Indexing

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Outline

- Types of indexes
- B+ trees

Indexes

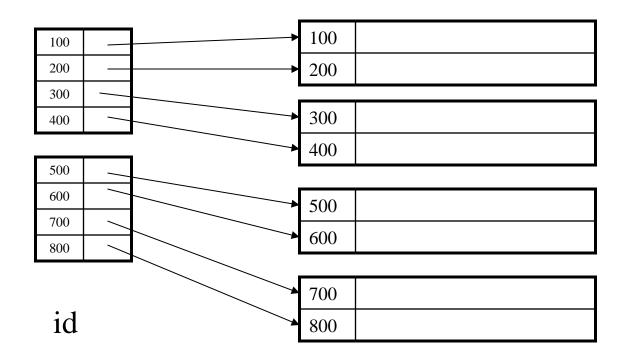
- An <u>index</u> is a data structure that speeds up selections on the <u>search key field(s)</u>
- *Fields* = *attributes*
- Search key = any subset of the fields of a relation
 - Search key is not the same as key (minimal set of fields that uniquely identify a record in a relation).
- Entries in an index: (k, r), where:
 - k =the key
 - r = the record OR record id OR a list of record ids

Index Classification

- Clustered/unclustered
 - Clustered = records sorted & stored in the order of search key
 - Unclustered = records are not sorted in key order
- Dense/sparse
 - Dense = each record has an entry in the index
 - Sparse = only some records have
- B+ tree / hash table / ...

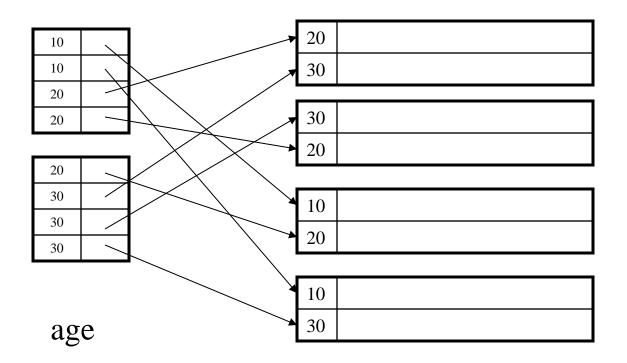
Clustered Index

- Records are sorted on the index attribute
 - Often for index on primary key
 - E.g., employee(<u>id</u>, name, age, salary)



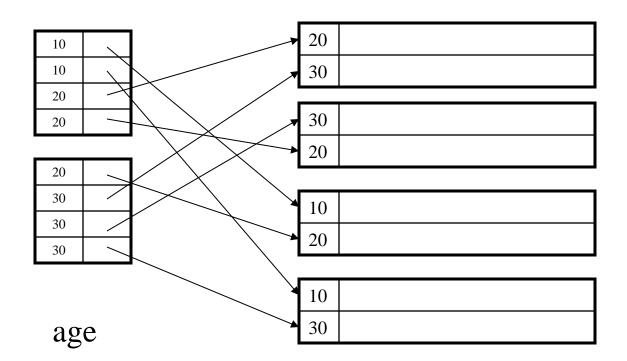
Unclustered Indexes

Often for indexes on attributes other than primary key



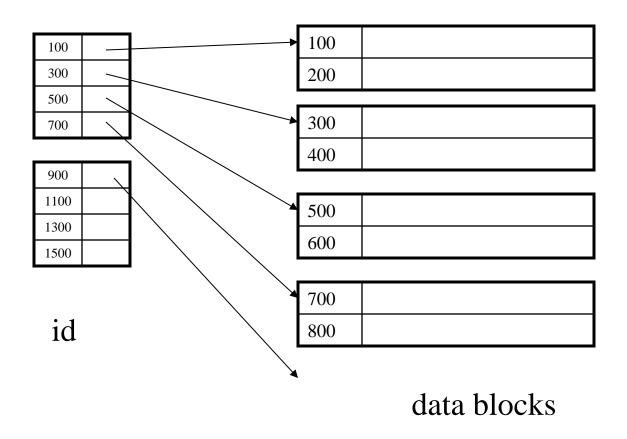
Dense Index

- <u>Dense</u> index: one key per data record
- See Sections 14.1.2 14.1.3 in book [GVW]



