Context-Free Path Querying Can be Fast if Cooked Properly

Arseniy Terekhov

Saint Petersburg State University St. Petersburg, Russia

Artyom Khoroshev

!!! !!!

St. Petersburg, Russia

Semyon Grigorev s.v.grigoriev@spbu.ru semen.grigorev@jetbrains.com Saint Petersburg State University St. Petersburg, Russia JetBrains Research St. Petersburg, Russia

ABSTRACT

Recently proposed matrix multiplication based algorithm for context-free path querying (CFPQ) offloads the most performancecritical parts onto boolean matrices multiplication. Thus, it is possible to achieve high performance of CFPQ by means of modern parallel hardware and software. In this paper, we provide results of empirical performance comparison of different implementations of this algorithm on both real-world data and synthetic data for the worst cases.

KEYWORDS

Context-free path querying, transitive closure, graph databases, linear algebra, context-free grammar, GPGPU, CUDA, boolean matrix, matrix multiplication

INTRODUCTION

Formal language constrained path querying, or formal language constrained path problem [3], is a graph analysis problem when formal languages are used as a constraints for navigational path queryes. Namely, in this approach concatenation of the labels along the path is treated as a word, and a specification of the language which should contain specific words is a constraint. While regular path querying (RPQ) is actively used in many different graph query languages and graph analysis engines, more expressive one, contxt-free path querying (CFPQ) [20] at the start stage and activly developed. Context-free constraints allow one to express such important class of queryes as same generation quey [1] which can not be expressed in terms of regular constraints.

Several algorithms for CFPQ based on such parsing techniques as (G)LL, (G)LR, and CYK are proposed recently [4, 5, 8, 10, 13, 15, 16, 18, 21]. But recent research by Jochem Kuijpers et.al. [12] shows that existing solutions are not applicable for real-world graph analysis because running time and memory consumption are poor. At the same time, Nikita Mishin et.al in [14] shows that matrix-based CFPQ algorithm can demonstrate good performance on real-world data. Matrix-based algorithm is proposed by Rustam Azimov [2] and offloads the most critical computations onto boolean matrices multiplication. As a result, it is easy to implement, and allows one to utilize modern massiveparallel hardware for CFPQ. But only algorithm performance without integration with graph storage is provided in the paper while J. Kuijpers provides evaluation of integrated with Neo4j¹ algorithms. Also, in [12] matrix-based algorithm is evaluated in simple single-thread Java implementation, while N. Mishin

In this work we show that CFPQ in relational semantics (according Hellings [9]) can be fast enough to be applicable to realworld graph analysis. We use RedisGraph² [6] garph data base as a storage. This data base use adjacency matrices as arepresenataion of graph and GraphBLAS [11] for matrices manipualtion. These facts allow us to integrate matrix-based CFPQ algorithm to RedisGraph with minimal effort. We make the following contributions in this paper.

- (1) We provide a number of implementations of the matrix multiplication based CFPQ algorithm which uses Redis-Graph as a graph storage. The first implementation is CPU-based and utilize SuteSparse [?] implemenation of GraphBLAS API for matrices manipulation. The second implementation is GPGPU-based and include both existing implementation from [?] and our own CUSP3-based implenetation. The source code is available on GitHub: https://github.com/YaccConstructor/RedisGraph.
- (2) We extend the dataset !!!
- (3) We provide evaluation which shows that !!!.

MATRIX-BASED ALGORITHM FOR CFPQ

Matrix-based algorithm for CFPQ was proposed by Rustam Azimov [2]. This algorithm can be expressed in terms of operations over matrices (see listing 1), and it is a sufficient advantage for implementation. It was shown that the utilization of GPGPU improves the context-free path querying performance significantly in comparison to other implementations [2] even if float matrices are used instead of boolean matrices.

Listing 1 Context-free path quering algorithm

```
1: function ContextFreePathQuerying(D, G)
        n \leftarrow the number of nodes in D
 2:
        E \leftarrow the directed edge-relation from D
 3:
        P \leftarrow the set of production rules in G
        T \leftarrow the matrix n \times n in which each element is \emptyset
 5:
        for all (i, x, j) \in E do
                                                   ▶ Matrix initialization
 6:
             T_{i,j} \leftarrow T_{i,j} \cup \{A \mid (A \rightarrow x) \in P\}
 7:
        while matrix T is changing do
 8:
             T \leftarrow T \cup (T \times T)
                                     ▶ Transitive closure calculation
 9:
10:
        return T
```

Here D = (V, E) is the input graph and $G = (N, \Sigma, P)$ is the input grammar. Each cell of the matrix T contains the set of

shows that the most efficient implementation should utilize highperformance matrix multioplication libraries which are highly parallel, or even utilize GPGPU.

