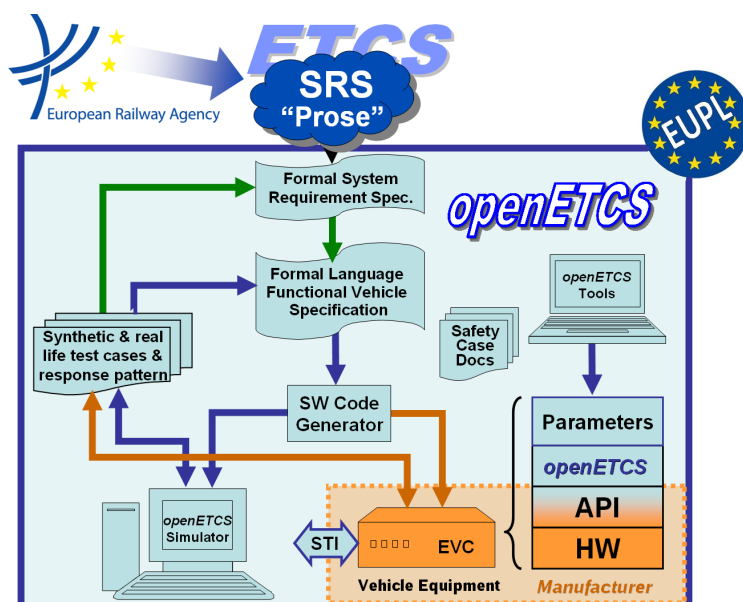


Event-B Model of Subset 026, Section 3.13

April 2013



Funded by:



Federal Ministry
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Région de
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Work-Package 7: “Toolchain”

**OETCS
April 2013**

Event-B Model of Subset 026, Section 3.13

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Model Description

Prepared for openETCS@ITEA2 Project

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This document describes a formal model of the requirements of section 3.13 of the subset 026 of the ETCS specification 3.3.0 [Eur12]. This section describes the speed and distance monitoring subsystem of ETCS.

The model is expressed in the formal language Event-B [Abr10] and developed within the Rodin tool [Jas12]. This formalism allows an iterative modeling approach. In general, one starts with a very abstract description of the basic functionality and step-wise adds additional details until the desired level of accuracy of the model is reached. Rodin provides the necessary proof support to ensure the correctness of the refined behavior.

In this document we present an Event-B model of the speed and distance monitoring subsystem of ETCS. At first, we describe shortly the background of Event-B, then the overall approach taken to model this section and finally present the model in detail.

The section 3.13 of the SRS gives a very detailed description of the calculation of many necessary values for speed and distance monitoring. As Event-B is a system modeling approach, we give an abstract model of the system. The calculations are abstracted as functions and the system ensures the correct parameter flow to the functions. We illustrate the model decomposition capabilities of Event-B and Rodin by decomposing the overall model into different functional parts.

For a short introduction on Event-B and the usage of Rodin with models on github see https://github.com/openETCS/model-evaluation/blob/master/model/B-Systemrel/Event_B/rodin-projects-github.pdf?raw=true

1 Modeling Strategy

The section 3.13 of the SRS describes the speed and distance monitoring together with the necessary parameters and data. The model starts with an abstract modeling of dataflow of the various intermediate calculated values. This model is partitioned into functional parts, the model is decomposed using shared variables and the respective sub-models are refined until the basic calculation functions are reached.

2 Model Overview

The overview of the speed and distance monitoring is shown in Fig. 1 from the SRS.

The on-board system comprises only the middle layer. The upper layer gives train related inputs as parameters, the lower layer track related inputs. The system itself takes the current position, speed and acceleration of the train and computes commands for the train interface and for the driver machine interface. For the train interface, this consists of the command for the service and emergency brakes. For the driver machine interface this consists of the status indication for the driver.

The Event-B modeling starts with machines describing the dataflow of all inputs, outputs and intermediate values of the model. For example, the values that are calculated for $T_{brake_service}$ in *Traction / Braking Models* are written into a variable by an event that calculates then and these values are read as input by the event that calculates T_{bs} for *SBI* limit.

