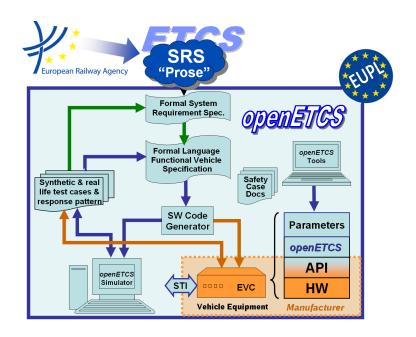


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Work-Package 7: "Toolchain"

Event-B Model of Subset 026, Section 3.13

Matthias Güdemann June 2013



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OETCS June 2013

Event-B Model of Subset 026, Section 3.13

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Model Description

Prepared for openETCS@ITEA2 Project

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This document describes a formal model of the requirements of section 3.13 of the subset 026 of the ETCS specification 3.3.0 [Eur12]. This section describes the speed and distance monitoring subsystem of ETCS.

The model is expressed in the formal language Event-B [Abr10] and developed within the Rodin tool [Jas12]. This formalism allows an iterative modeling approach. In general, one starts with a very abstract description of the basic functionality and step-wise adds additional details until the desired level of accuracy of the model is reached. Rodin provides the necessary proof support to ensure the correctness of the refined behavior.

In this document we present an Event-B model of the speed and distance monitoring subsystem of ETCS. At first, we describe shortly the background of Event-B, then the overall approach taken to model this section and finally present the model in detail.

The section 3.13 of the SRS gives a very detailed description of the calculation of many necessary values for speed and distance monitoring. As Event-B is a system modeling approach, we give an abstract model of the system. The calculations are abstracted as functions and the system ensures the correct parameter flow to the functions. We illustrate the model decomposition capabilities of Event-B and Rodin by decomposing the overall model into different functional parts.

For a short introduction on Event-B and the usage of Rodin with models on github see https://github.com/openETCS/model-evaluation/blob/master/model/B-Systerel/Event_B/rodin-projects-github.pdf?raw=true

1 Modeling Strategy

The section 3.13 of the SRS describes the speed and distance monitoring together with the necessary parameters and data. The model starts with an abstract modeling of dataflow of the various intermediate calculated values. This model is partitioned into functional parts, the model is decomposed using shared variables and the respective sub-models are refined until the basic calculation functions are reached.

2 Model Overview

The overview of the speed and distance monitoring is shown in Fig. 1 from the SRS.

The on-board system comprises only the middle layer. The upper layer gives train related inputs as parameters, the lower layer track related inputs. The system itself takes the current position, speed and acceleration of the train and computes commands for the train interface and for the driver machine interface. For the train interface, this consists of the command for the service and emergency brakes. For the driver machine interface this consists of the status indication for the driver.

The Event-B modeling starts with machines describing the dataflow of all inputs, outputs and intermediate values of the model. For example, the values that are calculated for $T_brake_service$ in $Traction/Braking\ Models$ are written into a variable by an event that calculates them and these values are then read as input by the event that calculates T_bs for SBI limit.

This approach is conducted for each intermediate value of the system until a single machine is created with one variable for each intermediate value as well as for each input and output. On

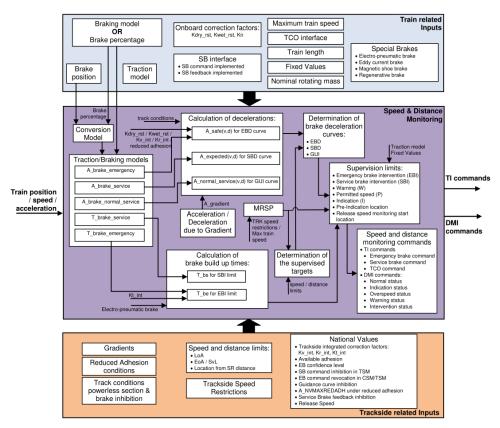


Figure 1. Speed and Distance Monitoring Overview ([Eur12] p. 85)

this level of modeling, all events only define the necessary input values and write a new value to their output variable. This value is provided as event parameter on this abstraction level.

The next step is to decompose the single machine into different sub-machines, in general one machine for each functional part of the model. This allows for model structuring and complexity reduction for each machine. For this we use the Rodin decomposition plug-in ¹ using the shared-variable decomposition approach [SPHB11]. This approach splits the set of events of a machine into several disjoint sets and assigns one such set to each sub-machine. It also allows to distribute the variables over several machines, effectively implementing a shared variable distributed system.

The borders for the subsystem decomposition are shown in Fig. 2. The dashed lines show the separate sub-machines. The dataflows that cross these lines are represented by the shared variables of the decomposed model.

Each of the sub-machines with its shared variables is then further refined until the desired level of detail is reached. The overview of these refinements is shown in Fig. 3.

This refinement and context overview is very different from the others, as first an abstract global model was developed and then this model was decomposed into sub-models which are further refined. The contexts are shared between the decomposed models as far as possible. In this case, all resulting contexts and machines are kept in the same Rodin project. It is also possible to create a new project for each sub-machine which will reduce the complexity of each single project.

 $^{{}^{1}}http://wiki.event-b.org/index.php/Decomposition_Plug-in_User_Guide$

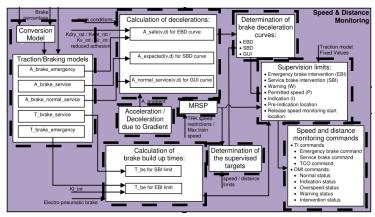


Figure 2. Decomposition of System

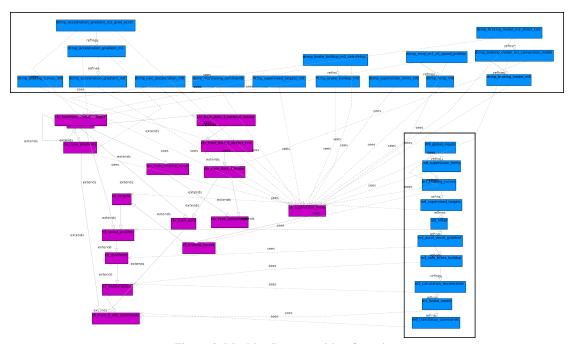


Figure 3. Machine Decomposition Overview

The global model is shown in the lower right. The first machine describes the global input and output variables of the system. The further refinements represent the iterative addition of more functions as shown in Fig. 2. For example the machine 1 adds the brake model with its inputs and outputs and the machine 2 adds the calculation of deceleration which uses the outputs of the braking model.

The last machine is then decomposed into the nine machines representing each a single functional block. This structure is shown in the upper part of Fig. 3, this also illustrates the further independent refinement of the decomposed sub-machine.

The context hierarchy also reflects this structuring. The contexts define the data types for the intermediate values, as well as the functions that calculate these values. These functions are generally not further refined in the Event-B model, as this is not part of the system modeling.

3 Model Benefits

The modeled section of the SRS provides many details for calculation of various values. The main content from a system modeling point of view is the model. So while in this case the same benefits from using Rodin as for [Mat13a, Mat13b, Mat13c] are present, the main advantage here is the model structuring facility.

• Model Decomposition The shared variable model decomposition [SPHB11] allows for decomposing an Event-B model and for separate refining of the machines of the resulting sub-models while retaining correctness of the refinement proofs.

It should be noted that this section contains mainly very specific implementation details and no general requirements. Currently, the proof support for non-linear arithmetic (in particular for floating point numbers) is limited in Rodin, so the modeling contains mainly the system level. It describes in particular the decomposition of the model, the various inputs and outputs of the different model components and the refinement stops when the functional level is reached. This means that for calculations, the last refinement level in general describes a function with the required input and output value and correct types.

4 Detailed Model Description

4.1 Context 0 - Train Inputs, TI and DMI command

The first context introduces many basic type for the model, *t_locations*, *t_speed*, *t_acceleration*, *t_TI_commands*, *t_DMI_commands*, *t_time* and *t_train_modes*.

The commands for the train interface (TI) are represented by the constants $c_emergency_brake$, $c_service_brake$, c_TCO , $c_no_command$. For the driver machine interface (DMI) the commands are represented by the constants c_normal , $c_indication$, $c_overspeed$, $c_warning$ and $c_intervention$.

