## Verse Tutorial Drone

November 7, 2022

### 1 1. Getting Started

A verse scenario is defined by a map, a set of agents and, if there exist multiple agents, a sensor.

In this section, we are going to look at how to create a simple scenario in Verse. In this scenario we will have a drone following a straight track and will avoid by moving upwards to avoid a static obstacle at known position in the track.

#### 1.1 1.1 Instantiate map

The map of a scenario specifies the tracks that the agents can follow. In this example, we will only look at a simple map with two types of tracks: 1) type T0, which describe straight track that align with x-axis and 2) type TAvoidUp, which describes set of tracks with upward direction that the agent can follow while avoiding the obstacle. The types of tracks will also be referred as track modes in later sections. We will discuss in detail how to create maps in later sections. In this section we will import a pre-defined map.

```
[1]: from tutorial_map import M3
map1 = M3()
```

```
`polytope` failed to import `cvxopt.glpk`.
will use `scipy.optimize.linprog`
```

#### 1.2 1.2 Creating agent

To create such a scenario in Verse, we first need to create an agent for Verse. An agent in Verse is defined by a set of tactical modes, a decision logic to determine the transition between tactical modes, and a flow function that defines continuous evolution. The agent's tactical mode and decision logic are provided as python code strings and the flow function is provided as a python function.

The tactical mode of the agents corresponds to an agent's decision. For example, in this drone avoidance example, the tactical mode for the agent can be Normal and AvoidUp. The decision logic also need to know the available track modes from the map. The tactical modes and track modes are provided as Enums to Verse.

```
[2]: from enum import Enum, auto class CraftMode(Enum):
```

```
Normal = auto()
AvoidUp = auto()

class TrackMode(Enum):
   T0 = auto()
   TAvoidUp = auto()
```

We also require the user to provide the continuous and discrete variables of the agents together with the decision logic. The variables are provided inside class with name State. Variables end with \_mode will be identify by verse as discrete variables. In the example below, craft\_mode and track\_mode are the discrete variables and x, y, z, vx, vy, vz are the continuous variables. The type hints for the discrete variables are necessary to associate discrete variables with the tactical modes and lane modes defined above

```
[3]: class State:
    x: float
    y: float
    z: float
    vx: float
    vy: float
    vz: float
    vz: float
    craft_mode: CraftMode
    track_mode: TrackMode

def __init__(self, x, y, z, vx, vy, vz, craft_mode, track_mode):
    pass
```

The decision logic describe for an agent takes as input its current state and the (observable) states of the other agents if there's any, and updates the tactical mode of the ego agent. In this example, the decision logic is traight forward: When the x position of the drone is close to the obstacle (20m), the drone will start moving upward. There's no other agents in this scenario. The decision logic of the agent can be written in an expressive subset of Python inside function decisionLogic.

We incoperate the above definition of tactical modes and decision logic into code strings and combine it with an imported agent flow, we can then obtain the agent for this sceanio.

```
[5]: from tutorial_agent import DroneAgent
```

/home/younger/work/GraphGeneration/venv/lib/python3.8/site-packages/tqdm/auto.py:22: TqdmWarning:

IProgress not found. Please update jupyter and ipywidgets. See https://ipywidgets.readthedocs.io/en/stable/user\_install.html

#### 1.3 Creating scenario

With the agent and map defined, we can now define the scenario.

```
[6]: from verse.scenario import Scenario scenario = Scenario()
```

We can set the initial condition of the agent and add the agent

and set the map for the sceanrio

```
[8]: scenario.set_map(map1)
```

Since we only have one agent in the scenario, we don't need to specify a sensor.

We can then compute simulation traces or reachable states for the scenario

```
[9]: traces_simu = scenario.simulate(60, 0.2)
traces_veri = scenario.verify(60, 0.2)
```

```
[[0.1554601575803395, 0.3955486440796425, -0.3045528704609429, 0.0, 0.0, 0.0]] {'drone1': ['Normal', 'T0']} {'drone1': ('AvoidUp', 'TAvoidUp')}
```

We can visualize the results using functions provided with Verse

```
[10]: from verse.plotter.plotter3D import *
   import pyvista as pv
   import warnings
   warnings.filterwarnings("ignore")
   from verse.plotter.plotter2D import *
   import plotly.graph_objects as go

fig = go.Figure()
   fig = reachtube_tree(traces_veri, None, fig, 1, 3)
   fig.show()
```

