

## University of Southern Denmark

## DM852 13 April 2020

## Heuristics & Approximations Algorithms

Submitted To:
Marco Chiarandini
Lene Monrad Favrholdt
IMADA
Institute of Mathematics &
Computer Science

Submitted By: Alexander Lerche Falk Spring - Master of Computer Science

## Contents

1	Introduction	2
2	Nearest Neightbour	3
3	K Nearest Neightbours with a randomized twist	5
4	Furthest Neightbour Cluster - Custom	7
5	Two Opt & Three Opt	8
6	Closing Notes	9
Aı	ppendices	10
$\mathbf{A}$	Nearest Neightbour Results	10
В	K-Nearest Neightbour Results	12
$\mathbf{C}$	Furthest Neightbour Cluster - Results	14
D	Furthest Neightbour Cluster - Code	16
$\mathbf{E}$		
	Two Opt - Local Search Algorithm	16
$\mathbf{F}$	Nearest Neightbour with Two Opt - Results	17

#### 1 Introduction

The goal of this project is to show the knowledge acquired by the student in regards to Heuristic- and Local Search Algorithms. The algorithms are developed to suit the Capacitated Vehicle Routing Problem (CVRP). CVRP is a combinatorial optimization problemm, where a set of n customers has to be visited by m vehicles. Each customer can only be visited one vehicle. The sum of demands by the customers assigned to a vehicle must not overseed the capacity of the vehicle. All vehicles start and end their route at the depot (the starting point). The objective is to minimise the travelling cost and try to use as few vehicles as possible. Heuristics and Local Search algorithms are applied to CVRP, where the heuristics are laying the foundation of possible solutions of routes, and the Local Search algorithms try to improve the solutions. Three heuristic algorithms have been developed:

- Nearest Neightbour Pick nearest customer from the depot or current customer without breaking the capacity
- Furthest Neightbour (with nearest clustering) Pick customer furthest away from the depot, find the closest customers until the capacity is reached, and generate a route by using Nearest Neightbour
- K-Nearest Neightbour Pick k nearest customers and randomly pick one of the k options. Proceed until no more customers without breaking the capacity

Two local search algorithms have been developed:

- Two Opt Pick a route generated by some heuristic. Pick two edges, swap the edges, and compare the distance from before and after the swap. If better, make the swap.
- Three Opt Pick a route generated by some heuristic. Pick three edges, swap the edges, and compare the distance from before and after the swap. If better, make the swap.

At the end of the report, comparison of the heuristics and results are presented.

### 2 Nearest Neightbour

The Nearest Neightbour algorithm is a simple, yet powerful, approach to tackle CVRP. The algorithm goes starts at the depot and picks the nearest customer by iterating through all of the customers. It marks the customer as visited, adds it to a vehicle, and continues until the capacity of the vehicle is reached (or nearly reached). It returns to the depot and start over with the remaining customers with a new vehicle.

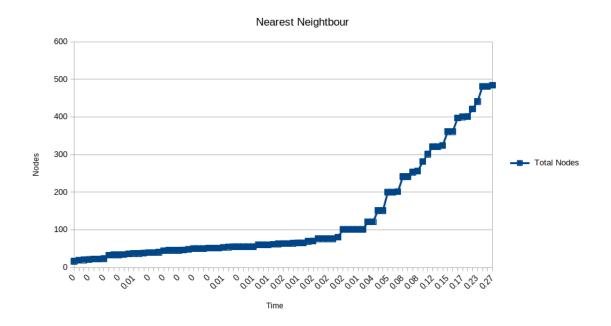
The algorithm is described in pseudocode:

```
Algorithm 1 Nearest Neightbour
```

```
Require: Set of customers
Ensure: Solution (solution to the CVRP instance)
 1: j \leftarrow \text{random node } j
 2: i = j \leftarrow \text{starting point}
 3: \mathbb{W} = \{1, 2, ..., n\} \setminus \{j\} \leftarrow \text{set of customers minus the randomly picked}
 4: function NearestNeightbour(instance, W)
         while W \neq \emptyset do
 5:
             let j \in W \mid c_{ij} = min\{c_{ij} \mid j \in W\}
 6:
             Shortest node by edge (i, j) is added to vehicle route
 7:
             Set W = W \setminus \{j\} \leftarrow Customer i is marked visited
 8:
             i = j \leftarrow \text{setting i to next in line}
 9:
```

