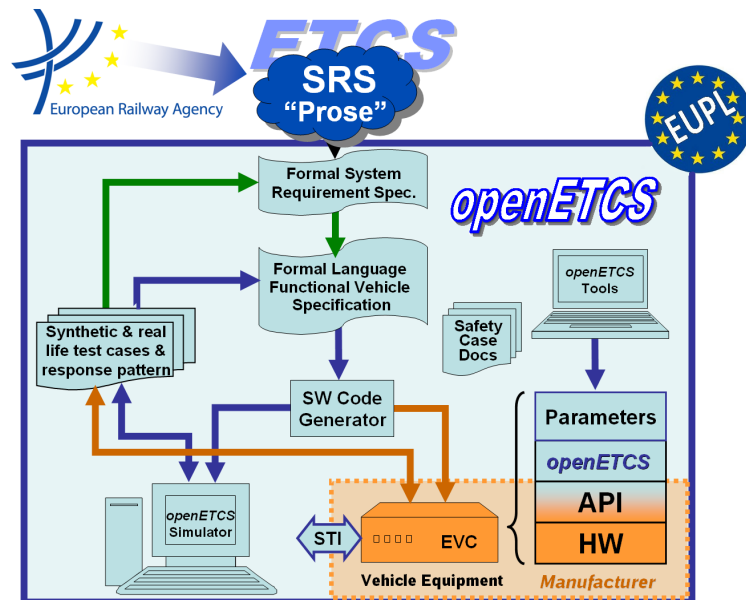


Work-Package 7: "Toolchain"

Event-B Model of Subset 026, Section 5.9

Matthias Güdemann

June 2013



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Work-Package 7: “Toolchain”

**OETCS
June 2013**

Event-B Model of Subset 026, Section 5.9

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Model Description

Prepared for openETCS@ITEA2 Project

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This document describes a formal model of the requirements of section 5.9 of the subset 026 of the ETCS specification 3.3.0 [Eur12]. This section describes the on-sight procedure.

The model is expressed in the formal language Event-B [Abr10] and developed within the Rodin tool [Jas12]. This formalism allows an iterative modeling approach. In general, one starts with a very abstract description of the basic functionality and step-wise adds additional details until the desired level of accuracy of the model is reached. Rodin provides the necessary proof support to ensure the correctness of the refined behavior.

In this document we present an Event-B model of the procedure on-sight. We use the iUML plugin which allows for modeling in UML state-charts to create a graphical model of the procedure which is as close as possible as its description as flowchart in the section 5.9. The state machine is iteratively developed using the refinement feature of Event-B. At each refinement step, we present the reasoning for the step, together with newly introduced variables and events.

For a short introduction on Event-B and the usage of Rodin with models on github see https://github.com/openETCS/model-evaluation/blob/master/model/B-Systemrel/Event_B/rodin-projects-github.pdf?raw=true

1 Modeling Strategy

The section 5.9 of the SRS describes the procedure on-sight, in particular it describes the sequence of mode changes, necessary driver acknowledge and train brake to enter OS mode, dependent on the current train mode.

For better understanding and to automate many tasks for state based modeling, we use the iUML plugin [?] which automatically generates Event-B code representing a state machine specification.

2 Model Overview

Figure 1 shows the structure of the Event-B model. The left column represents the abstract state machines, the right column the contexts. An arrow from one machine to another machine represents a refinement relation, an arrow from a machine to a context represents a sees relation and arrow from one context to another represents an extension relation.

The modeling starts with the very abstract possibility to establish and to terminate a communication session in the machine $m0$, the set of entities is defined in the context $c0$. This basic functionality is refined in the succeeding machines to incorporate a more detailed description of the flowchart.

3 Model Benefits

The Event-B model in Rodin has some interesting properties which are highlighted here. Some stem from the fact that Rodin is well integrated into the Eclipse platform which renders many useful plugins available, both those explicitly developed for integration with Rodin, but also other without Rodin in mind. Other interesting properties stem from the fact that Rodin and Event-B provide an extensive proof support for properties.

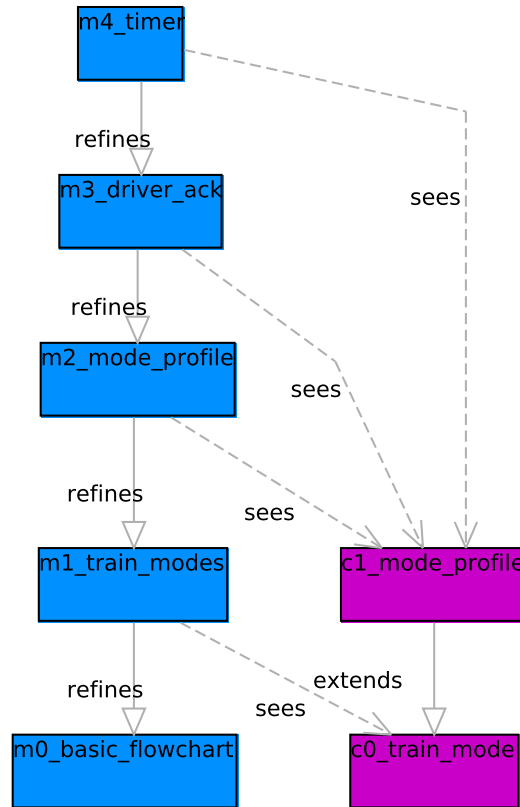


Figure 1. Overview on State Machine and Context Hierarchy

- **Graphical Modeling** Through the iUML plugin, Rodin supports graphical modeling of UML/SysML state machines. Transitions are labeled with events and a fully automatic transformation [SBS09] creates an Event-B representation of the state machine models.
- **Refinement** In addition to the general refinement which is possible in the Event-B approach, the graphical modeling allows to refine the graphical state chart models too. For each refinement step, the new details are graphically emphasized.
- **Model Animation** Through the ProB plugin, the graphical models can be animated just as textual Event-B models. In this case active transitions can be highlighted which helps understand model behavior.
- **Safety Properties** Using Rodin's proof support and the formalization as invariants, it is possible to formalize and prove the identified safety properties of the case study (see *inv2* and *inv10* in Section 4.9).

