```
3.0
                        -2.000000x_2 + 3.000000x_3
                                                              -2.000000x_5
                                                                                       -1.000000x_7
x_8
     1.0
           +2.000000x_1 +1.000000x_2 +2.000000x_3 +1.000000x_4 -3.000000x_5 -2.000000x_6
x_9
     9.0
                        +1.000000x_2 -1.000000x_3 +2.000000x_4 +2.000000x_5 +3.000000x_6 +3.000000x_7
x_{10}
x_{11}
     9.0
           +2.000000x_1 + 2.000000x_2 - 3.000000x_3 - 1.000000x_4 - 3.000000x_5 - 1.000000x_6 - 3.000000x_7
           -2.000000x_1 + 3.000000x_2 + 3.000000x_3 + 3.000000x_4 + 1.000000x_5
                                                                                       -3.000000x_7
     7.0
x_{12}
           x_{13}
     8.0
                                    -1.000000x_3
     13.0
           -3.000000x_1
                                                              +1.000000x_5
                                                                                       -1.000000x_7
x_{14}
x_{15}
     6.0
           +2.000000x_1 -2.000000x_2 +2.000000x_3
                                                                          +2.000000x_6 +3.000000x_7
     6.0
           -3.000000x_1 + 3.000000x_2
                                                                          +1.000000x_6 +3.000000x_7
x_{16}
x_{17}
     15.0
                        -1.000000x_2 + 3.000000x_3 + 2.000000x_4 - 2.000000x_5 - 1.000000x_6 + 2.000000x_7
           +2.000000x_1 - 2.000000x_2 - 2.000000x_3 + 2.000000x_4 - 1.000000x_5 + 2.000000x_6
     0.0
 z
```

No initialization required –; Proceed to Optimize.

```
x_8
     3.0
                        -2.000000x_2 + 3.000000x_3
                                                              -2.000000x_5
                                                                                       -1.000000x_7
     1.0
           +2.000000x_1 +1.000000x_2 +2.000000x_3 +1.000000x_4 -3.000000x_5 -2.000000x_6
x_9
     9.0
                        +1.000000x_2 -1.000000x_3 +2.000000x_4 +2.000000x_5 +3.000000x_6 +3.000000x_7
x_{10}
     9.0
           x_{11}
x_{12}
     7.0
           -2.000000x_1 + 3.000000x_2 + 3.000000x_3 + 3.000000x_4 + 1.000000x_5
           -3.000000x_1 + 2.000000x_2 + 2.000000x_3 + 1.000000x_4 - 1.000000x_5 + 2.000000x_6 + 3.000000x_7
     8.0
x_{13}
                                                              +1.000000x_5
x_{14}
     13.0
           -3.000000x_1
                                    -1.000000x_3
                                                                                       -1.000000x_7
     6.0
           +2.000000x_1 -2.000000x_2 +2.000000x_3
                                                                          +2.000000x_6 +3.000000x_7
x_{15}
     6.0
x_{16}
           -3.000000x_1 + 3.000000x_2
                                                                          +1.000000x_6 +3.000000x_7
                        -1.000000x_2 + 3.000000x_3 + 2.000000x_4 - 2.000000x_5 - 1.000000x_6 + 2.000000x_7
     15.0
x_{17}
           +2.000000x_1 - 2.000000x_2 - 2.000000x_3 + 2.000000x_4 - 1.000000x_5 + 2.000000x_6
     0.0
z
```