The Nearest Neightbour has a running time of  $\mathcal{O}(n^2)$ , which is a quadric function. This means, that for every execution step done by the algorithm, the input size n has to be checked: n \* n. In the developed code, a parameter has been added to perform performance testing on the algorithms. Every instance is executed by each of the algorithms, where time, cost, and numbers of nodes are saved. In Figure 1 (see appendix A for data), it is shown when the input size grows, the execution time grows quadric:

Figure 1: Algorithm analysis of Nearest Neightbour.  $X=Time,\,Y=Nodes$ 



### 3 K Nearest Neightbours with a randomized twist

The K-Nearest Neightbour algorithm is the same as Nearest Neightbour but with a twist. The Nearest Neightbour algorithm has to downside of ending in a local optimum. This means, the solution is optimal within the set of candidate solutions. It is different from the global optimum, which is the optimal solution for all possible solutions. KNN tries to escape the local optimum by taking an unforseen step instead of always following the closest node. It starts by picking the k nearest neightbours and then by voting, it picks one of the k nearest neightbours. The vote in this case is done by randomly choosing a customer and then continue with the same approach.

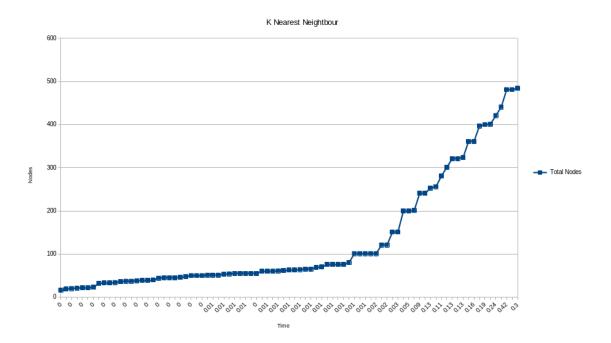
The algorithm is described in pseudocode:

```
Algorithm 2 K-Nearest Neightbour
```

```
Require: Set of customers
Ensure: Solution (solution to the CVRP instance)
 1: j \leftarrow \text{random node } j
 2: i = j \leftarrow \text{starting point}
 3: \mathbb{W} = \{1, 2, ..., n\} \setminus \{j\} \leftarrow \text{set of customers minus the randomly picked}
 4: C = \emptyset \leftarrow \text{empty set to store closest points to i}
 5: function KNEARESTNEIGHTBOUR(instance, W)
 6:
         while W \neq \emptyset do
             let j \in W \mid c_{ij} = min\{c_{ij} \mid j \in W\}
 7:
             Every j is added to C
 8:
             Sort C ascending and take the first k customers
 9:
10:
             Set j to a random pick in C
             Set W = W \setminus \{j\} \( \subseteq \text{Customer j is marked visited} \)
11:
             i = j \leftarrow \text{setting i to next in line}
12:
```

The K-Nearest Neightbour has a running time of  $\mathcal{O}(n^2 + k)$ , which is a quadric function. The execution steps for the input size is the same as the nearest neightbour, but it adds the extra execution by randomly picking one of the k nearest neighbours. In Figure 2 (see appendix B for data), it is shown when the input size grows, the execution time grows quadric:

Figure 2: Algorithm analysis of K-Nearest Neightbour.  $X=Time,\,Y=Nodes$ 



#### 4 Furthest Neightbour Cluster - Custom

NN and KNN takes the nearest neightbours into consideration and keeps growing by using the nearest neightbour. This can lead to issues with the later vehicles only having the customers left, which are far away from each other. Depending on the instance, KNN - and especially - NN can grow in one direction, and not taking the rest of the instance into account. The project has tried to accommodate the issue by picking the customer furthest away from the depot. The algorithm has been named Furthest Neightbour Cluster - lacking of better naming. The algorithm picks the customer furtest away from the depot, finds the closest nodes to the picked customer (like a cluster), and uses NN to find a suitable route within this cluster. Capacity is taking into consideration when picking the closest customers.

The algorithm is described in pseudocode:

```
Algorithm 3 Furthest Neightbour Cluster
```

