



# Generalized Few-Shot Node Classification

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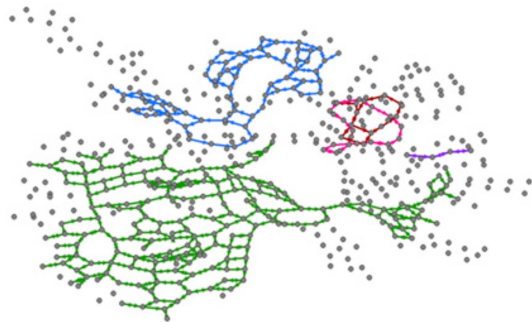
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# Roadmap

- **Motivation**
- **Proposed Model – STAGER**
- **Imbalanced Episodic Training**
- **Experiments**
- **Conclusion**

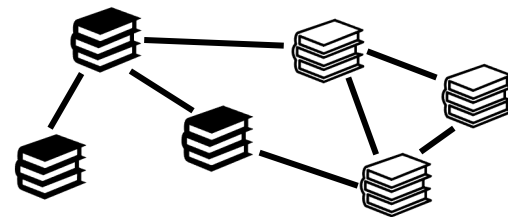
# Graph data is ubiquitous



**Traffic graph [1]**



**Social graph [2]**



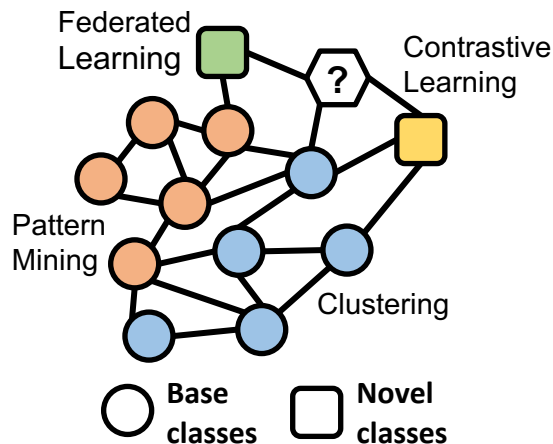
**Citation graph [3]**

[1] Li, Daqing, et al. "Percolation transition in dynamical traffic network with evolving critical bottlenecks." Proceedings of the National Academy of Sciences 112.3 (2015): 669-672.

[2] R. Zafarani and H. Liu, (2009). Social Computing Data Repository at ASU [<http://socialcomputing.asu.edu>]. Tempe, AZ: Arizona State University, School of Computing, Informatics and Decision Systems Engineering.

[3] Jie Tang, Jing Zhang, Limin Yao, Juanzi Li, Li Zhang, and Zhong Su. ArnetMiner: Extraction and Mining of Academic Social Networks. KDD. 2008

# (Generalized) few-shot node classification

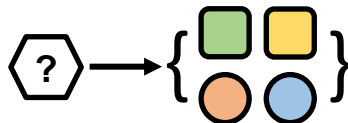


- **shot:** # of labeled samples per class
- **Base classes:** classes with many shots
- **Novel classes:** classes with few shots

- Existing few-shot node classification researches [1-3]



- This work: a more realistic setting



# Underestimated Novel Classes

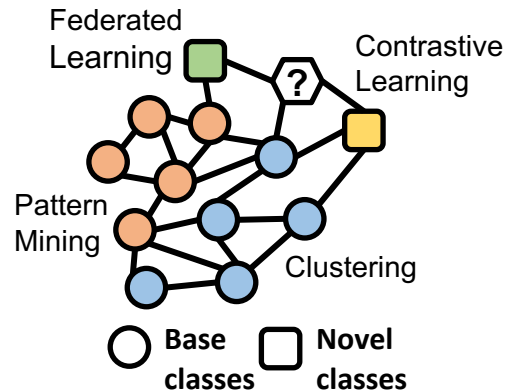


$$P(y_i|\mathcal{G}, v_i) = \sum_{C \in \{novel, base\}} \overbrace{P(y_i|C_i, \mathcal{G}, v_i)}^{\text{fine-grained classification given priori}} \underbrace{P(C_i|\mathcal{G}, v_i)}_{\text{A rough classification priori}}$$

- A given graph  $\mathcal{G} = \{\mathbf{A}, \mathbf{X}\}$ ,
  - A rough classification  $C_i$ , i.e., novel or base classes
  - If  $C_i = \textit{base}$ : standard node classification
  - If  $C_i = \textit{novel}$ : few-shot node classification
  - If  $C_i$  is unknown:
- $$\mathbb{E}[P(C_i = \textit{base}|\mathcal{G}, v_i)] \gg \mathbb{E}[P(C_i = \textit{novel}|\mathcal{G}, v_i)]$$