Sparse Index

• *Sparse* index: one key per data block



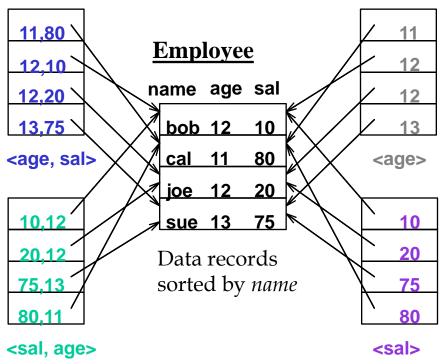
Query Types

- Equality query: <attribute> = <value>
 - E.g., age = 20, sal = 75
- Range query: <attribute> <inequality operator> <value>
 - Inequality operator: <, >, <=, >=
 - E.g., age > 20 or sal <= 75

Composite Search Keys

• *Composite Search Keys*: Search key = a list of fields.

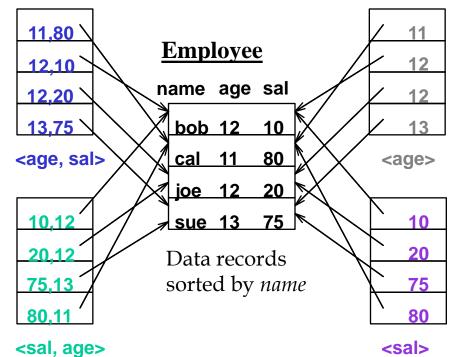
Keys in index sorted by <age,sal>: i.e., first by age; if ties, by sal



Keys sorted by *<sal>*

Questions

- Which index is useful for queries:
 - -Sal > 75
 - Age = 12 and sal > 10
 - -Age > 12



Outline

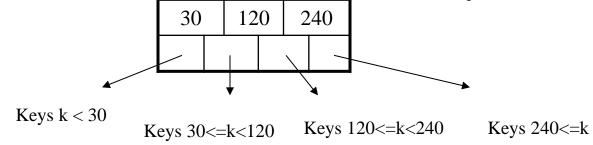
- Types of indexes
- B+ trees

B+ Trees

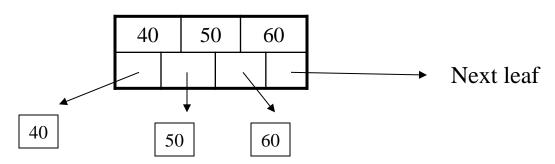
- Search trees
- Idea in B Trees:
 - make 1 node = 1 block
- Idea in B+ Trees:
 - Make leaves into a linked list
 - Efficiently support range queries

B+ Trees Basics

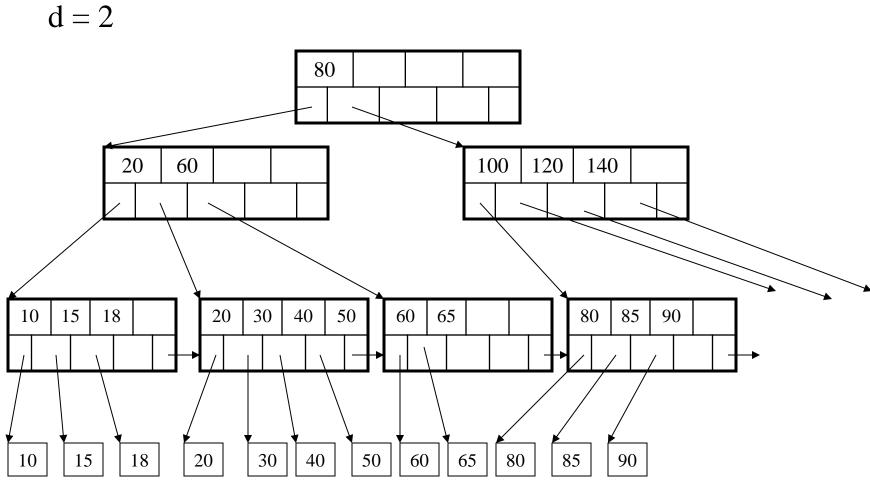
- Parameter d = the **degree** (also called order)
- Each node has $\geq = d$ and $\leq = 2d$ keys (except root)



• Each leaf has >=d and <= 2d keys:



B+ Tree Example



B+ Tree Design

- How large is d?
- Example:
 - Key size = 4 bytes
 - Pointer size = 8 bytes
 - Block size = 4096 byes
- 2d * 4 + (2d+1) * 8 <= 4096
- $d = 170 (\sim 170.33)$

B+ Trees in Practice

- Typical order d = 100.
- Typical fill-factor (minimum in practice): 66.7% (i.e., 2/3) (note minimum fill factor in design: 50%)
 - Minimum # of keys in a node = 133 (200 * 2/3)
- Capacities (# of records which the index supports):
 - Height 1 (tree with a single root): 133 records
 - Height 2: $133^2 = 17$, 689 records (134*133 to be exact)
 - Height 3: $133^3 = 2$, 352, 637 records ($134^2 *133$)
 - Height 4: $133^4 = 312,900,721$ records $(134^3 * 133)$

B+-tree in Practice

• Can often hold top levels in buffer pool:

```
Level 1 = 1 page = 4KB
Level 2 = 133 pages = 532KB
Level 3 = 17,689 pages = 70, 756KB ~ 70MB
```

Searching a B+ Tree

- Equality search:
 - Start at the root
 - Proceed down, to the leaf

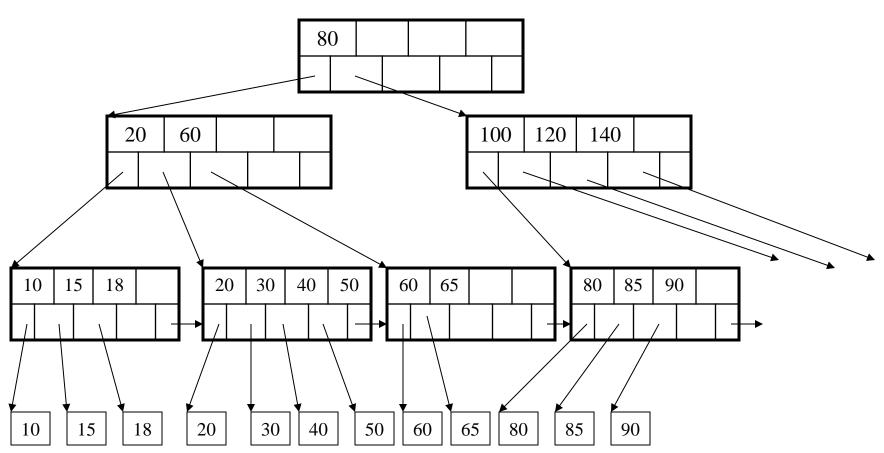
Select name From people Where age = 25

- Range query:
 - Finding the first leaf
 - Then sequential traversal of leaves

Select name
From people
Where 20 <= age
and age <= 30

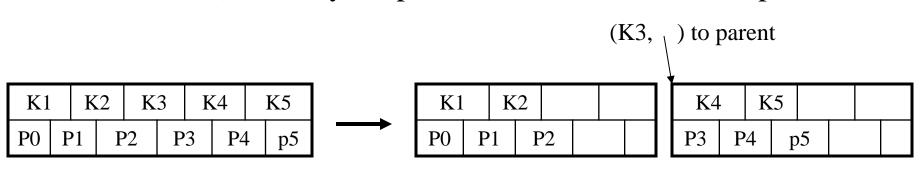
Example

20 <= age and age <= 55



Insert (K, P)

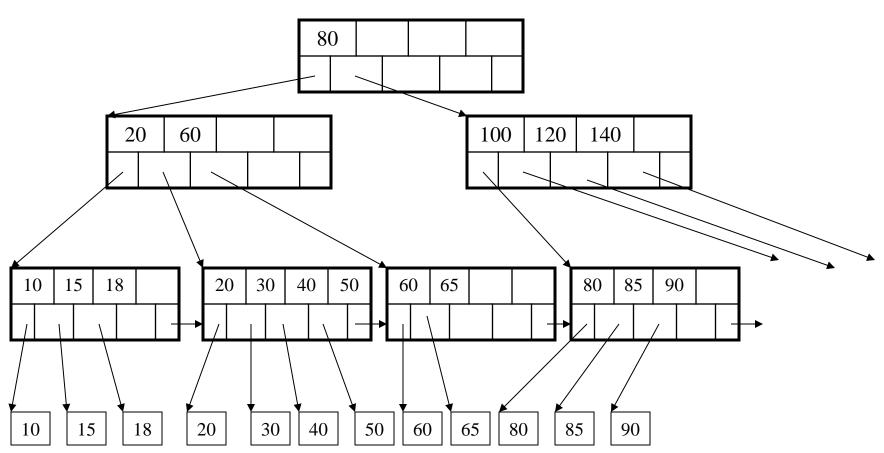
- Find leaf where K belongs, insert
- If no overflow (2d keys or less), stop
- If overflow (2d+1 keys), split node, insert middle into parent:

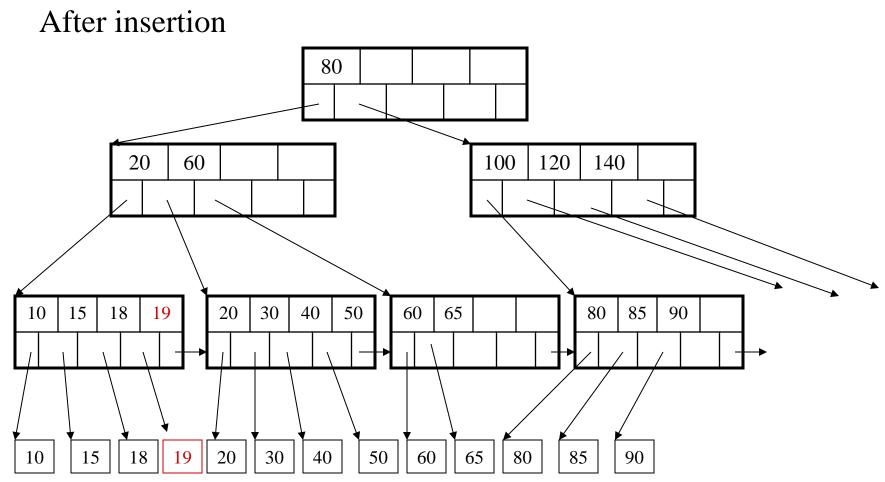


Notes

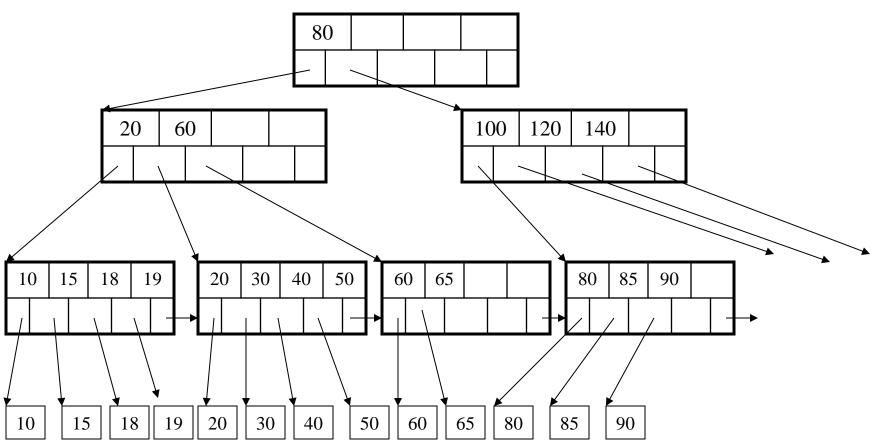
- Splitting of leaf may lead to splitting of its parent and ancestors
- When splitting a leaf, middle key (e.g., K3) is also kept in the new node on the right
- No need to retain middle key in the split node when splitting an internal node (but need to insert it into parent)
- When root is split, new root has only one key

