

# Evaluation of Matrix-Based Context-Free Path Querying Algorithm

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## ABSTRACT

A clear and well-documented  $\text{\LaTeX}$  document is presented as an article formatted for publication by ACM in a conference proceedings or journal publication. Based on the “acmart” document class, this article presents and explains many of the common variations, as well as many of the formatting elements an author may use in the preparation of the documentation of their work.

## CCS CONCEPTS

• **Computer systems organization** → **Embedded systems**; *Redundancy*; Robotics; • **Networks** → Network reliability;

## KEYWORDS

datasets, neural networks, gaze detection, text tagging

### ACM Reference format:

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## 1 INTRODUCTION

Graph querying, Context-Free Path Querying (CFPQ), applications in different areas. Performance is important for practical tasks.

Matrix-based algorithm. Pretty simple. Performance problems. CPU/GPGPU based implementation. Investigate and compare.

There is no publically available standartized dataset for algorithms evaluation. We collect some data and propose possible candidate for it.

Research question: comparison of differend implementations of matrix-based CFPQ. We implement and compare performance.

Contribution

- Implementation. Source code is available on GitHub:!!!!
- Evaluation
- Dataset for evaluation. Available. Data format. Reference values.

This paper is organized as follows. !!!!

## 2 MATRIX-BASED ALGORITHM FOR CFPQ

Matrix-based algorithm for CFPQ was proposed by Rustam Azimov [2]. This algorithm can be expressed in few lines of code in terms of matrices operations, and it is a sufficient advantage for implementation. It was shown that GPGPU utilization for queries evaluation can significantly improve performance in comparison with other implementations [2] even float matrices used instead of boolean matrices.

Pseudocode of the algorithm is presented in listing 1.

**Algorithm 1** Context-free path querying algorithm

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1: function CONTEXTFREEPATHQUERYING( $D, G$ )
2:    $n \leftarrow$  the number of nodes in  $D$ 
3:    $E \leftarrow$  the directed edge-relation from  $D$ 
4:    $P \leftarrow$  the set of production rules in  $G$ 
5:    $T \leftarrow$  the matrix  $n \times n$  in which each element is  $\emptyset$ 
6:   for all  $(i, x, j) \in E$  do ▷ Matrix initialization
7:      $T_{i,j} \leftarrow T_{i,j} \cup \{A \mid (A \rightarrow x) \in P\}$ 
8:   end for
9:   while matrix  $T$  is changing do
10:     $T \leftarrow T \cup (T \times T)$  ▷ Transitive closure calculation
11:   end while
12:   return  $T$ 
13: end function

```

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Here  $D = (V, E)$  be the input graph and  $G = (N, \Sigma, P)$  be the input grammar. Each cell of the matrix  $T$  contains the set of nonterminals such that  $N_k \in T[i, j] \iff \exists p = v_i \dots v_j$ —path in  $D$ , such that  $N_k \xRightarrow{*}_G \omega(p)$ , where  $\omega(p)$  is a word formed by labels along path  $p$ . Thus, this algorithm solves reachability problem, or, according Hellings [3], process CFPQs by using relational query semantics.

As you can see, performance-critical part of this algorithm is a matrix multiplication. Note, that the set of nonterminals is finite, we can represent the matrix  $T$  as a set of boolean matrices: one for each nonterminal. In this case the matrix update operation be  $T_{N_i} \leftarrow T_{N_i} + (T_{N_j} \times T_{N_k})$  for each production  $N_i \rightarrow N_j N_k$  in  $P$ . Thus we can reduce CFPQ to boolean matrices multiplication. After such transformation we can apply the next optimization: we can skip update if there are no changes in the matrices  $T_{N_j}$  and  $T_{N_k}$  at the previous iteration.

Thus, the most important part is efficient implementation of operations over boolean matrices, and in this work we compare effects of utilization of different approaches to matrices multiplication. All our implementations are based on the optimized version of the algorithm.

### 3 IMPLEMENTATION

We implement matrix-based algorithm for CFPQ by using a number of different programming languages and tools. Our goal is to investigate effects of the next features of implementation.

- **GPGPU utilization.** It is well-known that GPGPUs are suitable for matrices operations, but performance of whole solution depends on task details: overhead on data transferring may negate effect of parallel computations. Moreover, it is believed that GPGPUs is not suitable for boolean calculations [?]. Can GPGPUs utilization for CFPQ improve performance in comparison with CPU version?
- **Existing libraries utilization** is a good practice in software engineering. Is it possible to achieve high performance by using existing libraries for matrices operations or we need to create own solution to get more control?
- **Low-level programming.** GPGPU programming is traditionally low-level programming by using C-based languages (CUDA C, OpenCL C). On the other hand, there are number of approaches to create GPGPU-based solution by using

such high-level languages as Python. Can we get high-performance solution by using such approaches?

- **Sparse** Real graphs often are sparse.

We provide next implementations to compare different approaches to algorithms implementation.

- **CPU-based solutions**
  - Python + Scipy [4] (sparse matrices)
  - C + m4ri [1] (4 russian method)
- **GPGPU-based solutions**
  - CUDA C, manual implementation of 4 russian method.
  - CUDA C, manual implementation of naive boolean matrix multiplication
  - Python + numba<sup>1</sup> manual implementation of naive boolean matrix multiplication

Brief overview of approaches.

Generic notes on optimizations. Notes on data transferring. On matrix changes tracking (we should multiply pair of matrices only if one of them changed in last iteration)

#### 3.1 m4ri

Description of impl 1 [1]

#### 3.2 Python sparse CPU

Description of impl 2

#### 3.3 CUDA naive

Description of impl 3

#### 3.4 CUDA 4 russian method

Description of impl 4

#### 3.5 Python + CUDA

Description of impl 5

#### 3.6 Smth else?

Description of impl n

### 4 DATASET DESCRIPTION

The dataset includes the next data.

- RDFs [?]
- Worst case [?]
- Cycle to full
- Sparse graphs [?]

All data is presented in text-based format to simplify usage in different environments. Grammars are stored in the files with yrd extension. Graphs are stored in the files with txt extension.

Data organized as follows. Folders and subfolders

### 5 EVALUATION

We evaluate all described implementations on all data and queries from presented dataset.

For evaluation we use PC with the next characteristics.

<sup>1</sup> Numba is a JIT compiler which supports GPGPU for subset of Python programming. Official page: <http://numba.pydata.org/>. Access date: 03.05.2019

$$S \rightarrow SS$$
**Figure 1: grammar 1**

$$S \rightarrow SS$$
**Figure 2: grammar 2**

$$S \rightarrow SS$$
**Figure 3: grammar 1**

$$S \rightarrow SS$$
**Figure 4: grammar 1**

- OS
- CPU
- RAM
- GPU
- Libs versions
- Python runtime

Compiler options, Python runtime, etc.

RDFs and two types of queries. Form paper []

Worst case and same generation query.

Cycle which fills to full graph and two queries.

Results: tables, graphics, etc

## 6 DISCUSSION

Discussion of evaluation results.

## 7 CONCLUSION AND FUTURE WORK

We present !!!

Our evaluation shows that !!!

First direction for future research is a more detailed CFPQ algorithms investigation. We should do More evaluation on sparse matrices on GPGPUs.

Also it is necessary to implement and evaluate solutions for graphs which is not fit in RAM. There is a set of technics for huge matrices multiplication. Is it possible to dopt it for CFPQ

Another direcion is a dataset improvement. More data. More grammars/queries.

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