This approach is conducted for each intermediate value of the system until a single machine is created with one variable for each intermediate value as well as for each input and output. On

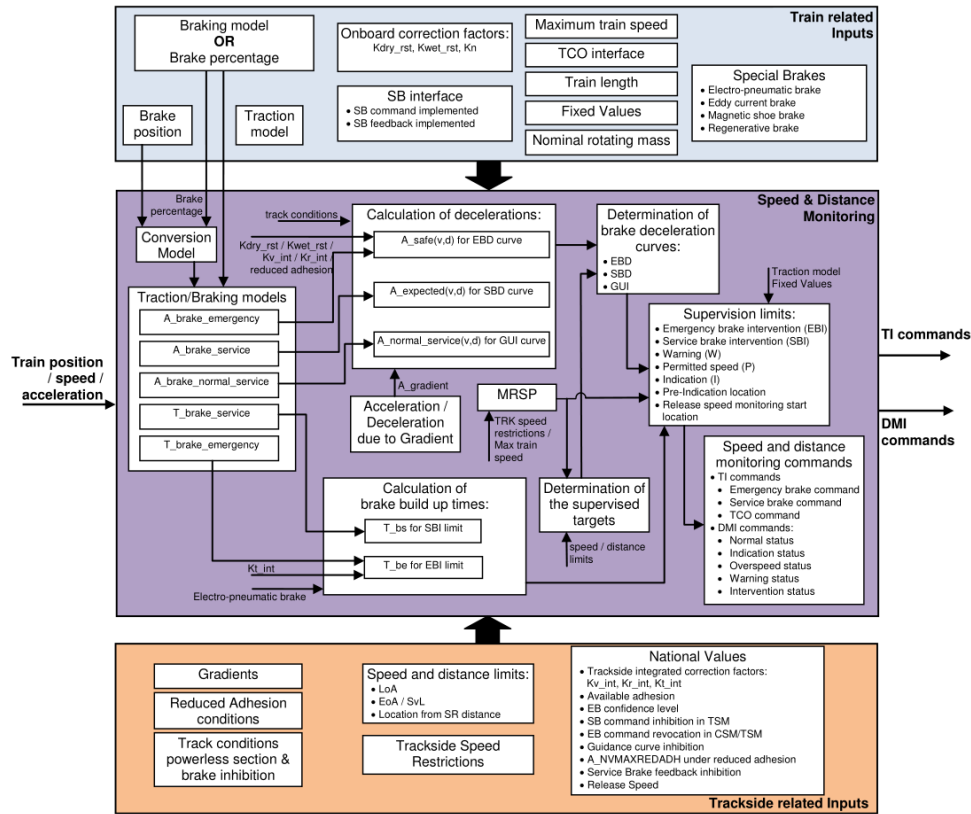


Figure 1. Speed and Distance Monitoring Overview ([Eur12] p. 85)

this level of modeling, all events only define the necessary input values and write a new value to their output variable. This value is provided as event parameter on this abstraction level.

The next step is to decompose the single machine into different sub-machines, in general one machine for each functional part of the model. This allows for model structuring and complexity reduction for each machine. For this we use the Rodin decomposition plug-in¹ using the shared-variable decomposition approach [SPHB11]. This approach splits the set of events of a machine into several disjoint sets and assigns one such set to each sub-machine. It also allows to distribute the variables over several machines, effectively implementing a shared variable distributed system.

The borders for the subsystem decomposition are shown in Fig. 2. The dashed lines show the separate sub-machines. The dataflows that cross these lines are represented by the shared variables of the decomposed model.

Each of the sub-machines with its shared variables is then further refined until the desired level of detail is reached. The overview of these refinements is shown in Fig. 3.

This refinement and context overview is very different from the others, as first an abstract global model was developed and then this model was decomposed into sub-models which are further refined. The contexts are shared between the decomposed models as far as possible. In this case, all resulting contexts and machines are kept in the same Rodin project. It is also possible to create a new project for each sub-machine which will reduce the complexity of each single project.

