

# Formal Languages Theory is Not Only a Parsing

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## Paths in graphs

- Graph analysis
  - Graph database querying
  - Network analysis (social networks, Internet, etc)
- Static code analysis
  - ► Alias analysis
  - ► Taint analysis
  - ► Types-related problems
  - Static analysis of string-embedded languages
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# Language constrained path querying

Language-constrained path querying, language reachability

- $\bullet$   $\Sigma$  is a set of terminals
- $L(\Sigma)$  is a language over  $\Sigma$
- G = (V, E, D) is a directed graph,  $E \subseteq V \times D \times V$ ,  $D \subseteq \Sigma$
- $p = v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \cdots v_{n-1} \xrightarrow{l_{n-1}} v_n$  is a path in G
- $w(p) = w(v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \cdots v_{n-1} \xrightarrow{l_{n-1}} v_n) = l_0 l_1 \cdots l_{n-1}$
- $R = \{p \mid w(p) \in L(\Sigma)\}$ 
  - ▶ **Problem**: R can be an infinite in some cases
- Task may be formulated in other way:

$$Q = \{(v_0, v_n) \mid \exists p = v_0 \xrightarrow{l_0} \cdots \xrightarrow{l_{n-1}} v_n \ (w(p) \in L(\Sigma))\}$$

## Regular constarints

- $L(\Sigma)$  is a regular language
  - Graph databases query languages (SPARQL, Cypher, PGQL)
  - OpenCypher: https://goo.gl/5h5a8P

#### Context-free constraints

- $L(\Sigma)$  is a context-free language
- Graph databases and semantic networks
  - ► Sevon P., Eronen L. "Subgraph queries by context-free grammars." 2008
  - ► Zhang X. et al. "Context-free path queries on RDF graphs." 2016
  - Hellings J. "Conjunctive context-free path queries." 2014
- Static code analysis
  - Thomas Reps et al. "Precise interprocedural dataflow analysis via graph reachability." 1995
  - Qirun Zhang et al. "Efficient subcubic alias analysis for C." 2014
  - ▶ Dacong Yan et al. "Demand-driven context-sensitive alias analysis for Java." 2011
  - ► Jakob Rehof and Manuel Fahndrich. "Type-base flow analysis: from polymorphic subtyping to CFL-reachability." 2001

#### Context-free constarints

- Kai Wang et. al. Graspan: A Single-machine Disk-based Graph System for Interprocedural Static Analyses of Large-scale Systems Code. 2017
  - "We have identified a total of 1127 unnecessary NULL tests in Linux, 149 in PostgreSQL, 32 in httpd."
  - "Our analyses reported 108 new NULL pointer dereference bugs in Linux, among which 23 are false positives"
  - ▶ "For PostgreSQL and httpd, we detected 33 and 14 new NULL pointer bugs; our manual validation did not find any false positives among them."

#### Linear-conjunctive constraints

- $\bullet$   $L(\Sigma)$  is a linear-conjunctive language
  - Interleaving of balcned brackets:

$$L_1 = \{a^n b^n | n \ge 0\}; L_2 = \{c^m d^m | m \ge 0\}; L_3 = L_1 \odot L_2 = \{ab; acbcdd; cdab; \dots\}$$

• Qirun Zhang and Zhendong Su. Context-sensitive data-dependence analysis via linear conjunctive language reachability. 2017

# Chelenges

- Theoretical open problem
  - ▶ Is there exists an algorithm with time complexity  $O(|V|^{3-\varepsilon}), \varepsilon > 0$
- Practical utilisation of solutions from "classical" parsing
  - ► Algorithms: CYK, (Generalized) LL, (Generalized) LR, Earley, ...
  - ► Techniques: parser combinators, parser generators, ...
  - Advanced techniques: GPGPU utilization, advanced data structures (compact parse forest representation, graph structured stack), ...
- Huge amount of data requires efficien implementation of parallel and/or destributed query processing

#### Our experiments

- Generalized LL for CFPQ (GLL)
  - ▶ Based on Generalized LL: Scott E., Johnstone A. "GLL parsing"
  - ► Time complexity:  $O\left(|V|^3 * \max_{v \in V} (deg^+(v))\right)$
  - ► Semyon Grigorev and Anastasiya Ragozina. "Context-free path querying with structural representation of result." 2017
- GPGPU utilization for CFPQ (GPGPU)
  - ▶ Based on Valiant L. "General context-free recognition in less than cubic time." 1974
  - ► Time complexity:  $O(|V|^2|N|^3(BMM(|V|) + BMU(|V|)))$ 
    - ★ BMM(n) boolean matrix multiplication  $n \times n$
    - ★ BMU(n) cell-by-cell or  $n \times n$
  - Rustam Azimov, Semyon Grigorev. "Context-Free Path Querying by Matrix Multiplication." 2017
- Parser-Combinators for Context-Free Path Querying (in Scala)