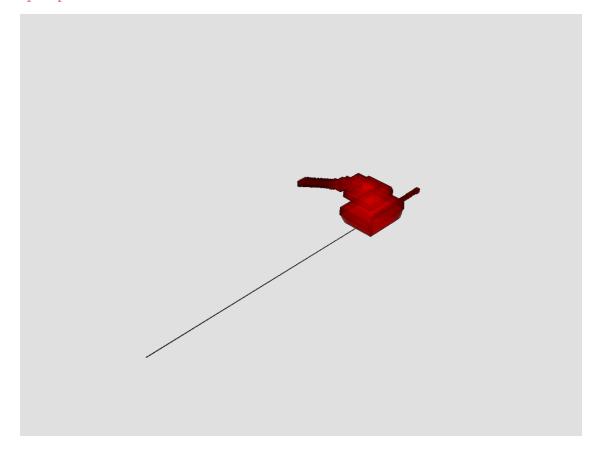
```
pv.set_jupyter_backend(None)
fig = pv.Plotter()
fig = plot3dMap(map1, ax=fig)
fig = plot3dReachtube(traces_veri, 'drone1', 1, 2, 3, color = 'r', ax=fig)
fig.set_background('#e0e0e0')
fig.show()
```

```
ERROR:root:<<Cannot triangulate; no input points
2022-11-07 16:15:09.234 ( 5.026s) [ 1A1B9740]

vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x6c02850): <<Cannot triangulate;
no input points

ERROR:root:<<Cannot triangulate; no input points
2022-11-07 16:15:09.431 ( 5.222s) [ 1A1B9740]

vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x6db9920): <<Cannot triangulate;
no input points
```



## 2 2. Adding multiple agents

In the previous section, we played around with a scenario with a single drone. In this example, we will create a scenario with multiple agents and explore the potential of Verse to handle multi-agent scenarios.

In this example, we will look at a two drone collision avoidance example. In this example, we have two drones running in a map with three parallel tracks arranged in vertical directions. The two drones are running in the same direction on the middle track. However, the later drone is moving faster than the drone in the front and it will perform a track switch while getting close to the front drone to avoid collision.

We will first setup a new scenario and add the map.

```
[11]: from verse.scenario import Scenario
from tutorial_map import M4
scenario = Scenario()
scenario.set_map(M4())
```

```
[12]: from enum import Enum, auto
      class CraftMode(Enum):
          Normal = auto()
          MoveUp = auto()
          MoveDown = auto()
      class TrackMode(Enum):
          T0 = auto()
          T1 = auto()
          T2 = auto()
          M01 = auto()
          M10 = auto()
          M12 = auto()
          M21 = auto()
      class State:
          x: float
          y: float
          z: float
          vx: float
          vy: float
          vz: float
          craft_mode: CraftMode
          track_mode: TrackMode
          def __init__(self, x, y, z, vx, vy, vz, craft mode, track mode):
              pass
```

Verse's decision logic support python any and all functions, which allows the decision logic to

quantify over other agents in the scenario. This enable user to easily create multi-agent scenario. In addition, the support of user defined functions, such as the is\_close function in example, enable user to write more complicated decision logic. In this case, the decision logic will take an additional argument others, which provides the states for other agents. Notice the type hint for both ego and others. The updated agent's decision logic looks like following.

```
[13]: from typing import List
      import copy
      def is_close(ego, other):
          res = ((other.x - ego.x < 10 and other.x-ego.x > 8) or\
              (other.y-ego.y < 10 and other.y-ego.y > 8) or\
              (other.z-ego.z < 10 and other.z-ego.z > 8))
          return res
      def decisionLogic(ego: State, others: List[State], track_map):
          next = copy.deepcopy(ego)
          if ego.craft_mode == CraftMode.Normal:
              if any(ego.x<other.x and (is_close(ego, other) and ego.track_mode ==__
       →other.track_mode) for other in others):
                  if track_map.h_exist(ego.track_mode, ego.craft_mode, CraftMode.
       →MoveUp):
                      next.craft_mode = CraftMode.MoveUp
                      next.track_mode = track_map.h(
                          ego.track_mode, ego.craft_mode, CraftMode.MoveUp)
                  if track_map.h_exist(ego.track_mode, ego.craft_mode, CraftMode.
       →MoveDown):
                      next.craft_mode = CraftMode.MoveDown
                      next.track mode = track map.h(
                          ego.track_mode, ego.craft_mode, CraftMode.MoveDown)
          if ego.craft_mode == CraftMode.MoveUp:
              if track map.altitude(ego.track mode)-ego.z > -1 and track map.
       →altitude(ego.track_mode)-ego.z < 1:</pre>
                  next.craft_mode = CraftMode.Normal
                  if track_map.h_exist(ego.track_mode, ego.craft_mode, CraftMode.
       →Normal):
                      next.track_mode = track_map.h(
                          ego.track_mode, ego.craft_mode, CraftMode.Normal)
          if ego.craft_mode == CraftMode.MoveDown:
              if track_map.altitude(ego.track_mode)-ego.z > -1 and track_map.
       →altitude(ego.track_mode)-ego.z < 1:</pre>
                  next.craft_mode = CraftMode.Normal
                  if track_map.h_exist(ego.track_mode, ego.craft_mode, CraftMode.
       →Normal):
```

