

The formula for the integration of finding the volume between two functions is

$$V = \pi \int_a^b (R^2) dx$$

where  $R$  is the top function minus the bottom function.

**Example:**

Region  $R$  is bounded by the lines  $y = 4, x = 6$ , y-axis, and the x-axis. Region  $R$  is rotated around the x-axis.

$$R = 4 - 0$$

$$R = 4$$

$$\begin{aligned} V &= \pi \int_0^6 R^2 dx \\ &= \pi \int_0^6 16 dx \\ &= \pi \cdot 16x \Big|_0^6 \\ &= \pi \cdot (16(6) - 16(0)) \\ &= \pi 96 \qquad \qquad \qquad = 96\pi \end{aligned}$$