



## Course Project for Signal and System

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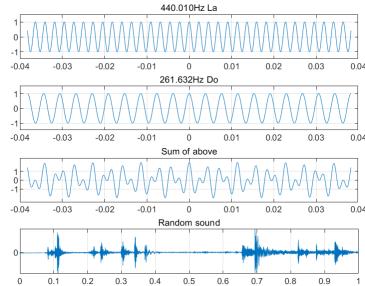
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### I. WHERE THE STORY BEGINS

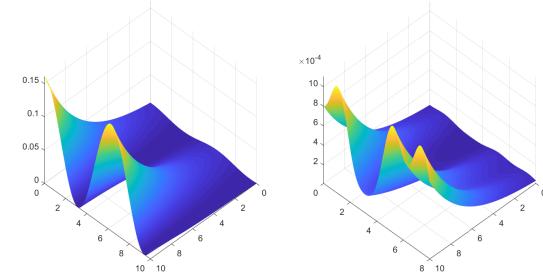
When we play the piano, we can press a key, such as Do. Its waveform is like the second curve in the Figure 1. Also we can get La which like the first curve in Figure 1. Then we press these two keys at the same time. Then we will get the third curve in the Figure 1.

But when we get a signal which like the third curve, we want to know which two buttons generate it. We want to know how to build this signal.

Generally we want to decompose a signal, which like the 4th curve in the Figure 1, into the combination of some simple signal.



**Figure 1**



**Figure 2**

In fact, many physical problems have the same properties, such as heat transfer problem. If we have a rod, which temperature function is  $T = \cos(x)$ . The change of its temperature with time t presents a simple exponential decay form, as I showed in the first sub-graph of Figure 2.

But for a more complex temperature function  $T = f(x)$  like the second sub-graph of Figure 2, if we can decompose it into the composition of a series sine and cosine function, we can simply migrate it to  $T = F(x, t)$ .

Let's start with simple one: a sinusoidal signal of 4 beats per second. We can construct a rotating vector whose length is the same as this sinusoidal signal value of the current time. The graph of this vector will like the second sub-graph in Figure 3. We can find a magic phenomenon. When the frequency of this rotating vector is equal to this sinusoidal signal's frequency, a large number of points in this image are biased to the same side.

If we imagine this graph is having some kind of mass to it, like metal wire. We can find, as we change the frequency, the center of mass wobbles around a bit at origin. But when the frequency is equal to our signal frequency, the mass center is unusually far to the right. If we draw the x position of the mass center changed by the frequency into a  $f - x$  graph. It will be like the third sub-figure

in Figure 3. There is a high peak at 4 Hz position.

**Figure 3**

**Figure 4**

And we can do the same operation in a combination of two signal:  $\cos(2\pi 3t) + \cos(2\pi 5t)$ . Then we can get similar result: two peaks at 3 and 5 Hz.

II. WHEN THE  
INFINITE SUM HAS  
TO BE APPLIED

III. OPEN THE GATE  
TO FREQUENCY  
DOMAIN

IV. FROM  
PERIODICITY TO  
APERIODICITY