## Linear Regression - Association of Tennis Professionals data

May 10, 2024

```
[8]: import pandas as pd
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression

# load and investigate the data here:
df = pd.read_csv('./tennis_stats.csv')

# perform exploratory analysis here:
df.info()
```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1721 entries, 0 to 1720
Data columns (total 24 columns):

#	Column	Non-Null Count	Dtype
0	Player	1721 non-null	object
1	Year	1721 non-null	int64
2	FirstServe	1721 non-null	float64
3	FirstServePointsWon	1721 non-null	float64
4	${ t First Serve Return Points Won}$	1721 non-null	float64
5	SecondServePointsWon	1721 non-null	float64
6	${\tt SecondServeReturnPointsWon}$	1721 non-null	float64
7	Aces	1721 non-null	int64
8	${\tt BreakPointsConverted}$	1721 non-null	float64
9	BreakPointsFaced	1721 non-null	int64
10	${\tt BreakPointsOpportunities}$	1721 non-null	int64
11	BreakPointsSaved	1721 non-null	float64
12	DoubleFaults	1721 non-null	int64
13	${\tt ReturnGamesPlayed}$	1721 non-null	int64
14	ReturnGamesWon	1721 non-null	float64
15	ReturnPointsWon	1721 non-null	float64
16	${\tt ServiceGamesPlayed}$	1721 non-null	int64
17	ServiceGamesWon	1721 non-null	float64
18	TotalPointsWon	1721 non-null	float64
19	TotalServicePointsWon	1721 non-null	float64
20	Wins	1721 non-null	int64
21	Losses	1721 non-null	int64

22 Winnings 1721 non-null int64 23 Ranking 1721 non-null int64

 ${\tt dtypes: float64(12), int64(11), object(1)}$ 

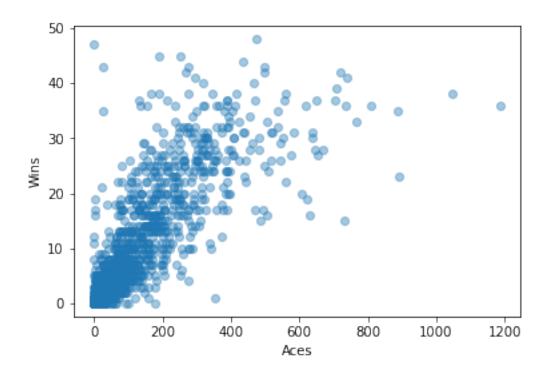
memory usage: 322.8+ KB

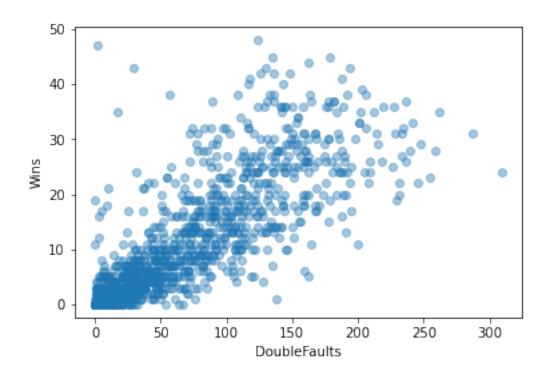
## [11]: df.describe()