With the updated decision logic, we can now spawn the two agents with their initial conditions.

```
[14]: from tutorial_agent import DroneAgent
drone1 = DroneAgent(
    'drone1', file_name="dl_sec2.py", t_v_pair=(1, 1), box_side=[0.4]*3)
drone1.set_initial(
    [[1.5, -0.5, -0.5, 0, 0, 0], [2.5, 0.5, 0.5, 0, 0, 0]],
    (CraftMode.Normal, TrackMode.T1)
)

drone2 = DroneAgent(
    'drone2', file_name="dl_sec2.py", t_v_pair=(1, 0.5), box_side=[0.4]*3)
drone2.set_initial(
    [[19.5, -0.5, -0.5, 0, 0, 0], [20.5, 0.5, 0.5, 0, 0, 0]],
    (CraftMode.Normal, TrackMode.T1)
)
```

We can then add both agents to the scenario

```
[15]: scenario.add_agent(drone1) scenario.add_agent(drone2)
```

With multiple agents in the scenario, we now need to add the sensor. The sensor defines how an agent is visible to other agents. In this example, we will use the default sensor function, which allows all agents to see all variables of other agents.

```
[16]: from tutorial_sensor import DefaultSensor scenario.set_sensor(DefaultSensor())
```

With the scenario fully constructed, we can now simulte or verify the scenario using the simulate/verify function provided by Verse.

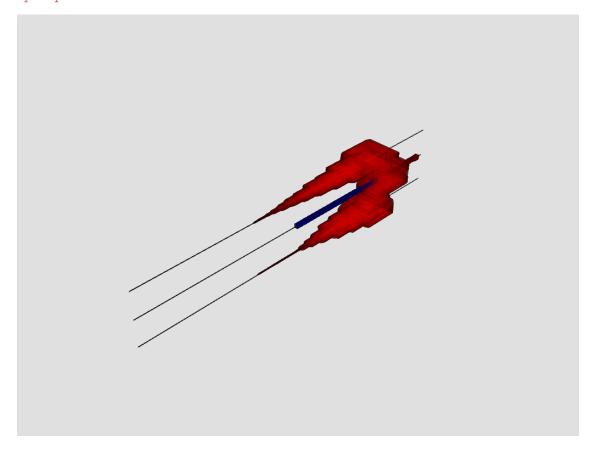
```
[17]: traces_simu = scenario.simulate(60, 0.2)
    traces_veri = scenario.verify(60, 0.2)

[[1.7282577505653176, 0.08540687746402953, 0.07775026721030665, 0.0, 0.0, 0.0],
    [19.730277006707553, -0.35131880977723906, 0.09544590274581732, 0.0, 0.0, 0.0]]
    {'drone1': ['Normal', 'T1'], 'drone2': ['Normal', 'T1']}
    {'drone1': ('MoveDown', 'M12'), 'drone2': ['Normal', 'T1']}
    {'drone1': ('MoveUp', 'M10'), 'drone2': ['Normal', 'T1']}
    {'drone1': ('Normal', 'T2'), 'drone2': ['Normal', 'T1']}
    {'drone1': ('Normal', 'T0'), 'drone2': ['Normal', 'T1']}
```

