Q1. Design MapReduce algorithms to take a very large file of integers and produce the output as same set of integers, but with each integer appearing only once.

Q2. Suppose there are 100 items, numbered 1 to 100, and also 100 baskets, also numbered 1 to 100. Item i is in basket b if and only if i divides b with no remainder. Thus, item 1 is in all the baskets, item 2 is in all fifty of the even-numbered baskets, and so on. Basket 12 consists of items {1, 2, 3, 4, 6, 12}. If the support threshold is 5, which items are frequent?

Q3. For the data of Q2, what is the confidence of the following association rules?

- (a) $\{5, 7\} \rightarrow 2$.
- (b) $\{2, 3, 4\} \rightarrow 5$.

Q4. If we use a triangular matrix to count pairs, and n, the number of items, is 20, what pair's count is in a[100]?

Q5. Apply the A-Priori Algorithm with support threshold 5 to the data of Q2.

Q6. Here is a collection of twelve baskets. Each contains three of the six items 1 through 6. $\{1, 2, 3\}$ $\{2, 3, 4\}$ $\{3, 4, 5\}$ $\{4, 5, 6\}$ $\{1, 3, 5\}$ $\{2, 4, 6\}$ $\{1, 3, 4\}$ $\{2, 4, 5\}$ $\{3, 5, 6\}$ $\{1, 2, 4\}$ $\{2, 3, 5\}$ $\{3, 4, 6\}$ Suppose the support threshold is 4. On the first pass of the PCY Algorithm we use a hash table with 11 buckets, and the set $\{i, j\}$ is hashed to bucket $i \times j$ mod 11.

- (a) By any method, compute the support for each item and each pair of items
- (b) Which pairs hash to which buckets?
- (c) Which buckets are frequent?
- (d) Which pairs are counted on the second pass of the PCY Algorithm?