4 Detailed Model Description

This section describes in more detail the formal model, beginning from the most abstract Event-B machine. For each refinement, the state machine will be shown and in general only the important manual changes in the model generated from the state machine. The full generated code and the manual changes are available as a Rodin project. At each step the additional modeled functionality and its representation will be described. In particular the initialization event is not shown for the refined machines. If not mentioned explicitly, sets are initialized empty, integers with value 0 and Boolean variables with false.

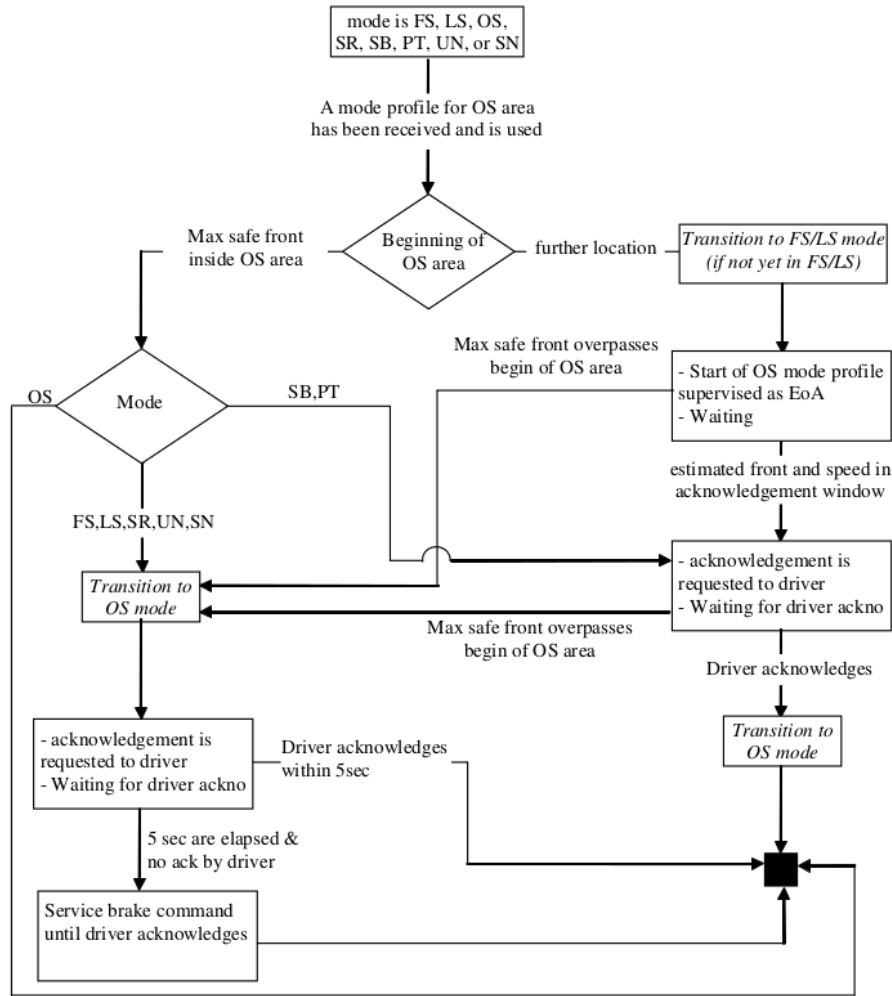


Figure 2. Flowchart for "On-Sight" Procedure [Eur12]

4.1 Machine 0 - Basic Flowchart

The first state machine $m0$ (see Fig. 3) represents an abstract view of the flowchart describing the on-sight procedure which is shown in §5.9.7 of the SRS [Eur12] (see Fig. 2).

The flowchart is translated into a iUML state machine as follows: the initial state represents the initial situation of the procedure flowchart. The diamonds of the flowchart represent different cases and are therefore into transitions with different target states in the state chart. The nodes of the flowchart are combined for abstraction by combining nodes with multiple incoming flows (or an initial node) with direct successor nodes.

For example the state *ack_and_transition* can be reached from the initial state via the event *use_profile_OS_inside_area_mode_SB_PT* and corresponds to the two lower right nodes of the flowchart. This is justified, as the flow passes two diamonds in the flowchart, verifying that the i) max safe front of the train is inside the OS area and ii) the train mode is *BS* or *PT*. The complete model is automatically generated from this state machine. Note however, that in this abstraction level, there is no concrete notion of train modes, these appear in the first refinement.

The transitions *switch_to_OS_mode* signal the completion of the on-sight procedure, the internal switch to OS mode in the train happens elsewhere. The state *OS_mode* signals the final state.