We can visualize the results using functions provided with Verse

```
[18]: from verse.plotter.plotter3D import *
      import pyvista as pv
      import warnings
      warnings.filterwarnings("ignore")
      from verse.plotter.plotter2D import *
      import plotly.graph_objects as go
      fig = go.Figure()
      fig = reachtube_tree(traces_veri, None, fig, 1, 3)
      fig.show()
      pv.set_jupyter_backend(None)
      fig = pv.Plotter()
      fig = plot3dMap(M4(), ax=fig)
      fig = plot3dReachtube(traces_veri, 'drone1', 1, 2, 3, color = 'r', ax=fig)
      fig = plot3dReachtube(traces_veri, 'drone2', 1, 2, 3, color = 'b', ax=fig)
      fig.set_background('#e0e0e0')
      fig.show()
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:15:28.728 ( 24.520s) [
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x6fd7520): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:15:28.827 ( 24.619s) [
                                                   1A1B9740]
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x662c4f0): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:15:32.886 ( 28.677s) [
                                                   1A1B97407
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x74d38d0): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:15:34.529 ( 30.320s) [
                                                   1A1B9740]
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x9034b90): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:15:35.422 ( 31.214s) [
                                                   1A1B9740]
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x806e420): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
```

```
2022-11-07 16:15:35.886 ( 31.678s) [ 1A1B9740] vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x8075a00): <<Cannot triangulate; no input points
```



# 3 3. Adding safety assertions

```
[19]: from enum import Enum, auto

class CraftMode(Enum):
    Normal = auto()
    MoveUp = auto()
    MoveDown = auto()

class TrackMode(Enum):
    T0 = auto()
    T1 = auto()
    T2 = auto()
    M01 = auto()
    M10 = auto()
```

```
M12 = auto()
M21 = auto()

class State:
    x: float
    y: float
    z: float
    vx: float
    vx: float
    vy: float
    vz: float
    vz: float
    craft_mode: CraftMode
    track_mode: TrackMode

def __init__(self, x, y, z, vx, vy, vz, craft_mode, track_mode):
        pass
```

Verse allow checking safety conditions while performing simulation and verification. The safety conditions in verse can be specified using Python assert statements in the decision logic. With the any and all functions, the user can also define safety conditions between different agents. In this example, we are going to add two safety conditions: 1) the distance between two agents in all x,y,z direction should always be greater than or equal to 1.0m and 2) both drones should never enter region  $40 \le x \le 50$ ,  $-5 \le y \le 5$ ,  $-10 \le z \le -6$ . The two safety asserts in the decisionLogic is shown below.

```
[20]: from typing import List
import copy

def decisionLogic(ego: State, others: List[State], track_map):
    next = copy.deepcopy(ego)
    '''
    '''
    '''

assert not any(ego.x-other.x < 1 and ego.x-other.x >-1 and \
    ego.y-other.y < 1 and ego.y-other.y > -1 and \
    ego.z-other.z < 1 and ego.z-other.z > -1 \
    for other in others),\
    "Safe Seperation"

assert not (ego.x > 40 and ego.x<50 and\
    ego.y>-5 and ego.y<5 and\
    ego.z > -10 and ego.z<-6),\
    "Unsafe Region"

return next</pre>
```

We can then construct the two agents and the scenario exactly as previous section.

```
[21]: from verse.scenario import Scenario
      from tutorial_map import M4
      scenario = Scenario()
      scenario.set_map(M4())
      from tutorial_agent import DroneAgent
      drone1 = DroneAgent(
          'drone1', file_name="dl_sec3.py", t_v_pair=(1, 1), box_side=[0.4]*3)
      drone1.set initial(
          [[1.5, -0.5, -0.5, 0, 0, 0], [2.5, 0.5, 0.5, 0, 0, 0]],
          (CraftMode.Normal, TrackMode.T1)
      scenario.add_agent(drone1)
      drone2 = DroneAgent(
          'drone2', file_name="dl_sec3.py", t_v_pair=(1, 0.5), box_side=[0.4]*3)
      drone2.set_initial(
          [[19.5, -0.5, -0.5, 0, 0, 0], [20.5, 0.5, 0.5, 0, 0, 0]],
          (CraftMode.Normal, TrackMode.T1)
      scenario.add_agent(drone2)
      from tutorial_sensor import DefaultSensor
      scenario.set sensor(DefaultSensor())
```