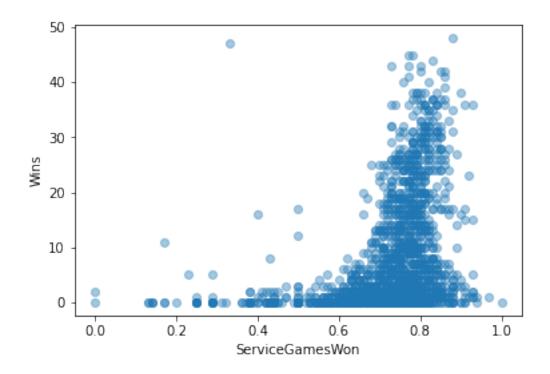
[11]:		Year	FirstServe	FirstServePointsWo	on \		
	count	1721.000000	1721.000000	1721.00000	00		
	mean	2013.646717	0.598053	0.68073	38		
	std	2.488018	0.054533	0.07042	22		
	min	2009.000000	0.360000	0.27000	00		
	25%	2012.000000	0.570000	0.65000	00		
	50%	2014.000000	0.600000	0.69000	00		
	75%	2016.000000	0.630000	0.72000	00		
	max	2017.000000	0.880000	0.89000	00		
		FirstServeRet	urnPointsWon	SecondServePoints	sWon	\	
	count		1721.000000	1721.000	0000		
	mean		0.261673	0.479	9733		
	std		0.056639	0.066	3902		
	min		0.000000	0.060	0000		
	25%		0.240000	0.460	0000		
	50%		0.270000	0.490	0000		
	75%		0.290000	0.520	0000		
	max		0.480000	0.920	0000		
		SecondServeRe	turnPointsWon	Aces Bre	eakPo	intsConverted	\
	count		1721.000000	1721.000000		1721.000000	
	count mean		1721.000000 0.466432			1721.000000 0.369407	
				97.105171			
	mean		0.466432	97.105171 137.966077		0.369407	
	mean std		0.466432 0.068447	97.105171 137.966077 0.000000		0.369407 0.162987	
	mean std min		0.466432 0.068447 0.000000	97.105171 137.966077 0.000000 7.000000		0.369407 0.162987 0.000000	
	mean std min 25%		0.466432 0.068447 0.000000 0.440000 0.480000 0.500000	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000	
	mean std min 25% 50%		0.466432 0.068447 0.000000 0.440000 0.480000	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000		0.369407 0.162987 0.000000 0.320000 0.380000	
	mean std min 25% 50% 75%	BreakPointsFa	0.466432 0.068447 0.000000 0.440000 0.480000 0.500000	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000	R	0.369407 0.162987 0.000000 0.320000 0.380000 0.430000	\
	mean std min 25% 50% 75%	BreakPointsFa 1721.000	0.466432 0.068447 0.000000 0.440000 0.500000 0.750000	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000	R	0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000	\
	mean std min 25% 50% 75% max		0.466432 0.068447 0.000000 0.440000 0.500000 0.750000 ced BreakPoi	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000 1185.000000		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000	\
	mean std min 25% 50% 75% max	1721.000	0.466432 0.068447 0.000000 0.440000 0.500000 0.750000 ced BreakPoi:	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000 1185.000000 ntsOpportunities 1721.000000		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000 eturnGamesWon 1721.000000	
	mean std min 25% 50% 75% max count mean	1721.000 112.003	0.466432 0.068447 0.000000 0.440000 0.500000 0.750000 ced BreakPoid	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000 1185.000000 ntsOpportunities 1721.000000 102.918071		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000 eturnGamesWon 1721.000000 0.173823	
	mean std min 25% 50% 75% max  count mean std	1721.000 112.003 119.247	0.466432 0.068447 0.000000 0.440000 0.500000 0.750000 ced BreakPoid	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000 1185.000000 ntsOpportunities 1721.000000 102.918071 122.761670		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000 eturnGamesWon 1721.000000 0.173823 0.080880	\
	mean std min 25% 50% 75% max  count mean std min	1721.000 112.003 119.247 1.000	0.466432 0.068447 0.000000 0.440000 0.500000 0.750000 ced BreakPoi: 000 486 651 000	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000 1185.000000  ntsOpportunities 1721.000000 102.918071 122.761670 0.000000		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000 eturnGamesWon 1721.000000 0.173823 0.080880 0.000000	
	mean std min 25% 50% 75% max  count mean std min 25%	1721.000 112.003 119.247 1.000 15.000	0.466432 0.068447 0.000000 0.440000 0.500000 0.750000 ced BreakPoi: 000 486 651 000 000	97.105171 137.966077 0.000000 7.000000 34.000000 140.000000 1185.000000  ntsOpportunities 1721.000000 102.918071 122.761670 0.000000 9.000000		0.369407 0.162987 0.000000 0.320000 0.380000 0.430000 1.000000 eturnGamesWon 1721.000000 0.173823 0.080880 0.000000 0.130000	\