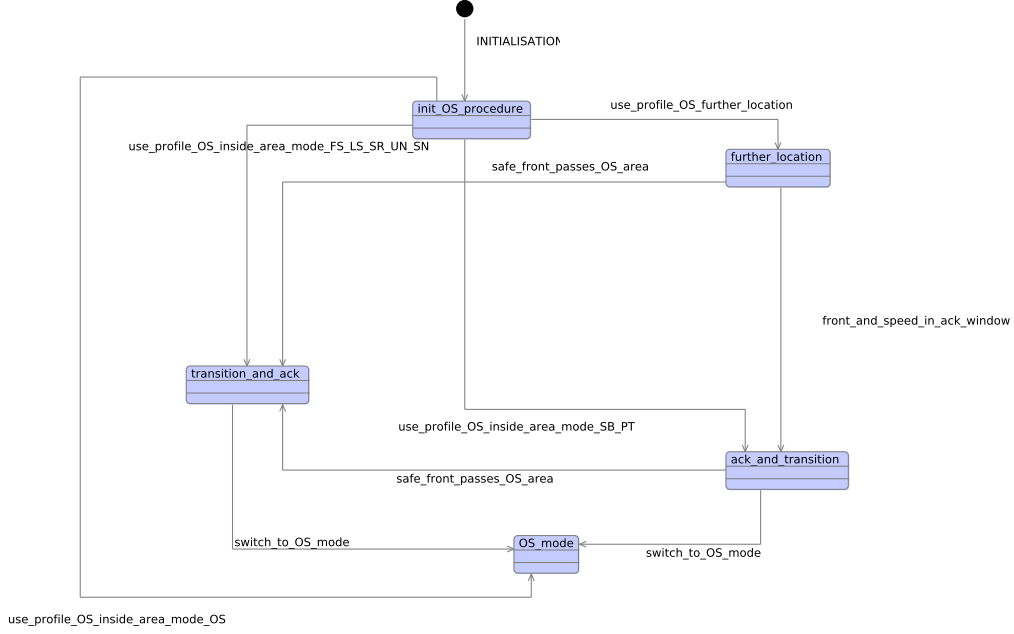


Figure 3. Basic Flowchart Representation

4.2 Context 0 - Train Modes

The first context $c0$ specifies the possible modes of the train, these are of type t_train_modes . There is one Event-B constant for each possible mode. The constant $c_initial_mode$ represents the initial mode of the train when the procedure on-sight is started. The constant $c_supervision_mode$ is one mode from the supervision modes.

SETS

t_train_modes

CONSTANTS

c_FS full supervision
 c_LS limited supervision
 c_OS on sight
 c_SR staff responsible
 c_SB stand-by
 c_PT post-trip
 c_UN unfitted
 c_SN national system
 $c_initial_mode$
 $c_supervision_mode$

AXIOMS

$axm1 : partition(t_train_modes, \{c_FS\}, \{c_LS\}, \{c_OS\}, \{c_SR\}, \{c_SB\}, \{c_PT\}, \{c_UN\}, \{c_SN\})$
 $axm2 : c_initial_mode \in \{c_FS, c_OS, c_PT\}$
 $axm3 : c_supervision_mode \in \{c_LS, c_FS\}$

END

4.3 Machine 1 - Train Modes

The first machine refinement adds the variable $current_mode$ which tracks the current mode of the train. This variable is initialized with the value of $c_initial_mode$.

The state of this variable is used to constrain the guards of the events that depend on the train modes, i.e., corresponding to those that lead from the “Mode” diamond in the flowchart (see Fig. 2). Its state is changed in the *transition_to_supervision_mode* event which assigns the value of *c_supervision_mode* or in the *transition_to_OS_mode* event which assigns the on-sight mode.

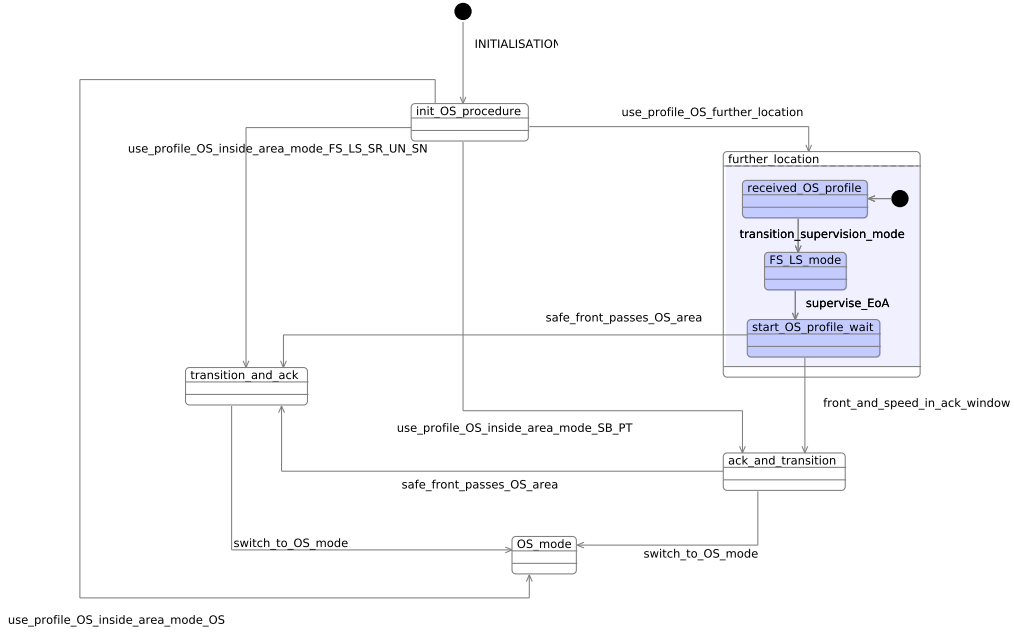


Figure 4. First Refinement with Train Modes

The refined state chart is shown in Fig. 4. The state *further_location* is refined to contain three sub-states and two events. This switches the train to supervision mode, and starts EoA supervision. The train stays in this state until either the maximal safe front passes the OS area or the estimated front and speed leave the acknowledge window. The exiting transitions are changed to originate from the *start_OS_profile_wait* state instead of its super-state. This is possible as the sub-states correctly refine the super-state.

