```
-3.000000x_1 + 1.000000x_2 + 3.000000x_3 - 1.000000x_4
                                                                  -1.000000x_6 + 2.000000x_7 - 1.0000000x_8
x_9
                                            +3.000000x_4 +1.000000x_5 -1.000000x_6 +1.000000x_7
     9.0
          +1.000000x_1 +1.000000x_2
x_{10}
     3.0
          -2.000000x_1 + 3.000000x_2 - 3.000000x_3 + 2.000000x_4
                                                                   -3.000000x_6
x_{11}
     1.0
          -3.000000x_1
                                +2.000000x_3 +3.000000x_4 +3.0000000x_5 -3.000000x_6 +1.000000x_7 +3.000000x_8
x_{12}
          +2.000000x_1 -2.000000x_2 +1.000000x_3 +2.000000x_4
                                                                              -2.000000x_7
     7.0
x_{13}
    12.0
          +3.000000x_1
                                 -2.000000x_3 -3.000000x_4 +3.000000x_5 +1.000000x_6 +2.000000x_7 +2.000000x_8
x_{14}
          10.0
x_{15}
x_{16}
          -1.000000x_1 + 1.000000x_2
                                                       +3.000000x_5 -2.000000x_6 -3.000000x_7 -3.000000x_8
          -1.000000x_1 - 2.000000x_2 + 1.000000x_3 - 3.000000x_4 - 3.000000x_5 - 2.000000x_6
    11.0
                                                                                         -1.000000x_8
x_{17}
    15.0
                                 -3.000000x_3 + 2.000000x_4 + 1.000000x_5 + 1.000000x_6
x_{18}
                                 13.0
          +1.000000x_1
x_{19}
     7.0
                      -1.000000x_2 +3.000000x_3 -3.000000x_4 -2.000000x_5 +2.000000x_6
x_{20}
    15.0
          -3.000000x_1 + 1.000000x_2 - 2.000000x_3 + 2.000000x_4
                                                                  +2.000000x_6 +2.000000x_7 +1.000000x_8
x_{21}
                     9.0
x_{22}
    11.0
          +3.000000x_1 + 3.000000x_2 - 2.000000x_3 - 1.000000x_4 + 1.000000x_5 + 1.000000x_6
                                                                                         -2.000000x_8
x_{23}
                     -2.000000x_2 -2.000000x_3 -2.000000x_4 +1.000000x_5
     0.0
                                                                              -1.000000x_7 + 2.000000x_8
```

No initialization required –; Proceed to Optimize.

```
-3.000000x_1 + 1.000000x_2 + 3.000000x_3 - 1.000000x_4
    13.0
                                                                   -1.000000x_6 + 2.000000x_7 - 1.000000x_8
x_9
x_{10}
     9.0
          +1.000000x_1 +1.000000x_2
                                            +3.000000x_4 +1.000000x_5 -1.000000x_6 +1.000000x_7
     3.0
          -2.000000x_1 + 3.000000x_2 - 3.000000x_3 + 2.000000x_4
                                                                   -3.000000x_6
x_{11}
                                 x_{12}
     1.0
          -3.000000x_1
                                                                               -2.000000x_7
     7.0
          +2.000000x_1 -2.000000x_2 +1.000000x_3 +2.000000x_4
x_{13}
    12.0
          +3.000000x_1
                                 -2.000000x_3 -3.000000x_4 +3.000000x_5 +1.000000x_6 +2.000000x_7 +2.000000x_8
x_{14}
    10.0
          x_{15}
          -1.000000x_1 + 1.000000x_2
                                                        +3.000000x_5 -2.000000x_6 -3.000000x_7 -3.000000x_8
x_{16}
    11.0
          -1.000000x_1 - 2.000000x_2 + 1.000000x_3 - 3.000000x_4 - 3.000000x_5 - 2.000000x_6
                                                                                          -1.000000x_8
x_{17}
    15.0
                                 -3.000000x_3 + 2.000000x_4 + 1.000000x_5 + 1.000000x_6
x_{18}
    13.0
          +1.000000x_1
                                 -1.000000x_3 + 2.000000x_4 - 1.000000x_5 + 2.000000x_6 + 3.000000x_7 + 3.000000x_8
x_{19}
     7.0
                      -1.000000x_2 + 3.000000x_3 - 3.000000x_4 - 2.000000x_5 + 2.000000x_6
                                                                                          -3.000000x_8
x_{20}
    15.0
          -3.000000x_1 + 1.000000x_2 - 2.000000x_3 + 2.000000x_4
                                                                   +2.000000x_6 +2.000000x_7 +1.000000x_8
x_{21}
                     9.0
x_{22}
     11.0
          +3.000000x_1 +3.000000x_2 -2.000000x_3 -1.000000x_4 +1.000000x_5 +1.000000x_6
                                                                                          -2.000000x_8
x_{23}
     0.0
                      -2.000000x_2 -2.000000x_3 -2.0000000x_4 +1.0000000x_5
                                                                              -1.0000000x_7 + 2.0000000x_8
```