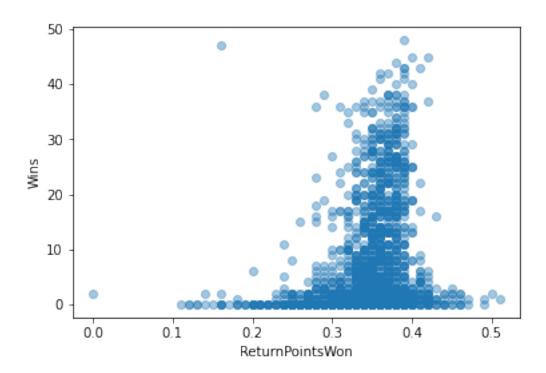
```
ReturnPointsWon
                              ServiceGamesPlayed
                                                   ServiceGamesWon
                                                                     TotalPointsWon
                 1721.000000
                                      1721.000000
                                                        1721.000000
                                                                        1721.000000
      count
      mean
                    0.342208
                                       197.650203
                                                           0.715590
                                                                           0.473155
      std
                    0.049369
                                       221.208703
                                                           0.123287
                                                                           0.037139
                                                                           0.220000
     min
                    0.000000
                                         0.000000
                                                           0.000000
      25%
                    0.320000
                                        22.000000
                                                           0.670000
                                                                           0.460000
      50%
                                                                           0.480000
                    0.350000
                                        86.000000
                                                           0.750000
      75%
                    0.370000
                                       348.000000
                                                           0.790000
                                                                           0.500000
                                                                           0.820000
                    0.510000
                                       916.000000
                                                           1.000000
     max
             TotalServicePointsWon
                                            Wins
                                                       Losses
                                                                    Winnings \
                       1721.000000
                                    1721.000000
                                                  1721.000000
                                                               1.721000e+03
      count
      mean
                           0.599245
                                        7.876816
                                                     9.278908 2.344928e+05
      std
                           0.057718
                                       10.183716
                                                     8.996450 2.530537e+05
                                                     0.000000 1.080000e+02
     min
                           0.250000
                                        0.000000
      25%
                           0.570000
                                        0.000000
                                                     2.000000 4.931100e+04
      50%
                           0.610000
                                        3.000000
                                                     5.000000 1.252120e+05
      75%
                                                    17.000000 3.500750e+05
                           0.630000
                                       13.000000
                           0.820000
                                       48.000000
                                                    36.000000 1.074562e+06
      max
                 Ranking
            1721.000000
      count
              269.610691
     mean
      std
              277.341947
     min
                3.000000
      25%
               83.000000
      50%
              166.000000
      75%
              333.000000
      max
             1443.000000
      [8 rows x 23 columns]
[34]: # Explore features visually
      plt.plot(df['Aces'], df['Wins'], 'o', alpha=0.4) # good feature
      plt.xlabel("Aces")
      plt.ylabel("Wins")
      plt.show()
      plt.plot(df['DoubleFaults'], df['Wins'], 'o', alpha=0.4) # good feature
      plt.xlabel("DoubleFaults")
      plt.ylabel("Wins")
      plt.show()
      plt.plot(df['ServiceGamesWon'], df['Wins'], 'o', alpha=0.4)
      plt.xlabel("ServiceGamesWon")
      plt.ylabel("Wins")
      plt.show()
      plt.plot(df['ReturnPointsWon'], df['Wins'], 'o', alpha=0.4)
      plt.xlabel("ReturnPointsWon")
```