MACHINE m1_train_modes
REFINES m0_basic_flowchart
SEES c0_train_mode
VARIABLES

current_mode

INVARIANTS

inv1 : *current_mode* ∈ *t_train_modes*

EVENTS

Event *safe_front_passes_OS_area* ≡

extends *safe_front_passes_OS_area*

when

isin_ack_and_transition_or_isin_further_location : *ack_and_transition* = TRUE ∨
further_location = TRUE
isin_start_OS_profile_wait : *start_OS_profile_wait* = TRUE

then

enter_transition_and_ack : *transition_and_ack* := TRUE
leave_ack_and_transition : *ack_and_transition* := FALSE
leave_further_location : *further_location* := FALSE
leave_start_OS_profile_wait : *start_OS_profile_wait* := FALSE

end

Event *switch_to_OS_mode* ≡

```

extends switch_to_OS_mode
  when
    isin_ack_and_transition_or_isin_transition_and_ack : ack_and_transition = TRUE ∨
    transition_and_ack = TRUE
  then
    leave_ack_and_transition : ack_and_transition := FALSE
    enter_OS_mode : OS_mode := TRUE
    leave_transition_and_ack : transition_and_ack := FALSE
  end
Event front_and_speed_in_ack_window ≡
extends front_and_speed_in_ack_window
  when
    isin_further_location : further_location = TRUE
    isin_start_OS_profile_wait : start_OS_profile_wait = TRUE
  then
    enter_ack_and_transition : ack_and_transition := TRUE
    leave_further_location : further_location := FALSE
    leave_start_OS_profile_wait : start_OS_profile_wait := FALSE
  end
Event use_profile_OS_further_location ≡
extends use_profile_OS_further_location
  when
    isin_init_OS_procedure : init_OS_procedure = TRUE
  then
    leave_init_OS_procedure : init_OS_procedure := FALSE
    enter_further_location : further_location := TRUE
    enter_received_OS_profile : received_OS_profile := TRUE
  end
Event use_profile_OS_inside_area_mode_OS ≡
extends use_profile_OS_inside_area_mode_OS
  when
    isin_init_OS_procedure : init_OS_procedure = TRUE
    grd1 : current_mode = c_OS
  then
    enter_OS_mode : OS_mode := TRUE
    leave_init_OS_procedure : init_OS_procedure := FALSE
  end
Event use_profile_OS_inside_area_mode_SB_PT ≡
extends use_profile_OS_inside_area_mode_SB_PT
  when
    isin_init_OS_procedure : init_OS_procedure = TRUE
    grd1 : current_mode ∈ {c_SB, c_PT}
  then
    enter_ack_and_transition : ack_and_transition := TRUE
    leave_init_OS_procedure : init_OS_procedure := FALSE
  end
Event use_profile_OS_inside_area_mode_FS_LS_SR_UN_SN ≡
extends use_profile_OS_inside_area_mode_FS_LS_SR_UN_SN
  when
    isin_init_OS_procedure : init_OS_procedure = TRUE
    grd1 : current_mode ∈ {c_FS, c_LS, c_SR, c_UN, c_SN}
  then
    leave_init_OS_procedure : init_OS_procedure := FALSE
    enter_transition_and_ack : transition_and_ack := TRUE
  end
Event transition_supervision_mode ≡

```

```

when
    isin_received_OS_profile : received_OS_profile = TRUE
then
    leave_received_OS_profile : received_OS_profile := FALSE
    act1 : current_mode := c_supervision_mode
    enter_FS_LS_mode : FS_LS_mode := TRUE
end
Event transition_to_OS_mode ≡
begin
    act1 : current_mode := c_OS
end
END

```

4.4 Context 1 - Mode Profiles

This context extension introduces the type $t_mode_profile$ for mode profiles, t_train_fronts for train fronts (e.g., max safe front, estimated front), t_speed for train speed and $t_locations$ for on track locations.

The context also defines several functions, notably one which signals whether a mode profile specifies an OS area, one which signals whether a given train front overpasses the OS area for a specific mode profile, one that signals whether a train front and train speed are in the acknowledge window for a specific mode profile, one that signals whether a given train front is in the OS area of a given mode profile and finally a function that returns the EoA from a given profile.