The other constants provide default values for the initialization of variables of that type.

```
CONTEXT c0_train_ti_dmi_commands
SETS
     t_locations all possible locations on track
     t_speed train speed measurement
     t_acceleration train acceleration
     t_TI_commands track interface commands
     t_DMI_commands driver machine interface commands
     t time
     t_train_modes
CONSTANTS
     c_emergency_brake
     c_service_brake
     c_TCO traction cut off
     c_no_command empty command
     c_normal
     c\_indication
     c_overspeed
```

```
c_warning
      c\_intervention
      c\_v0
      c_a0
      c_l0
      c_a_brake0
      c\_T\_brake0
AXIOMS
        axm1: partition(t\_TI\_commands, \{c\_no\_command\}, \{c\_emergency\_brake\},
                \{c\_service\_brake\}, \{c\_TCO\})
        axm2: partition(t\_DMI\_commands, \{c\_normal\}, \{c\_indication\},
                \{c\_overspeed\}, \{c\_warning\}, \{c\_intervention\})
        axm3 : c_v0 \in t\_speed
        axm4 : c_a0 \in t_acceleration
        axm5 : c_l0 \in t_locations
        axm6 : c\_a\_brake0 \in t\_speed \rightarrow t\_acceleration
                       default brake profile
        axm7 : c_T_brake0 \in t_time
                       default brake buildup time
```

END

4.2 Machine 0 - Train Status and Commands

This first machine introduces the external input variables, i.e., the position, speed and acceleration of the train as well as the output variables, i.e., the TI commands and the DMI commands. The input variables are read by the event *update_train_style* and the output variables by the event *new_outputs*.

```
MACHINE m0_trainstatus_commands
SEES c0_train_ti_dmi_commands
VARIABLES
     v_current current speed of train
     a_current current acceleration of train
     loc_current current position of train as track location
     status current current DMI status
INVARIANTS
      inv1 : v\_current \in t\_speed
      inv2: a\_current \in t\_acceleration
      inv3 : loc\_current \in t\_locations
      inv4: cmd\_current \in t\_TI\_commands
      inv5: status\_current \in t\_DMI\_commands
EVENTS
Initialisation
   begin
            act1 : v\_current := c\_v0
            act2 : a\_current := c\_a0
            act3 : loc\_current := c\_l0
            act4 : cmd\_current := c\_no\_command
            act5 : status\_current := c\_normal
```

```
end
Event update_train_state \widehat{=}
    any
            l\_speed
            l\_accel
            l\_loc
    where
              grd1: l\_speed \in t\_speed
              grd2: l\_accel \in t\_acceleration
              grd3: l\_loc \in t\_locations
    then
              act1 : v\_current := l\_speed
              act2 : a\_current := l\_accel
              act3 : loc\_current := l\_loc
    end
Event new\_outputs =
    any
            l_ti_cmd
            l_dmi_status
    where
              grd1: l\_ti\_cmd \in t\_TI\_commands
              grd2: l\_dmi\_status \in t\_DMI\_commands
    then
              act1 : cmd\_current := l\_ti\_cmd
              act2 : status\_current := l\_dmi\_status
    end
END
```

4.3 Machine 1 - Brake Model

The first refinement adds the notion of the brake model. This is represented by the variables describing the speed dependent acceleration functions for emergency, service and normal service braking. The variables $T_brake_service$ and $T_brake_emergency$ describe the brake build-up times for the brakes.

```
MACHINE m1_brake_model
REFINES m0_trainstatus_commands
SEES c0_train_ti_dmi_commands
VARIABLES
     A_brake_emergency emergency brake acceleration
     A_brake_service service brake acceleration
     A\_brake\_normal\_service
     T_brake_service
     T_brake_emergency
EVENTS
Event set\_A\_brake\_emergency =
   any
           l_a_brake
    where
            grd1: l\_a\_brake \in t\_speed \rightarrow t\_acceleration
   then
            act1 : A\_brake\_emergency := l\_a\_brake
   end
Event set_A_brake_service =
```

```
any
             l_a_brake
    where
              grd1: l\_a\_brake \in t\_speed \rightarrow t\_acceleration
    then
              act1 : A\_brake\_service := l\_a\_brake
    end
Event set\_A\_brake\_normal\_service =
    any
            l\_a\_brake
    where
              grd1: l\_a\_brake \in t\_speed \rightarrow t\_acceleration
    then
              act1 : A\_brake\_normal\_service := l\_a\_brake
    end
Event set\_T\_brake\_service =
    any
            l\_T\_brake
    where
              \mathbf{grd1} : l\_T\_brake \in t\_time
    then
              act1 : T_brake_service := l_T_brake
    end
Event set\_T\_brake\_emergency =
    any
            l\_T\_brake
    where
              grd1: l\_T\_brake \in t\_time
    then
              act1 : T\_brake\_emergency := l\_T\_brake
    end
END
```

4.4 Context 1 - Decelerations

This context extension adds a distance type and a function that maps the speed and distance to an acceleration.

```
CONTEXT c1_decelerations

EXTENDS c0_train_ti_dmi_commands

SETS

t\_distance

CONSTANTS

f\_A\_deceleration0

AXIOMS

axm1: f\_A\_deceleration0 \in t\_speed \times t\_distance \rightarrow t\_acceleration

END
```

4.5 Machine 2 - Calculate Decelerations

This refinement adds the calculation of deceleration to the model. This is represented by three variables which are functions that map speed and distance to an acceleration. There is one function for each on of EBD, SBD and GUI.

```
MACHINE m2_calculation_deceleration
REFINES m1_brake_model
SEES c1_decelerations
VARIABLES
      A\_safe
      A_{expected}
      A_normal_service
EVENTS
Event set\_A\_safe =
    any
             l_a_decel
    where
               grd1: l\_a\_decel \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd2: A\_brake\_emergency \in t\_speed \rightarrow t\_acceleration
    then
               act1 : A\_safe := l\_a\_decel
    end
Event set\_A\_expected =
    anv
             l_a_decel
    where
               grd1: l\_a\_decel \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd2 : A\_brake\_service \in t\_speed \rightarrow t\_acceleration
    then
               act1 : A\_expected := l\_a\_decel
    end
Event set\_A\_normal\_service =
    any
             l\_a\_decel
    where
               grd1: l\_a\_decel \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd2: A\_brake\_normal\_service \in t\_speed \rightarrow t\_acceleration
    then
               act1 : A\_normal\_service := l\_a\_decel
    end
END
```

4.6 Machine 3 - Calculation of Brake Buildup Time

The next machine refinement adds the brake buildup calculation to the model. This is represented by two variables, T_be for the emergency brake and T_se for the service brake.

```
MACHINE m3_safe_brake_buildup
REFINES m2_calculation_deceleration
SEES c1_decelerations
VARIABLES

T_be
```

```
T_bs
EVENTS
Event set\_T\_be =
    any
            l\_t\_be
    where
             grd1: l\_t\_be \in t\_time
              grd2: T\_brake\_emergency \in t\_time
    then
              act1 : T\_be := l\_t\_be
    end
Event set\_T\_bs =
    any
            l_t_bs
    where
              grd1: l\_t\_bs \in t\_time
              grd2: T\_brake\_service \in t\_time
    then
             act1 : T_bs := l_t_bs
    end
END
```

4.7 Machine 4 - Acceleration due to Gradient

The refinement adds the notion of the acceleration due to gradient. This is represented by the variable $A_gradient$ which is a function that maps speed to acceleration.

```
MACHINE m4_accel_decel_gradient

REFINES m3_safe_brake_buildup

SEES c2_gradients

VARIABLES

A_gradient

EVENTS

Event set_A_gradient 
any

l_a_gradient

where

grd1:l_a_gradient ∈ t_acceleration
then

act1:A_gradient := l_a_gradient
end

END
```

4.8 Context 3 - Speed Profiles

This context extension introduces the type *speed_profiles* which maps locations to speeds. It also defines one constant value of that type which is used as default value for variables of that type.

```
CONTEXT c3_speed_profiles

EXTENDS c2_gradients

CONSTANTS

c_speed_profile0
```

```
t\_speed\_profiles
AXIOMS
axm1 : t\_speed\_profiles \subseteq t\_locations \times t\_speed
axm2 : c\_speed\_profile0 \in t\_speed\_profiles
END
```

4.9 Machine 5 - Most Restrictive Speed Profile

This machine refinement introduces the most restrictive speed profile to the model. This is represented by the variable *MRSP* of the type *speed_profile*.

```
MACHINE m5_MRSP
REFINES m4_accel_decel_gradient
SEES c3_speed_profiles
VARIABLES

MRS P
EVENTS
Event set_MRSP =
any

l_sp
where

grd1 : l_sp ∈ t_speed_profiles
then

act1 : MRS P := l_sp
end
END
```