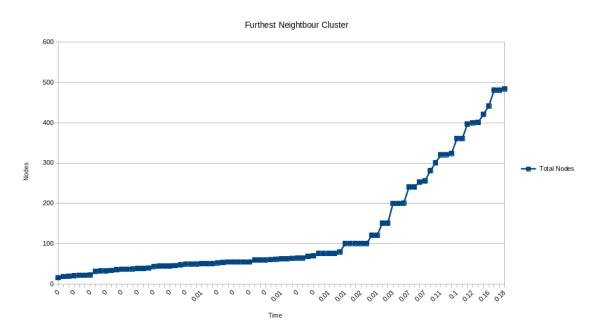
```
Require: Set of customers
Ensure: Solution (solution to the CVRP instance)
 1: j \leftarrow depot
 2: i = j \leftarrow \text{starting point}
 3: \mathbb{W} = \{1, 2, ..., n\} \setminus \{j\} \leftarrow \text{set of customers minus the randomly picked}
 4: F = \emptyset \leftarrow empty set to store closest customer to furthest customer
    function FurthestNeightbourCluster(instance, W)
         while W \neq \emptyset do
 6:
             let j \in W \mid c_{ij} = max\{c_{ij} \mid j \in W\}
 7:
             Furthest node by edge (i, j) is stored in j
 8:
 9:
             Set W = W \setminus \{j\} \( \tau \) Customer j is marked visited
             while W \neq \emptyset & Capacity not reached do
10:
                 let k \in W \mid c_{ik} = min\{c_{ik} \mid k \in W\}
11:
                 Shortest node by edge (j, k) is stored in k
12:
                 Set W = W \setminus \{k\} \leftarrow \text{Customer k} is marked visited
13:
                 i = depot as starting point
14:
```

The Furthest Neightbour Cluster has a running time of  $\mathcal{O}(3n^2)$ , which is a quadric function. We can calculate it by looking into the code and analyze. The first While-loop takes up  $\mathcal{O}(n)$  and the For-loop inside it takes up  $\mathcal{O}(n)$ . Then the While-loop inside the outer While-loop takes up the same as before:  $\mathcal{O}(n)$  and the same with the For-loop inside:  $\mathcal{O}(n)$ . The last While- and For-loop takes up the same:  $\mathcal{O}(n)$ . This gives us the following:  $(\mathcal{O}(n) * \mathcal{O}(n)) + (\mathcal{O}(n)) * \mathcal{O}(n)) + (\mathcal{O}(n) * \mathcal{O}(n)) = \mathcal{O}(3n^2)$ .

In Appendix D, the code for the algorithm is shown.

In Figure 3 (see appendix E for data), it is shown when the input size grows, the execution time grows quadric:

Figure 3: Algorithm analysis of K-Nearest Neightbour. X = Time, Y = Nodes



## 5 Two Opt & Three Opt

Heuristics generates solutions which can be global optimal, but tends to end up in a local optimum. One way of getting out of this is by using Local Search Optimization algorithms. These algorithms takes an existing solution to an optimization problem and try to optimize the solution. In this project, the goal is to minimize the total cost of the vehicle routes, and we can use Two Opt and Three Opt to try improving our existing solutions.

Two opt takes two routes and compare their distances. A swap is possible if the distance is being reduced in at least one route, while still preserving the maximum capacity limit of both routes.

Three Opt does the same as Two Opt, but instead of looking and two routes, it takes three into consideration.

Using the Nearest Neightbour heuristics to analysise the cost reduction using local search showed an improvement of 171424 - 167016 = 4408 (sum of total costs from

.csv files / see appendix F for results) over all of the instances. And this is by only running Two Opt once on every solution of each instance.

### 6 Closing Notes

Heuristics give fast and good results. They are not global optimum but if the objective is to find a solution, and not the best, they are good for this. To get closer to global optimum, local search algorithms tries to get us closer. The issue with local search algorithms are: when to stop improving. Shown in the above results, Two Opt was only ran once to improve existing solutions, but it could have been run continiously and set a kill switch, when it is no longer improving. One issue with this is, when it gets stuck in a local optimum. In that case, other approaches should be taken to try and get away from the local optimum. An example of this could be by making bad moves.