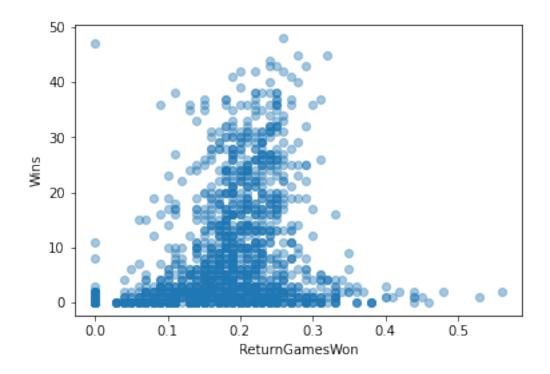
```
plt.ylabel("Wins")
plt.show()
plt.plot(df['ReturnGamesWon'], df['Wins'], 'o', alpha=0.4)
plt.xlabel("ReturnGamesWon")
plt.ylabel("Wins")
plt.show()
plt.plot(df['TotalPointsWon'], df['Wins'], 'o', alpha=0.4)
plt.xlabel("TotalPointsWon")
plt.ylabel("Wins")
plt.show()
plt.plot(df['FirstServe'], df['Wins'], 'o', alpha=0.4)
plt.xlabel("FirstServe")
plt.ylabel("Wins")
plt.show()
plt.plot(df['FirstServeReturnPointsWon'], df['Wins'], 'o', alpha=0.4)
plt.xlabel("FirstServeReturnPointsWon")
plt.ylabel("Wins")
plt.show()
plt.plot(df['BreakPointsFaced'], df['Wins'], 'o', alpha=0.4) #good feature
plt.xlabel("BreakPointsFaced")
plt.ylabel("Wins")
plt.show()
plt.plot(df['BreakPointsConverted'], df['Wins'], 'o', alpha=0.4) #good feature
plt.xlabel("BreakPointsConverted")
plt.ylabel("Wins")
plt.show()
plt.plot(df['BreakPointsOpportunities'], df['Wins'], 'o', alpha=0.4) #good__
\hookrightarrow feature
plt.xlabel("BreakPointsOpportunities")
plt.ylabel("Wins")
plt.show()
```