Dataset	Method	$b \rightarrow b$	$b \rightarrow n$	$n \rightarrow b$	$n \rightarrow n$
Amazon Clothing	APPNP	100.0	0.0	69.6	30.4
	MetaGNN	100.0	0.0	61.2	38.8
Cora-Full	APPNP	99.2	0.8	66.8	33.2
	MetaGNN	99.0	1.0	72.4	27.6

TABLE I: Test nodes (%) classified from base classes to base classes (i.e.,  $b \rightarrow b$ ), from base classes to novel classes (i.e.,  $b \rightarrow n$ ), from novel classes to base classes (i.e.,  $n \rightarrow b$ ), and from novel classes to novel classes (i.e.,  $n \rightarrow n$ ), respectively.





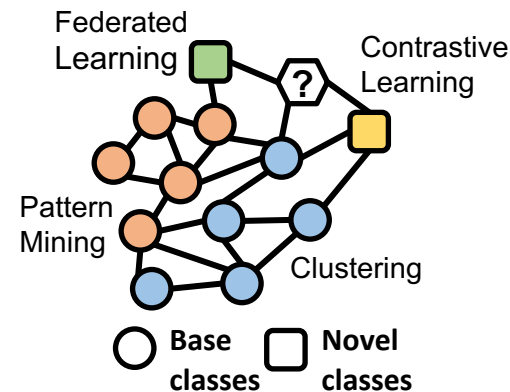
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# Epistemic Uncertainty

- Epistemic uncertainty: how well the model fits the data and **is reducible as the size of training data increases** [1-2]
- $P(C_i = base|G, v_i)$  or  $P(C_i = novel|G, v_i)$  ?
- **Number of shots  $\leftrightarrow$  epistemic uncertainty**
- Measure epistemic uncertainty by a **ranked** classification output from a preliminary classifier  $g_1$  :  

$$\tilde{\mathbf{Z}} = \text{rank}(\text{softmax}(g_1(\mathbf{A}, \mathbf{X}, \phi_1)))$$



*Implementation detail: dropout variational inference on  $\phi_1$  [2-3]*

*The selection of  $g_1$ : show in a case study*

# Proposed Model – STAGER (1)



**Classifier [1,3]:** sum of predictions

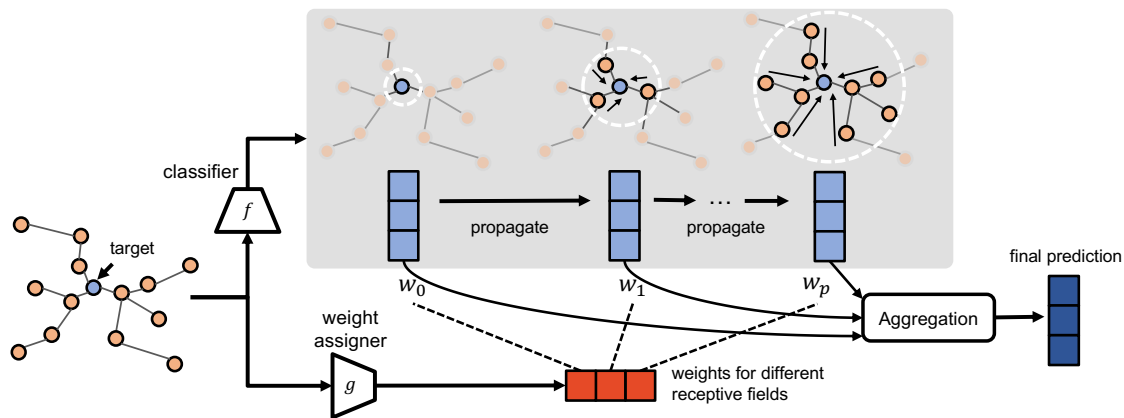
$$\mathbf{H}^{(0)} = \text{MLP}(\mathbf{X}, \theta)$$

$$\mathbf{H}^{(j+1)} = \tilde{\mathbf{A}}\mathbf{H}^{(j)}$$

$$\mathbf{Z} = \text{softmax}\left(\sum_{j=0}^p \underbrace{(\mathbf{W}[:, j] \mathbf{1}^T)}_{\text{Node-specific weight assignments}} \odot \mathbf{H}^{(j)}\right)$$

Node-specific weight assignments

- For the **base** classes, **local** classifier.
- For the **novel** classes, **long-range** propagation [1-2]