# Appendices

A Nearest Neightbour Results

Golden.04.xml         15746.0         0.26         481           Golden.13.xml         980.0         0.1         253           Golden.17.xml         924.0         0.08         241           Golden.19.xml         1756.0         0.15         361           Golden.05.xml         9443.0         0.07         201           Golden.09.xml         575.0         0.08         256           Golden.10.xml         5824.0         0.07         241           Golden.15.xml         1413.0         0.13         301           Golden.15.xml         1545.0         0.17         397           Golden.20.xml         2288.0         0.21         421           Golden.20.xml         11380.0         0.14         361           Golden.14.xml         1281.0         0.12         321           Golden.16.xml         1897.0         0.26         481           Golden.10.xml         764.0         0.13         324           Golden.03.xml         12054.0         0.19         401           Golden.03.xml         12054.0         0.19         401           Golden.08.xml         12876.0         0.23         441           Golden.08.xml         150	Instance	Cost	Time	Total Nodes
Golden.17.xml         924.0         0.08         241           Golden.19.xml         1756.0         0.15         361           Golden.05.xml         9443.0         0.07         201           Golden.01.xml         5824.0         0.07         241           Golden.18.xml         1413.0         0.13         301           Golden.15.xml         1545.0         0.17         397           Golden.20.xml         2288.0         0.21         421           Golden.20.xml         11380.0         0.14         361           Golden.14.xml         1281.0         0.12         321           Golden.16.xml         1897.0         0.26         481           Golden.10.xml         764.0         0.13         324           Golden.10.xml         764.0         0.13         324           Golden.03.xml         12054.0         0.19         401           Golden.08.xml         12876.0         0.23         441           Golden.08.xml         12876.0         0.23         441           Golden.02.xml         9689.0         0.13         281           Golden.02.xml         9689.0         0.02         63           A-n63-k0.xml         1505	$Golden_04.xml$	15746.0	0.26	481
Golden_19.xml         1756.0         0.15         361           Golden_05.xml         9443.0         0.07         201           Golden_09.xml         575.0         0.08         256           Golden_18.xml         1413.0         0.13         301           Golden_15.xml         1545.0         0.17         397           Golden_20.xml         2288.0         0.21         421           Golden_16.xml         11380.0         0.14         361           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         1265.0         0.27         484           Golden_02.xml         1505.0         0.02         63           A-n63-k10.xml         1505.0         0.02         63           A-n64-k09.xml         1294.0         0.01         54           A-n69-k09.xml         1555.0	$Golden_13.xml$	980.0	0.1	253
Golden_05.xml         9443.0         0.07         201           Golden_09.xml         575.0         0.08         256           Golden_01.xml         5824.0         0.07         241           Golden_18.xml         1413.0         0.13         301           Golden_15.xml         1545.0         0.17         397           Golden_16.xml         11380.0         0.14         361           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_08.xml         12876.0         0.23         441           Golden_02.xml         9689.0         0.13         281           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.	$Golden_17.xml$	924.0	0.08	241
Golden_09.xml         575.0         0.08         256           Golden_01.xml         5824.0         0.07         241           Golden_18.xml         1413.0         0.13         301           Golden_15.xml         1545.0         0.17         397           Golden_10.xml         2288.0         0.21         421           Golden_10.xml         11380.0         0.14         361           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         1165.0         0.27         484           Golden_02.xml         1294.0         0.01         61           A-n37-k05.xml         1505.0         0.02         63           A-n69-k09.xml         1555	$Golden_19.xml$	1756.0	0.15	361
Golden_01.xml         5824.0         0.07         241           Golden_18.xml         1413.0         0.13         301           Golden_15.xml         1545.0         0.17         397           Golden_16.xml         2288.0         0.21         421           Golden_16.xml         11380.0         0.14         361           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         1165.0         0.27         484           Golden_02.xml         1294.0         0.01         61           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0	$Golden_05.xml$	9443.0	0.07	201
Golden_18.xml         1413.0         0.13         301           Golden_15.xml         1545.0         0.17         397           Golden_20.xml         2288.0         0.21         421           Golden_14.xml         1281.0         0.12         321           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         974.0         0.17         400           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         1165.0         0.27         484           Golden_02.xml         1505.0         0.02         63           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n38-k05.xml         160	$Golden_09.xml$	575.0	0.08	256
Golden_15.xml         1545.0         0.17         397           Golden_20.xml         2288.0         0.21         421           Golden_16.xml         11380.0         0.14         361           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_11.xml         974.0         0.17         400           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n64-k09.xml         1583.0 <td><math>Golden_01.xml</math></td> <td>5824.0</td> <td>0.07</td> <td>241</td>	$Golden_01.xml$	5824.0	0.07	241
Golden_20.xml         2288.0         0.21         421           Golden_07.xml         11380.0         0.14         361           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         974.0         0.17         400           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n65-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1583.0 <td><math>Golden_18.xml</math></td> <td>1413.0</td> <td>0.13</td> <td>301</td>	$Golden_18.xml$	1413.0	0.13	301