4.10 Context 4 - Targets

This context extension introduces the type $t_targets$ which represents a target, i.e., a pair of location and speed.

```
CONTEXT c4_targets

EXTENDS c3_speed_profiles

CONSTANTS

t\_targets
c\_target0

AXIOMS

axm1 : t\_targets \subseteq t\_locations \times t\_speed

axm2 : c\_target0 \in t\_targets

END
```

4.11 Machine 6 - Supervised Targets

This refinement adds limit of authority, end of authority and supervision limit to the model. For each there exists one variable of type $t_targets$.

```
MACHINE m6_supervised_targets REFINES m5_MRSP
```

```
SEES c4_targets
VARIABLES
     LOA
     EOA
     SvL
EVENTS
Event set\_EOA \cong
    any
           l_target
    where
             grd1: l\_target \in t\_targets
             grd2 : MRSP \in t\_speed\_profiles
    then
             act1 : EOA := l\_target
    end
Event set\_LOA =
    any
           l_target
    where
             grd1: l\_target \in t\_targets
             grd2 : MRSP \in t\_speed\_profiles
    then
             act1 : LOA := l\_target
    end
Event set\_SvL \cong
    any
           l_target
    where
             grd1: l\_target \in t\_targets
             grd2 : MRSP \in t\_speed\_profiles
    then
             act1 : SvL := l\_target
    end
END
```

4.12 Context 5 - Braking Curves

This context extension introduces the type *t_braking_curves* and a constant of that type.

```
CONTEXT c5_braking_curves
EXTENDS c4_targets
SETS

t_braking\_curves
CONSTANTS

c_curve0
AXIOMS

axm1 : c_curve0 \in t_braking\_curves
END
```

4.13 Machine 7 - Braking Curves

This machine refinement adds the braking curves to the model, these are represented by the three variables *EBD*, *SBD* and *GUI* of the appropriate type.

```
MACHINE m7_braking_curves
REFINES m6_supervised_targets
SEES c5_braking_curves
VARIABLES
      EBD
      SBD
      GUI
EVENTS
Event set\_EBD =
    any
             l_curve
    where
               grd1: l\_curve \in t\_braking\_curves
               grd2: A\_safe \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd3: A\_expected \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd4: A\_normal\_service \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd5 : LOA \in t\_targets
               grd6 : EOA \in t\_targets
               grd7 : SvL \in t\_targets
    then
               act1 : EBD := l\_curve
    end
Event set\_SBD \cong
    any
             l_curve
    where
               grd1: l\_curve \in t\_braking\_curves
               grd2: A\_safe \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd3: A\_expected \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd4: A\_normal\_service \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd5 : LOA \in t\_targets
               grd6 : EOA \in t\_targets
               grd7 : SvL \in t\_targets
    then
               act1 : SBD := l\_curve
Event set\_GUI \cong
    any
             l_curve
    where
               grd1: l\_curve \in t\_braking\_curves
               grd2: A\_safe \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd3: A\_expected \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd4: A\_normal\_service \in t\_speed \times t\_distance \rightarrow t\_acceleration
               grd5 : LOA \in t\_targets
               grd6 : EOA \in t\_targets
               grd7 : SvL \in t\_targets
    then
               act1 : GUI := l\_curve
    end
END
```

4.14 Context 6 - Supervision Limits

This context adds the type $t_supervision_limits$ to the model, as well as a constant value of that type.

```
CONTEXT c6_supervision_limits
EXTENDS c5_braking_curves
SETS

t_supervision_limits
CONSTANTS

c_slimit0

AXIOMS

axm1 : c_slimit0 ∈ t_supervision_limits
END
```

4.15 Machine 8 - Supervision Limit

This machine refinement adds the supervision limits to the model, emergency brake intervention (*EBI*), service brake intervention (*SBI*), warning limit (*warning_limit*), permitted speed (*P_limit*), indication limit (*I_limit*), pre-indication location (*PI_limit*) and the release start speed monitoring location (*RSM_start*).

```
MACHINE m8 supervision limits
REFINES m7_braking_curves
SEES c6_supervision_limits
VARIABLES
     EBI emergency brake intervention
     SBI service brake intervention
     W_limit warning limit
     P_limit permitted speed
     I_limit indication limit
     PIl pre-indication_location
     RS M_start release speed monitoring start location
EVENTS
Event set\_EBI =
    anv
           l_limit
    where
             grd1: l\_limit \in t\_supervision\_limits
             grd2 : MRSP \in t\_speed\_profiles
             grd3 : EBD \in t\_braking\_curves
             grd4 : SBD \in t\_braking\_curves
             grd5 : GUI \in t\_braking\_curves
             grd6: T\_bs \in t\_time
             grd7: T\_be \in t\_time
    then
             act1 : EBI := l\_limit
    end
Event set\_SBI \cong
    any
           l_limit
    where
```

```
grd1: l\_limit \in t\_supervision\_limits
              grd2 : MRSP \in t\_speed\_profiles
              grd3 : EBD \in t\_braking\_curves
              grd4 : SBD \in t\_braking\_curves
              grd5 : GUI \in t\_braking\_curves
              grd6: T\_bs \in t\_time
              grd7: T\_be \in t\_time
    then
              act1 : SBI := l\_limit
    end
Event set_W_{limit} =
    any
            l_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
              grd2 : MRSP \in t\_speed\_profiles
              grd3 : EBD \in t\_braking\_curves
              grd4 : SBD \in t\_braking\_curves
              grd5 : GUI \in t\_braking\_curves
              grd6: T\_bs \in t\_time
              grd7: T\_be \in t\_time
    then
              act1 : W_{limit} := l_{limit}
    end
Event set_I_limit =
    any
            l\_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
              grd2 : MRSP \in t\_speed\_profiles
              grd3 : EBD \in t\_braking\_curves
              grd4 : SBD \in t\_braking\_curves
              grd5 : GUI \in t\_braking\_curves
              grd6: T\_bs \in t\_time
              grd7: T\_be \in t\_time
    then
              act1 : I\_limit := l\_limit
    end
Event set_P_{limit} =
    any
            l\_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
              grd2 : MRSP \in t\_speed\_profiles
              grd3 : EBD \in t\_braking\_curves
              grd4 : SBD \in t\_braking\_curves
              grd5 : GUI \in t\_braking\_curves
              grd6: T\_bs \in t\_time
              grd7: T\_be \in t\_time
    then
              act1 : P\_limit := l\_limit
    end
Event set\_PIl\_limit =
    any
            l\_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
              grd2 : MRSP \in t\_speed\_profiles
```

```
grd3 : EBD \in t\_braking\_curves
              grd4 : SBD \in t\_braking\_curves
              grd5 : GUI \in t\_braking\_curves
              grd6: T\_bs \in t\_time
              grd7: T\_be \in t\_time
    then
              act1 : PIl := l\_limit
    end
Event set\_RSM\_start\_limit =
            l_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
              grd2 : MRSP \in t\_speed\_profiles
              grd3 : EBD \in t\_braking\_curves
              grd4 : SBD \in t\_braking\_curves
              grd5 : GUI \in t\_braking\_curves
              grd6: T\_bs \in t\_time
              grd7: T\_be \in t\_time
    then
              act1 : RSM\_start := l\_limit
    end
END
```

5 Model Decomposition

The decomposition strategy chosen for this model is "A-style" (for Abrial) which means shared variable decomposition [SPHB11]. In this case the events of an Event-B machine are separated into *n* disjoint sets. Each of these sets represents one decomposed sub-machine. Variables can be shared between machines, if they are read / written by them. In this case-study, all events that write a single variable are in one machine, events that read this variable are in another machine. Only the sub-machine in which a variable is written can do data-refinement on these variables, in the other machines, these variables are marked as shared and cannot be refined.

For the model decomposition, an additional refinement of the model is necessary. The machine m9 does not really add detail to the refined machine m8. The only changes are that the variables which are read by an event are explicitly added to the conditions by specifying a typing condition for them. This assures that the model decomposition preserves these necessary variables in the sub-machines and only removes the unneeded ones.

The overview of the decomposition in the Rodin tool using the decomposition plug-in is shown in Fig. 4. It lists the decomposed machine, the decomposition style, the sub-components and the events in each sub-machine (only shown for a single one).

In the following sections, the sub-components, their respective refinement and the required context definitions will be explained.