## Performance comparison setup

```
0: \mathbf{S} 	o subClassOf^{-1} \mathbf{S} \ subClassOf 1: \mathbf{S} 	o type^{-1} \mathbf{S} \ type 2: \mathbf{S} 	o subClassOf^{-1} \ subClassOf 3: \mathbf{S} 	o type^{-1} \ type Query 1
```

 $0: \mathbf{S} \to \mathbf{B} \ subClassOf$   $1: \mathbf{S} \to subClassOf$   $2: \mathbf{B} \to subClassOf^{-1} \mathbf{B} \ subClassOf$   $3: \mathbf{B} \to subClassOf^{-1} \ subClassOf$ Query 2

# Performance comparison result

Nº	#V	#E	Query 1 (ms)			Query 2 (ms)	
			CYK <sup>1</sup>	GLL	GPGPU	GLL	GPGPU
1	144	323	1044	10	12	1	1
2	129	351	6091	19	13	1	0
3	131	397	13971	24	30	1	10
4	179	413	20981	25	15	11	9
5	337	834	82081	89	32	3	6
6	291	685	515285	255	22	66	2
7	341	711	420604	261	20	45	24
8	671	2604	3233587	697	24	29	23
9	733	2450	4075319	819	54	8	6
10	6224	11840	_	1926	82	167	38
11	5864	19600	-	6246	185	46	21
12	5368	20832	_	7014	127	393	40

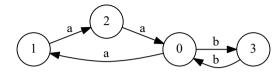
<sup>&</sup>lt;sup>1</sup>Zhang, et al. "Context-free path queries on RDF graphs."

#### Info

- E-mail: semen.grigorev@jetbrains.com
- GitHub-community YaccConstructor: https://github.com/YaccConstructor

## Example

Input graph



query is a grammar G which specifies the language  $L=\{a^nb^n\mid n\geq 1\}$ 

 $0: S \rightarrow a S b$ 

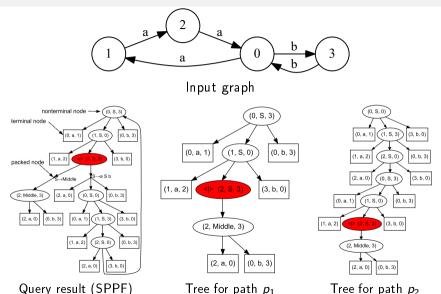
 $1: \ S \rightarrow \textit{Middle}$ 

2:  $Middle \rightarrow a b$ 

Query result is an infinite set of paths

- $p_1 = 0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3$
- $p_2 = 0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{a} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3 \xrightarrow{b} 0 \xrightarrow{b} 3 \xrightarrow{b} 0$
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# Structural representation of query result

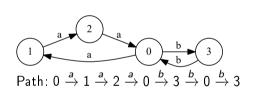


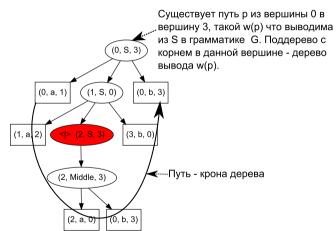
Semyon Grigorev (JetBrains Research)

CFPQ

ee for path p<sub>2</sub>

#### Paths extraction



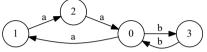


## Key idea

Context-free languages are closed under intersection with regular languages

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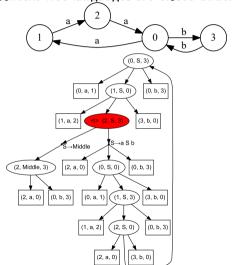
Context-free languages are closed under intersection with regular languages



- $0: S \rightarrow a S b$
- $1: S \rightarrow \textit{Middle}$
- $2: \quad \textit{Middle} \rightarrow \textit{a b}$

# Key idea

#### Context-free languages are closed under intersection with regular languages



 $0: S \rightarrow aSb$ 1 ·  $S \rightarrow Middle$ 2: Middle  $\rightarrow$  a b  $(0, S, 3) \rightarrow (0, a, 1) (1, S, 0) (0, b, 3)$  $(1, S, 0) \rightarrow (1, a, 2) (2, S, 3) (3, b, 0)$  $(2, 5, 3) \rightarrow (2, a, 0) (0, 5, 0) (0, b, 3)$  $(2, S, 3) \rightarrow (2, Middle, 3)$  $(0, S, 0) \rightarrow (0, a, 1) (1, S, 3) (3, b, 0)$  $(1, S, 3) \rightarrow (1, a, 2) (2, S, 0) (0, b, 3)$  $(2, S, 0) \rightarrow (2, a, 0) (0, S, 3) (3, b, 0)$  $(0, Middle, 3) \rightarrow (2, a, 0) (0, b, 3)$