Insert K=19

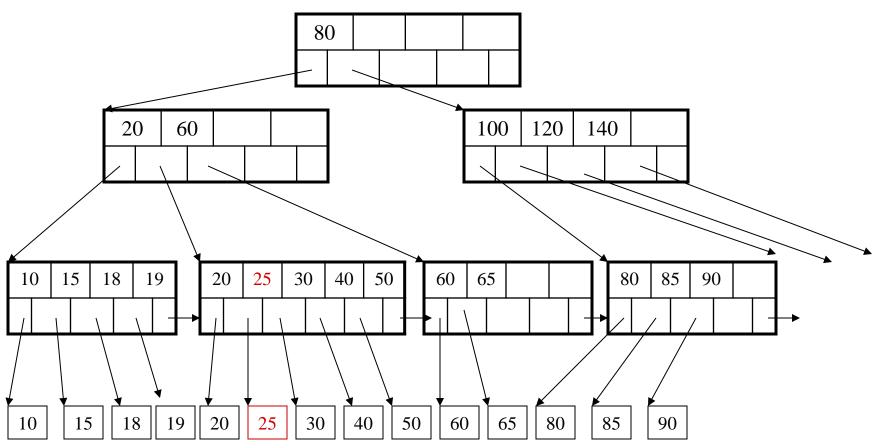




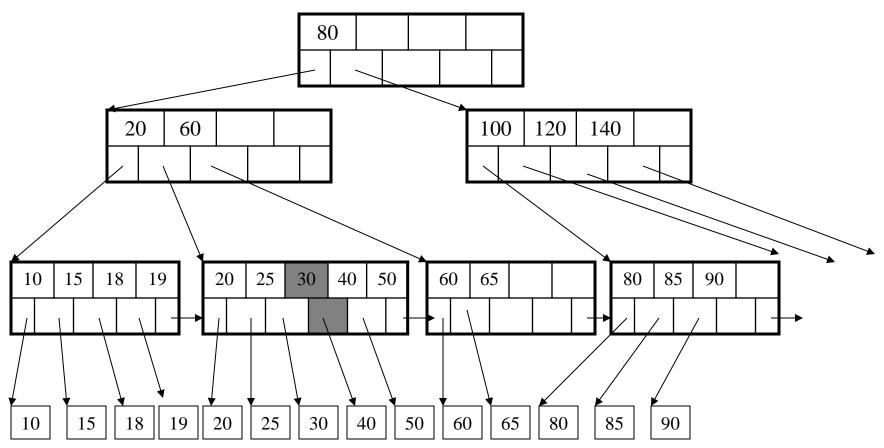
Now insert 25



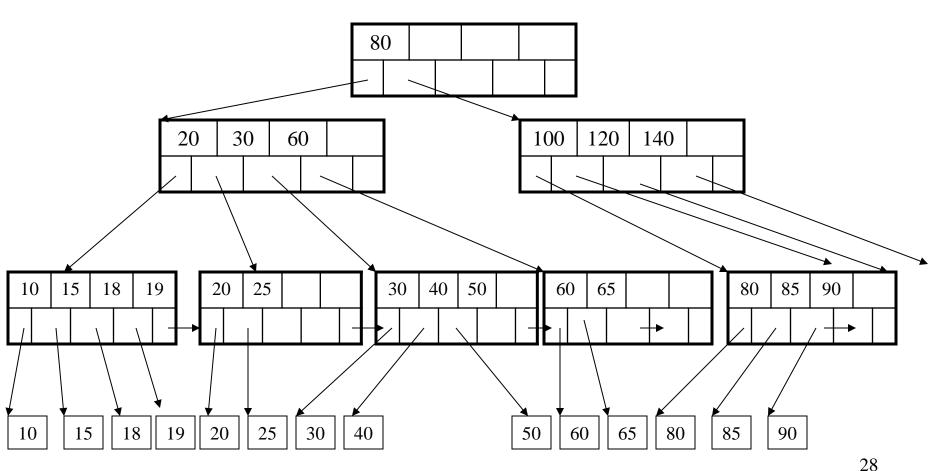
After insertion



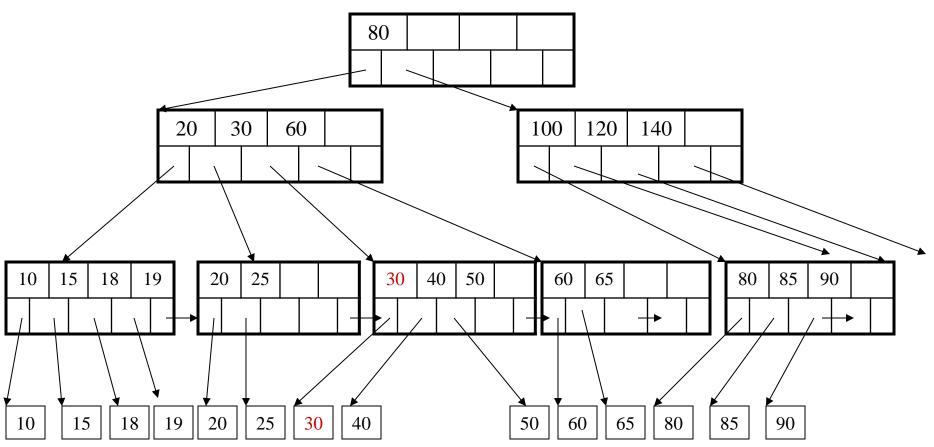
But now have to split!