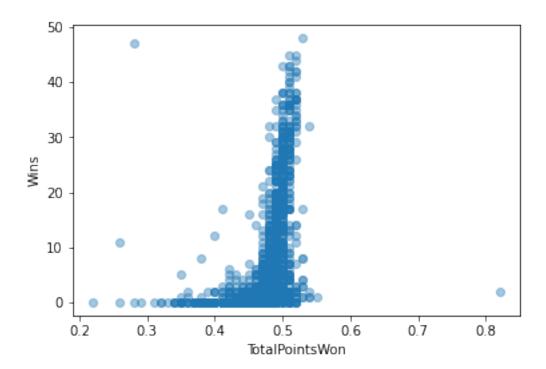


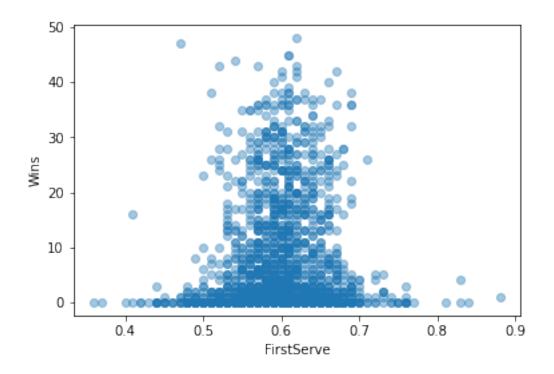


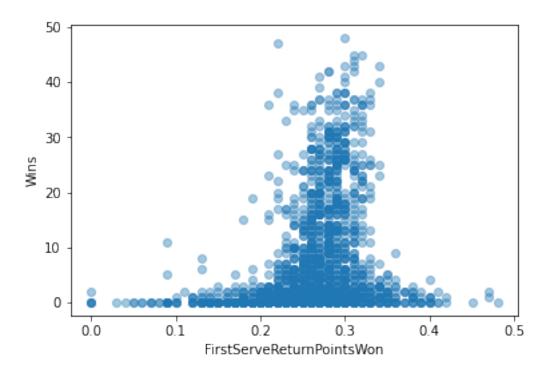


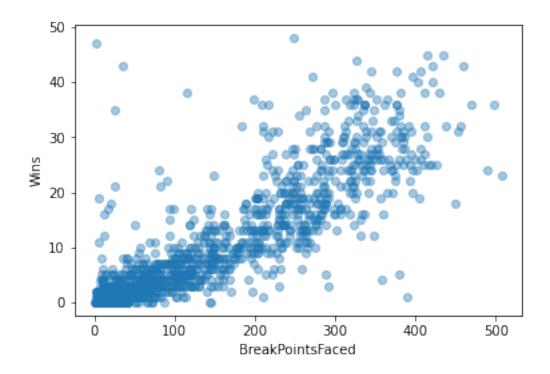


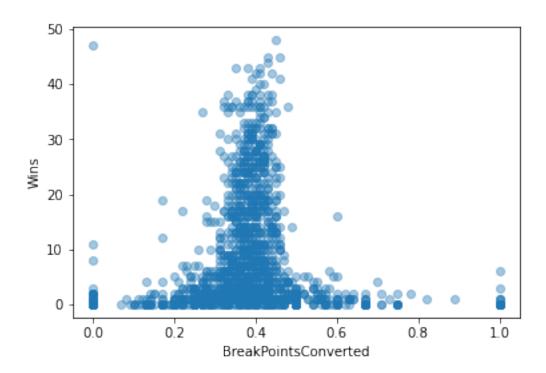


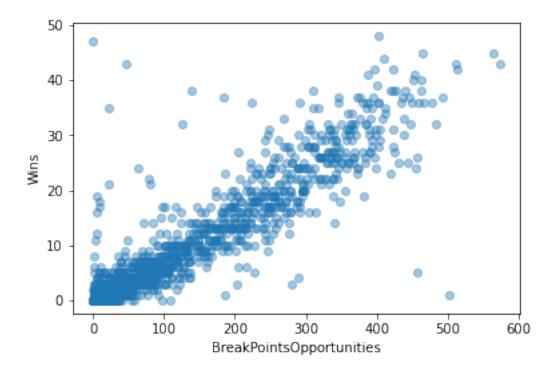








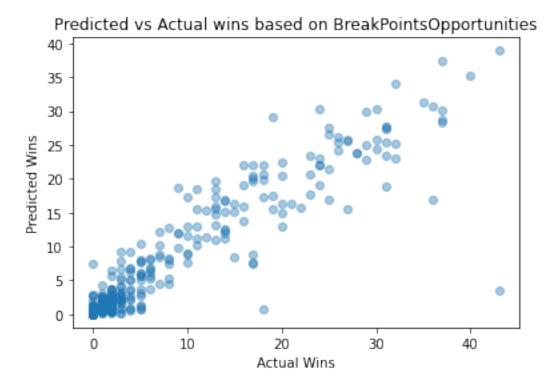




intercept of -0.0094

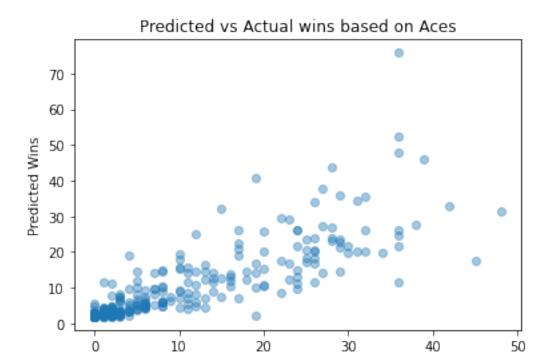
This model has an R^2 value of 0.86

plt.show()



```
[51]: # New single feature linear regression
      features = df[['Aces']]
      x_train, x_test, y_train, y_test = train_test_split(features, labels,_
      →train_size=0.8)
      SingleLR = LinearRegression()
      SingleLR.fit(x_train, y_train)
      print("The line for Aces vs Wins has a slope of \%.4f and an intercept of \%.4f"_{\sqcup}
      →% (SingleLR.coef_, SingleLR.intercept_))
      R_squared = SingleLR.score(x_test, y_test)
      print("This model has an R^2 value of %.2f" % R_squared)
      prediction = SingleLR.predict(x_test)
      plt.scatter(y_test, prediction, alpha=0.4)
      plt.xlabel("Actual Wins")
      plt.ylabel("Predicted Wins")
      plt.title("Predicted vs Actual wins based on Aces")
      plt.show()
```