5.1 dcmp - Braking Model

The braking model has the following input variables: *a_current*, *v_current* and *loc_current*. These variables are written by the event *update_train_state*. The variables and this event are marked as "DO NOT REFINE", i.e., they are shared variables and an external event.

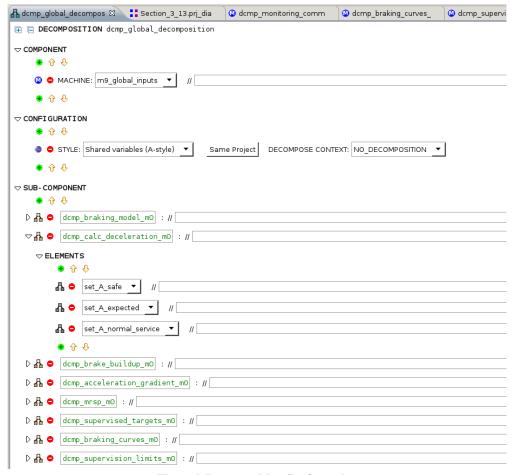


Figure 4. Decomposition Configuration

The output variables are $T_brake_service$, $T_brake_emergency$, $A_brake_normal_service$, $A_brake_service$ and $A_brake_emergency$.

```
MACHINE dcmp_braking_model_m0
SEES c6_supervision_limits
VARIABLES
     A_brake_normal_service Private variable
     A_brake_service Private variable
     a_current Shared variable, DO NOT REFINE
     v_current Shared variable, DO NOT REFINE
     T_brake_service Shared variable, DO NOT REFINE
     A_brake_emergency Private variable
     loc_current Shared variable, DO NOT REFINE
     T_brake_emergency Shared variable, DO NOT REFINE
EVENTS
Event update\_train\_state =
                                 External event, DO NOT REFINE
   anv
           l\_speed
           l\_accel
          l\_loc
    where
            grd1: l\_speed \in t\_speed
            grd2: l\_accel \in t\_acceleration
            grd3: l\_loc \in t\_locations
```

```
then
              act1 : v\_current := l\_speed
              act2 : a\_current := l\_accel
              act3 : loc\_current := l\_loc
Event set\_A\_brake\_emergency \widehat{=}
    anv
             l_a_brake
    where
              grd1: l\_a\_brake \in t\_speed \rightarrow t\_acceleration
    then
              act1 : A\_brake\_emergency := l\_a\_brake
    end
Event set\_A\_brake\_service =
            l_a_brake
    where
              grd1: l\_a\_brake \in t\_speed \rightarrow t\_acceleration
    then
              act1 : A\_brake\_service := l\_a\_brake
    end
Event set\_A\_brake\_normal\_service \widehat{=}
    any
             l\_a\_brake
    where
              grd1: l\_a\_brake \in t\_speed \rightarrow t\_acceleration
    then
              act1 : A_brake_normal_service := l_a_brake
    end
Event set_T_brake_service =
    any
            l\_T\_brake
    where
              grd1: l\_T\_brake \in t\_time
    then
              act1 : T\_brake\_service := l\_T\_brake
    end
Event set\_T\_brake\_emergency =
    any
            l\_T\_brake
    where
              grd1: l\_T\_brake \in t\_time
    then
              act1: T\_brake\_emergency := l\_T\_brake
    end
END
```

5.1.1 Context - Train Data 1 Brake

This context introduces the type *t_brake_percentage* and a function that takes the train speed, the brake percentage, the train length and the brake position as arguments and returns a Boolean value indicating whether the conversion model is applicable. It also introduces functions that calculate the conversion model for the emergency and for the service brake, as well as the conversion model for the brake buildup time of the service and emergency brake.

On the system level description of this Event-B model, these functions are not implemented in more detail. Their specification and implementation details can be found in §3.13.3 of the SRS.

```
CONTEXT ctx_train_data_1_brake
EXTENDS ctx_train_data
SETS
      t_brake_position
CONSTANTS
      t_brake_percentage
      c_brake_percentage0
      f_conversion_model_applicable
      f_conversion_model_A_emergency
      f_conversion_model_A_service
      f_conversion_model_T_brake_service
      f\_conversion\_model\_T\_brake\_emergency
AXIOMS
        axm1: t\_brake\_percentage \subseteq t\_percentage
        \verb"axm2": c\_brake\_percentage" 0 \in t\_brake\_percentage
        axm3: f\_conversion\_model\_applicable \in t\_speed \times t\_brake\_percentage \times t\_length \times t\_brake\_position \rightarrow BOOL
                        cf. 3.13.3.2.1
        axm4: f\_conversion\_model\_A\_emergency \in t\_brake\_percentage \rightarrow (t\_speed \rightarrow t\_acceleration)
                        cf. 3.13.3.3
        axm5: f\_conversion\_model\_A\_service \in t\_brake\_percentage \rightarrow (t\_speed \rightarrow t\_acceleration)
        axm6: f\_conversion\_model\_T\_brake\_service \in t\_brake\_position \times t\_length \times t\_speed \rightarrow t\_time
                        cf. 3.13.3.4
        axm7: f\_conversion\_model\_T\_brake\_emergency \in t\_brake\_position \times t\_length \times t\_speed \rightarrow t\_time
END
```

5.1.2 dcmp - Braking Model Conversion Model

In the first refinement of the sub-machine adds the variables <code>brake_percentage</code> of type brake percentage and <code>brake_percentage_via_train_data</code> of Boolean type. These variables are modified by the event <code>specify_brake_percentage</code> and <code>remove_brake_percentage_data</code>. The Boolean variable signals the specification of the brake percentage via train data.

The value of the brake percentage is used in some events to compute concrete values for the conversion model instead of using an event parameter. For example in the event $calc_A_brake_emergency_conversion_model$, the function $f_conversion_model_A_emergency$ is used with the value of $brake_percentage$ to compute the conversion model. This replaces the event parameter l_a_brake by defining a witness for it.

```
refines set_A_brake_emergency
                                            l_brake_position
                where
                                                 grd2 : brake_percentage_via_train_data = TRUE
                                                 grd3: f\_conversion\_model\_applicable(c\_train\_max\_speed \mapsto brake\_percentage \mapsto c\_train\_length \mapsto
                                            l\_brake\_position) = TRUE
                                                  grd4: l\_brake\_position \in t\_brake\_position
                with
                                                 1_a_brake : l_a_brake = f_conversion_model_A_emergency(brake_percentage)
               then
                                                  act1: A\_brake\_emergency := f\_conversion\_model\_A\_emergency(brake\_percentage)
               end
Event calc\_A\_brake\_service\_conversion\_model =
refines set_A_brake_service
               any
                                            l_brake_position
                where
                                                  grd2 : brake_percentage_via_train_data = TRUE
                                                  grd3: f\_conversion\_model\_applicable(c\_train\_max\_speed \mapsto brake\_percentage \mapsto c\_train\_length \mapsto
                                            l\_brake\_position) = TRUE
                                                  grd4: l\_brake\_position \in t\_brake\_position
                with
                                                  l_a_brake : l_a_brake = f_conversion_model_A_service(brake_percentage)
               then
                                                  act1: A\_brake\_service := f\_conversion\_model\_A\_service(brake\_percentage)
               end
Event calc\_T\_brake\_service\_conversion\_model =
refines set_T_brake_service
               any
                                            l\_brake\_position
                                            l_target_speed
                where
                                                  grd2 : brake_percentage_via_train_data = TRUE
                                                  grd3: f\_conversion\_model\_applicable(c\_train\_max\_speed \mapsto brake\_percentage \mapsto c\_train\_length \mapsto
                                            l\_brake\_position) = TRUE
                                                  grd4: l\_brake\_position \in t\_brake\_position
                                                  grd5: l\_target\_speed \in t\_speed
                with
                                                  1_{T_brake} : l_{T_brake} = f_{conversion\_model\_T\_brake\_service}(l_brake\_position \mapsto c_{train\_length} \mapsto c_{
                                            l_target_speed)
               then
                                                  act1: T\_brake\_service := f\_conversion\_model\_T\_brake\_service(l\_brake\_position \mapsto c\_train\_length \mapsto
                                            l\_target\_speed)
               end
refines set_T_brake_emergency
               any
                                            l\_brake\_position
                                            l\_target\_speed
                where
                                                 grd1: brake\_percentage\_via\_train\_data = TRUE
                                                 {\tt grd2}: f\_conversion\_model\_applicable(c\_train\_max\_speed \ \mapsto \ brake\_percentage \ \mapsto \ c\_train\_length \ \mapsto \ c
                                            l\_brake\_position) = TRUE
                                                  grd3: l\_brake\_position \in t\_brake\_position
                                                  grd4: l\_target\_speed \in t\_speed
                with
                                                  1\_T\_brake : l\_T\_brake = f\_conversion\_model\_T\_brake\_emergency(l\_brake\_position \mapsto c\_train\_length \mapsto c\_train\_
                                            l_target_speed)
```

```
then
            act1 : T_brake\_emergency
                                                      f\_conversion\_model\_T\_brake\_emergency(l\_brake\_position
           c\_train\_length \mapsto l\_target\_speed)
Event specifiy\_brake\_percentage =
    anv
           l_brake
    where
             grd1: l\_brake \in t\_brake\_percentage
             grd2 : brake_percentage_via_train_data = FALSE
    then
             act1 : brake\_percentage := l\_brake
             act2 : brake_percentage_via_train_data := TRUE
    end
Event remove_brake_percentage_data =
    when
             grd1 : brake_percentage_via_train_data = TRUE
    then
             act1 : brake_percentage := c_brake_percentage0
             act2 : brake_percentage_via_train_data := FALSE
    end
END
```