Golden_07.xml         11380.0         0.14         361           Golden_14.xml         1281.0         0.12         321           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_10.xml         974.0         0.17         400           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         9689.0         0.13         281           Golden_02.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n64-k99.xml         1294.0         0.01         61           A-n54-k90.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n65-k99.xml         1583.0 </td <td><math>Golden_15.xml</math></td> <td>1545.0</td> <td>0.17</td> <td>397</td>	$Golden_15.xml$	1545.0	0.17	397
Golden_07.xml         11380.0         0.14         361           Golden_14.xml         1281.0         0.12         321           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         9689.0         0.13         281           Golden_02.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n65-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1715.0 </td <td><math>Golden_20.xml</math></td> <td>2288.0</td> <td>0.21</td> <td>421</td>	$Golden_20.xml$	2288.0	0.21	421
Golden_14.xml         1281.0         0.12         321           Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_12.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n65-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1583.0         0.01         64           A-n45-k07.xml         1614.0         0.0         45           A-n39-k06.xml         1054.0	$Golden_07.xml$	11380.0	0.14	361
Golden_16.xml         1897.0         0.26         481           Golden_10.xml         764.0         0.13         324           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_12.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n64-k09.xml         1590.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n68-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1583.0         0.01         60           A-n46-k07.xml         1614.0         0.0         45           A-n63-k09.xml         2056.0	$Golden_14.xml$	1281.0	0.12	
Golden_10.xml         764.0         0.13         324           Golden_11.xml         974.0         0.17         400           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_12.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n64-k09.xml         1555.0         0.02         69           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n68-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1583.0         0.01         60           A-n63-k09.xml         1715.0         0.01         64           A-n63-k09.xml         1614.0	$Golden_16.xml$	1897.0	0.26	
Golden_03.xml         974.0         0.17         400           Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         9689.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n65-k09.xml         1422.0         0.01         65           A-n64-k09.xml         1583.0         0.01         60           A-n64-k09.xml         1715.0         0.01         63           A-n39-k06.xml         1054.0         0.0         39           A-n33-k05.xml         765.0	$Golden_10.xml$	764.0	0.13	324
Golden_03.xml         12054.0         0.19         401           Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n38-k05.xml         966.0         0.0         38           A-n65-k09.xml         1422.0         0.01         65           A-n64-k09.xml         1715.0         0.01         64           A-n45-k07.xml         1614.0         0.0         45           A-n39-k06.xml         1054.0         0.0         39           A-n33-k05.xml         765.0         0.0         34           A-n39-k05.xml         1076.0         <				
Golden_08.xml         12876.0         0.23         441           Golden_06.xml         9689.0         0.13         281           Golden_12.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n62-k08.xml         1422.0         0.01         65           A-n64-k09.xml         1583.0         0.01         65           A-n64-k09.xml         1715.0         0.01         64           A-n45-k07.xml         1614.0         0.0         45           A-n39-k06.xml         1054.0         0.0         39           A-n33-k06.xml         765.0         0.0         34           A-n39-k05.xml         1076.0				
Golden_06.xml         9689.0         0.13         281           Golden_12.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n38-k05.xml         966.0         0.0         38           A-n65-k09.xml         1422.0         0.01         65           A-n64-k09.xml         1715.0         0.01         64           A-n45-k07.xml         1614.0         0.0         45           A-n39-k06.xml         1054.0         0.0         39           A-n34-k05.xml         969.0         0.0         34           A-n39-k05.xml         1076.0         0.0         39           A-n46-k07.xml         1159.0         0				
Golden_12.xml         1165.0         0.27         484           Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n53-k07.xml         1270.0         0.01         53           A-n65-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1583.0         0.01         60           A-n64-k09.xml         1715.0         0.01         64           A-n45-k07.xml         1614.0         0.0         45           A-n39-k06.xml         1054.0         0.0         39           A-n34-k05.xml         969.0         0.0         34           A-n39-k05.xml         1076.0         0.0         39           A-n46-k07.xml         1159.0				
Golden_02.xml         9245.0         0.22         321           A-n63-k10.xml         1505.0         0.02         63           A-n61-k09.xml         1294.0         0.01         61           A-n37-k05.xml         965.0         0.01         37           A-n54-k07.xml         1690.0         0.01         54           A-n69-k09.xml         1555.0         0.02         69           A-n62-k08.xml         1486.0         0.01         62           A-n53-k07.xml         1270.0         0.01         53           A-n38-k05.xml         966.0         0.0         38           A-n65-k09.xml         1422.0         0.01         65           A-n60-k09.xml         1583.0         0.01         60           A-n64-k09.xml         1715.0         0.01         64           A-n45-k07.xml         1614.0         0.0         45           A-n39-k06.xml         1054.0         0.0         39           A-n34-k05.xml         765.0         0.0         34           A-n39-k05.xml         1076.0         0.0         39           A-n46-k07.xml         1159.0         0.0         46           A-n45-k06.xml         1158.0         0.0<				
