Polarized Neutron Scattering

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Overview

1 Theory

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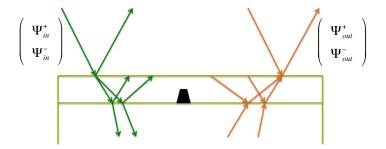
Theory

- First, we solve the perfectly smooth multilayer in the presence of magnetization in the layers.
- Then we use the Green's function method to obtain the first order contribution to the scattering amplitude.
- For magnetic dipoles, the scattering depends only on the magnetization perpendicular to the wavevector transfer:

$$\delta v_{\perp}(\mathbf{r}) \sim \sigma \cdot \mathbf{m}_{\perp}(\mathbf{r})$$

Homogeneous solution

- The magnetic fields will cause birefringence of the plane waves.
- The Green's function will again contain the homogeneous solution as a function of the source location s.



Birefringence of homogeneous solution



Required parameters for magnetic neutron scattering

- Magnetic materials for layers and/or particles
- Beam polarization
- Detector polarization analysis

Magnetic materials

- Magnetic materials are defined by their magnetization in A/m.
- The external guide field is a parameter of the multilayer and is also expressed in A/m.

Beam polarization

 A spin 1/2 particle's state is fully determined by its density matrix, which is positive semidefinite, Hermitian, trace 1:

$$\hat{\rho} = \sum_{j} p_{j} |\psi_{j}\rangle\langle\psi_{j}|$$

The density matrix can be defined by its Bloch vector a:

$$\hat{\rho} = \frac{1}{2} \left(I + \sigma \cdot \mathbf{a} \right)$$

with $|\mathbf{a}| \leq 1$.

Polarization analysis

- Orientation of polarization analysis: unit vector û.
- Transmission ratios of up and down components: T_+ and T_- .
- Efficiency:

$$P_{\text{eff}} = \frac{T_+ - T_-}{T_+ + T_-}$$

Total transmission:

$$T_{total} = \frac{T_+ + T_-}{2}$$