$$\int_{0}^{1} \frac{\ln t \, dt}{1+t} = -\frac{\pi^2}{12}.$$