¹http://wiki.event-b.org/index.php/Decomposition_Plug-in_User_Guide

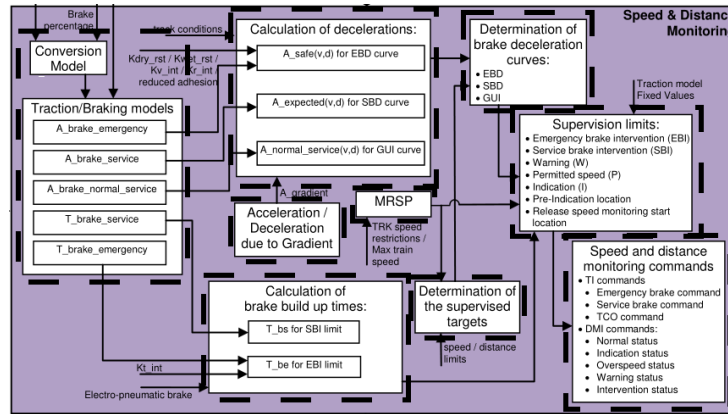


Figure 2. Decomposition of System

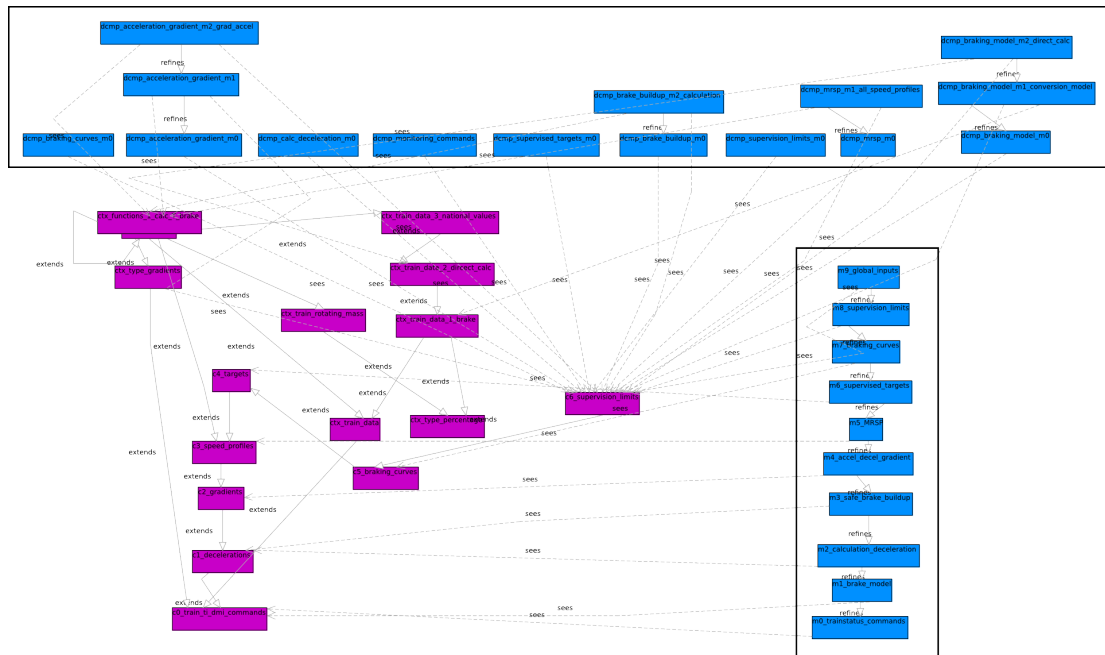


Figure 3. Machine Decomposition Overview

The global model is shown in the lower right. The first machine describes the global input and output variables of the system. The further refinements represent the iterative addition of more functions as shown in Fig. 2. For example the machine 1 adds the brake model with its inputs and outputs and the machine 2 adds the calculation of deceleration which uses the outputs of the braking model.