5.1.3 Context - Train Data 2 Direct Calculation

The next context introduces the type representing the combination of the different brake types of the train. It also defines functions that calculate the braking models for different brake combinations for the service brake and the emergency brake, as well as functions to calculate the brake buildup time for the service and emergency brake with the brake combination as argument. It also defines a function that calculates the normal brake function dependent on the brake position and the acceleration constants c_SB01 and c_SB02 (cf. §3.13.2.2.3.1.10).

```
CONTEXT ctx_train_data_2_direct_calc
EXTENDS ctx_train_data_1_brake
SETS
      t_brake_combination cf. 3.13.2.2.3.1.7, i.e., combination of regenerative, eddy current and magnetic brake
CONSTANTS
      c v zero target speed zero
      f_calc_A_brake_service_direct
      f_calc_A_brake_emergency_direct
      f_calc_A_brake_normal_direct cf. 3.13.2.2.3.1.9
     c_SB01
      c_SB02
      f_calc_T_brake_service
      f_calc_T_brake_emergency
AXIOMS
       axm1 : c\_v\_zero \in t\_speed
       axm2: f\_calc\_A\_brake\_service\_direct \in t\_brake\_combination \rightarrow (t\_speed \rightarrow t\_acceleration)
       axm3: f\_calc\_A\_brake\_emergency\_direct \in t\_brake\_combination \rightarrow (t\_speed \rightarrow t\_acceleration)
       axm4: f\_calc\_A\_brake\_normal\_direct \in t\_brake\_position \times t\_acceleration \times t\_acceleration
                                                                    \rightarrow (t_speed \rightarrow t_acceleration)
                       cf. 3.13.2.2.3.1.10
                     the accelerations are the c_SB01 and c_SB02 constants
```

```
\begin{array}{l} \textbf{axm5} & : c\_SB01 \in t\_acceleration \\ \textbf{axm6} & : c\_SB02 \in t\_acceleration \\ \textbf{axm7} & : f\_calc\_T\_brake\_service \in t\_brake\_combination \rightarrow t\_time \\ \textbf{axm8} & : f\_calc\_T\_brake\_emergency \in t\_brake\_combination \rightarrow t\_time \\ \textbf{END} \end{array}
```

5.1.4 dcmp - Braking Model Direct Calculation

This machine refinement uses the brake combinations and the corresponding functions from the context to produce more concrete events. For events that compute a function mapping speed to acceleration, the functions of the context and the constants for SB01 and SB02 are used to eliminate the event parameters by providing witnesses for them.

```
MACHINE dcmp_braking_model_m2_direct_calc
REFINES dcmp_braking_model_m1_conversion_model
SEES c6_supervision_limits, ctx_train_data_2_direct_calc
EVENTS
Event calc_A_brake_emergency_direct \widehat{=}
refines set_A_brake_emergency
    anv
            l\_brake\_combination
    where
             grd1: l\_brake\_combination \in t\_brake\_combination
    with
             l_a_brake : l_a_brake = f_calc_A_brake_emergency_direct(l_brake_combination)
    then
             act1: A\_brake\_emergency := f\_calc\_A\_brake\_emergency\_direct(l\_brake\_combination)
    end
Event calc\_A\_brake\_service\_direct =
refines set_A_brake_service
    any
            l_brake_combination
    where
             grd2: l\_brake\_combination \in t\_brake\_combination
    with
             l_a_brake : l_a\_brake = f\_calc\_A\_brake\_service\_direct(l\_brake\_combination)
    then
             act1: A\_brake\_service := f\_calc\_A\_brake\_service\_direct(l\_brake\_combination)
    end
Event set_A_brake_normal_service =
refines set_A_brake_normal_service
    any
            l_brake_position
    where
             grd1: l\_brake\_position \in t\_brake\_position
    with
             1_a_brake : l_a_brake = f_calc_A_brake_normal_direct(l_brake_position \mapsto c_S B01 \mapsto c_S B02)
    then
             act1: A\_brake\_normal\_service := f\_calc\_A\_brake\_normal\_direct(l\_brake\_position \mapsto c\_SB01 \mapsto c\_SB02)
Event set_T_brake_service =
refines set_T_brake_service
    any
```

```
l\_brake\_combination
    where
             grd1: l\_brake\_combination \in t\_brake\_combination
    with
             1\_T\_brake : l\_T\_brake = f\_calc\_T\_brake\_service(l\_brake\_combination)
    then
             act1: T\_brake\_service := f\_calc\_T\_brake\_service(l\_brake\_combination)
    end
Event set_T_brake_emergency =
refines set_T_brake_emergency
    anv
            l\_brake\_combination
             grd1: l\_brake\_combination \in t\_brake\_combination
    with
             1\_T\_brake : l\_T\_brake = f\_calc\_T\_brake\_emergency(l\_brake\_combination)
    then
             act1: T\_brake\_emergency := f\_calc\_T\_brake\_emergency(l\_brake\_combination)
    end
END
```

5.2 dcmp - Calc Deceleration

The deceleration calculation model has the following input variables: *a_current*, *v_current* and *loc_current*. The output variables it calculates are *A_normal_service*, *A_expected* and *A_safe* which each map train speed and distance to an acceleration.

```
MACHINE dcmp_calc_deceleration_m0
SEES c6_supervision_limits
EVENTS
Event set\_A\_safe =
    any
             l\_a\_decel
    where
               grd1: l\_a\_decel \in t\_speed \times t\_distance \rightarrow t\_acceleration
    then
               act1 : A\_safe := l\_a\_decel
    end
Event set\_A\_expected =
    any
             l_a_decel
    where
               grd1: l\_a\_decel \in t\_speed \times t\_distance \rightarrow t\_acceleration
    then
               act1 : A\_expected := l\_a\_decel
    end
Event set\_A\_normal\_service =
             l\_a\_decel
    where
               grd1: l\_a\_decel \in t\_speed \times t\_distance \rightarrow t\_acceleration
    then
               act1 : A\_normal\_service := l\_a\_decel
    end
END
```

5.3 dcmp - Brake Buildup

The brake buildup time calculation has the following input variables: $a_current$, $v_current$ and $loc_current$. The output variables are T_be , T_se , $T_brake_service$ and $T_brake_emergency$.

```
MACHINE dcmp_brake_buildup_m0
SEES c6_supervision_limits
VARIABLES
     T be Shared variable, DO NOT REFINE
     T_bs Shared variable, DO NOT REFINE
     a_current Shared variable, DO NOT REFINE
     v_current Shared variable, DO NOT REFINE
     T_brake_service Shared variable, DO NOT REFINE
     loc_current Shared variable, DO NOT REFINE
     T_brake_emergency Shared variable, DO NOT REFINE
INVARIANTS
      typing_T_be : T\_be \in t\_time
      typing_T_bs : T_bs \in t_time
      typing_a_current : a_current \in t_acceleration
      typing_v_current : v_current \in t_speed
      typing_T_brake_service : T_brake_service \in t_time
      typing_loc_current : loc\_current \in t\_locations
      typing_T_brake_emergency : T_brake_emergency \in t_time
EVENTS
Initialisation
   begin
            act1 : v\_current := c\_v0
            act2 : a\_current := c\_a0
            act3 : loc\_current := c\_l0
            act9 : T\_brake\_service := c\_T\_brake0
            act10 : T_brake_emergency := c_T_brake0
            act14 : T_be := c_T_brake0
            act15 : T_bs := c_T_brake0
   end
Event update_train_state \widehat{=}
                                  External event, DO NOT REFINE
   any
           l_speed
           l\_accel
           l\_loc
    where
            grd1: l\_speed \in t\_speed
            grd2: l\_accel \in t\_acceleration
            grd3: l\_loc \in t\_locations
    then
            act1 : v\_current := l\_speed
            act2 : a\_current := l\_accel
            act3 : loc\_current := l\_loc
   end
Event set_T_brake_service =
                                   External event, DO NOT REFINE
   any
          l_T_brake
    where
            grd1: l\_T\_brake \in t\_time
```

```
then
             act1 : T\_brake\_service := l\_T\_brake
    end
Event set_T_brake_emergency =
                                         External event, DO NOT REFINE
    any
            l\_T\_brake
    where
             grd1: l\_T\_brake \in t\_time
    then
             act1 : T\_brake\_emergency := l\_T\_brake
    end
Event set_T_be =
    any
            l\_t\_be
             grd1: l\_t\_be \in t\_time
    then
             act1 : T\_be := l\_t\_be
    end
Event set\_T\_bs =
    any
    where l_t_bs
             grd1: l\_t\_bs \in t\_time
    then
             act1 : T\_bs := l\_t\_bs
    end
END
```