 x_5 enters and x_{20} leaves

```
-1.000000x_6 +2.000000x_7 -1.000000x_8 \\
        -3.000000x_1 + 1.000000x_2 + 3.000000x_3 - 1.000000x_4
x_9
   12.5
        +1.000000x_1 +0.500000x_2 +1.500000x_3 +1.500000x_4 -0.500000x_{20}
                                                             +1.000000x_7 - 1.500000x_8
x_{10}
    3.0
                                                     -3.000000x_6
        -2.000000x_1 + 3.000000x_2 - 3.000000x_3 + 2.000000x_4
x_{11}
   11.5
        -3.000000x_1 - 1.500000x_2 + 6.500000x_3 - 1.500000x_4 - 1.500000x_{20}
                                                              +1.000000x_7 - 1.500000x_8
x_{12}
    7.0
        +2.000000x_1 -2.000000x_2 +1.000000x_3 +2.000000x_4
                                                              -2.000000x_7
x_{13}
   22.5
        x_{14}
        13.5
x_{15}
x_{16}
   15.5
        -1.000000x_1 - 0.500000x_2 - 3.500000x_3 + 1.500000x_4 + 1.500000x_{20} - 5.000000x_6
    0.5
                                                                      +3.500000x_8
x_{17}
x_{18}
   18.5
                 -0.500000x_2 -1.500000x_3 +0.500000x_4 -0.500000x_{20} +2.000000x_6
                                                                      -1.500000x_8
    9.5
x_{19}
        3.5
x_5
                 -0.500000x_2 + 1.500000x_3 - 1.500000x_4 - 0.500000x_{20} + 1.000000x_6
                                                                       -1.500000x_8
   15.0
        -3.000000x_1 + 1.000000x_2 - 2.000000x_3 + 2.000000x_4
x_{21}
                                                     +2.000000x_6 +2.000000x_7 +1.000000x_8
x_{22}
    5.5
                14.5
        +3.000000x_1 + 2.500000x_2 - 0.500000x_3 - 2.500000x_4 - 0.500000x_{20} + 2.000000x_6
                                                                      -3.500000x_8
x_{23}
                 3.5
```

 x_6 enters and x_{17} leaves

```
x_9
      12.9
  12.5
      +1.000000x_1 +0.500000x_2 +1.500000x_3 +1.500000x_4 -0.500000x_{20}
                                              +1.000000x_7 - 1.500000x_8
x_{10}
x_{11}
   2.7
      -1.400000x_1 + 3.300000x_2 - 0.900000x_3 + 1.100000x_4 - 0.900000x_{20} + 0.600000x_{17}
                                                     -2.100000x_8
  11.5
      -3.000000x_1 - 1.500000x_2 + 6.500000x_3 - 1.500000x_4 - 1.500000x_{20}
                                              +1.000000x_7 - 1.500000x_8
x_{12}
   7.0
      +2.000000x_1 -2.000000x_2 +1.000000x_3 +2.000000x_4
                                              -2.000000x_7
x_{13}
  22.9
      x_{14}
  13.3
      x_{15}
x_{16}
      15.6
x_6
   0.1
      -0.200000x_1 - 0.100000x_2 - 0.700000x_3 + 0.300000x_4 + 0.300000x_{20} - 0.200000x_{17}
                                                     +0.700000x_8
x_{18}
  18.7
      -0.400000x_1 - 0.700000x_2 - 2.900000x_3 + 1.100000x_4 + 0.100000x_{20} - 0.400000x_{17}
                                                     -0.100000x_8
   9.6
      x_{19}
   3.6
      -0.800000x_8
x_5
  15.2
      x_{21}
x_{22}
   5.7
      +2.600000x_1 + 2.300000x_2 - 1.900000x_3 - 1.900000x_4 + 0.100000x_{20} - 0.400000x_{17}
x_{23}
  14.7
   3.6
```