The last machine is then decomposed into the nine machines representing each a single functional block. This structure is shown in the upper part of Fig. 3, this also illustrates the further independent refinement of the decomposed sub-machine.

The context hierarchy also reflects this structuring. The contexts define the data types for the intermediate values, as well as the functions that calculate these values. These functions are generally not further refined in the Event-B model, as this is not part of the system modeling.

3 Model Benefits

The modeled section of the SRS provides many details for calculation of various values. The main content from a system modeling point of view is the model. So while in this case the same benefits from using Rodin as for [Mat13a, Mat13b, Mat13c] are present, the main advantage here is the model structuring facility.

- **Model Decomposition** The shared variable model decomposition [SPHB11] allows for decomposing an Event-B model and for separate refining of the machines of the resulting sub-models while retaining correctness of the refinement proofs.

4 Detailed Model Description

4.1 Context 0 - Train Inputs, TI and DMI command

The first context introduces many basic type for the model, *t_locations*, *t_speed*, *t_acceleration*, *t_TI_commands*, *t_DMI_commands*, *t_time* and *t_train_modes*.

The commands for the train interface (TI) are represented by the constants *c_emergency_brake*, *c_service_brake*, *c_TCO*, *c_no_command*. For the driver machine interface (DMI) the commands are represented by the constants *c_normal*, *c_indication*, *c_overspeed*, *c_warning* and *c_intervention*.

The other constants provide default values for the initialization of variables of that type.

CONTEXT c0_train_ti_dmi_commands
SETS

t_locations all possible locations on track
t_speed train speed measurement
t_acceleration train acceleration
t_TI_commands track interface commands
t_DMI_commands driver machine interface commands
t_time
t_train_modes

CONSTANTS

c_emergency_brake
c_service_brake
c_TCO traction cut off
c_no_command empty command
c_normal
c_indication
c_overspeed
c_warning
c_intervention
c_v0
c_a0
c_l0
c_a_brake0
c_T_brake0

AXIOMS

```

axm1 : partition(t_TI_commands, {c_no_command}, {c_emergency_brake},
               {c_service_brake}, {c_TCO})

axm2 : partition(t_DMI_commands, {c_normal}, {c_indication},
               {c_overspeed}, {c_warning}, {c_intervention})
axm3 : c_v0 ∈ t_speed
axm4 : c_a0 ∈ t_acceleration

axm5 : c_l0 ∈ t_locations
axm6 : c_a_brake0 ∈ t_speed → t_acceleration
               default brake profile

axm7 : c_T_brake0 ∈ t_time
               default brake buildup time

```

END

4.2 Machine 0 - Train Status and Commands

This first machine introduces the external input variables, i.e., the position, speed and acceleration of the train as well as the output variables, i.e., the TI commands and the DMI commands. The input variables are read by the event *update_train_style* and the output variables by the event *new_outputs*.

MACHINE m0_trainstatus_commands

SEES c0_train_ti_dmi_commands

VARIABLES

```

v_current  current speed of train
a_current  current acceleration of train
loc_current current position of train as track location
cmd_current current TI command
status_current current DMI status

```

INVARIANTS

```

inv1 : v_current ∈ t_speed
inv2 : a_current ∈ t_acceleration
inv3 : loc_current ∈ t_locations
inv4 : cmd_current ∈ t_TI_commands
inv5 : status_current ∈ t_DMI_commands

```

EVENTS

Initialisation

begin

```

act1 : v_current := c_v0
act2 : a_current := c_a0
act3 : loc_current := c_l0
act4 : cmd_current := c_no_command
act5 : status_current := c_normal

