for our query. The cool thing is that query execution mechanism may be fully separated from graph representation. We need only to have access to two very low-level functions, one for working with edges and one for vertices. The first one would allow to get all edges outgoing from current vertex and also satisfies given predicate. The second one will allow to check if current vertex satisfies given predicate. That interface is presented on fig .8. It has two type parameters:  $L$  for edge labels and  $N$  for nodes. We have implementation of that input for the next data sources:

- Neo4jInput — input source for working with graph database Neo4j;
- GraphxInput — input source for working with graph presented in memory using GraphX library;
- LinearInput — input source for working with linear input data like strings.

As far as required functions is very simple, we hope that this interface can be implemented for arbitrary storage of graph-structured data. Note, that currently we use  $\text{Int}$  as unique identifier for nodes (the  $\text{nodeId}$  parameter). It may be a technical restriction by the next two reason.

```
trait Input[+L, +N] {
  def filterEdges(nodeId: Int,
    predicate: L => Boolean): Seq[(L, Int)]
  def checkNode(nodeId: Int,
    predicate: N => Boolean): Option[N]
}
```

Figure 8: Generalized input interface

- It is impossible to use our library for correct processing of graph with more than  $\text{MAX\_INT}$  nodes).
- It is necessary to provide such identifiers. Many systems use unique identifiers by default, but in some cases it may be necessary to implement required functionality manually.

## 4.3 Semantic Actions

Each path query produces a parse result stored in SPPF. This representation is very rich but hard to use and understand. That is why our library provides a mechanism which allows you to extract and process any useful data stored in parse result. This mechanism is called semantic actions. In general, they give you an opportunity to apply any function to parsed token or sequence. Now, let's understand how actions can be used in queries and how they are implemented in our library.

There are two main semantic action binders  $\wedge$  and  $\&$ . First of them is used when we need to perform some action on primitive tokens such as vertices or edges.

```
// Defined in Terminal[+L] (edge) parser
def ^[U](f: L => U) =
  new SymbolWithAction[L, Nothing, U] {...
```

```
// Defined in Vertex[+N] parser
def ^[U](f: N => U) =
  new SymbolWithAction[Nothing, N, U] {...
```

Second is used when we need to process a result of combination of parsers.

```
// Defined in Symbol[+L, +N, +V] parser
def &[U](f: V => U) =
  new SymbolWithAction[L, N, U] {...
```

But actually, they both have the same behaviour, they produce a new parser that has the same parsing possibilities as an original parser but also have a binded function. Then, every SPPF node that will be produced by parser with binded function will have a reference to this function too.

So, these operations in composition with other combinators provides an instrument for data processing on which most queries are based. For example,  $\wedge$  can extract some data from tokens and  $\&$  applied to sequence of tokens can collect and process data returned by terminal parsers.

The main idea of execution of semantic actions remained the same as in the original Meerkat library excepting one aspect. For each node we still just execute all actions of its children, collect results and pass them as argument to current function. But what

should executor do if SPPF has ambiguous nodes? Previous implementation just throws an exception in that case and it is reasonable because original library is written for linear parsing and most grammars allows disambiguation in that case.

However, even unambiguous grammar can produce ambiguous derivations during parsing of graphs. That's why we provide a feature that makes it possible to extract "all" trees stored in SPPF. The number of path deriving from given grammar can be infinite, for example, when graph has cycles. This reason we can provide only a lazy stream of trees that allows to take as much of them as you need. Our solution is based on breadth first search that yields an unambiguous SPPF corresponding to some derivation immediately after it was found.

Composition of trees extraction and semantic action execution gives us a function that we called `executeQuery`. It parses graph from all positions producing a list of SPPF roots, then it extracts all derivations from all roots, executes semantic actions and returns a stream of results.

## 5 EXAMPLES

In this section we introduce and describe some examples of our library usage. We show that combinators are expressive enough for realistic queries and allows to create generic queries easily.