# Proposed Model – STAGER (2)



**Classifier:**

$$\mathbf{H}^{(0)} = \text{MLP}(\mathbf{X}, \theta)$$

$$\mathbf{H}^{(j+1)} = \tilde{\mathbf{A}}\mathbf{H}^{(j)}$$

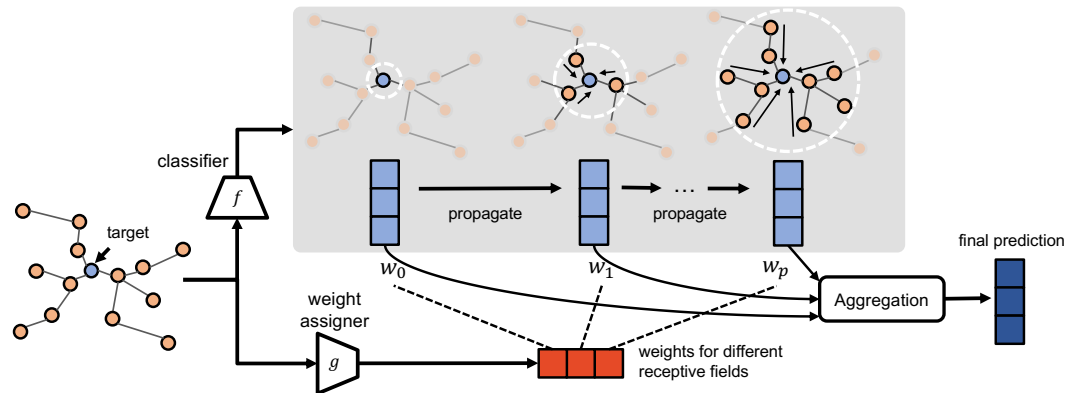
$$\mathbf{Z} = \text{softmax}\left(\sum_{j=0}^p (\mathbf{W}[:, j] \mathbf{1}^T) \odot \mathbf{H}^{(j)}\right)$$



**uncertainty (shot)-aware weight assigner:**

$$\mathbf{W} = \text{MLP}(\tilde{\mathbf{Z}}, \phi_2)$$

$$\tilde{\mathbf{Z}} = \text{rank}(\text{softmax}(g_1(\mathbf{A}, \mathbf{X}, \phi_1)))$$





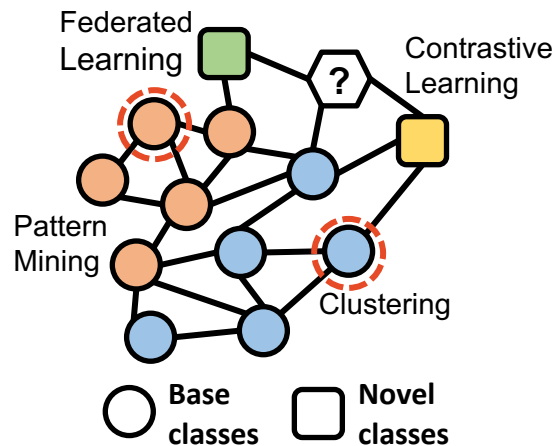
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# Meta-learning-based training paradigm



- Existing episodic training [1-5]: **mimic the few-shot scenarios using labeled base samples**
- a few-shot episode:  $\mathcal{S}_i = \{v_i, \dots, v_{N \times K}\}, \mathcal{Q}_i = \{v'_i, \dots, v'_{N \times I}\}$
- N: # of novel classes
- K: shots of the novel classes



$$\phi^* = \arg \min_{\phi} \mathbb{E}_{v_i \in \mathcal{Q}} \mathcal{L}_{cla}(z(\mathcal{G}, \theta^*, \phi, v_i), y_i)$$

$$\theta^* = \arg \min_{\theta} \mathbb{E}_{v_j \in \mathcal{S}} \mathcal{L}_{cla}(z(\mathcal{G}, \theta, \phi, v_j), y_j)$$

Meta-learner  $\phi$  learns from the learning of the learner

Learner  $\theta$  learns to converge

# Imbalanced episodic training



- Goal: Learning to **distinguish few-shot and many-shot samples**
- Key idea: **mimic the few-shot vs. many-shot scenarios**

$$\mathcal{S}_i = \{v_1, \dots, v_{N \times K}\}, \mathcal{Q}_i = \{v'_1, \dots, v'_{N \times I}\}$$