```

end

Event *update_train_state* ≡

any

```

l_speed
l_accel
l_loc

```

where

```

grd1 : l_speed ∈ t_speed
grd2 : l_accel ∈ t_acceleration

```

```

    then
        grd3 :  $l\_loc \in t\_locations$ 

        act1 :  $v\_current := l\_speed$ 
        act2 :  $a\_current := l\_accel$ 
        act3 :  $loc\_current := l\_loc$ 
    end
Event new_outputs  $\hat{=}$ 
    any
        l_ti_cmd
        l_dmi_status
    where
        grd1 :  $l\_ti\_cmd \in t\_TI\_commands$ 
        grd2 :  $l\_dmi\_status \in t\_DMI\_commands$ 
    then
        act1 :  $cmd\_current := l\_ti\_cmd$ 
        act2 :  $status\_current := l\_dmi\_status$ 
    end
END

```

4.3 Machine 1 - Brake Model

The first refinement adds the notion of the brake model. This is represented by the variables describing the speed dependent acceleration functions for emergency, service and normal service braking. The variables $T_brake_service$ and $T_brake_emergency$ describe the brake build-up times for the brakes.

```

MACHINE m1_brake_model
REFINES m0_trainstatus_commands
SEES c0_train_ti_dmi_commands
VARIABLES

    A_brake_emergency emergency brake acceleration
    A_brake_service service brake acceleration
    A_brake_normal_service
    T_brake_service
    T_brake_emergency
EVENTS
Event set_A_brake_emergency  $\hat{=}$ 
    any
        l_a_brake
    where
        then
            grd1 :  $l\_a\_brake \in t\_speed \rightarrow t\_acceleration$ 
        then
            act1 :  $A\_brake\_emergency := l\_a\_brake$ 
        end
Event set_A_brake_service  $\hat{=}$ 
    any
        l_a_brake
    where
        then
            grd1 :  $l\_a\_brake \in t\_speed \rightarrow t\_acceleration$ 
        then
            act1 :  $A\_brake\_service := l\_a\_brake$ 
        end
Event set_A_brake_normal_service  $\hat{=}$ 

```

```

    any
    where  $l\_a\_brake$ 
    then  $grd1 : l\_a\_brake \in t\_speed \rightarrow t\_acceleration$ 
    end  $act1 : A\_brake\_normal\_service := l\_a\_brake$ 
Event  $set\_T\_brake\_service \hat{=}$ 
    any
    where  $l\_T\_brake$ 
    then  $grd1 : l\_T\_brake \in t\_time$ 
    end  $act1 : T\_brake\_service := l\_T\_brake$ 
Event  $set\_T\_brake\_emergency \hat{=}$ 
    any
    where  $l\_T\_brake$ 
    then  $grd1 : l\_T\_brake \in t\_time$ 
    end  $act1 : T\_brake\_emergency := l\_T\_brake$ 
END

```

4.4 Context 1 - Decelerations

This context extension adds a distance type and a function that maps the speed and distance to an acceleration.

```

CONTEXT c1_decelerations
EXTENDS c0_train_ti_dmi_commands
SETS

     $t\_distance$ 
CONSTANTS

     $f\_A\_deceleration0$ 
AXIOMS

     $axm1 : f\_A\_deceleration0 \in t\_speed \times t\_distance \rightarrow t\_acceleration$ 
END

```

4.5 Machine 2 - Calculate Decelerations

This refinement adds the calculation of deceleration to the model. This is represented by three variables which are functions that map speed and distance to an acceleration. There is one function for each on of EBD, SBD and GUI.

```

MACHINE m2_calculation_deceleration
REFINES m1_brake_model
SEES c1_decelerations
VARIABLES

     $A\_safe$ 

```

```

    A_expected
    A_normal_service
EVENTS
Event set_A_safe  $\hat{=}$ 
  any
    where
      l_a_decel
    then
      grd1 : l_a_decel  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
      grd2 : A_brake_emergency  $\in$  t_speed  $\rightarrow$  t_acceleration
    then
      act1 : A_safe := l_a_decel
    end
Event set_A_expected  $\hat{=}$ 
  any
    where
      l_a_decel
    then
      grd1 : l_a_decel  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
      grd2 : A_brake_service  $\in$  t_speed  $\rightarrow$  t_acceleration
    then
      act1 : A_expected := l_a_decel
    end
Event set_A_normal_service  $\hat{=}$ 
  any
    where
      l_a_decel
    then
      grd1 : l_a_decel  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
      grd2 : A_brake_normal_service  $\in$  t_speed  $\rightarrow$  t_acceleration
    then
      act1 : A_normal_service := l_a_decel
    end
END

