MCV4U

CALCULUS & VECTORS

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Alexandru Stan Vectors

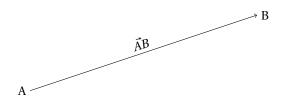
1 Vectors

Vectors are mathematical entities that extend our understanding beyond the one-dimensional quantities. Unlike scalar values that only have magnitude, vectors incorporate both magnitude and direction, offering a versatile toolkit for describing dynamic systems.

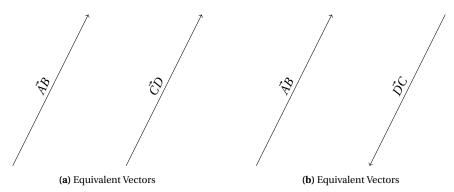
- Scalar Quantities: Mass, Temperature, Time, Distance, Speed, Energy, Work, Power, etc.
- Vector Quantities: Displacement, Velocity, Acceleration, Force, Momentum, etc.

When written in mathematical equations, vectors are usually represented via a a symbol with a vector indicator (i.e \vec{v}) or via a jointery of the two points (i.e \vec{AB} is a vector from point A to point B) Vectors can also be represented in many other ways, but the most common ways are: algebraically, numerically, and geometrically. Below are examples of each:

- Algebraically: $\vec{a} = \langle x, y \rangle$
- Numerically: $\vec{a} = [a, b, c]$ (Can also be written as a column matrix)
- Geometrically:



Vectors can be equal (or equivalent) to each other. For two vectors to be equal (or equivalent) they must have the same magnitude and direction. Vectors can also be opposite to each other; to be opposing vectors must have the same magnitude but opposite directions (i.e $\vec{v} = -\vec{v}$).



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4 Derivatives

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- 4.5 The Chain, Product, and Quotient Rules
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- 5 Curve Sketching
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