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 $^{^2\}mathrm{Redis}\mathrm{Graph}$ is a graph data base which is based on Property Graph Model. Project web page: https://oss.redislabs.com/redisgraph/. Access data: 12.11.2019.

³CUSp is an open source library for sparse matrix multiplication on GPGPU. !!!.

Access date: 12.11.2019.

nonterminals such that $N_k \in T[i,j] \iff \exists p = v_i \dots v_j$ —path in D, such that $N_k \stackrel{*}{\Longrightarrow} \omega(p)$, where $\omega(p)$ is a word formed by the labels along the path p. Thus, this algorithm solves reachability problem, or, according to Hellings [9], processes CFPQs by using relational query semantics.

The performance-critical part of the algorithm is matrix multiplication. Note, that the set of nonterminals is finite, and we can represent the matrix T as a set of boolean matrices: one for each nonterminal. In this case the operation of matrix update is $T_{N_i} \leftarrow T_{N_i} + (T_{N_j} \times T_{N_k})$ for each production $N_i \rightarrow N_j \ N_k$ in P. Thus we can reduce CFPQ to boolean matrices multiplication. After such transformation, we can apply the next optimization: we can skip update if the matrices T_{N_j} and T_{N_k} have not been changed at the previous iteration.

Thus, the most important part is the efficient implementation of operations over boolean matrices. In this paper, we compare the effects of different approaches to matrices multiplication. All our implementations are based on the optimized version of the algorithm.

3 IMPLEMENTATION

Previous works show [2, 14] that existing linear algebra libraries utilization is a right way to get high-performance CFPQ implementation in minimal effort. But non of these works do not provide evaluation with data storage, only pure time of algorithm execution was mesured.

We provide a number of implementations of matrix-based CFPQ algorithm. All of them a based on RedisGraph — we use RedisGraph as a storage and implement CFPQ as an extension by using provided mechanism. Note thet currenly we do not provide full integration with querying mechanism: one can not use Cypher, which uses in RedisGraph as a query language. Instead, in current omplementation query provided explicately as an file with grammar in Chomsky normal form [?]. So, we can evaluate querying algorithms, but we should improve integration to make our solution applicable.

 $\ensuremath{\mathbf{CPU}}\xspace$ based implementation. Details on CPU implemenattion

 $\ensuremath{\mathbf{GPGPU}}$ -based implementation. Details on GPGPU implementation

4 DATASET DESCRIPTION

In our evaluation we use combined dataset which contains the following parts.

- CFPQ_Data dataset which provided in⁴ [14] and contains both syntethic and real-world graphs and queryes. Realworld data includes RDFs, syntatic cases include theoretical worst-case and random graphs.
- Dataset which provided in [12]. We integrate both Geospecies and Synthetic data sets into CFPQ_Data and use it in our evaluation.
- New bigger RDFs, such as !!!!. In [14] was shown that matrix-based algorithm is performed enough to handle bigger RDFs than used in initial data sets, such as [21]. So, we add a number of big RDFs to CFPQ_Data and use them in our evaluation.

The variants of the *same generation query* [1] is used in almost all cases because it is an important example of real-world queries that are context-free but not regular.

[RDF] The set of the real-world RDF files (ontologies) from [21] and two variants of the same generation query which describes hierarchy analysis. The first query is the grammar G_4 :

$$s \rightarrow SCOR \ s \ SCO$$
 $s \rightarrow TR \ s \ T$
 $s \rightarrow SCOR \ SCO$ $s \rightarrow TR \ T$

The second one is the grammar G_5 : $s \rightarrow SCOR s SCO \mid SCO$.

[Worst] The theoretical worst case for CFPQ time complexity proposed by Hellings [10]: the graph is two cycles of coprime lengths with a single common vertex. The first cycle is labeled by the open bracket and the second cycle is labeled by the close bracket. Query is a grammar for the A^nB^n language. The example of such graph and grammar is presented in figure:

$$s \to A s B$$
$$s \to A B$$

[Full] The case when the input graph is sparse, but the result is a full graph. Such a case may be hard for sparse matrices representations. As an input graph, we use a cycle, all edges of which are labeled by the same token. As a query we use two grammars which describe the sequence of tokens of arbitrary length: the simple ambiguous grammar $G_2: s \rightarrow s \mid A$, and the highly ambiguous grammar $G_3: s \rightarrow s \mid A$.