CONTEXT c1_mode_profile
EXTENDS c0_train_mode
SETS

$t_mode_profile$
 t_train_fronts
 t_speed
 $t_locations$

CONSTANTS

$f_mode_profile_OS_mode$ indicates whether mode profile demands OS mode
 $f_safe_train_front_overpasses$
 $f_estimated_train_front_speed_in_window$
 $c_profile0$
 $f_safe_front_in_OS_area$
 $f_EoA_from_profile$
 c_loc0
 c_front0

AXIOMS

axm1 : $f_mode_profile_OS_mode \in t_mode_profile \rightarrow BOOL$
axm2 : $f_safe_train_front_overpasses \in t_train_fronts \times t_mode_profile \rightarrow BOOL$
 train front overpasses begin OS area
axm3 : $f_estimated_train_front_speed_in_window \in t_train_fronts \times t_mode_profile \times t_speed \rightarrow BOOL$
 est. train front and speed in ack window
axm4 : $c_profile0 \in t_mode_profile$
axm5 : $f_safe_front_in_OS_area \in t_train_fronts \times t_mode_profile \rightarrow BOOL$
axm6 : $f_EoA_from_profile \in t_mode_profile \rightarrow t_locations$

```

axm7 : c_loc0 ∈ t_locations
axm10 : c_front0 ∈ t_train_fronts
END

```

4.5 Machine 2 - Mode Profiles

The second refinement of the machine introduces the notion of mode profiles, train fronts (max safe and estimated) and the end of authority (EoA) location into the model. These are represented by the variables *EoA_loc*, *mode_profile_OS*, *safe_train_front* and *estimated_train_front*.

The train fronts can be changed by the events *update_estimated_front* and *update_safe_front*. The current values of the fronts, the current mode profile and its corresponding EoA are used as parameters for the Boolean functions that guard the events, e.g., for the event *safe_front_passes_OS_area* or for the event *front_and_speed_in_ack_window*.

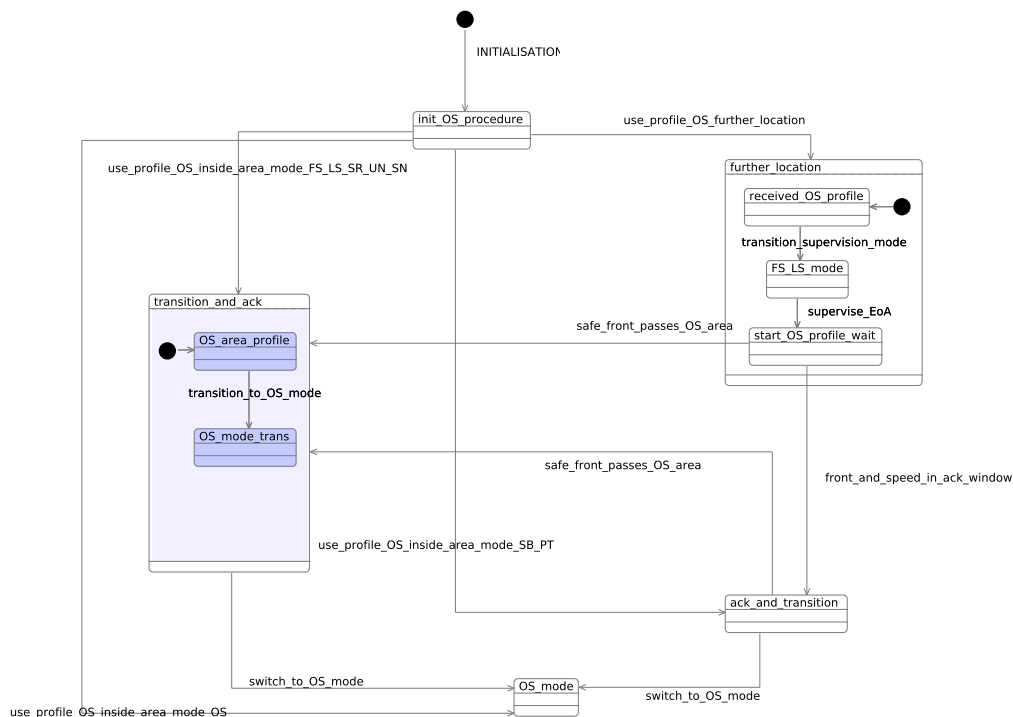


Figure 5. Second Refinement

The second refinement of the state machine is shown in Fig. 5. Here the state *transition_and_ack* is refined with two sub-states. The transition between the two new sub-states is *transition_to_OS_mode* which sets the current train mode to on-sight.

```
MACHINE m2_mode_profile
REFINES m1_train_modes
SEES c1_mode_profile
VARIABLES
```

EoA_loc
mode_profile_OS
safe_train_front
estimated_train_front

INVARIANTS

inv1 : *EoA loc* $\in t$ *locations*

```

    inv2 : mode_profile_OS ∈ t_mode_profile
    inv3 : safe_train_front ∈ t_train_fronts
    inv4 : estimated_train_front ∈ t_train_fronts
EVENTS
Event safe_front_passes_OS_area ≡
extends safe_front_passes_OS_area
    where

        isin_ack_and_transition_or_isin_further_location : ack_and_transition = TRUE ∨
        further_location = TRUE
        isin_start_OS_profile_wait : start_OS_profile_wait = TRUE
        grd1 : f_safe_train_front_overpasses(safe_train_front ↦ mode_profile_OS) = TRUE
        grd2 : l_safe_train_front ∈ t_train_fronts
    then

        enter_transition_and_ack : transition_and_ack := TRUE
        leave_ack_and_transition : ack_and_transition := FALSE
        leave_further_location : further_location := FALSE
        leave_start_OS_profile_wait : start_OS_profile_wait := FALSE
        enter_OS_area_profile : OS_area_profile := TRUE
    end
Event front_and_speed_in_ack_window ≡
extends front_and_speed_in_ack_window
    any

        l_train_speed
    where

        isin_further_location : further_location = TRUE
        isin_start_OS_profile_wait : start_OS_profile_wait = TRUE
        grd3 : l_train_speed ∈ t_speed
        grd1 : f_estimated_train_front_speed_in_window(estimated_train_front ↦ mode_profile_OS ↦
        l_train_speed) = TRUE
    then

        enter_ack_and_transition : ack_and_transition := TRUE
        leave_further_location : further_location := FALSE
        leave_start_OS_profile_wait : start_OS_profile_wait := FALSE
    end
Event update_estimated_front ≡
    any

        l_front
    where

    then
        grd1 : l_front ∈ t_train_fronts
    end
    act1 : estimated_train_front := l_front
Event update_safe_front ≡
    any

        l_front
    where

    then
        grd1 : l_front ∈ t_train_fronts
    end
    act1 : safe_train_front := l_front
END