The line for Aces vs Wins has a slope of 0.0624 and an intercept of 1.8811 This model has an  $R^2$  value of 0.70



Actual Wins

```
[54]: # Double feature linear regression
      features = df[['BreakPointsOpportunities', 'BreakPointsFaced']]
      labels = df[['Winnings']]
      DoubleLR = LinearRegression()
      x_train, x_test, y_train, y_test = train_test_split(features, labels,_
      →train_size=0.8)
      DoubleLR.fit(x_train, y_train)
      r2 = DoubleLR.score(x_test, y_test)
      print("R^2 for BreakPointsOpportunities and BreakPointsFaced vs Winnings is %.
      \rightarrow 2f'' % r2)
      features = df[['Aces', 'DoubleFaults']]
      DoubleLR = LinearRegression()
      x_train, x_test, y_train, y_test = train_test_split(features, labels,_

→train_size=0.8)
      DoubleLR.fit(x_train, y_train)
      r2 = DoubleLR.score(x_test, y_test)
      print("R^2 for Aces and DoubleFaults vs Winnings is %.2f" % r2)
```

 $R^2$  for BreakPointsOpportunities and BreakPointsFaced vs Winnings is 0.80  $R^2$  for Aces and DoubleFaults vs Winnings is 0.72

```
[56]: print("BreakPoints Opportunities and BreakPoints Faced are better predictors

→for Winnings than Aces and DoubleFaults")
```

BreakPoints Opportunities and BreakPoints Faced are better predictors for Winnings than Aces and DoubleFaults

```
[61]: # multiple linear regression
     from sklearn.preprocessing import StandardScaler
     mlr = LinearRegression()
     features = df.drop(columns=['Player', 'Wins', 'Losses', 'Winnings', 'Ranking'])
     labels = df['Winnings']
     features.info()
     <class 'pandas.core.frame.DataFrame'>
     RangeIndex: 1721 entries, 0 to 1720
     Data columns (total 19 columns):
         Column
                                     Non-Null Count Dtype
         _____
                                     _____ ____
      0
         Year
                                     1721 non-null
                                                     int64
      1
         FirstServe
                                     1721 non-null float64
      2
         FirstServePointsWon
                                     1721 non-null
                                                    float64
      3
         FirstServeReturnPointsWon
                                     1721 non-null
                                                    float64
      4
         SecondServePointsWon
                                     1721 non-null
                                                    float64
      5
         SecondServeReturnPointsWon 1721 non-null
                                                    float64
                                     1721 non-null
                                                    int64
      7
         BreakPointsConverted
                                     1721 non-null
                                                    float64
         BreakPointsFaced
                                     1721 non-null int64
         BreakPointsOpportunities
                                     1721 non-null int64
      10 BreakPointsSaved
                                     1721 non-null float64
      11 DoubleFaults
                                     1721 non-null int64
      12 ReturnGamesPlayed
                                     1721 non-null
                                                     int64
      13 ReturnGamesWon
                                     1721 non-null
                                                    float64
      14 ReturnPointsWon
                                     1721 non-null
                                                     float64
      15 ServiceGamesPlayed
                                     1721 non-null int64
      16 ServiceGamesWon
                                     1721 non-null
                                                     float64
      17 TotalPointsWon
                                     1721 non-null
                                                     float64
      18 TotalServicePointsWon
                                     1721 non-null
                                                     float64
     dtypes: float64(12), int64(7)
     memory usage: 255.6 KB
[65]: scaler = StandardScaler()
     scaledFeatures = scaler.fit_transform(features)
     x_train, x_test, y_train, y_test = train_test_split(scaledFeatures, labels,_
      →train_size=0.8)
     mlr.fit(x_train, y_train)
     r2 = mlr.score(x_test, y_test)
     print("Using a standardized form of all numerical features, the R^2 value for ⊔
      →multiple linear regression predicting Winnings is %.2f" % r2)
```

Using a standardized form of all numerical features, the  $R^2$  value for multiple linear regression predicting Winnings is 0.82

[]:[