



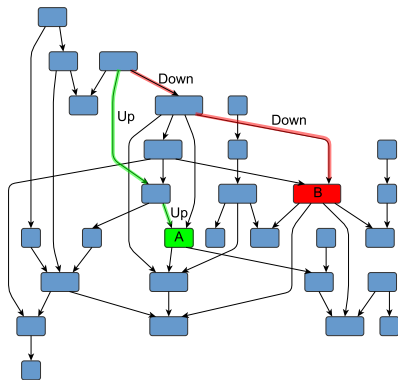
Parsing techniques for graph analysis

Semyon Grigorev, Kate Verbitskaia

JetBrains Research, Programming Languages and Tools Lab
Saint Petersburg University

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Language-constrained paths filtering



Navigation through a graph

- Are nodes A and B on the same level of hierarchy?
- Is there a path of form $Up^n Down^n$?
- Find all paths of form $Up^n Down^n$ which start from a node A.

- (How) Can this automaton generate SQL queries? (при чём тут скуль?)
- (How) Can this program produce some specific chain of calls?

Language-constrained paths filtering: more formal

- $\mathbb{G} = (\Sigma, N, P)$ — context-free grammar
- $G = (V, E, L)$ — directed graph
 - ▶ $v \xrightarrow{l} u \in E \subseteq V \times L \times V$
 - ▶ $L \subseteq \Sigma$
- $p = v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \dots \xrightarrow{l_{n-2}} v_{n-1} \xrightarrow{l_{n-1}} v_n$ — path in G
- $\omega(p) = \omega(v_0 \xrightarrow{l_0} v_1 \xrightarrow{l_1} \dots \xrightarrow{l_{n-2}} v_{n-1} \xrightarrow{l_{n-1}} v_n) = l_0 l_1 \dots l_{n-1}$
- $R = \{p \mid \text{exists } N_i \in N \text{ such that } \omega(p) \in L(\mathbb{G}, N_i)\}$

- Graph analysis
 - ▶ Graph database querying
 - ▶ Network graph analysis
- Code analysis
 - ▶ Static analysis CFL(linear conjunctive) reachability
 - ★ alias analysis
 - ★ points-to analysis
 - ▶ Dynamically generated strings analysis
 - ▶ Multiple input parsing
- ...

- Do not use the power of advanced parsing techniques
 - ▶ Mostly based on CYK
(Xiaowang Zhang, et al. “Context-free path queries on RDF graphs.”;
Jelle Hellings. “Conjunctive context-free path queries.”)
 - ▶ Do not provide useful structural representation of result
- Impose restrictions on input
 - ▶ Problems with cycles in the input graph
(Petteri Sevon, Lauri Eronen. “Subgraph queries by context-free grammars.”)

Open problems

- Effective algorithm development
- Result representation for debugging; further processing
- GPGPU utilization
- Processing of different types of grammars (ECFG, conjunctive, etc)

Bar-Hillel theorem

- Context-free languages are closed under intersection with regular languages
- Parsing algorithms are constructive proof of Bar-Hille theorem for one simple case ...
- ... so, classical parsing can be generalized for arbitrary regular language processing

Example

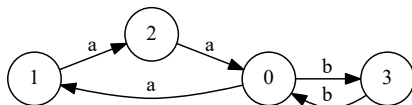


Figure: Input graph

0 : $S \rightarrow a S b$

1 : $S \rightarrow \textit{Middle}$

2 : $\textit{Middle} \rightarrow a b$

Figure: Query: a grammar for the language $L = \{a^n b^n; n \geq 1\}$ with an additional marker for the middle of a path

Example

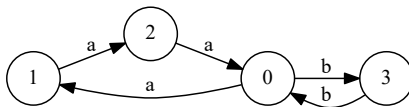
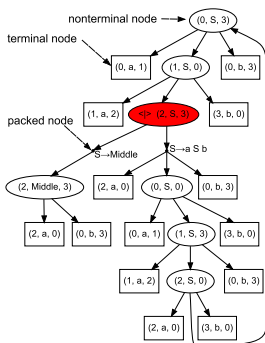
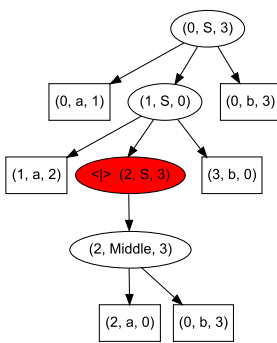


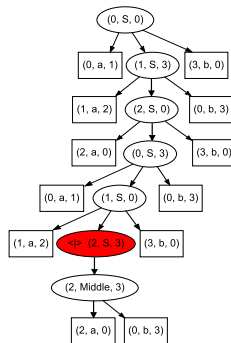
Figure: Input graph



Query result: SPFF



Tree for path from 0 to 3



Tree for path from 0 to 0

- Relaxed parsing of dynamically generated SQL-queries
 - ▶ Based on RNLGR parsing algorithm (Elizabeth Scott, Adrian Johnstone)
- Context-free path querying with structural representation of result
 - ▶ Based on GLL parsing algorithm (Elizabeth Scott, Adrian Johnstone)
- Combinators for context-free path querying
 - ▶ Based on the Meerkat: a general parser combinator library for Scala (Ali Afroozeh, Anastasia Izmaylova)
- Context-free path querying by matrix multiplication
 - ▶ Inspired by Valiant and Okhotin (почему тут без имён?)

- Other grammars and language classes intersection
 - ▶ Context-free grammars intersection: Mark-Jan Nederhof, “The language intersection problem for non-recursive context-free grammars”
 - ▶ Approximated intersection of regular and conjunctive/boolean languages
 - ▶ ...
- Mechanization in Coq
 - ▶ Bar-Hillel theorem
 - ▶ GLL-based algorithms
 - ▶ ...
- New areas for application

Contact information

- Semyon Grigorev: semen.grigorev@jetbrains.com
- Ekaterina Verbitskaia: kajigor@gmail.com
- YaccConstructor: <https://github.com/YaccConstructor>