```

4.6 Machine 3 - Driver Acknowledge

The third machine refinement introduces the driver acknowledgment. In two cases, the driver is asked to acknowledge. This is modeled by additional Boolean variables, two for acknowledging OS mode and two for acknowledging the service brake. Each time, one variable signals that the driver has been informed that he has to acknowledge, e.g., for the service brake this is the *currently_asking_driver_brake_ack* variable, and to signal the completed acknowledge there is the *driver_responded_brake_ack* variable. There is also the Boolean variable *service_brake* which signals the active service brake of the train.

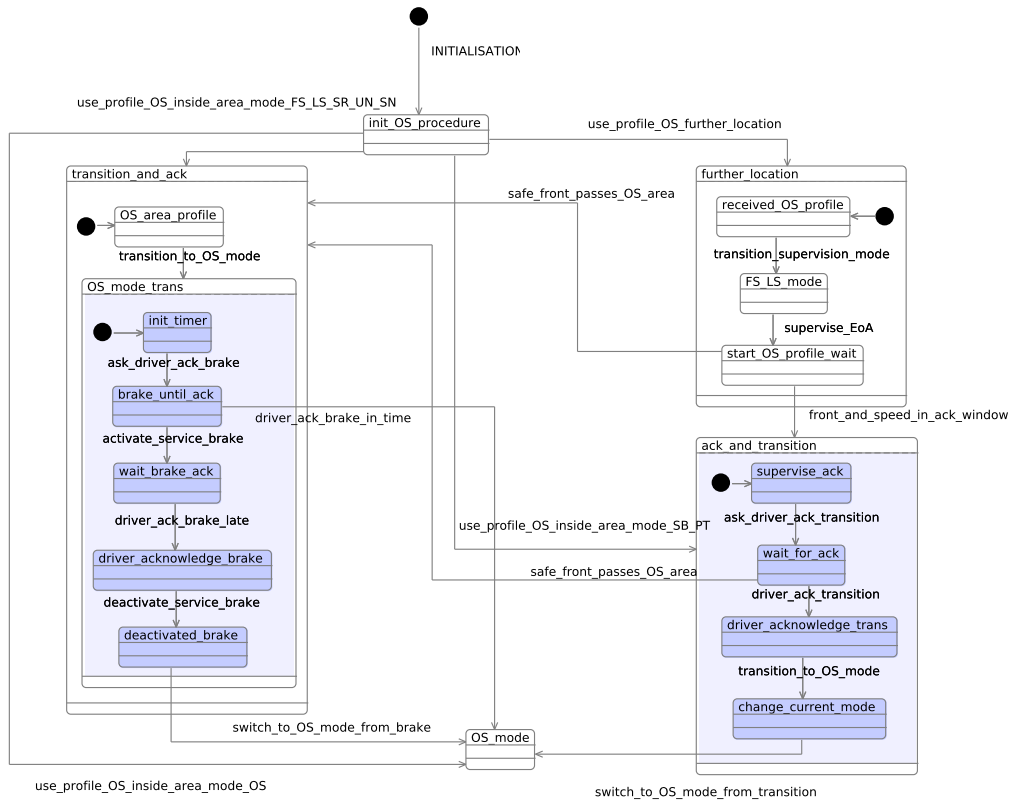


Figure 6. Third Refinement with Driver Acknowledge

The third refinement of the state machine is shown in Fig. 6. Here the two states *ack_and_transition* and *OS_mode_trans* are refined.

For *ack_and_transition* there are four new sub-states defined. There is first an event to ask the driver to acknowledge the switch to on-sight mode, then the OBU waits for the driver acknowledgment. If the max safe train front passes the OS area without driver acknowledge, then the *transition_and_ack* state is entered, else the train mode is switched to on-sight and the final state is entered. Here the outgoing transitions from the abstract *ack_and_transition* state are change to originate from *wait_for_ack* or *change_current_mode* respectively. Again this is possible as the sub-states correctly refine the abstract behavior of the super state.

The abstract *OS_mode_trans* state is refined by five sub-states. First the driver is asked to acknowledge the imminent service brake. If he does so in time, then the procedure finishes and the final state is entered, else the service brake is activated and stays activated until the driver acknowledges and the final state is entered.

At this refinement stage, it is possible to prove that whenever the final state is reached, the mode of the train is on-sight (*inv6*).