```

4.6 Machine 3 - Calculation of Brake Buildup Time

The next machine refinement adds the brake buildup calculation to the model. This is represented by two variables, T_{be} for the emergency brake and T_{se} for the service brake.

```

MACHINE m3_safe_brake_buildup
REFINES m2_calculation_deceleration
SEES c1_decelerations
VARIABLES
  T_be
  T_bs
EVENTS
Event set_T_be  $\hat{=}$ 
  any
    where
      l_t_be
    then
      grd1 : l_t_be  $\in$  t_time
      grd2 : T_brake_emergency  $\in$  t_time
    then
      act1 : T_be := l_t_be
    end

```

```

Event set_T_bs  $\hat{=}$ 
  any
    l_t_bs
  where
    grd1 : l_t_bs  $\in$  t_time
    grd2 : T_brake_service  $\in$  t_time
  then
    act1 : T_bs := l_t_bs
  end
END

```

4.7 Machine 4 - Acceleration due to Gradient

The refinement adds the notion of the acceleration due to gradient. This is represented by the variable *A_gradient* which is a function that maps speed to acceleration.

```

MACHINE m4_accel_decel_gradient
REFINES m3_safe_brake_buildup
SEES c2_gradients
VARIABLES
  A_gradient
EVENTS
Event set_A_gradient  $\hat{=}$ 
  any
    l_a_gradient
  where
    grd1 : l_a_gradient  $\in$  t_acceleration
  then
    act1 : A_gradient := l_a_gradient
  end
END

```

4.8 Context 3 - Speed Profiles

This context extension introduces the type *speed_profiles* which maps locations to speeds. It also defines one constant value of that type which is used as default value for variables of that type.

```

CONTEXT c3_speed_profiles
EXTENDS c2_gradients
CONSTANTS
  c_speed_profile0
  t_speed_profiles
AXIOMS
  axm1 : t_speed_profiles  $\subseteq$  t_locations  $\times$  t_speed
  axm2 : c_speed_profile0  $\in$  t_speed_profiles
END

```

4.9 Machine 5 - Most Restrictive Speed Profile

This machine refinement introduces the most restrictive speed profile to the model. This is represented by the variable *MRSP* of the type *speed_profile*.

```

MACHINE m5_MRSP
REFINES m4_accel_decel_gradient
SEES c3_speed_profiles
VARIABLES

    MRSP
EVENTS
Event set_MRSP  $\triangleq$ 
    any

        l_sp
    where

        grd1 :  $l\_sp \in t\_speed\_profiles$ 
    then

        act1 :  $MRSP := l\_sp$ 
    end
END

```

4.10 Context 4 - Targets

This context extension introduces the type *t_targets* which represents a target, i.e., a pair of location and speed.

```

CONTEXT c4_targets
EXTENDS c3_speed_profiles
CONSTANTS

    t_targets
    c_target0
AXIOMS

    axm1 :  $t\_targets \subseteq t\_locations \times t\_speed$ 

    axm2 :  $c\_target0 \in t\_targets$ 
END

```

4.11 Machine 6 - Supervised Targets

This refinement adds limit of authority, end of authority and supervision limit to the model. For each there exists one variable of type *t_targets*.

```

MACHINE m6_supervised_targets
REFINES m5_MRSP
SEES c4_targets
VARIABLES

    LOA
    EOA
    SvL
EVENTS
Event set_EOA  $\triangleq$ 