### 5.1 Complicated Query to Map

Let's form a complex query for our city graph. Let us capture one city, let's say city with name  $a$ . Now having a city graph and captured vertex we would like to know all paths such if as  $i$  city from beginning of our path we visit country  $X$  then as  $i$  city from end of our path we visit country  $X$  too. And also the middle city in our path is our captured city  $a$ . In a terms of combinators we can define our path as shown on fig. 9. Here `reduceChoice` is a function which transforms a list of queries to one query which is formed by reducing given list with `|` combinator. The `pathPart` query recursively defines a path of our way. Also, `middleCity` is a vertex query which parses our captured city  $a$  and `roadTo` query parses a `roadTo` edge.

```
val countriesList = List("X", "Y")
val path =
  (reduceChoice(countriesList.map(pathPart)) |
   middleCity)
def pathPart(country: String) =
  syn(city(country) ~ roadTo ~ path ~
      roadTo ~ city(country))

val middleCity = V(_.value() == "a")
val roadTo = E(_.value() == "road_to")
def city(country: String) =
  V(_.country == country)
```

Figure 9: Path query

Now we would like, to get from our query only city combinator result. For that purpose let us modify it to make return result. In our library we have a `^` and `&` functions for that. Then we will have definition of our combinators as presented in fig. 11.

```
def reduceChoice(xs: List[Nonterminal]) =
  xs match {
    case x :: Nil => x
    case x :: y :: xs =>
      syn(xs.foldLeft(x | y)(_ | _))
  }
```

Figure 10: Reduce choice function implementation

```
val middleCity =
  syn(V(_.value() == "a") ^&) & (List(_))
def pathPart(country: String) = syn(
  (city(country) ~ roadTo ~
   path ~ roadTo ~ city(country) & {
     case a ~ (b: List[_]) ~ Entity =>
       a +: b :+ c })
```

Figure 11: Fixed queries

Now we execute our query. It is evident that for the graph presented on fig. 4 we can get only three paths which satisfies given criteria:

- single-vertex path  $a$ ;
- $b \rightarrow a \rightarrow d$
- $c \rightarrow b \rightarrow a \rightarrow d \rightarrow e$

A simplified SPPF for this query is presented in Fig. 5: rounded rectangles represent nonterminals and other rectangles represent productions. Every rectangle contains a nonterminal name or a production rule, as well as start and end nodes of the path in the input graph derived from the corresponding rectangle. Gray rectangles are start nonterminals.

### 5.2 Same Generation Query

Yet another example of first order functions usage is generalisation of classical same generation query which is one of basic context-free path queries. One of application of such queries is hierarchy analysing in RDF storages [39]. Let suppose that we have RDF graphs with two pairs of relation (each pair is relation and its revers): ( $subClassOf$ ;  $subClassOf^{-1}$ ) and ( $type$ ;  $type^{-1}$ ). We want to evaluate two queries which detect all pairs of nodes which are connected by path derivable in grammars  $G_1$  (Fig. 12) and  $G_2$  respectively (Fig. 13).

```
0: S → subClassOf-1 S subClassOf
1: S → type-1 S type
2: S → subClassOf-1 subClassOf
3: S → type-1 type
```

Figure 12: Context-free grammar  $G_1$  for query 1

Of course, these queries can be written in Meerkat easily because it supports context-free queries: code is presented in Fig. 14 and Fig. 15.

As you can see, grammars and code representations for these two queries looks pretty similar. May we avoid code duplication

```

0:  $S \rightarrow B \text{ subClassOf}$ 
0:  $S \rightarrow \text{subClassOf}$ 
1:  $B \rightarrow \text{subClassOf}^{-1} B \text{ subClassOf}$ 
2:  $B \rightarrow \text{subClassOf}^{-1} \text{subClassOf}$ 

```

Figure 13: Context-free grammar  $G_2$  for query 2

```

val query1: Nonterminal = syn(
  "subclassof-1" ~ query1.? ~ "subclassof" |
  "type-1" ~ query1.? ~ "type")

```

Figure 14: The same generation query (Query 1) in Meerkat

```

val S = syn(
  "subclassof-1" ~ S ~ "subclassof")
val query2 = syn(S ~ "subclassof")

```

Figure 15: The same generation query (Query 2) in Meerkat

and generalize them? Yes, we can and not only for these two queries. The function `sameGen` presented in Fig 16 is a generalization of the same generation query and is independent of the environment such as the input graph structure or other parsers and also uses a function `reduceChoice` presented in 10. It can be used for the creation of other queries, including the one presented in Fig 14: it is the result of the application of `sameGen` to the appropriate relations (which can be treated as opening and closing brackets). Another application of the `sameGen` is a Query 2, which can be founded in Fig. 18.

```

def sameGen(brs) =
  reduceChoice(
    bs.map { case (lbr, rbr) =>
      lbr ~ syn(sameGen(bs).?) ~ rbr })

```

Figure 16: Generic function for the same generations query

We show that parser combinators provide a simple and safe way to creation of generic queries. By using this ability, it may be possible to create a library of “standard templates” for most popular generic queries like same generation query or for domain specific queries (for example, for specific static code analysis problem).