A-n63-k10.xml       1505.0       0.02       63         A-n61-k09.xml       1294.0       0.01       61         A-n37-k05.xml       965.0       0.01       37         A-n54-k07.xml       1690.0       0.01       54         A-n69-k09.xml       1555.0       0.02       69         A-n62-k08.xml       1486.0       0.01       62         A-n53-k07.xml       1270.0       0.01       53         A-n38-k05.xml       966.0       0.0       38         A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n39-k06.xml       1054.0       0.0       39         A-n34-k05.xml       765.0       0.0       34         A-n39-k05.xml       903.0       0.0       34         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37     <				
A-n61-k09.xml       1294.0       0.01       61         A-n37-k05.xml       965.0       0.01       37         A-n54-k07.xml       1690.0       0.01       54         A-n69-k09.xml       1555.0       0.02       69         A-n62-k08.xml       1486.0       0.01       62         A-n53-k07.xml       1270.0       0.01       53         A-n38-k05.xml       966.0       0.0       38         A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n39-k06.xml       1054.0       0.0       39         A-n34-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       45         A-n45-k06.xml       1158.0       0.0       45         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44				
A-n37-k05.xml       965.0       0.01       37         A-n54-k07.xml       1690.0       0.01       54         A-n69-k09.xml       1555.0       0.02       69         A-n62-k08.xml       1486.0       0.01       62         A-n53-k07.xml       1270.0       0.01       53         A-n38-k05.xml       966.0       0.0       38         A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n39-k06.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n54-k07.xml       1690.0       0.01       54         A-n69-k09.xml       1555.0       0.02       69         A-n62-k08.xml       1486.0       0.01       62         A-n53-k07.xml       1270.0       0.01       53         A-n38-k05.xml       966.0       0.0       38         A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n39-k06.xml       1054.0       0.0       39         A-n33-k06.xml       765.0       0.0       34         A-n34-k05.xml       903.0       0.0       34         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n69-k09.xml1555.00.0269A-n62-k08.xml1486.00.0162A-n53-k07.xml1270.00.0153A-n38-k05.xml966.00.038A-n65-k09.xml1422.00.0165A-n60-k09.xml1583.00.0160A-n64-k09.xml1715.00.0164A-n45-k07.xml1614.00.045A-n63-k09.xml2056.00.0163A-n39-k06.xml1054.00.039A-n34-k05.xml765.00.033A-n34-k05.xml903.00.034A-n39-k05.xml1076.00.039A-n46-k07.xml1159.00.046A-n45-k06.xml1158.00.045A-n37-k06.xml1164.00.037A-n55-k09.xml1392.00.055A-n44-k06.xml1251.00.04411				
A-n62-k08.xml1486.00.0162A-n53-k07.xml1270.00.0153A-n38-k05.xml966.00.038A-n65-k09.xml1422.00.0165A-n60-k09.xml1583.00.0160A-n64-k09.xml1715.00.0164A-n45-k07.xml1614.00.045A-n63-k09.xml2056.00.0163A-n39-k06.xml1054.00.039A-n34-k05.xml765.00.034A-n33-k06.xml903.00.034A-n39-k05.xml1076.00.039A-n46-k07.xml1159.00.046A-n45-k06.xml1158.00.045A-n37-k06.xml1164.00.037A-n55-k09.xml1392.00.055A-n44-k06.xml1251.00.04411				
A-n53-k07.xml       1270.0       0.01       53         A-n38-k05.xml       966.0       0.0       38         A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       34         A-n34-k05.xml       969.0       0.0       34         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n38-k05.xml       966.0       0.0       38         A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n34-k05.xml       765.0       0.0       34         A-n34-k05.xml       969.0       0.0       34         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n65-k09.xml       1422.0       0.01       65         A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       34         A-n34-k05.xml       969.0       0.0       34         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n60-k09.xml       1583.0       0.01       60         A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n39-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n64-k09.xml       1715.0       0.01       64         A-n45-k07.xml       1614.0       0.0       45         A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n39-k05.xml       903.0       0.0       33         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n45-k07.xml       1614.0       0.0       45         A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n33-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n63-k09.xml       2056.0       0.01       63         A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n33-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n39-k06.xml       1054.0       0.0       39         A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n33-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n33-k05.xml       765.0       0.0       33         A-n34-k05.xml       969.0       0.0       34         A-n33-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n34-k05.xml       969.0       0.0       34         A-n33-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n33-k06.xml       903.0       0.0       33         A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n39-k05.xml       1076.0       0.0       39         A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n46-k07.xml       1159.0       0.0       46         A-n45-k06.xml       1158.0       0.0       45         A-n37-k06.xml       1164.0       0.0       37         A-n55-k09.xml       1392.0       0.0       55         A-n44-k06.xml       1251.0       0.0       44       11				
A-n45-k06.xml 1158.0 0.0 45 A-n37-k06.xml 1164.0 0.0 37 A-n55-k09.xml 1392.0 0.0 55 A-n44-k06.xml 1251.0 0.0 44 11				
A-n37-k06.xml 1164.0 0.0 37 A-n55-k09.xml 1392.0 0.0 55 A-n44-k06.xml 1251.0 0.0 44 11				
A-n55-k09.xml 1392.0 0.0 55 A-n44-k06.xml 1251.0 0.0 44 11				
A-n44-k06.xml 1251.0 0.0 44 11				
11 1100 1100:111111 1000:0 0:0 00				
A-n48-k07.xml 1316.0 0.01 48				
A-n80-k10.xml 2054.0 0.01 80				
A-n32-k05.xml 926.0 0.0 32				
		962 N		