MACHINE m3_driver_ack
REFINES m2_mode_profile
SEES c1_mode_profile
VARIABLES

currently_asking_driver_OS_ack
driver_responded_OS_ack
service_brake_active
currently_asking_driver_brake_ack
driver_responded_brake_ack

INVARIANTS

inv6 : $OS_mode = TRUE \Rightarrow current_mode = c_OS$

EVENTS

Event *ask_driver_ack_brake* $\hat{=}$

when

isin_init_timer : *init_timer* = TRUE
grd1 : *currently_asking_driver_brake_ack* = FALSE

then

act1 : *currently_asking_driver_brake_ack* := TRUE
enter_brake_until_ack : *brake_until_ack* := TRUE
act2 : *driver_responded_brake_ack* := FALSE
leave_init_timer : *init_timer* := FALSE

end

Event *ask_driver_ack_transition* $\hat{=}$

when

isin_supervise_ack : *supervise_ack* = TRUE
grd1 : *currently_asking_driver_OS_ack* = FALSE

then

act1 : *currently_asking_driver_OS_ack* := TRUE
leave_supervise_ack : *supervise_ack* := FALSE
enter_wait_for_ack : *wait_for_ack* := TRUE
act2 : *driver_responded_OS_ack* := FALSE

end

Event *driver_ack_brake_in_time* $\hat{=}$

extends *switch_to_OS_mode*

when

isin_ack_and_transition_or_isin_transition_and_ack : *ack_and_transition* = TRUE \vee
transition_and_ack = TRUE
isin_brake_until_ack : *brake_until_ack* = TRUE
grd1 : *currently_asking_driver_brake_ack* = TRUE

then

leave_ack_and_transition : *ack_and_transition* := FALSE
enter_OS_mode : *OS_mode* := TRUE
leave_transition_and_ack : *transition_and_ack* := FALSE
leave_OS_mode_trans : *OS_mode_trans* := FALSE
leave_OS_area_profile : *OS_area_profile* := FALSE
act2 : *driver_responded_brake_ack* := TRUE
leave_brake_until_ack : *brake_until_ack* := FALSE
act1 : *currently_asking_driver_brake_ack* := FALSE

end

Event *driver_ack_brake_late* $\hat{=}$

when

grd1 : *currently_asking_driver_brake_ack* = TRUE
isin_wait_brake_ack : *wait_brake_ack* = TRUE

```

    then
        act1 : currently_asking_driver_brake_ack := FALSE
        enter_driver_acknowledge_brake : driver_acknowledge_brake := TRUE
        act2 : driver_responded_brake_ack := TRUE
        leave_wait_brake_ack : wait_brake_ack := FALSE
    end
Event driver_ack_transition ≡
    when
        grd1 : currently_asking_driver_OS_ack = TRUE
        isin_wait_for_ack : wait_for_ack = TRUE
    then
        act2 : driver_responded_OS_ack := TRUE
        enter_driver_acknowledge_trans : driver_acknowledge_trans := TRUE
        leave_wait_for_ack : wait_for_ack := FALSE
        act1 : currently_asking_driver_OS_ack := FALSE
    end
Event activate_service_brake ≡
    when
        grd1 : service_brake_active = FALSE
        isin_brake_until_ack : brake_until_ack = TRUE
    then
        act1 : service_brake_active := TRUE
        leave_brake_until_ack : brake_until_ack := FALSE
        enter_wait_brake_ack : wait_brake_ack := TRUE
    end
Event deactivate_service_brake ≡
    when
        grd1 : service_brake_active = TRUE
        isin_driver_acknowledge_brake : driver_acknowledge_brake = TRUE
    then
        enter_deactivated_brake : deactivated_brake := TRUE
        act2 : service_brake_active := FALSE
        act3 : driver_responded_brake_ack := FALSE
        leave_driver_acknowledge_brake : driver_acknowledge_brake := FALSE
    end
END

```

4.7 Machine 4 - Timeout

The fourth machine refinement introduces the timer and the timeout event for the acknowledge window for the driver. This refinement is done completely in the textual model, therefore the state machine as shown in Fig. 7 is left unchanged and there is no colored highlighting.

The timeout is represented by the Boolean variable *timer_expired* which is modified by the *expire_timer* event. The variable is used in the guards of *driver_ack_brake_in_time*, *driver_ack_brake_late* and *activate_service_brake*.

At this refinement stage, it is possible to prove that when the timer has expired and the train has transitioned to OS mode then the transition *driver_ack_brake_in_time* cannot be enabled (*inv2*), and in the state *brake_until_ack* the transition *activate_service_brake* is enabled (*inv4*).

```

MACHINE m4_timeout
REFINES m3_driver_ack
SEES c1_mode_profile