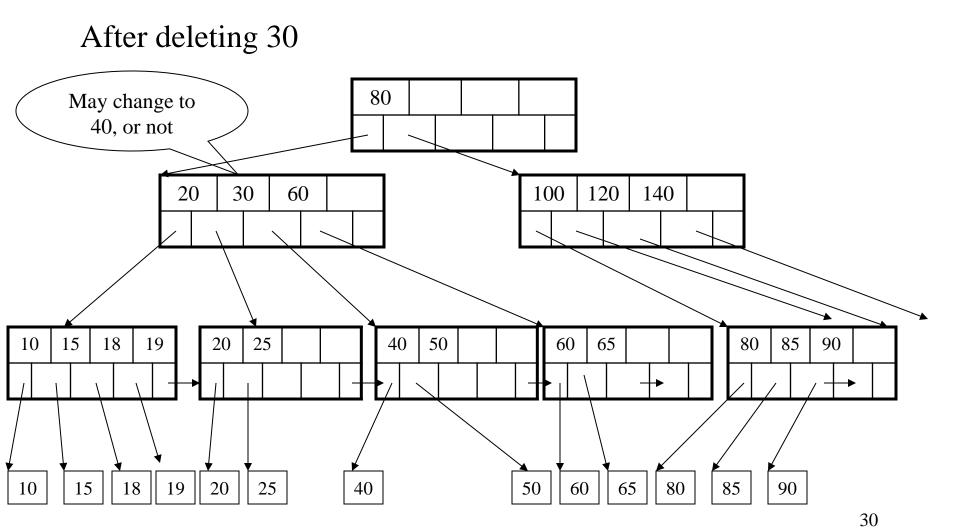


After the split

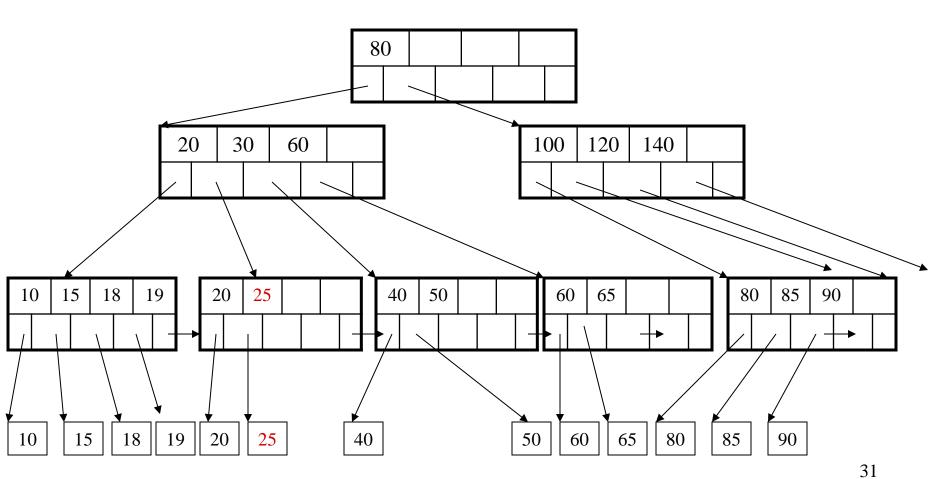


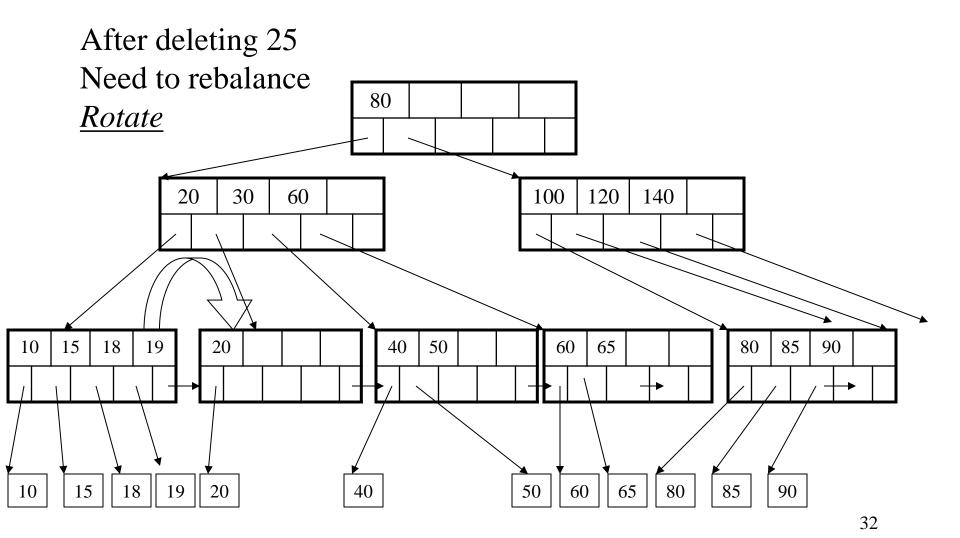
Delete 30



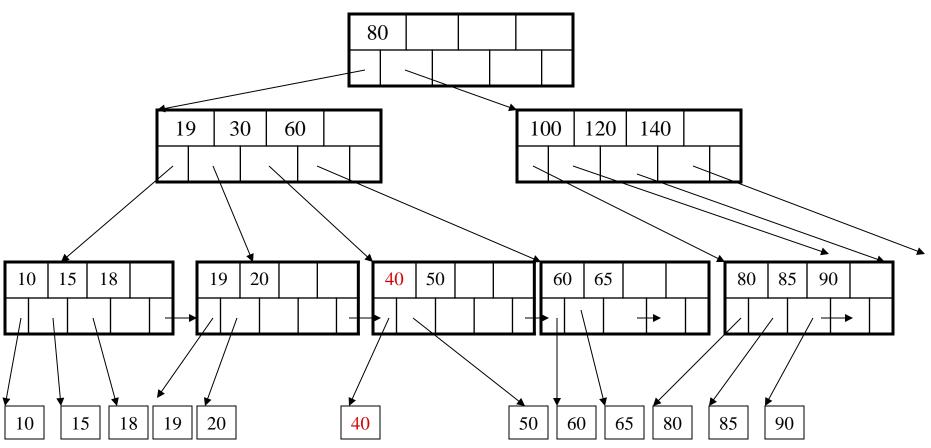


Now delete 25



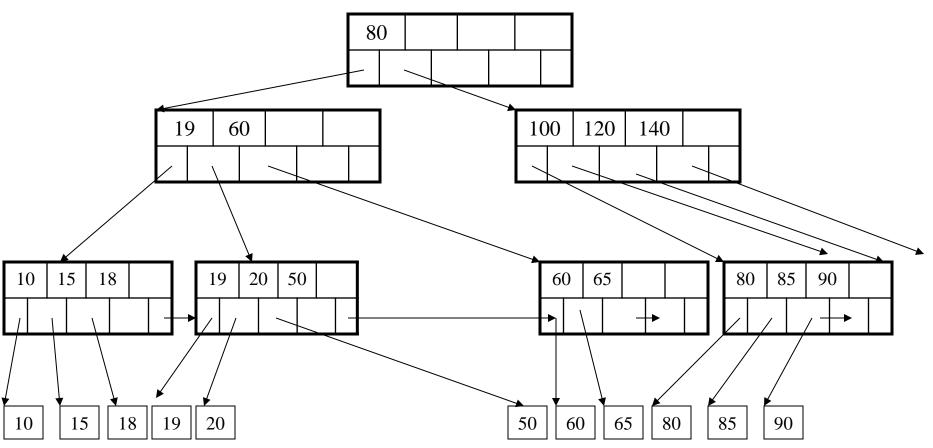


Now delete 40



After deleting 40 Rotation not possible Need to *merge* nodes

Final tree



Deletion Strategy

- If a node is below the min capacity after deletion...
- Try the following in the given order
 - 1. move a key from immediate left sibling;
 - 2. move a key from immediate right sibling;
 - 3. merge with immediate left sibling;
 - 4. merge with immediate right sibling

• Cases 3 and 4 may lead to further removal of key from parent, and more fixing

Another insertion example