5.3.1 Context - Brake Buildup Functions

This context defines 4 functions that calculate the brake buildup time for the service and emergency brake. For each there are two functions, one for the conversion model and one without conversion model. The service break is not safety-critical, therefore it does not take a correction factor into account (cf. §3.13.6.3.1.1).

```
CONTEXT ctx_functions_1_calc_T_brake

EXTENDS ctx_functions_0

CONSTANTS

f\_T\_brake\_service\_conversion
f\_T\_brake\_emergency\_conversion
f\_T\_brake\_emergency
AXIOMS

axm1 : f\_T\_brake\_service\_conversion \in t\_time \times t\_brake\_combination \rightarrow t\_time
axm2 : f\_T\_brake\_service \in t\_time \times t\_brake\_combination \rightarrow t\_time
axm3 : f\_T\_brake\_emergency\_conversion \in t\_time \times t\_correction\_factor \rightarrow t\_time
axm4 : f\_T\_brake\_emergency \in t\_time \times t\_brake\_combination \rightarrow t\_time
END
```

5.3.2 dcmp - Brake Buildup Calculation

This refinement applies the calculation functions defined in the context to the calculation events. It adds the notions of train data to the machine which controls whether the conversion model is used for the brake buildup time calculation. This is represented by two variables each, a Boolean variable that signals whether a concrete train data has been supplied and a variable of type t_time representing the supplied value.

```
MACHINE dcmp_brake_buildup_m2_calculation
REFINES dcmp_brake_buildup_m0
SEES c6_supervision_limits, ctx_functions_1_calc_T_brake
VARIABLES
     T\_brake\_service\_data
     T_brake_service_via_train_data
     T_brake_emergency_data
     T_brake_emergency_via_train_data
INVARIANTS
       inv1: T_brake_service_data \in t_time
      inv2: T_brake_service_via_train_data \in BOOL
       inv3: T_brake_emergency_data \in t_time
       inv4: T_brake_emergency_via_train_data \in BOOL
EVENTS
Event set\_T\_be =
refines set_T_be
   anv
           l_brake_combination
    where
             grd1 : T_brake_emergency_via_train_data = TRUE
             grd2: l\_brake\_combination \in t\_brake\_combination
    with
             l_t_be : l_t_be = f_T_brake_emergency(T_brake_emergency \mapsto l_brake_combination)
   then
             act1 : T\_be := f\_T\_brake\_emergency(T\_brake\_emergency \mapsto l\_brake\_combination)
   end
Event calc\_T\_be\_conversion\_model =
refines set_T_brake_emergency
             grd1 : T_brake_emergency_via_train_data = FALSE
    with
             1_{T_brake} : l_T_brake = f_T_brake\_emergency\_conversion(T_brake\_service \mapsto c_Kt_int)
   then
             act1 : T_brake_emergency := f_T_brake_emergency_conversion(T_brake_service \mapsto c_Kt_int)
   end
Event set_T_bs =
refines set_T_bs
   any
           l_brake_combination
    where
             grd1 : T_brake_service_via_train_data = TRUE
             \verb|grd2|: l_brake_combination| \in t_brake_combination|
    with
             l_t_bs : l_t_bs = f_T_brake\_service(T_brake\_service\_data \mapsto l_brake\_combination)
   then
```

```
act1: T\_bs := f\_T\_brake\_service(T\_brake\_service\_data \mapsto l\_brake\_combination)
    end
Event calc\_T\_bs\_conversion\_model \widehat{=}
refines set_T_bs
    anv
           l_brake_combination
    where
             grd1 : T_brake_service_via_train_data = FALS E
             grd2: l\_brake\_combination \in t\_brake\_combination
    with
             l_tbs : l_tbs = f_Tbrake_emergency(T_brake_service \mapsto l_brake_combination)
    then
             act1 : T_bs := f_T_brake_emergency(T_brake_service \mapsto l_brake_combination)
    end
Event specify\_T\_brake\_service\_train\_data =
           l_T_brake
    where
             grd1: l\_T\_brake \in t\_time
             grd2 : T_brake_service_via_train_data = FALS E
    then
             act1 : T_brake_service_data := l_T_brake
             act2 : T_brake_service_via_train_data := TRUE
Event remove\_T\_brake\_service\_data =
    when
             grd1 : T_brake_service_via_train_data = TRUE
    then
             act1 : T\_brake\_service\_via\_train\_data := FALSE
    end
Event specify\_T\_brake\_emergency\_train\_data =
           l_T_brake
    where
             grd1: l\_T\_brake \in t\_time
             grd2 : T_brake_emergency_via_train_data = FALSE
    then
             act1: T\_brake\_emergency\_data := l\_T\_brake
             act2 : T_brake_emergency_via_train_data := TRUE
    end
Event remove\_T\_brake\_emergency\_data =
    when
             grd1 : T_brake_emergency_via_train_data = TRUE
    then
             act1 : T\_brake\_emergency\_via\_train\_data := FALSE
    end
END
```

5.4 dcmp - Acceleration Gradient

The calculation of the acceleration gradient has the current train state as input values (i.e., speed, location and acceleration). Its output value is the acceleration due to gradient, represented by the variable *A_gradient*.

```
MACHINE dcmp_acceleration_gradient_m0
SEES c6_supervision_limits
VARIABLES
     a_current Shared variable, DO NOT REFINE
     v_current Shared variable, DO NOT REFINE
     loc_current Shared variable, DO NOT REFINE
     A_gradient Private variable
INVARIANTS
      typing_a_current : a\_current \in t\_acceleration
       typing_v_current : v_current \in t_speed
       typing_loc_current : loc_current \in t_locations
       typing_A\_gradient : A\_gradient \in t\_acceleration
      m4\_accel\_decel\_gradient\_inv1 : A\_gradient \in t\_acceleration
EVENTS
Initialisation
    begin
             act1 : v\_current := c\_v0
             act2 : a\_current := c\_a0
             act3 : loc\_current := c\_l0
             act16 : A\_gradient := c\_a0
    end
Event update_train_state \widehat{=}
                                   External event, DO NOT REFINE
    any
           l_speed
           l_accel
           l_loc
    where
             grd1: l\_speed \in t\_speed
             grd2: l\_accel \in t\_acceleration
             grd3: l\_loc \in t\_locations
    then
             act1 : v\_current := l\_speed
             act2 : a\_current := l\_accel
             act3 : loc\_current := l\_loc
    end
Event set\_A\_gradient =
    any
           l_a_gradient
    where
             grd1: l\_a\_gradient \in t\_acceleration
    then
             act1 : A\_gradient := l\_a\_gradient
    end
END
```