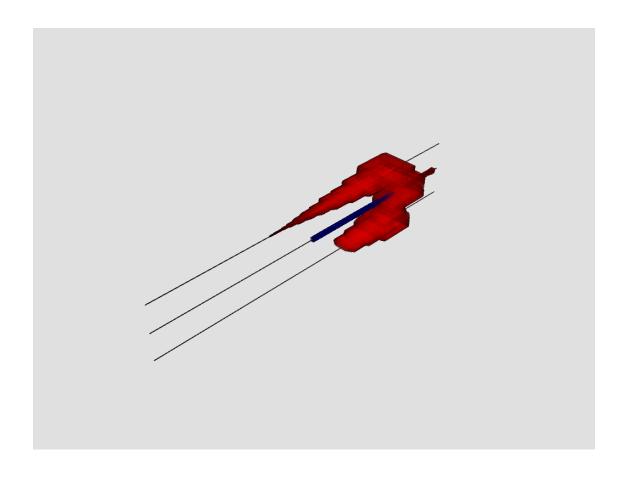
We can then simulate and verify the scenario and visualize the result. We can see from the result that dronel enters the unsafe region, which causes a safety condition violation.

```
[22]: traces_simu = scenario.simulate(60, 0.2) traces_veri = scenario.verify(60, 0.2)
```

```
[[1.6111335651903043, 0.07348944779204591, -0.16302361304087332, 0.0, 0.0, 0.0], [20.050869485505267, -0.3774960641282338, 0.2993567780810662, 0.0, 0.0, 0.0]] assert hit for drone1: "Unsafe Region" @ {'ego': State(x=40.155662519148656, y=-0.0052531542151459665, z=-8.003024308341452, vx=1.1811397597899211, vy=-3.885780586188048e-16, vz=-1.8096635301390052e-14, craft_mode='Normal', track_mode='T2'), 'others': [State(x=40.720812681318904, y=-0.06252528803051342, z=0.13935740713066597, vx=0.3937132532633005, vy=-9.43689570931383e-16, vz=-1.9761969838327786e-14, craft_mode='Normal', track_mode='T1')], 'track_map': <tutorial_map.M4 object at 0x7f87f4b9b6d0>} {'drone1': ['Normal', 'T1'], 'drone2': ['Normal', 'T1']} {'drone1': ('MoveDown', 'M12'), 'drone2': ['Normal', 'T1']} {'drone1': ('Norwal', 'T2'), 'drone2': ['Normal', 'T1']} assert hit for drone1: "Unsafe Region" 69 {'drone1': ('Normal', 'T0'), 'drone2': ['Normal', 'T1']}
```

```
[23]: from verse.plotter.plotter3D import *
      import pyvista as pv
      import warnings
      warnings.filterwarnings("ignore")
      from verse.plotter.plotter2D import *
      import plotly.graph_objects as go
      fig = go.Figure()
      fig = reachtube_tree(traces_veri, None, fig, 1, 3)
      fig.show()
      pv.set_jupyter_backend(None)
      fig = pv.Plotter()
      fig = plot3dMap(M4(), ax=fig)
      fig = plot3dReachtube(traces_veri, 'drone1', 1, 2, 3, color = 'r', ax=fig)
      fig = plot3dReachtube(traces_veri, 'drone2', 1, 2, 3, color = 'b', ax=fig)
      fig.set_background('#e0e0e0')
      fig.show()
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:16:35.385 ( 91.177s) [
                                                  1A1B9740]
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x7a53ff0): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:16:35.518 ( 91.309s) [
                                                   1A1B9740]
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x92b55e0): <<Cannot triangulate;
     no input points
     ERROR:root:<<Cannot triangulate; no input points</pre>
     2022-11-07 16:16:38.978 ( 94.770s) [
                                                   1A1B97407
     vtkDelaunay3D.cxx:456 ERR| vtkDelaunay3D (0x7ead3e0): <<Cannot triangulate;
```

no input points



# 4 4. Creating agent flow function

In previous sections, we discussed about how to create the decision logic for agents in Verse, in section we will look into detail about how the agent flows are specified and how the pieces are combined together for an agent in Verse.