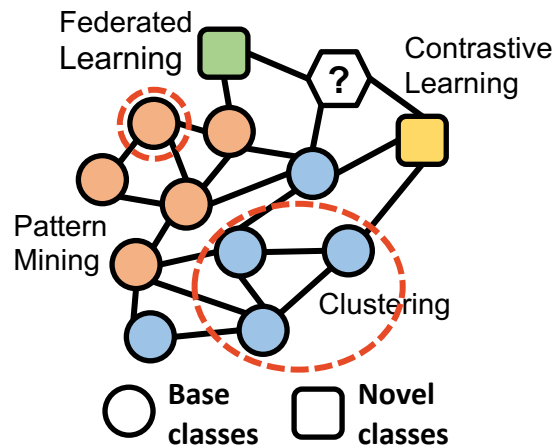


$$\mathcal{S}_i = \{\underbrace{v_1, \dots, v_{N \times K}}_{\text{pseudo-novel classes}}, \underbrace{v_{N \times K+1}, \dots, v_{N \times K+M \times L}}_{\text{pseudo-base classes}}\},$$

pseudo-novel classes      pseudo-base classes




$$\mathcal{Q}_i = \{\underbrace{v'_1, \dots, v'_{N \times I}}_{\text{pseudo-novel classes}}, \underbrace{v'_{N \times I+1}, \dots, v'_{(N+M) \times I}}_{\text{pseudo-base classes}}\}$$

- N: # of **pseudo-novel** classes
- K: shots of **pseudo-novel** classes
- M: # of **pseudo-base** classes
- L: shots of **pseudo-base** classes





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# Experimental settings



- Datasets
- Training nodes:
  - Novel: N-way K-shot
  - Base: many-way many-shot
- Test nodes: fixed for every class
- Baselines:
  - Classic neural node classifier: APPNP, GPRGNN
  - Few-shot node classifier: Meta-GNN, GPN, G-Meta
  - Imbalanced node classifier: GraphSMOTE
- Metric: accuracy in 10 runs

Dataset	Nodes	Edges	Features	Labels
Amazon Clothing	24919	91680	9034	77
Amazon Electronics	42318	43556	8669	167
Aminer	40672	288270	7202	137
Cora-Full	18800	62685	8710	56

# Main results on the effectiveness



Dataset	Setting	Class	standard		few-shot			imbalanced		STAGER-I
			APPNP	GPRGNN	MetaGNN	GPN	G-META	G-SMOTE	STAGER	
Amazon Clothing	5w1s	Base	67.4±1.6	64.7±0.5	64.0±0.5	46.1±3.3	48.7±2.7	67.4±1.6	<b>69.3±1.1</b>	67.3±0.4
		Novel	31.4±0.9	31.5±5.4	28.3±0.4	36.1±5.1	39.2±2.9	31.4±0.9	32.4±2.0	<b>41.3±1.0</b>
		All	48.5±1.0	47.3±3.0	45.4±0.4	40.9±2.9	43.7±2.2	48.5±1.0	<u>50.0±1.0</u>	<b>53.7±0.5</b>
	5w3s	Base	70.5±0.9	69.7±1.0	66.1±1.2	62.9±1.9	63.3±1.7	69.4±0.7	<b>72.3±1.5</b>	68.4±1.0
		Novel	48.6±2.5	50.1±3.8	40.4±0.8	46.1±6.7	47.6±6.3	45.6±2.3	53.9±2.1	<b>66.0±2.4</b>
		All	59.1±1.2	59.4±2.1	52.6±1.0	54.1±3.4	55.1±3.5	57.0±1.4	<u>62.7±1.1</u>	<b>67.2±1.1</b>
	10w1s	Base	73.3±0.3	70.7±1.2	67.6±0.5	42.7±2.4	48.2±2.1	73.3±0.3	<b>76.7±1.5</b>	66.7±0.5
		Novel	45.2±0.6	37.7±3.1	41.5±0.5	39.7±5.7	39.9±4.9	45.2±0.6	43.1±2.7	<b>59.6±0.6</b>
		All	58.6±0.3	53.5±1.6	54.0±0.4	40.9±3.5	43.9±2.0	58.6±0.3	<u>59.0±1.6</u>	<b>63.0±0.5</b>
	10w3s	Base	69.2±0.6	67.5±1.1	65.6±1.2	59.5±2.7	57.4±1.9	68.1±0.7	<b>70.9±0.7</b>	69.3±0.4
		Novel	61.4±0.4	58.0±1.5	53.6±0.2	49.6±7.1	54.1±2.8	53.6±3.8	61.8±1.2	<b>64.6±0.7</b>
		All	65.2±0.4	62.5±1.3	59.2±0.2	54.3±3.4	55.6±1.6	60.5±1.9	<u>66.2±0.8</u>	<b>66.8±0.5</b>
Amazon Elec.	5w1s	Base	60.1±1.8	58.4±0.9	59.7±0.3	19.1±2.1	22.5±3.1	60.1±1.8	<b>65.8±2.1</b>	63.9±1.0
		Novel	7.8±0.8	5.1±1.1	6.4±0.3	16.6±5.4	15.3±6.7	7.8±0.8	8.0±0.7	<b>19.7±1.6</b>
		All	27.2±0.4	24.8±0.4	26.2±0.2	17.5±3.8	18.0±5.0	27.2±0.4	<u>29.4±1.4</u>	<b>36.1±1.1</b>
	5w3s	Base	64.2±1.8	55.1±0.9	63.0±0.7	43.7±1.6	43.6±2.4	63.0±1.4	<b>69.1±1.6</b>	69.0±2.9
		Novel	21.6±1.5	13.3±2.0	23.1±0.2	32.7±4.8	28.1±5.6	12.0±4.0	29.8±2.7	<b>40.7±2.2</b>
		All	37.4±1.5	28.8±1.4	37.9±0.3	36.8±3.4	33.9±3.5	30.9±2.5	44.3±1.8	<b>51.2±2.3</b>
	10w1s	Base	64.4±1.2	59.7±1.3	53.1±1.6	18.5±1.4	20.8±2.2	64.4±1.2	<b>69.0±0.9</b>	61.3±0.8
		Novel	8.0±1.3	5.7±1.1	4.9±0.1	15.3±3.7	15.0±3.7	8.0±1.3	11.3±1.5	<b>15.4±0.3</b>
		All	34.4±1.0	31.0±1.1	27.7±0.2	16.8±2.3	17.7±2.0	34.4±1.0	<b>38.3±1.2</b>	36.9±0.4
	10w3s	Base	58.6±0.4	55.2±0.9	48.8±0.7	43.8±1.7	46.3±1.6	62.9±0.7	<b>72.3±1.1</b>	66.5±0.1
		Novel	22.4±1.1	14.8±1.0	16.5±0.2	27.5±2.9	26.2±3.2	13.8±0.3	20.3±2.4	<b>38.1±2.3</b>
		All	39.4±0.5	33.7±0.7	31.6±0.4	35.1±1.4	35.6±1.8	36.8±0.2	<u>44.7±1.5</u>	<b>51.4±1.1</b>