### 5.3 Classical Movies Queries

```

!!!!!!!!!!!!!!!!!!!!!!!!!!!!
!!!!!!!!!!!!!!!!!!!!!!!!!!!!
Mov!!!!!!!!!!!!!!!!!!!!!!!!!!!!
MovMovMov! Mov! Mov! Mov! Mov! Mov! Mov! Mov! Mov!
Mov! Mov! Mov! Mov!!!!!!!!!!!!!!!!!!!!

```

## 6 EVALUATION

In this section, we present an evaluation of our graph querying library. We measure its performance on a classical set of ontology

```

val query1 = syn(sameGen(List(
  ("subclassof-1", "subclassof"),
  ("type-1", "type"))))

```

Figure 17: Query 1 as an application of `sameGen`

```

val query2 = syn(
  sameGen(List(("subclassof-1", "subclassof"))) ~
  "subclassof")

```

Figure 18: Query 2 as an application of `sameGen`

graphs [39]: both when the graph is loaded into the RAM and for the integration with the Neo4j database and compare it with the solution based on the GLL parsing algorithm [7] and the Trails [14] library for graph traversals. We also show how may-alias static code analysis can be done by means of the developed library.

All tests have been performed on a computer running Fedora 27 with quad-core Intel Core i7 2.5 GHz CPU and 8 GB of RAM.

### 6.1 Ontology querying

Querying for ontologies is a well-known graph querying problem. We evaluate our library on some popular ontologies which are presented as RDF files in the paper [39]. First, we convert RDF files to a labelled directed graph in the following manner: we create two edges (*subject*, *predicate*, *object*) and (*object*, *predicate*<sup>-1</sup>, *subject*) for every RDF triple (*subject*, *predicate*, *object*). Then the graph is either loaded into the Neo4j database or is loaded directly into the memory. Then we run two queries from the paper [7] for these graphs. The grammars for the queries are presented in Fig. 17 and Fig. 18.

The performance results are shown in the table 2 where *#results* is a number of pairs of the nodes between which at least one S-path exists.

The Meerkat-based and the GLL-based [7] solutions show the same results (column *#results*) and the Query 1 runs up to two times faster on the Meerkat-based solution than on the GLL-based, meanwhile the GLL-based solution is faster for the Query 2. Querying the database is naturally 2 – 4 times slower than querying the graphs located in the RAM.

### 6.2 Static code analysis

Alias analysis is a fundamental static analysis problem [18]: it checks may-alias relations between code expressions and can be formulated as a context-free language (CFL) reachability problem [26] which is closely related to context-free path querying problem. In this analysis, a program is represented as a Program Expression Graph (PEG) [40]. Vertices in a PEG correspond to program expressions and edges are relations between them. There are two types of edges possible while analyzing C source code: **D**-edge and **A**-edge.

- Pointer dereference edge (**D**-edge). For each pointer dereference *\*e* there is a directed **D**-edge from *e* to *\*e*.
- Pointer assignment edge (**A**-edge). For each assignment *\*e<sub>1</sub> = e<sub>2</sub>* there is a directed **A**-edge from *e<sub>2</sub>* to *\*e<sub>1</sub>*

Ontology	#nodes	#edges	Query 1					Query 2				
			#results	In memory graph (ms)	DB query (ms)	Trails (ms)	GLL (ms)	#results	In memory graph (ms)	DB query (ms)	Trails (ms)	GLL (ms)
atom-primitive	291	685	15454	64	67	2849	232	122	29	79	453	19
biomedical-measure-primitive	341	711	15156	112	108	3715	482	2871	18	18	60	26
foaf	256	815	4118	11	11	432	29	10	1	1	1	1
funding	778	1480	17634	69	68	367	179	1158	9	9	76	13
generations	129	351	2164	4	4	9	12	0	1	0	0	0
people_pets	337	834	9472	37	37	75	80	37	1	1	2	1
pizza	671	2604	56195	333	325	7764	793	1262	17	18	905	50
skos	144	323	810	1	2	6	6	1	1	0	0	0
travel	131	397	2499	11	13	34	21	63	1	1	1	2
univ-bench	179	413	2540	10	10	31	24	81	1	1	2	1
wine	733	2450	66572	405	401	3156	606	133	2	3	4	5

Table 2: Comparison of Meerkat, Trails and GLL performance on ontologies

$$\begin{aligned}
 M &\rightarrow \bar{D} V D \\
 V &\rightarrow (M? \bar{A})^* M? (A M?)^*
 \end{aligned}$$

Figure 19: Context-Free grammar for the may-alias problem

For the sake of simplicity, we add edges labelled by  $\bar{D}$  and  $\bar{A}$  which correspond to the reversed **D**-edge and **A**-edge, respectively.