In this example, we will look at a simple kinetic bicycle model. The dynamics equations of the car are given by

$$\dot{x} = v\cos(\theta)$$

$$\dot{y} = v\sin(\theta)$$

$$\dot{\theta} = \frac{v}{L} * \tan(\delta)$$

$$\dot{x} = a$$

which are implemented as in the car\_dynamics function below

```
[24]: import numpy as np
  def car_dynamics(t, state, u):
      x, y, theta, v = state
      delta, a = u
      x_dot = v*np.cos(theta+delta)
```

```
y_dot = v*np.sin(theta+delta)
theta_dot = v/1.75*np.tan(delta)
v_dot = a
return [x_dot, y_dot, theta_dot, v_dot]
```

The flow function define the continuous time evolution of agents' continuous states. It takes as input the initial states of the agent and the a time, and outputs the state of the agent from that initial states at that time. In Verse, the flow function is implemented by the TC\_simulate function in the agent class. The TC\_simulate takes as input a mode, a initial continuous states, a time bound, a simulation time step and the map. It will output simulation of agent dynamics at given mode starting from the initial continuous states, until the time bound with time step as an np array. Below shows an implementation of the TC\_simulate function for the car agent. Note some detail helper functions for the car dynamics placed in tutorial\_utils are not shown explicitly in the example below.

```
[25]: from tutorial_utils import car_action_handler
      from typing import List
      import numpy as np
      from scipy.integrate import ode
      def TC simulate(mode: List[str], initialCondition, time bound, time step,
       →track_map=None)->np.ndarray:
          time_bound = float(time_bound)
          number_points = int(np.ceil(time_bound/time_step))
          t = [round(i*time_step,10) for i in range(0,number_points)]
          init = initialCondition
          trace = [[0]+init]
          for i in range(len(t)):
              steering, a = car_action_handler(mode, init, track_map)
              r = ode(car_dynamics)
              r.set_initial_value(init).set_f_params([steering, a])
              res:np.ndarray = r.integrate(r.t + time_step)
              init = res.flatten().tolist()
              trace.append([t[i] + time_step] + init)
          return np.array(trace)
```

With the TC\_simulate function specified, we can now combine all parts together to construct a new car agent. An agent class for Verse should have four attributes: 1) id: an unique identifier for each agent in a scenario, 2) controller: a ControllerIR object, which is an intermediate representation of decisionLogic in Verse. It can be constructed automatically by passing in the decision logic code strings described in previous sections, 3) TC\_simulate function, and 4) functions for setting initial condition of the agent, which can be inherited from BaseAgent class.

```
[26]: from verse.parser.parser import ControllerIR from verse.agents import BaseAgent
```

```
class CarAgent(BaseAgent):
    def __init__(self, id, code = None, file_name = None):
        self.id = id
        self.decision_logic = ControllerIR.parse(code, file_name)
        self.TC_simulate = TC_simulate
```

We are going to test this CarAgent in a two car scenario with simple braking decision logic in an one track map. We can setup the scenario in Verse as we discussed in the previous section and simulate/verify the scenario. The results are visualized below.

```
[27]: from enum import Enum, auto
      class AgentMode(Enum):
          Normal = auto()
          Brake = auto()
      class TrackMode(Enum):
          T0 = auto()
      from verse.scenario import Scenario
      from tutorial_map import M1
      scenario = Scenario()
      scenario.set_map(M1())
      car1 = CarAgent('car1', file_name="dl_sec4.py")
      car1.set_initial([[0,-0.5,0,2],[1,0.5,0,2]], (AgentMode.Normal, TrackMode.T0))
      car2 = CarAgent('car2', file_name="dl_sec4.py")
      car2.set_initial([[15,-0.5,0,1],[16,0.5,0,1]], (AgentMode.Normal, TrackMode.T0))
      scenario.add_agent(car1)
      scenario.add_agent(car2)
      traces_simu = scenario.simulate(10, 0.01)
      traces_veri = scenario.verify(10, 0.01)
      import plotly.graph_objects as go
      from verse.plotter.plotter2D import *
      fig = go.Figure()
      fig = simulation_tree(traces_simu, None, fig, 0, 1, [0, 1], 'lines', 'trace')
      fig.show()
      fig = go.Figure()
      fig = reachtube_tree(traces_veri, None, fig, 0, 1, [0, 1], 'lines', 'trace')
      fig.show()
```

[[0.7720903939661031, 0.14376538475355127, 0.0, 2.0], [15.14391195463344,

```
-0.03417741189921775, 0.0, 1.0]]
{'car1': ['Normal', 'T0'], 'car2': ['Normal', 'T0']}
{'car1': ('Brake', 'T0'), 'car2': ['Normal', 'T0']}
```

## 5 5. Creating map

In this section, we will look at how to create a map for Verse by extending the map we used in the previous section from 1 lane to 2 lanes.