5.4.1 Context - MRSP and Gradients

This context introduces functions to calculate an acceleration due to gradient (cf. 3.13.4) and to calculate the current most restrictive speed profile from the set of applicable speed profiles for a location.

```
CONTEXT ctx_functions_0
```

```
EXTENDS ctx_type_gradients
CONSTANTS
     f_accel_due_gradient
     f\_grad\_uphill
     f_compensate_gradient_profile
     f_{mrsp}
AXIOMS
      axm1: f\_accel\_due\_gradient \in
             t\_locations \times t\_locations \times t\_gradients \times t\_mass\_percentage \times t\_speed\_profiles \rightarrow
     t acceleration
                   (loc, SvL, compensated grad, mass, speed profile)
                  calculates acceleration due to gradient according to 3.13.4
      axm2: f\_grad\_uphill \in t\_gradients \rightarrow BOOL
                   indicates whether gradient is uphil or downhill
      axm3: f\_compensate\_gradient\_profile \in t\_locations \times t\_locations \times t\_gradient\_profiles \rightarrow
     t_gradients
                   (loc, SvL, profile) compensates for gradient profile (cf. 3.13.4.2.1)
      axm4: f_mrsp
                                t_speed_profiles × t_speed_profiles × t_speed_profiles ×
     t_speed_profiles
                         × t_speed_profiles × t_speed_profiles × t_speed_profiles ×
     t_speed_profiles
                       \times t_train_modes \times t_speed \times t_length \rightarrow t_speed_profiles
                   function which calculates the most restrictive speed profile
                  (MRSP) from the following inputs:
                  SSP, Axle Load SP, TSR, signalling related, mode related, LX speed,
                  override function related, SR to ensure permitted brake distance,
                  train mode, max train speed, train length
```

END

5.4.2 dcmp - Rotating Mass

This machine introduces the notion of rotating mass into the model. the rotating mass is represented by two variables, the Boolean one *rotating_mass_specified* which signals whether an explicit value for the mass has been specified and *M_rotating_mass* which represents a concrete value, given as percentage of the train mass.

Here the event $set_A_gradient$ the event parameter $l_a_gradient$ is replaced by a witness which is the application of the function to calculate the gradient to the train location and the event parameters.

```
MACHINE dcmp_acceleration_gradient_m1
REFINES dcmp_acceleration_gradient_m0
SEES c6_supervision_limits, ctx_functions_0
VARIABLES

rotating_mass_specified
```

```
M rotating nom
INVARIANTS
                              inv1: rotating\_mass\_specified \in BOOL
                               inv2 : M\_rotating\_nom \in t\_mass\_percentage
EVENTS
Event set\_A\_gradient =
refines set_A_gradient
                 any
                                                   l_mass
                                                   l S v L
                                                   l_grad
                                                   l_{-}TSR
                  where
                                                          grd2: l\_mass \in t\_mass\_percentage
                                                          grd3: l\_SvL \in t\_locations
                                                          grd4: l\_grad \in t\_gradients
                                                          grd5: l\_TSR \in t\_speed\_profiles
                  with
                                                         l_a_gradient: l_a_gradient = f_accel_due_gradient(loc_current \mapsto l_SvL \mapsto l_grad \mapsto l_mass \mapsto l_gradient(loc_current \mapsto l_svL \mapsto l_grad \mapsto l_grad \mapsto l_gradient(loc_current \mapsto l_svL \mapsto l_grad \mapsto l_grad \mapsto l_grad \mapsto l_gradient(loc_current \mapsto l_grad \mapsto 
                  then
                                                          act1: A\_gradient := f\_accel\_due\_gradient(loc\_current \mapsto l\_SvL \mapsto l\_grad \mapsto l\_mass \mapsto l\_TSR)
                 end
Event specify_rotating_mass \widehat{=}
                 any
                                                   l_mass
                  where
                                                          grd1 : rotating\_mass\_specified = FALSE
                                                          grd2: l\_mass \in t\_mass\_percentage
                  then
                                                          act1 : M\_rotating\_nom := l\_mass
                                                          act2 : rotating_mass_specified := TRUE
                 end
Event delete_rotating_mass_data \widehat{=}
                  when
                                                          grd1 : rotating\_mass\_specified = TRUE
                 then
                                                          act1 : rotating_mass_specified := FALSE
                                                          act2 : M_rotating_nom := c_mass_percentage0
                  end
END
```

5.4.3 dcmp - Acceleration due to Gradient Calculation

This machine refines the calculation of the acceleration due to gradient by splitting the calculation event into three refined ones. One to calculate the acceleration if a concrete rotating mass has been specified and two for an unknown rotating mass. In this case, there is one event for an uphill gradient which uses the maximal rotating mass value (constant c_M _rotating_max and for a downhill gradient which uses the minimal rotating mass (c_M _rotating_min) for the calculation (cf. 3.13.4.3.2).

```
MACHINE dcmp_acceleration_gradient_m2_grad_accel REFINES dcmp_acceleration_gradient_m1 SEES c6_supervision_limits, ctx_functions_0
```

```
EVENTS
Event calc_A_gradient_mass_known =
refines set_A_gradient
               any
                                            l\_SvL
                                            l_grad
                                            l\_TSR
                where
                                                 grd3: l\_SvL \in t\_locations
                                                 grd4 : l\_grad \in t\_gradients
                                                 grd5: l\_TSR \in t\_speed\_profiles
                                                  grd6: rotating\_mass\_specified = TRUE
               with
                                                  1_{mass} : l_{mass} = M_{rotating\_nom}
               then
                                                  \textbf{act1} : A\_gradient := f\_accel\_due\_gradient(loc\_current \mapsto l\_SvL \mapsto l\_grad \mapsto M\_rotating\_nom \mapsto l\_TSR)
               end
Event calc_A_gradient_mass_unknown_uphill =
refines set_A_gradient
               any
                                            l\_SvL
                                            l_grad
                                            l\_TSR
                where
                                                 grd3: l\_SvL \in t\_locations
                                                 grd4 : l\_grad \in t\_gradients
                                                 grd5: l\_TSR \in t\_speed\_profiles
                                                  grd6: f\_grad\_uphill(l\_grad) = TRUE
                                                  grd7 : rotating\_mass\_specified = FALSE
               with
                                                 1_{mass} : l_{mass} = c_{M_{rotating_{max}}}
               then
                                                 act1: A\_gradient := f\_accel\_due\_gradient(loc\_current \mapsto l\_SvL \mapsto l\_grad \mapsto c\_M\_rotating\_max \mapsto l\_SvL \mapsto l\_grad \mapsto c\_M\_rotating\_rotating\_max \mapsto l\_SvL \mapsto l\_grad \mapsto c\_M\_rotating\_max \mapsto l\_SvL \mapsto l\_grad \mapsto c\_M\_rotating\_max \mapsto l\_SvL \mapsto l\_grad \mapsto l
                                            l\_TSR)
               end
Event calc\_A\_gradient\_mass\_unknown\_downhill \widehat{=}
refines set_A_gradient
               any
                                            l\_SvL
                                            l\_grad
                                           l\_TSR
                where
                                                 grd3: l\_SvL \in t\_locations
                                                 grd4 : l\_grad \in t\_gradients
                                                  grd5: l\_TSR \in t\_speed\_profiles
                                                  grd6: f\_grad\_uphill(l\_grad) = FALSE
                                                  grd7 : rotating\_mass\_specified = FALSE
                with
                                                 1_{mass} : l_{mass} = c_{M_{rotating}} min
               then
                                                  \textbf{act1} : A\_gradient := f\_accel\_due\_gradient(loc\_current \mapsto l\_SvL \mapsto l\_grad \mapsto c\_M\_rotating\_min \mapsto l\_TSR)
                end
END
```

5.5 dcmp - MRSP

This machine introduces the notion of the most restrictive speed profile (MRPS) into the system. The input for this machine is the current train state, the variable *MRSP* of type *speed_profile* is its output value.

```
MACHINE dcmp_mrsp_m0
SEES c6_supervision_limits
VARIABLES
     MRS P Shared variable, DO NOT REFINE
     a_current Shared variable, DO NOT REFINE
     v_current Shared variable, DO NOT REFINE
     loc_current Shared variable, DO NOT REFINE
INVARIANTS
      \texttt{typing\_MRSP} : MRSP \in t\_speed\_profiles
       typing_a_current : a_current \in t_acceleration
       typing_v_current : v_current \in t_speed
       typing_loc_current : loc_current \in t_locations
EVENTS
Initialisation
    begin
             act1 : v\_current := c\_v0
             act2 : a\_current := c\_a0
             act3 : loc\_current := c\_l0
             act17 : MRSP := c\_speed\_profile0
    end
Event update_train_state \widehat{=}
                                   External event, DO NOT REFINE
    any
           l_speed
           l accel
           l\_loc
    where
             grd1: l\_speed \in t\_speed
             grd2: l\_accel \in t\_acceleration
             grd3: l\_loc \in t\_locations
    then
             act1 : v\_current := l\_speed
             act2 : a\_current := l\_accel
             act3 : loc\_current := l\_loc
    end
Event set\_MRSP \cong
    any
           l\_sp
    where
             grd1: l\_sp \in t\_speed\_profiles
    then
             act1 : MRSP := l\_sp
    end
END
```