The grammar for may-alias problem from [40] is presented in Fig. 19. It contains two nonterminals **M** and **V** and allows us to make two kinds of queries for each of them.

- **M**-production means that two l-value expressions are memory aliases i.e. may refer to the same memory location.
- **V**-production means that two expressions are value aliases i.e. may evaluate to the same pointer value.

We run the **M** and **V** queries on some open-source C projects: the results are in table 3. We can conclude that our solution is expressive and performant enough to be used for static analysis problems which can be expressed as CFPQs.

```

val M = syn("nd" ~ V ~ "d")
val V = syn((M.? ~ "na").* ~ M.? ~ ("a" ~ M.?).*)

```

Figure 20: Meerkat representation of may-alias problem grammar

### 6.3 Comparison with Trails

Trails [14] is a Scala graph combinator library. It provides traversers for describing paths in graphs which resemble parser combinators and calculates possibly infinite stream of all possible paths described by the composition of basic traversers. Both Trails and Meerkat-based solution support parsing of the graphs located in RAM, so we compare the performance of Trails and Meerkat-based solution on the ontology queries described above: the results are presented in

table 2. Trails and Meerkat-based solution compute the same results, but Trails is up to 10 times slower than Meerkat-based solution.

To summarize, we demonstrated that parser combinators are expressive enough to be used for implementing real queries. Our implementation is as performant as the other existing combinators library and is comparable to the GLL-based solution.

## 7 DISCUSSION AND CONCLUSION

We propose a native way to integrate a language for context-free path querying into a general-purpose programming language. Our solution can handle arbitrary context-free grammars and arbitrary input graphs. The proposed approach is language-independent and may be implemented for closely all general-purpose programming languages. We implement it in the Scala programming language and show that our implementation can be applied to the real world problems.

We can propose some possible directions for the future work. First of all, it is necessary to formulate the creation of a user-friendly interface for SPPF processing. We can just extract reachability information, but SPPF contains much more useful information. One such representation may be a set of paths with additional information about their structure. This may simplify debugging and query result processing.

In order to improve performance and investigate scalability of proposer solution it is necessary to try to implement parallel single machine and distributed GLL. It is not only algorithmic problem: to get practical solution we should choose appropriate tools, libraries for parallel and distributed computing for Scala.

Another direction is a semantic actions computation, otherwise known as attributed grammars handling. It increases the expressiveness of queries by means of the specification of user-defined actions, such as filters, over subqueries result. Although it is impossible in general, techniques such as lazy evaluation can provide a technically adequate solution. Another possible direction is utilization of relational programming (minikanren) which is aimed to search [? ]. For what class of semantic actions it is possible to



Program	#edges	#nodes	Code Size (KLOC)	In memory graph (ms)	Neo4j graph (ms)	Trails graph (ms)	M aliases	V aliases
wc-5.0	332	770	0.5	0	2	3	174	107
pr-5.0	815	2062	1.7	11	12	14	1131	63
ls-5.0	1687	4734	2.8	43	51	170	5682	253
bzip2-1.0.6	632	1508	5.8	8	13	21	813	71
gzip-1.8	2687	7510	31	111	120	537	4567	227

Table 3: Running may-alias queries on Meerkat on some C open-source projects

provide a precise general solution is a theoretical question to be answered.

Some important problems in static code analysis require languages more expressive than context-free one. For example, context-sensitive data-dependence analysis may be precisely expressed in terms of linear-conjunctive language [22] reachability, but not context-free [38]. While problem formulation is precise, it is possible to get only approximated solution, because emptiness problem for linear-conjunctive languages is undecidable. It would be an interesting task to support not only linear-conjunctive grammars, but arbitrary conjunctive grammars [21] in the library and investigate nature of approximation.

All these improvements may provide !!! Declarative code analysis tools and languages Flix [17]. Reps [27]

Improved version of OpenCypher [16], which is the one of the most popular graph query languages, provides context-free path querying mechanism. Detailed comparison with it may provide more information for direction of future work.

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