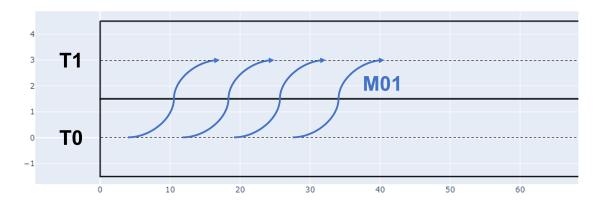
The map will contain a set of tracks, that the agent's continuous dynamics roughly follows. In addition, we also assume that an agent's decision logic does not depend on exactly which of the infinitely many tracks it is following, but instead, it depends only on which type of track it is following, or the track mode. In this example, as shown in the figure below, each of the lanes will have a track mode T0 and T1. In Verse, we can create the two types of tracks T0 and T1 using the Lane object, with each of them having one straight segment constructed by StraightLane as shown below.

```
[28]: from verse.map.lane_segment import StraightLane
from verse.map.lane import Lane

segment0 = StraightLane('seg0', [0,0], [500,0], 3)
lane0 = Lane('T0', [segment0])
segment1 = StraightLane('seg1', [0,3], [500,3], 3)
lane1 = Lane('T1', [segment1])
```

Verse currently implments StraightLane and CircularLane, which corresponding to straight line and circular curves. In addition, we allow each Lane to have multiple concatenated StraightLane or CircularLane.

In addition, we also define the transition between tracks. For example, every track for transitioning from point on T0 to a corresponding point on T1 has track mode M01. Therefore, in this example, our map will have a total of 4 track modes T0, T1, M01, and M10.



The map will have a mapping function g, which can provide the track that the agent is following given a track mode and the agent's current position. In this example, we can inherit the g function from the base class LaneMap

Finally, a Verse agent's decision logic can change its interal or tactical mode (E.g. Normal to SwitchLeft). When an agent changes its tactical mode, it may also update the track it's following and this is encoded in another function h, which takes the current track mode, the current and the next tactical mode, and generates the new track mode the agent should follow. In this example, the agents have tacical mode Normal, SwitchLeft and SwitchRight. Therefore, an example h function looks like following.

With all these pieces, we can now create the map for this scenario.

```
[30]: from verse.map import LaneMap

class Map2Lanes(LaneMap):
    def __init__(self):
        super().__init__()
        self.add_lanes([lane0, lane1])
        self.h = h
        self.h_exist = h_exist
```

We can then construct the scenario with two agents and simulate/verify the scenario with map we just created and the result is shown as below.

```
[31]: from enum import Enum, auto

class AgentMode(Enum):
    Normal = auto()
    SwitchLeft = auto()

class TrackMode(Enum):
    T0 = auto()
    T1 = auto()
    M01 = auto()
    M10 = auto()

from verse.scenario import Scenario
```

```
scenario = Scenario()
scenario.set_map(Map2Lanes())
from tutorial_agent import CarAgent
car1 = CarAgent('car1', file_name="./dl_sec5.py")
car1.set_initial([[0,-0.5,0,2],[0.5,0.5,0,2]], (AgentMode.Normal, TrackMode.TO))
car2 = CarAgent('car2', file_name="./dl_sec5.py")
car2.set_initial([[20,-0.5,0,1],[20.5,0.5,0,1]], (AgentMode.Normal, TrackMode.
 T0))
scenario.add_agent(car1)
scenario.add_agent(car2)
traces_simu = scenario.simulate(30, 0.01)
traces_veri = scenario.verify(30, 0.01)
import plotly.graph_objects as go
from verse.plotter.plotter2D import *
fig = go.Figure()
fig = simulation_tree(traces_simu, Map2Lanes(), fig, 1, 2, [1, 2], 'lines', __
 fig.show()
fig = go.Figure()
fig = reachtube_tree(traces_veri, Map2Lanes(), fig, 1, 2, [1, 2], 'lines', __
 fig.show()
[[0.3538739269603082, -0.3141663222842328, 0.0, 2.0], [20.226161145751156,
-0.015210822315415706, 0.0, 1.0]]
{'car1': ['Normal', 'T0'], 'car2': ['Normal', 'T0']}
{'car1': ('SwitchLeft', 'M01'), 'car2': ['Normal', 'T0']}
{'car1': ('Normal', 'T1'), 'car2': ['Normal', 'T0']}
```