[Sparse] Sparse graphs from [7] are generated by the GTgraph graph generator, and emulate realistic sparse data. Names of these graphs have the form Gn-p, where n corresponds to the total number of vertices, and p is the probability that some pair of vertices is connected. The query is the same generation query represented by the grammar G_1 (figure ??).

5 EVALUATION

We evaluate all the described implementations on all the datasets and the queries presented. We compare our implementations with [2]. We exclude the time required to load data from files. The time required for data transfer is included.

For evaluation, we use a PC with Ubuntu 18.04 installed. It has Intel core i7 8700k 3,7HGz CPU, DDR4 32 Gb RAM, and Geforce 1080Ti GPGPU with 11Gb RAM.

The results of the evaluation are summarized in the tables below. Time is measured in seconds unless specified otherwise. The result for each algorithm is averaged over 10 runs. The cell is left blank if the time limit is exceeded, or if there is not enough memory to allocate the data.

The results of the first dataset [RDF] are presented in table 1. We can see, that in this case the running time of all our implementations is smaller than of the reference implementation, and all implementations but [CuSprs] demonstrate similar performance. It is obvious that performance improvement in comparison with the first implementation is huge and it is necessary to extend the dataset with new RDFs of the significantly bigger size.

⁴CFPQ_Data data set GitHub repository: https://github.com/JetBrains-Research/CFPO Data. Access date: 12.11.2019.

Table 1: RDFs querying results (time in milliseconds)

RDF			Query G_4						Query G ₅					
Name	#V	#E	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
atm-prim	291	685	3	2	2	1	5	269	1	< 1	1	< 1	2	267
biomed	341	711	3	5	2	1	5	283	4	< 1	1	< 1	5	280
foaf	256	815	2	9	2	< 1	5	270	1	< 1	1	< 1	2	263
funding	778	1480	4	7	4	1	5	279	2	< 1	3	< 1	4	274
generations	129	351	3	3	2	< 1	5	273	1	< 1	1	< 1	2	263
people_pets	337	834	3	3	3	1	7	284	1	< 1	1	< 1	3	277
pizza	671	2604	6	8	3	1	6	292	2	< 1	2	< 1	5	278
skos	144	323	2	4	2	< 1	5	273	< 1	< 1	1	< 1	2	265
travel	131	397	3	5	2	< 1	6	268	1	< 1	1	< 1	3	271
unv-bnch	179	413	2	4	2	< 1	5	266	1	< 1	1	< 1	3	266
wine	733	2450	7	6	4	1	7	294	1	< 1	3	< 1	3	281

Table 2: Evaluation results for the worst case

#V	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
16	0.032	< 1	0.008	0.002	0.027	0.309
32	0.118	0.001	0.034	0.008	0.136	0.441
64	0.476	0.041	0.133	0.032	0.524	0.988
128	2.194	0.226	0.562	0.129	2.751	3.470
256	15.299	1.994	3.088	0.544	11.883	15.317
512	121.287	23.204	13.685	2.499	43.563	102.269
1024	1593.284	528.521	88.064	19.357	217.326	1122.055
2048	-	-	-	325.174	-	-

Results of the theoretical worst case ([Worst] dataset) are presented in table 2. This case is really hard to process: even for a graph of 1024 vertices, the query evaluation time is greater than 10 seconds even for the most performant implementation. We can see, that the running time grows too fast with the number of vertices.

Table 3: Sparse graphs querying results

Graph	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs
G5k-0.001	10.352	0.647	0.113	0.041	0.216	5.729
G10k-0.001	37.286	2.395	0.435	0.215	1.331	35.937
G10k-0.01	97.607	1.455	0.273	0.138	0.763	47.525
G10k-0.1	601.182	1.050	0.223	0.114	0.859	395.393
G20k-0.001	150.774	11.025	1.842	1.274	6.180	-
G40k-0.001	-	97.841	11.663	8.393	37.821	-
G80k-0.001	-	1142.959	88.366	65.886	-	-

The next is the **[Sparse]** dataset presented in table 3. The evaluation shows that sparsity of graphs (value of parameter p) is important both for implementations which use sparse matrices and for implementations which use dense matrices. Note that the behavior of the sparse matrices based implementation is as expected, but for dense matrices we can see, that more sparse graphs are processed faster. Reasons for such behavior demand further investigation. Note that we estimate only the query execution time, so it is hard to compare our results with the results presented in [7]. Nevertheless, the running time of our **[GPU_N]** implementation is significantly smaller than the one provided in [7].