More results in the paper

- Compared with **standard node classifiers** (APPNP, GPRGNN), STAGER is competitive.
- Few-shot node classifiers** (MetaGNN, GPN, G-Meta) cannot work well in the generalized setting.
- Imbalanced node classifier** G-SMOTE cannot fully use the labeled base classes.
- Imbalanced episodic training** facilitates a **better tradeoff** between the novel and base classes.



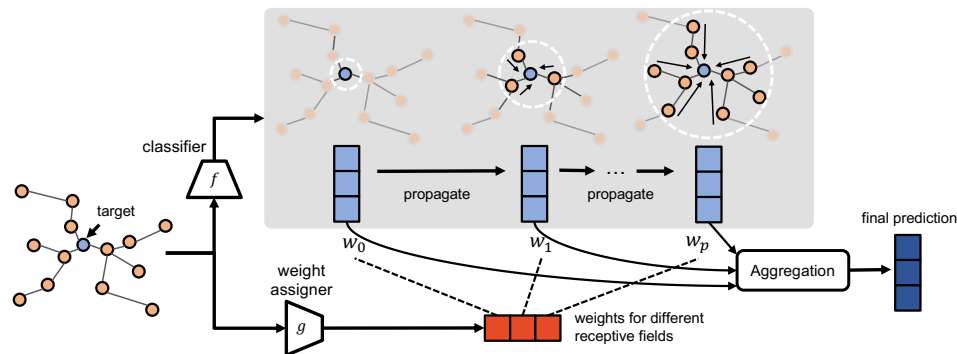
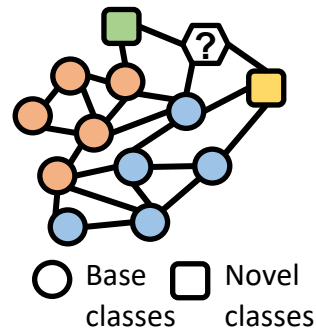
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# Conclusion

- **Problem:** generalized few-shot node classification
  - Classify nodes into the *joint set of base & novel classes*
- **Solution:** STAGER + imbalanced episodic training
  - *Uncertainty-aware* node classifier
  - *Few-shot vs. many-shot* scenarios
- **Experiments**
  - *The consistent advantage* over all classes



# Thank you!

## Q & A

