$$A = \left(\frac{\partial p}{\partial \varrho}\right)_T, \quad B = \left(\frac{\partial p}{\partial T}\right)_\varrho, \quad C = \left(\frac{\partial s}{\partial \varrho}\right)_T, \quad D = \left(\frac{\partial s}{\partial T}\right)_\varrho \tag{1}$$

$$\left(\frac{\partial p}{\partial \varrho}\right)_{s} = \left(\frac{\partial p}{\partial \varrho}\right)_{T} - \left(\frac{\partial p}{\partial T}\right)_{\varrho} \left(\frac{\partial s}{\partial \varrho}\right)_{T} / \left(\frac{\partial s}{\partial T}\right)_{\varrho} = A - \frac{B \cdot C}{D}$$

$$(2)$$

$$\left(\frac{\partial^2 p}{\partial \varrho^2}\right)_s = \left(\frac{\partial A}{\partial \varrho}\right)_s - \frac{\left(\frac{\partial B}{\partial \varrho}\right)_s CD + B\left(\frac{\partial C}{\partial \varrho}\right)_s D - BC\left(\frac{\partial D}{\partial \varrho}\right)_s}{D^2}$$
 (3)

$$= \left(\frac{\partial A}{\partial \varrho}\right)_s - \left(\frac{\partial B}{\partial \varrho}\right)_s \frac{C}{D} - \left(\frac{\partial C}{\partial \varrho}\right)_s \frac{B}{D} + \left(\frac{\partial D}{\partial \varrho}\right)_s \frac{BC}{D^2} \tag{4}$$

$$\left( \frac{\partial A}{\partial \varrho} \right)_s = \left( \frac{\partial^2 p}{\partial \varrho^2} \right)_T - \left( \frac{\partial^2 p}{\partial T \partial \varrho} \right) \left( \frac{\partial s}{\partial \varrho} \right)_T \bigg/ \left( \frac{\partial s}{\partial T} \right)_\varrho$$
 (5)

$$\left(\frac{\partial B}{\partial \varrho}\right)_{s} = \left(\frac{\partial^{2} p}{\partial T \partial \varrho}\right) - \left(\frac{\partial^{2} p}{\partial T^{2}}\right)_{\varrho} \left(\frac{\partial s}{\partial \varrho}\right)_{T} / \left(\frac{\partial s}{\partial T}\right)_{\varrho} \tag{6}$$

$$\left(\frac{\partial C}{\partial \varrho}\right)_{s} = \left(\frac{\partial^{2} s}{\partial \varrho^{2}}\right)_{T} - \left(\frac{\partial^{2} s}{\partial T \partial \varrho}\right) \left(\frac{\partial s}{\partial \varrho}\right)_{T} / \left(\frac{\partial s}{\partial T}\right)_{\varrho} \tag{7}$$

$$\left(\frac{\partial D}{\partial \varrho}\right)_{s} = \left(\frac{\partial^{2} s}{\partial T \partial \varrho}\right) - \left(\frac{\partial^{2} s}{\partial T^{2}}\right)_{\varrho} \left(\frac{\partial s}{\partial \varrho}\right)_{T} / \left(\frac{\partial s}{\partial T}\right)_{\varrho} \tag{8}$$

$$\begin{split} &\left(\frac{\partial^{2}p}{\partial\varrho^{2}}\right)_{s} = \left(\frac{\partial^{2}p}{\partial\varrho^{2}}\right)_{T} + \left[\left(\frac{\partial p}{\partial T}\right)_{\varrho} \left(\frac{\partial s}{\partial\varrho}\right)_{T}^{2} \left(\frac{\partial^{2}s}{\partial T^{2}}\right)_{\varrho}\right] \middle/ \left(\frac{\partial s}{\partial T}\right)_{\varrho}^{3} \\ &- \left[\left(\frac{\partial^{2}p}{\partial T^{2}}\right)_{\varrho} \left(\frac{\partial s}{\partial\varrho}\right)_{T}^{2} + \left(\frac{\partial p}{\partial T}\right)_{\varrho} \left(\frac{\partial s}{\partial\varrho}\right)_{T} \left(\frac{\partial^{2}s}{\partial T\partial\varrho}\right) + \left(\frac{\partial p}{\partial T}\right)_{\varrho} \left(\frac{\partial s}{\partial\varrho}\right)_{T} \left(\frac{\partial^{2}s}{\partial T\partial\varrho}\right)\right] \middle/ \left(\frac{\partial s}{\partial T}\right)_{\varrho}^{2} \\ &- \left[\left(\frac{\partial^{2}p}{\partial T\partial\varrho}\right) \left(\frac{\partial s}{\partial\varrho}\right)_{T} + \left(\frac{\partial p}{\partial T}\right)_{\varrho} \left(\frac{\partial^{2}s}{\partial\varrho^{2}}\right)_{T} + \left(\frac{\partial^{2}p}{\partial T\partial\varrho}\right) \left(\frac{\partial s}{\partial\varrho}\right)_{T}\right] \middle/ \left(\frac{\partial s}{\partial T}\right)_{\varrho} \end{split}$$

(9)