 $x_1$  enters and  $x_{16}$  leaves

```
3.0
                   -2.000000x_2 +3.000000x_3
                                                 -2.000000x_5
                                                                    -1.000000x_7
x_8
    5.0
         x_9
    9.0
                   +1.000000x_2 -1.000000x_3 +2.000000x_4 +2.000000x_5 +3.000000x_6 +3.000000x_7
x_{10}
    13.0
        x_{11}
    3.0
        x_{12}
    2.0
        +1.000000x_{16} -1.000000x_2 +2.000000x_3 +1.000000x_4 -1.000000x_5 +1.000000x_6
x_{13}
        +1.000000x_{16} -3.000000x_2 -1.000000x_3
    7.0
                                                 +1.000000x_5 -1.000000x_6 -4.000000x_7
x_{14}
    10.0
        -0.666667x_{16}
                                                          +2.666667x_6 +5.000000x_7
                             +2.000000x_3
x_{15}
    2.0
        -0.333333x_{16} + 1.000000x_2
                                                          +0.333333x_6 +1.000000x_7
x_1
    15.0
                   -1.000000x_2 + 3.000000x_3 + 2.000000x_4 - 2.000000x_5 - 1.000000x_6 + 2.000000x_7
x_{17}
         -0.666667x_{16}
                             -2.000000x_3 + 2.000000x_4 - 1.000000x_5 + 2.666667x_6 + 2.000000x_7
    4.0
```

 $x_4$  enters and  $x_{11}$  leaves

```
3.0
                    -2.000000x_2 +3.000000x_3
                                                   -2.000000x_5
                                                                        -1.000000x_7
x_8
         18.0
x_9
         -1.333333x_{16} + 9.000000x_2 - 7.000000x_3 - 2.000000x_{11} - 4.000000x_5 + 2.333333x_6 + 1.000000x_7
    35.0
x_{10}
x_4
    13.0
         -0.666667x_{16} + 4.000000x_2 - 3.000000x_3 - 1.000000x_{11} - 3.000000x_5 - 0.333333x_6 - 1.000000x_7
         42.0
x_{12}
         15.0
x_{13}
                                                   +1.000000x_5 -1.000000x_6 -4.000000x_7
         +1.000000x_{16} -3.000000x_2 -1.000000x_3
    7.0
x_{14}
x_{15}
    10.0
         -0.666667x_{16}
                               +2.000000x_3
                                                              +2.666667x_6 +5.000000x_7
    2.0
         -0.3333333x_{16} +1.000000x_2
                                                              +0.3333333x_6 +1.000000x_7
x_1
         -1.333333x_{16} +7.000000x_2 -3.000000x_3 -2.000000x_{11} -8.000000x_5 -1.666667x_6
    41.0
x_{17}
    30.0
         -2.000000x_{16} + 8.000000x_2 - 8.000000x_3 - 2.000000x_{11} - 7.000000x_5 + 2.000000x_6
```

 $x_2$  enters and  $x_8$  leaves

```
-1.000000x_5
   1.5
               -0.500000x_8 +1.500000x_3
                                                      -0.500000x_7
x_2
   28.5
      -1.333333x_{16} - 3.500000x_8 + 9.500000x_3 - 1.000000x_{11} - 13.000000x_5 - 1.666667x_6 - 2.500000x_7
x_9
x_{10}
   48.5
      19.0
      x_4
      61.5
x_{12}
   19.5
      +0.333333x_{16} - 1.500000x_8 + 3.500000x_3 - 1.000000x_{11} - 7.000000x_5 + 0.666667x_6 - 2.500000x_7
x_{13}
   2.5
      +1.000000x_{16} +1.500000x_8 -5.500000x_3
                                      +4.000000x_5 -1.000000x_6 -2.500000x_7
x_{14}
                                              +2.666667x_6 +5.000000x_7
x_{15}
   10.0
      -0.666667x_{16}
                      +2.000000x_3
   3.5
      -0.333333x_{16} -0.500000x_8 +1.500000x_3
                                       -1.000000x_5 +0.333333x_6 +0.500000x_7
x_1
      51.5
x_{17}
```