## B K-Nearest Neightbour Results

Instance	Cost	Time	Total Nodes
$Golden_04.xml$	27923.0	0.42	481
$Golden_13.xml$	1411.0	0.13	253
$Golden_17.xml$	1207.0	0.09	241
$Golden_19.xml$	2299.0	0.18	361
$Golden_05.xml$	13912.0	0.08	201
$Golden_09.xml$	965.0	0.09	256
$Golden_01.xml$	10802.0	0.07	241
$Golden_18.xml$	1686.0	0.14	301
$Golden_15.xml$	2165.0	0.19	397
$Golden_20.xml$	3025.0	0.24	421
$Golden_07.xml$	19552.0	0.16	361
$Golden_14.xml$	1773.0	0.13	321
$Golden_16.xml$	2633.0	0.29	481
$Golden_10.xml$	1231.0	0.13	324
$Golden_11.xml$	1538.0	0.19	400
$Golden_03.xml$	20616.0	0.22	401
$Golden_08.xml$	23087.0	0.24	441
$Golden_06.xml$	17759.0	0.11	281
$Golden_12.xml$	1920.0	0.3	484
$Golden_02.xml$	15024.0	0.14	321
A-n63-k10.xml	2060.0	0.01	63
A-n61-k09.xml	1742.0	0.01	61
A-n37-k05.xml	1170.0	0.0	37
A-n54-k07.xml	1860.0	0.0	54
A-n69-k09.xml	1755.0	0.01	69
A-n62-k08.xml	2189.0	0.01	62
A-n53-k07.xml	1616.0	0.01	53
A-n38-k05.xml	1202.0	0.0	38
A-n65-k09.xml	1882.0	0.01	65
A-n60-k09.xml	2285.0	0.01	60
A-n64-k09.xml	2292.0	0.01	64
A-n45-k07.xml	1585.0	0.0	45
A-n63-k09.xml	2487.0	0.01	63
A-n39-k06.xml	1441.0	0.0	39
A-n33-k05.xml	1205.0	0.0	33
A-n34-k05.xml	1397.0	0.0	34
A-n33-k06.xml	1107.0	0.0	33
A-n39-k05.xml	1289.0	0.0	39
A-n46-k07.xml	1453.0	0.0	46
A-n45-k06.xml	1613.0	0.0	45
A-n37-k06.xml	1509.0	0.0	37
A-n55-k09.xml	1812.0	0.01	55
A-n44-k06.xml	1503.0	0.0	44 13
A-n36-k05.xml	1307.0	0.0	36
A-n48-k07.xml	1717.0	0.0	48
A-n80-k10.xml	2732.0	0.01	80
A-n32-k05.xml	1282.0	0.0	32
P_n051_k10 vml	11/6 0	0.0	51

