

Баллы

4,00/4,00

Оценка

10,00 из 10,00 (100%)

Вопрос

1

Верно

Баллов: 1,00 из 1,00

Give the generating function for the sequence

$a_n = 2^n + 3^n$

in closed form.

Important note for this question and all the following ones: to check your answer, the system compares it to a list of recognized answers (it sounds ridiculous when the AI is a chess champion and writes essays, but that's how it is). So you have to respect a few guidelines to make sure it falls within the limited range of recognized answers:

- Please use the variable q
- Use $*$ as multiplication symbol: $3*q$ and not $3q$, $(1+q)*(1-2*q)$ and not $(1+q)(1-2*q)$
- Order monoms by increasing powers : $1+4*q^2$ and not $4*q^2+1$
- Do not put spacing: $3+2*q$ and not $3 + 2*q$

Example: $(1+4*q^2)/(1-q+5*q^3)$

Ответ:

$(2-5*q)/(1-5*q+6*q^2)$

Вопрос

2

Верно

Баллов: 1,00 из 1,00

Let f_n be the Fibonacci sequence ($f_0 = f_1 = 1$).

Find the generating function for the sequence

$f_0, 0, f_2, 0, f_4, 0, \dots$

Ответ:

$(1-q^2)/(1-3*q^2+q^4)$

Вопрос

3

Верно

Баллов: 1,00 из 1,00

The sequence is given by the recurrence relation

$a_n = a_{n-1} - a_{n-2} + a_{n-3} - a_{n-4},$

$a_0 = a_1 = 1, a_2 = a_3 = 3.$

Find the generating function for a_n in closed form.

Ответ:

$(1+3*q^2)/(1-q+q^2-q^3+q^4)$

Вопрос

4

Верно

Баллов: 1,00 из 1,00

The sequence a_n is given by the recurrence relation $a_n = 2a_{n-1} + 3$, with $a_0 = 1$.

Find the generating function for a_n in closed form.

Ответ:

$(1+2*q)/(1-3*q+2*q^2)$