```



```

    any
       $l_{target}$ 
    where
       $grd1 : l_{target} \in t_{targets}$ 
       $grd2 : MRS P \in t_{speed\_profiles}$ 
    then
       $act1 : EOA := l_{target}$ 
    end
  Event  $set\_LOA \hat{=}$ 
    any
       $l_{target}$ 
    where
       $grd1 : l_{target} \in t_{targets}$ 
       $grd2 : MRS P \in t_{speed\_profiles}$ 
    then
       $act1 : LOA := l_{target}$ 
    end
  Event  $set\_SvL \hat{=}$ 
    any
       $l_{target}$ 
    where
       $grd1 : l_{target} \in t_{targets}$ 
       $grd2 : MRS P \in t_{speed\_profiles}$ 
    then
       $act1 : SvL := l_{target}$ 
    end
END

```

4.12 Context 5 - Braking Curves

This context extension introduces the type $t_{braking_curves}$ and a constant of that type.

```

CONTEXT c5_braking_curves
EXTENDS c4_targets
SETS
   $t_{braking\_curves}$ 
CONSTANTS
   $c\_curve0$ 
AXIOMS
   $axm1 : c\_curve0 \in t_{braking\_curves}$ 
END

```

4.13 Machine 7 - Braking Curves

This machine refinement adds the braking curves to the model, these are represented by the three variables EBD , SBD and GVI of the appropriate type.

```

MACHINE m7_braking_curves
REFINES m6_supervised_targets
SEES c5_braking_curves
VARIABLES

```

EBD

```

    SBD
    GUI
EVENTS
Event set_EBD  $\hat{=}$ 
    any
        l_curve
    where
        grd1 : l_curve  $\in$  t_braking_curves
        grd2 : A_safe  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd3 : A_expected  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd4 : A_normal_service  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd5 : LOA  $\in$  t_targets
        grd6 : EOA  $\in$  t_targets
        grd7 : SvL  $\in$  t_targets
    then
        act1 : EBD := l_curve
    end
Event set_SBD  $\hat{=}$ 
    any
        l_curve
    where
        grd1 : l_curve  $\in$  t_braking_curves
        grd2 : A_safe  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd3 : A_expected  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd4 : A_normal_service  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd5 : LOA  $\in$  t_targets
        grd6 : EOA  $\in$  t_targets
        grd7 : SvL  $\in$  t_targets
    then
        act1 : SBD := l_curve
    end
Event set_GUI  $\hat{=}$ 
    any
        l_curve
    where
        grd1 : l_curve  $\in$  t_braking_curves
        grd2 : A_safe  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd3 : A_expected  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd4 : A_normal_service  $\in$  t_speed  $\times$  t_distance  $\rightarrow$  t_acceleration
        grd5 : LOA  $\in$  t_targets
        grd6 : EOA  $\in$  t_targets
        grd7 : SvL  $\in$  t_targets
    then
        act1 : GUI := l_curve
    end
END

```

4.14 Context 6 - Supervision Limits

This context adds the type *t_supervision_limits* to the model, as well as a constant value of that type.

```

CONTEXT c6_supervision_limits
EXTENDS c5_braking_curves
SETS

```

```

    t_supervision_limits
CONSTANTS

```

```

    c_slimit0
AXIOMS

    axm1 : c_slimit0 ∈ t_supervision_limits
END

```

4.15 Machine 8 - Supervision Limit

This machine refinement adds the supervision limits to the model, emergency brake intervention (*EBI*), service brake intervention (*SBI*), warning limit (*warning_limit*), permitted speed (*P_limit*), indication limit (*I_limit*), pre-indication location (*PI_limit*) and the release start speed monitoring location (*RSM_start*).

```

MACHINE m8_supervision_limits
REFINES m7_braking_curves
SEES c6_supervision_limits
VARIABLES

    EBI emergency brake intervention
    SBI service brake intervention
    W_limit warning limit
    P_limit permitted speed
    I_limit indication limit
    PI pre-indication_location
    RSM_start release speed monitoring start location
EVENTS
Event set_EBI ≡
    any
    where
        I_limit
        grd1 : I_limit ∈ t_supervision_limits
        grd2 : MRS P ∈ t_speed_profiles
        grd3 : EBD ∈ t_braking_curves
        grd4 : SBD ∈ t_braking_curves
        grd5 : GUI ∈ t_braking_curves
        grd6 : T_bs ∈ t_time
        grd7 : T_be ∈ t_time
    then
        act1 : EBI := I_limit
    end
Event set_SBI ≡
    any
    where
        I_limit
        grd1 : I_limit ∈ t_supervision_limits
        grd2 : MRS P ∈ t_speed_profiles
        grd3 : EBD ∈ t_braking_curves
        grd4 : SBD ∈ t_braking_curves
        grd5 : GUI ∈ t_braking_curves
        grd6 : T_bs ∈ t_time
        grd7 : T_be ∈ t_time
    then
        act1 : SBI := I_limit
    end
Event set_W_limit ≡
    any
    where
        I_limit

