

MCV4U

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# **CALCULUS & VECTORS**

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# **1 Vectors**

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## **1.3 Properties of Vectors**

## **1.4 Vectors as Forces**

## **1.5 Vectors as Velocity**

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# **3 Limits and Continuity**

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## **3.3 Asymptotes and Holes**

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