The last dataset is **[Full]**, and results are shown in table 4. As we expect, this case is very hard for sparse matrices based

implementations: the running time grows too fast. This dataset also demonstrates the impact of the grammar size. Both queries specify the same constraints, but the grammar G_3 in CNF contains 2 times more rules then the grammar G_2 , so, the running time for big graphs differs by more than twice.

Finally, we can conclude that GPGPU utilization for CFPQ can significantly improve performance, but more research on advanced optimization techniques should be done. On the other hand, the high-level implementation ([GPU_Py]) is comparable with other GPGPU-based implementations. So, it may be a balance between implementation complexity and performance. Highly optimized existing libraries can be of some use: the implementation based on m4ri is faster than the reference implementation and the other CPU-based implementation. Moreover, it is comparable with some GPGPU-based implementations in some cases. Sparse matrices utilization demands more thorough investigation. The main question is if we can create an efficient implementation for sparse boolean matrices multiplication.

6 DISCUSSION

First of all, note that dispite in [?] shows that CPU implementations (both dense and sparse matrix based) are relatively slow, our CPU implementation demonstrates good performance on real-world data.

Zeros in sparse matrices.

Overhead on matrices convertion and transferring when run on GPGPU.

No convertion when run on CPU. Beter then Neo4j and other BD with non-matrix representation of graphs.

7 CONCLUSION AND FUTURE WORK

We provide an CPU and GPGPU based context-free path querying implementations for RedisGraph and show that CFPQ can be fast enough to analize real-world data. But our implementations are on prototype stage and we should provide full integration of CFPQ to RedisGraph. First of all it is necessary to extend Cupher graph query language, which uses in RedisGraph, to support respective syntax for context-free constraints specification. There is a proposal whish describes such syntax extension⁵ and we plan

⁵Proposal with path pattern syntax for openCypher: https://github.com/thobe/openCypher/blob/rpq/cip/1.accepted/CIP2017-02-06-Path-Patterns.adoc. It is shown that context-free constraints are expressible in proposrd syntax. Access date: 12.11.2019

Table 4: Full querying results

#V	Query G ₂							Query G ₃					
# V	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs	Scipy	M4RI	GPU4R	GPU_N	GPU_Py	CuSprs	
100	0.007	0.002	0.002	< 1	0.003	0.278	0.023	0.076	0.005	0.001	0.007	0.290	
200	0.040	0.003	0.002	0.001	0.004	0.279	0.105	0.098	0.004	0.001	0.007	0.296	
500	0.480	0.003	0.003	0.001	0.004	0.329	1.636	0.094	0.007	0.001	0.010	0.382	
1000	3.741	0.007	0.005	0.001	0.006	0.571	13.071	0.106	0.009	0.001	0.009	0.839	
2000	40.309	0.063	0.019	0.003	0.017	1.949	93.676	0.108	0.030	0.005	0.026	3.740	
5000	651.343	0.366	0.125	0.038	0.150	99.651	1205.421	0.851	0.195	0.075	0.239	201.151	
10000	-	1.932	0.552	0.315	0.840	1029.042	-	4.690	1.055	0.648	1.838	-	
25000	-	33.236	7.252	5.314	15.521	-	-	70.823	15.240	10.961	36.495	-	
50000	-	360.035	58.751	44.611	129.641	-	-	775.765	130.203	91.579	226.834	-	
80000	-	1292.817	256.579	190.343	641.260	-	-	-	531.694	376.691	-	-	

to support proposed sintax in lib cypher-parser 6 which uses in Redis Graph.

In current version we use CUSP matrix multiplication library for GPGPU utilization, but it may be better to use GraphBLAST⁷ [19] — Gunrock⁸ [17] based implementation of GraphBLAS API for GPGPU. Firs of all, we should evaluate GraphBlast based implementation of CFPQ. Also, we should investigate to implement multi-GPU support for GraphBlast, because it should improve performance of huge real-world data processing.

Our implementations calculate queryes in respect to relational semantics, but in sume cases it is necessary to provide a path which satisfied constraints. As we know, matrix based algorithm for single path or all paths semantix is not prvided yet, and it is a direction for future research.

Another important question for future research is how to update query result dynamically when data changes. Mechanism for result updating allows one to recalculate qury faster and use result as an index for other queryes.

Also, futer improvements of the dataset are required. For example, it is necessary to include real-world cases from static code analysis [?].

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