Domain a all values of type a list Property P(12): for any value 12 of type int list, Sum (apped 11/2) = Som 11+Sum 12 Induction Order: R(11,12): llisa stret softix of 12. Partinon: E[]3, Ex: 11 x is unlie of type a and lisa valued type 15th IH: Sum (append 11 12) = Sum 11 + Sum 12 Case 13 1=[] Sum (append [] 12) = Sum (12) = 0+ Sum (12) = Sum (12) + Sum (12) Case 2: 11 = X:: (1' in Sum(append 11 (2) =)
Sim (append (X:: (1') (2) = Sum(X:: append (11'. (2)) = X + Sum (append (11 /21) BY the IH-3 = X + Sum 11 + Sum 12 # the return Statement for the Call Sum (X:: l1') = X + 3um l7' = Sum (X:: 11) + Sum 12 13.2 Domain: all values of type a list of Property: For any value X of type int list, mapf (snowlx) = snow (mapfelfx)
Induction order: Bll, X) Il is astrict suffix of X Partition: E[13, 84: 11 x is a value of type available of type alist IH: map f (snoc (x) = snoc (map fl) (fx) Vase 1: L=E] mapf(snoc[]x)= mapf(cx)=fx= snoc([])(fx) = Snoc (mapfe) (fx) Wee 2: 1 = 3 h: ! } map f (Snoc {h:: l'} x) = map f (h:: Snoc l'x = fh: mapf (snocl'x) BY the IH -> = fh : snoc (map fl') (fx) = 2000 (4 p. s. map EF) (F. X) = Snoc (map f & h :: + 3) (FX)

Thin 6: Fix an Oland type a for any occasil value los type a list, we have reverse la reverse la Romain: all values of type a list Property P(1): for any value & of type a list, Powerse 1 = newser 21 Order BULLO: 11 is a Street Suffix of 1/2 Partition: [C] [his a value of type a list & a value of type a list } Case 1: 2=[] Peverse [] = [] = reverse 2 [] lase 1: l= Eh ": st? prove: Peverse 2 2 hists G=append (reverse h::+)[] > by lemma 2 = rev_append h:: + [] > by +nm5 = Pewse 2 hist Lemma 2: Fix an Ocaml type a for any Ocaml value lof type a list and any value hof type a for append (revose l) [] = revesse l Domain's all values lot type a list Property PUL): append (revese () [] = reverse l Order All1, 12): 11 is a Strict suffix of 12 Partition & E[]3, Eh of I his a value of type a lisavament type alists Case 1: l=C7 prove, appoind (reverse []) [] = reverse [] S=append [][] = [] = reverse [] Case Lil= Thists prove: append (reverse hi:t)[] = reverse hiit G=append (snoc (rawse t) K) [] = Snoc (reverse t) ho: E] = Snac (Reverso t) h