```

```

    grd1 :  $l\_limit \in t\_supervision\_limits$ 
    grd2 :  $MRS P \in t\_speed\_profiles$ 
    grd3 :  $EBD \in t\_braking\_curves$ 
    grd4 :  $SBD \in t\_braking\_curves$ 
    grd5 :  $GUI \in t\_braking\_curves$ 
    grd6 :  $T\_bs \in t\_time$ 
    grd7 :  $T\_be \in t\_time$ 
  then
    act1 :  $W\_limit := l\_limit$ 
  end
Event set_I_limit  $\hat{=}$ 
  any
    where
      l_limit
      grd1 :  $l\_limit \in t\_supervision\_limits$ 
      grd2 :  $MRS P \in t\_speed\_profiles$ 
      grd3 :  $EBD \in t\_braking\_curves$ 
      grd4 :  $SBD \in t\_braking\_curves$ 
      grd5 :  $GUI \in t\_braking\_curves$ 
      grd6 :  $T\_bs \in t\_time$ 
      grd7 :  $T\_be \in t\_time$ 
    then
      act1 :  $I\_limit := l\_limit$ 
    end
Event set_P_limit  $\hat{=}$ 
  any
    where
      l_limit
      grd1 :  $l\_limit \in t\_supervision\_limits$ 
      grd2 :  $MRS P \in t\_speed\_profiles$ 
      grd3 :  $EBD \in t\_braking\_curves$ 
      grd4 :  $SBD \in t\_braking\_curves$ 
      grd5 :  $GUI \in t\_braking\_curves$ 
      grd6 :  $T\_bs \in t\_time$ 
      grd7 :  $T\_be \in t\_time$ 
    then
      act1 :  $P\_limit := l\_limit$ 
    end
Event set_PIl_limit  $\hat{=}$ 
  any
    where
      l_limit
      grd1 :  $l\_limit \in t\_supervision\_limits$ 
      grd2 :  $MRS P \in t\_speed\_profiles$ 
      grd3 :  $EBD \in t\_braking\_curves$ 
      grd4 :  $SBD \in t\_braking\_curves$ 
      grd5 :  $GUI \in t\_braking\_curves$ 
      grd6 :  $T\_bs \in t\_time$ 
      grd7 :  $T\_be \in t\_time$ 
    then
      act1 :  $PIl := l\_limit$ 
    end
Event set_RSM_start_limit  $\hat{=}$ 
  any
    where
      l_limit
      grd1 :  $l\_limit \in t\_supervision\_limits$ 
      grd2 :  $MRS P \in t\_speed\_profiles$ 

```

```

    grd3 :  $EBD \in t\_braking\_curves$ 
    grd4 :  $SBD \in t\_braking\_curves$ 
    grd5 :  $GVI \in t\_braking\_curves$ 
    grd6 :  $T\_bs \in t\_time$ 
    grd7 :  $T\_be \in t\_time$ 
  then
    act1 :  $RS\ M\_start := l\_limit$ 
  end
END

```

5 Model Decomposition

The machine m9 does not really add detail to the refined machine m8. The only changes are that the variables which are read by an event are explicitly added to the conditions by specifying a typing condition for them. This assures that the model decomposition preserves these necessary variables in the sub-machines and only removes the unneeded ones.

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