## C Furthest Neightbour Cluster - Results

Instance	Cost	Time	Total Nodes
Golden_04.xml	74042.0	0.19	481
Golden_13.xml		0.19 $0.05$	253
Golden_17.xml	3050.0	0.07	241
Golden_19.xml	6218.0	0.1	361
Golden_05.xml	36673.0	0.03	201
Golden_09.xml	2521.0	0.07	256
Golden_01.xml		0.05	241
Golden_18.xml	4350.0	0.07	301
Golden_15.xml	5432.0	0.15	397
Golden_20.xml	8151.0	0.14	421
Golden_07.xml		0.1	361
Golden_14.xml		0.11	321
$Golden_16.xml$	6905.0	0.17	481
$Golden_10.xml$	3519.0	0.11	324
Golden_11.xml	4729.0	0.12	400
$Golden_03.xml$	51120.0	0.12	401
$Golden_08.xml$	54002.0	0.16	441
$Golden_06.xml$	43663.0	0.07	281
$Golden_12.xml$	6295.0	0.18	484
$Golden_02.xml$	34681.0	0.1	321
A-n63-k10.xml	3343.0	0.01	63
A-n61-k09.xml	3200.0	0.01	61
A-n37-k05.xml	1762.0	0.0	37
A-n54-k07.xml	3374.0	0.0	54
A-n69-k09.xml	3756.0	0.0	69
A-n62-k08.xml	4130.0	0.0	62
A-n53-k07.xml	2817.0	0.0	53
A-n38-k05.xml	1982.0	0.0	38
A-n65-k09.xml	3420.0	0.0	65
A-n60-k09.xml	3699.0	0.01	60
A-n64-k09.xml	3872.0	0.0	64
A-n45-k07.xml	2592.0	0.0	45
A-n63-k09.xml	4233.0	0.0	63
A-n39-k06.xml	2262.0	0.0	39
A-n33-k05.xml	1970.0	0.0	33
A-n34-k05.xml	2076.0	0.0	34
A-n33-k06.xml	1608.0	0.0	33
A-n39-k05.xml	1942.0	0.0	39
A-n46-k07.xml	2592.0	0.0	46
A-n45-k06.xml	2617.0	0.0	45
A-n37-k06.xml	2217.0	0.0	37
A-n55-k09.xml	3250.0	0.0	55
A-n44-k06.xml	2345.0	0.0	44 15
A-n36-k05.xml	2343.0 1990.0	0.0	36
A-n48-k07.xml	2639.0	0.0	48
A-n80-k10.xml	4686.0	0.01	80
A-n32-k05.xml	2018.0	0.0	32
P_n051_k10 vml	1814.0	0.01	51

#### D Furthest Neightbour Cluster - Code

 $\mathbf{E}$ 

### Two Opt - Local Search Algorithm

#### Algorithm 4 Two\_Opt

```
Require: dist(A, B) returns distance from point A to B
```

- 1: **function** TWOOPT( $route\_i, route\_j, i\_to\_j, j\_to\_i$ )
- 2: **for all** i, j such that i, j are routes index combination **do** evaluate d1 = total length of the two edges before being swapped evaluate d2 = total length of the two edges after being swapped
- 3: if d1 > d2 then

Make the swap between two the routes

4: else

return

### F Nearest Neightbour with Two Opt - Results

Instance	Cost	Time	Total Nodes
P-n016-k08.xml	497	0	16
P-n019-k02.xml	247	0	19
P-n020-k02.xml	285	0	20
P-n021-k02.xml	$\frac{209}{219}$	0	21
P-n022-k02.xml	238	0	22
P-n022-k08.xml	690	0	22
P-n023-k08.xml	669	0	23
A-n32-k05.xml	911	0	32
A-n33-k05.xml		0	33
A-n33-k06.xml	890	0	33
A-n34-k05.xml		0	34
A-n36-k05.xml		0	36
A-n37-k05.xml		0	37
A-n37-k06.xml		0	
A-1137-k00.xml			37
	954	0	38
A-n39-k06.xml		0	39
A-n39-k05.xml		0	39
P-n040-k05.xml		0	40
A-n44-k06.xml		0	44
A-n45-k07.xml	1485	0	45
A-n45-k06.xml	1104	0	45
P-n045-k05.xml		0	45
A-n46-k07.xml	1107	0	46
A-n48-k07.xml	1277	0	48
P-n050-k10.xml		0	50
P-n050-k07.xml		0	50
P-n050-k08.xml		0.01	50
P-n051-k10.xml		0	51
CMT06.xml	722	0	51
CMT01.xml	722	0.01	51
A-n53-k07.xml	1227	0	53
A-n54-k07.xml	1554	0	54
A-n55-k09.xml	1324	0	55
P-n055-k08.xml	649	0.01	55
P-n055-k07.xml	700	0.01	55
P-n055-k15.xml	1079	0.01	55
P-n055-k10.xml	761	0	55
A-n60-k09.xml	1528	0.01	60
P-n060-k10.xml	846	0	60
P-n060-k15.xml	1119	0.01	60
A-n61-k09.xml	1202	0.01	61
A-n62-k08.xml	1456	0.01	62
A-n63-k10.xml	1482	0	63   18
A-n63-k09.xml	1985	0.01	63
A-n64-k09.xml	1630	0.01	64
A-n65-k09.xml	1331	0.01	65
P-n065-k10.xml	992	0.01	65
$\Delta_n60_k00$ vml	1501	0.01	60