 x_8 enters and x_{11} leaves

```
-1.666667x_1 -1.571429x_2 +4.428571x_3 -2.190476x_4 +0.428571x_{20} -0.285714x_{17} +2.000000x_7 +0.8000000
                10.7142857143
x_9
                10.5714285714
                                                                +2.000000x_1 -1.857143x_2 +2.142857x_3 +0.714286x_4 +0.142857x_{20} -0.428571x_{17} +1.000000x_7 +0.714286x_4 +0.142857x_{20} +0.142857x
x_{10}
                                                                -0.666667x_1 + 1.571429x_2 - 0.428571x_3 + 0.523810x_4 - 0.428571x_{20} + 0.285714x_{17}
                1.28571428571
x_8
x_{12}
               9.57142857143
                                                                -2.000000x_1 -3.857143x_2 +7.142857x_3 -2.285714x_4 -0.857143x_{20} -0.428571x_{17} +1.000000x_7 +0.73
                                                                +2.000000x_1 -2.000000x_2 +1.000000x_3 +2.000000x_4
                                 7.0
                                                                                                                                                                                                                                                                                                             -2.000000x_7
x_{13}
                23.2857142857
                                                                +2.000000x_1 -1.428571x_2 -0.428571x_3 -6.142857x_4 -0.428571x_{20} -0.714286x_{17} +2.000000x_7 -0.1486x_{17}
x_{14}
                                                                x_{15}
                                7.0
                6.85714285714
                                                               +3.333333x_1 - 11.285714x_2 + 6.714286x_3 - 7.761905x_4 + 1.714286x_{20} - 2.142857x_{17} - 3.000000x_7 + 3.23x_{10} + 3
x_{16}
                                 1.0
                                                                -0.666667x_1 +1.000000x_2 -1.000000x_3 +0.666667x_4
                                                                                                                                                                                                                                                                    +0.000000x_{17}
                                                                                                                                                                                                                                                                                                                                                   -0.33
x_6
                18.5714285714
                                                                -0.333333x_1 -0.857143x_2 -2.857143x_3 + 1.047619x_4 + 0.142857x_{20} - 0.428571x_{17}
                                                                                                                                                                                                                                                                                                                                                  +0.04
x_{18}
                                                                16.2857142857
x_{19}
                2.57142857143
                                                                +0.333333x_1 -1.857143x_2 +1.142857x_3 -1.619048x_4 +0.142857x_{20} -0.428571x_{17}
                                                                                                                                                                                                                                                                                                                                                  +0.38
x_5
                                                                x_{21}
                18.2857142857
                10.7142857143
                                                                x_{22}
                               12.0
                                                                +4.000000x_1 -1.000000x_2 -1.000000x_3 -3.000000x_4 +1.000000x_{20} -1.000000x_{17}
x_{23}
               5.14285714286
```

 x_{17} enters and x_{16} leaves

```
9.8
x_9
x_{10}
 9.2
  2.2
x_8
  x_{12}
 8.2
  7.0
  +2.000000x_1 -2.000000x_2 +1.000000x_3 +2.000000x_4
                  -2.000000x_7
x_{13}
 21.0
  x_{14}
  x_{15}
 3.8
x_{17}
 3.2
  1.0
  x_6
 17.2
  x_{18}
 20.4
  x_{19}
 1.2
  x_5
  19.2
x_{21}
 13.0
  x_{22}
  +2.444444x_1 + 4.266667x_2 - 4.133333x_3 + 0.622222x_4 + 0.200000x_{20} + 0.466667x_{16} + 1.400000x_7 - 0.511111x_{11}
x_{23}
 8.8
 5.6
  z
```

 x_{-1} enters and Final Dictionary Solution: 5.6 Num Pivots: 4