 $x_3$  enters and  $x_{14}$  leaves

```
+0.090909x_5 -0.272727x_6 -1.181818x_7
                2.18181818182
                                                          +0.272727x_{16} -0.090909x_8 -0.272727x_{14}
 x_2
                                                          +0.393939x_{16} - 0.909091x_8 - 1.727273x_{14} - 1.000000x_{11} - 6.090909x_5 - 3.393939x_6 - 6.818182x_7
 x_9
                32.8181818182
               51.4545454545
                                                           -0.151515x_{16} - 2.727273x_8 - 1.181818x_{14} - 2.000000x_{11} - 8.272727x_5 + 1.151515x_6 - 6.454545x_{7} + 1.151515x_{16} - 6.454545x_{16} + 1.151515x_{16} - 6.454545x_{16} + 1.151515x_{16} + 1.15151x_{16} + 1.151515x_{16} + 1.151515x_{16}
x_{10}
                                                           20.3636363636
x_4
               67.6363636364
                                                          x_{12}
                                                           +0.969697x_{16} -0.545455x_8 -0.636364x_{14} -1.000000x_{11} -4.454545x_5 +0.030303x_6 -4.090909x_7
x_{13}
               21.0909090909
              0.454545454545
                                                          +0.181818x_{16} +0.272727x_8 -0.181818x_{14}
                                                                                                                                                                                                        +0.727273x_5 -0.181818x_6 -0.454545x_7
 x_3
x_{15}
                10.9090909091
                                                            -0.303030x_{16} + 0.545455x_8 - 0.363636x_{14}
                                                                                                                                                                                                        +1.454545x_5 +2.303030x_6 +4.090909x_7
               4.18181818182
                                                           -0.060606x_{16} -0.090909x_8 -0.272727x_{14}
                                                                                                                                                                                                        +0.090909x_5 +0.060606x_6 -0.181818x_7
 x_1
x_{17}
               54.9090909091
                                                           +0.030303x_{16} - 1.454545x_8 - 1.363636x_{14} - 2.000000x_{11} - 9.545455x_5 - 3.030303x_6 - 6.909091x_7
                                                           -1.272727x_{16} - 2.909091x_8 - 0.727273x_{14} - 2.000000x_{11} - 12.090909x_5 + 1.272727x_6 - 5.818182x_7
               43.8181818182
```

 $x_6$  enters and  $x_3$  leaves

```
1.5
                                                                                                                                                 -0.500000x_8
                                                                                                                                                                                                                                                                                                                         -1.000000x_5 +1.500000x_3 -0.500000x_7
 x_2
 x_9
                      24.3333333333
                                                                                        54.3333333333
                                                                                        x_{10}
                      18.1666666667
                                                                                         x_4
                      57.33333333333
                                                                                         -3.000000x_{16} - 9.000000x_8 + 1.666667x_{14} - 3.000000x_{11} - 27.666667x_5 + 22.666667x_3 - 10.333333x_7 - 10.33333x_7 - 10.3333x_7 - 10.333x_7 - 10.333x_7 - 10.333x_7 - 10.333x_7 - 10.333x_7 - 10.33x_7 - 10
 x_{12}
                      21.1666666667
                                                                                        x_{13}
                                                                                         +1.000000x_{16} +1.500000x_8 -1.000000x_{14}
                                                                                                                                                                                                                                                                                                                         +4.000000x_5 -5.500000x_3 -2.500000x_7
                                            2.5
 x_6
x_{15}
                      16.666666667
                                                                                         +2.000000x_{16} +4.000000x_8 -2.666667x_{14}
                                                                                                                                                                                                                                                                                                                       +10.666667x_5 - 12.666667x_3 - 1.666667x_7
                                                                                                                                                 -0.000000x_8 - 0.333333x_{14}
                      4.333333333333
                                                                                                                                                                                                                                                                                                                        +0.333333x_5 -0.333333x_3 -0.333333x_7
 x_1
                      47.3333333333
                                                                                         -3.000000x_{16} - 6.000000x_8 + 1.666667x_{14} - 2.000000x_{11} - 21.666667x_5 + 16.666667x_3 \\ + 0.666667x_7 + 10.666667x_7 + 10.666667x_7
x_{17}
                                                                                         47.0
```

 $x_{-1}$  enters and Final Dictionary Solution: 47.0 Num Pivots: 5