5.5.1 dcmp - All Speed Profiles

This machine refines the calculation of the MRSP by refining the event *set_MRSP* to an event that takes all possible speed restrictions as event parameters and uses the function of the context of Section 5.4.1 to calculate the MRSP (cf. 3.11).

```
MACHINE dcmp_mrsp_m1_all_speed_profiles
REFINES dcmp_mrsp_m0
SEES c6_supervision_limits, ctx_functions_0
EVENTS
Event calculate_MRSP_from_all_speed_restrictions =
refines set_MRSP
              any
                                         l\_SSP
                                         l_AxleLoadS P
                                         l\_TSR
                                         l_S ignalRelatedS P
                                         l_mode
                                         l_modeRelatedSP
                                         l LXSP
                                         l_OverrideFuncSP
                                         l\_ensureBrakingDistanceSP
               where
                                               grd2: l\_SSP \in t\_speed\_profiles
                                               grd3: l\_AxleLoadSP \in t\_speed\_profiles
                                               grd4: l\_TSR \in t\_speed\_profiles
                                               grd5: l\_SignalRelatedSP \in t\_speed\_profiles
                                               grd6: l\_mode \in t\_train\_modes
                                               grd7: l\_modeRelatedSP \in t\_speed\_profiles
                                               grd8: l\_LXSP \in t\_speed\_profiles
                                               grd9: l\_OverrideFuncSP \in t\_speed\_profiles
                                               grd10: l\_ensureBrakingDistanceSP \in t\_speed\_profiles
               with
                                              \texttt{1\_sp} : l\_sp = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP)
                                                                                                                                                                                                                                                                                                                                             l_OverrideFuncSP
                                                                                                                                                                           l_modeRelatedSP
                                                                                                                                                                                                                                                                            l_{L}LXSP
                                         l_ensureBrakingDistanceSP
                                                                                                                                         \mapsto l\_mode \mapsto c\_train\_max\_speed \mapsto c\_train\_length)
               then
                                               \verb"act1": MRSP := f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_TSR \mapsto l\_SignalRelatedSP" \\ = f\_mrsp(l\_SSP \mapsto l\_AxleLoadSP \mapsto l\_A
                                                                                                                                                                           l_modeRelatedSP
                                                                                                                                                                                                                                                   \mapsto
                                                                                                                                                                                                                                                                           l\_LXSP
                                                                                                                                                                                                                                                                                                                                             l_OverrideFuncSP
                                         l_ensureBrakingDistanceSP
                                                                                                                                         \mapsto l\_mode \mapsto c\_train\_max\_speed \mapsto c\_train\_length)
               end
END
```

5.6 dcmp - Supervised Targets

This machine introduces has the current train state as inputs and produces as outputs the supervised locations: end of authority, limit of authority and supervised location, represented by *EOA*, *LOA* and *SvL*, each of type *t_targets*.

```
MACHINE dcmp_supervised_targets_m0
SEES c6_supervision_limits
VARIABLES

SvL Shared variable, DO NOT REFINE
LOA Shared variable, DO NOT REFINE
```

```
EOA Shared variable, DO NOT REFINE
EVENTS
Event set\_EOA \cong
    any
            l_target
    where
              grd1: l\_target \in t\_targets
    then
              act1 : EOA := l\_target
    end
Event set\_LOA \cong
    any
            l_target
    where
              \mathbf{grd1} : l\_target \in t\_targets
    then
              act1 : LOA := l\_target
    end
Event set\_SvL \cong
    any
            l\_target
    where
              grd1: l\_target \in t\_targets
    then
              act1 : SvL := l\_target
    end
END
```

5.7 dcmp - Braking Curves

This machine takes as input the current train state, the computed accelerations and the supervised targets. Its outputs are the braking curves for the mergency brake (*EBD*), the service brake (*SBD*) and the graphical representation for the driver (*GUI*).

```
MACHINE dcmp_braking_curves_m0
SEES c6_supervision_limits
VARIABLES
     SBD Shared variable, DO NOT REFINE
     GUI Shared variable, DO NOT REFINE
     EBD Shared variable, DO NOT REFINE
INVARIANTS
      typing\_SBD : SBD \in t\_braking\_curves
      typing_GUI : GUI \in t\_braking\_curves
      typing_EBD : EBD \in t\_braking\_curves
EVENTS
Event set\_EBD \cong
   any
          l\_curve
   where
            grd1: l\_curve \in t\_braking\_curves
   then
            act1 : EBD := l\_curve
```

```
end
Event set\_SBD \widehat{=}
    any
            l_curve
    where
              grd1: l\_curve \in t\_braking\_curves
    then
              act1 : SBD := l\_curve
Event set\_GUI \cong
    any
            l_curve
    where
              grd1: l\_curve \in t\_braking\_curves
    then
              act1 : GUI := l\_curve
    end
END
```

5.8 dcmp - Supervision Limits

This machine takes as inputs the current train state, the braking curves, the MRSP and the brake buildup times. It produces as outputs the following supervision limits: emergency brake intervention (*EBI*), service brake intervention (*SBI*), warning limit (*W_limit*), permitted (*P_limit*), indication limit (*I_limit*), pre-indication location (*PII*) and the release speed monitoring start location (*RSM_start*). Each of these variables is of type *t_supervision_limits*.

```
MACHINE dcmp_supervision_limits_m0
SEES c6_supervision_limits
VARIABLES
     SBI Shared variable, DO NOT REFINE
     PIl Shared variable, DO NOT REFINE
     W_limit Shared variable, DO NOT REFINE
     RS M_start Shared variable, DO NOT REFINE
     P_limit Shared variable, DO NOT REFINE
     EBI Shared variable, DO NOT REFINE
INVARIANTS
      typing_SBI : SBI \in t\_supervision\_limits
      typing_I_limit : I_limit \in t_supervision_limits
      typing_PI1 : PIl \in t\_supervision\_limits
      typing_W_limit : W_limit \in t_supervision_limits
      typing_RSM_start : RSM_start \in t_supervision_limits
      typing_P_limit : P_limit \in t_supervision_limits
      typing_EBI : EBI \in t\_supervision\_limits
EVENTS
Event set\_EBI =
   any
           l_limit
    where
            grd1: l\_limit \in t\_supervision\_limits
   then
            act1 : EBI := l\_limit
```

```
end
Event set\_SBI \cong
    any
            l\_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
    then
              act1 : SBI := l\_limit
    end
Event set_W_limit =
    any
            l\_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
    then
              act1 : W\_limit := l\_limit
    end
Event set_I_limit =
    any
            l\_limit
    where
              grd1: l\_limit \in t\_supervision\_limits
    then
              act1 : I\_limit := l\_limit
    end
Event set_P_limit =
    any
            l\_limit
    where
              \verb|grd1|: l\_limit \in t\_supervision\_limits|
    then
              act1 : P\_limit := l\_limit
    end
Event set\_PIl\_limit =
    any
            l\_limit
    where
              \verb|grd1|: l\_limit \in t\_supervision\_limits|
    then
              act1 : PIl := l\_limit
    end
Event set\_RSM\_start\_limit =
    any
            l\_limit
    where
              \verb|grd1|: l\_limit \in t\_supervision\_limits|
    then
              act1 : RSM\_start := l\_limit
    end
END
```

5.9 dcmp - Monitoring Commands

This machine takes as inputs the SBI, indication limit, pre-indication limit, warning limit, release speed monitoring start limit, permitted speed limit and the EBI. Its outputs are the DMI and the TI commands, i.e., the variables $status_current$ of type $t_DMI_commands$ and $cmd_current$ of type $t_TI_commands$.

```
MACHINE dcmp_monitoring_commands
SEES c6_supervision_limits
VARIABLES
     status_current Private variable
     cmd_current Private variable
INVARIANTS
      typing_status_current : status\_current \in t\_DMI\_commands
      typing_cmd_current : cmd_current \in t_TI_commands
    EVENTS
    Event new\_outputs =
         any
                l_ti_cmd
                l_dmi_status
                 grd1: l\_ti\_cmd \in t\_TI\_commands
                 grd2: l\_dmi\_status \in t\_DMI\_commands
         then
                 act1 : cmd\_current := l\_ti\_cmd
                 act2 : status\_current := l\_dmi\_status
         end
END
```

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