```

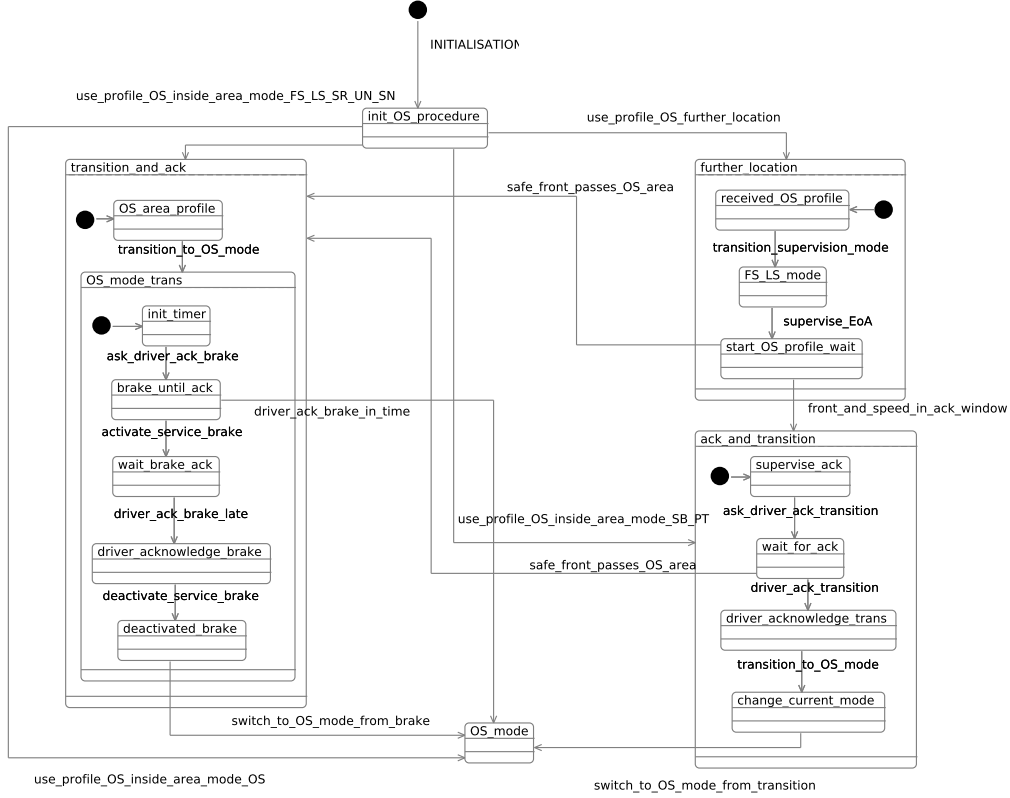


Figure 7. Fourth Refinement State Machine

VARIABLES

timer_expired

INVARIANTS

- inv2** : $timer_expired = TRUE \wedge OS_mode_trans = TRUE \Rightarrow$
 $\neg((ack_and_transition = TRUE \vee transition_and_ack = TRUE) \wedge$
 $brake_until_ack = TRUE \wedge$
 $currently_asking_driver_brake_ack = TRUE \wedge$
 $timer_expired = FALSE)$
 PROPERTY_5.9_02_01, timer expired and in OS_mode_trans state disables other transitions
- inv4** : $timer_expired = TRUE \wedge brake_until_ack = TRUE \Rightarrow$
 $(service_brake_active = FALSE \wedge$
 $brake_until_ack = TRUE \wedge$
 $timer_expired = TRUE)$
 PROPERTY_5.9_02_02, transition to activate brake is enabled

EVENTS

Event *driver_ack_brake_in_time* $\hat{=}$

extends *driver_ack_brake_in_time*

when

isin_ack_and_transition_or_isin_transition_and_ack : $ack_and_transition = TRUE \vee$
 $transition_and_ack = TRUE$
isin_brake_until_ack : $brake_until_ack = TRUE$
grd1 : $currently_asking_driver_brake_ack = TRUE$
grd2 : $timer_expired = FALSE$

then

leave_ack_and_transition : $ack_and_transition := FALSE$
enter_OS_mode : $OS_mode := TRUE$
leave_transition_and_ack : $transition_and_ack := FALSE$
leave_OS_mode_trans : $OS_mode_trans := FALSE$
leave_OS_area_profile : $OS_area_profile := FALSE$
act2 : $driver_responded_brake_ack := TRUE$

```

        leave_brake_until_ack : brake_until_ack := FALSE
        act1 : currently_asking_driver_brake_ack := FALSE
    end
Event driver_ack_brake_late ≡
extends driver_ack_brake_late
    when
        grd1 : currently_asking_driver_brake_ack = TRUE
        isin_wait_brake_ack : wait_brake_ack = TRUE
        grd2 : timer_expired = TRUE
    then
        act1 : currently_asking_driver_brake_ack := FALSE
        enter_driver_acknowledge_brake : driver_acknowledge_brake := TRUE
        act2 : driver_responded_brake_ack := TRUE
        leave_wait_brake_ack : wait_brake_ack := FALSE
    end
Event activate_service_brake ≡
extends activate_service_brake
    when
        grd1 : service_brake_active = FALSE
        isin_brake_until_ack : brake_until_ack = TRUE
        grd2 : timer_expired = TRUE
    then
        act1 : service_brake_active := TRUE
        leave_brake_until_ack : brake_until_ack := FALSE
        enter_wait_brake_ack : wait_brake_ack := TRUE
    end
Event expire_timer ≡
    when
        then
            grd1 : timer_expired = FALSE
        then
            act1 : timer_expired := TRUE
        end
END

```

4.8 Context 2 - Speed Limits

The third context extension adds the notion of the on-sight speed limit which is represented as the constant $c_OS_speed_limit$ of type t_speed . The context also adds the function $f_speed_exceeds$ which compares two speed values and returns $TRUE$ if the first argument exceeds the second.

```

CONTEXT c2_speed_limit
EXTENDS c1_mode_profile
CONSTANTS

```

```

    c_OS_speed_limit
    f_speed_exceeds

```

AXIOMS

```

axm1 : c_OS_speed_limit ∈ t_speed
      constant OS speed limit

axm2 : f_speed_exceeds ∈ t_speed × t_speed → BOOL
      f_speed_exceeds (x, y) is TRUE if speed x exceeds speed y, else FALSE

```

END

4.9 Machine 5 - Speed Supervision

The fifth refinement of the machine adds the notion of the current speed of the train to the model. This variable can be updated by two events *update_train_speed_brake* which can only be executed when the brake is active and only accepts speed as argument which does not exceed the current speed and *update_train_speed_no_brake* which requires that the brake is not active and accepts any speed as new value.

Once active, the service brake can now only be activated if the current speed of the train does not exceed the OS speed limit.

MACHINE m5_speed_supervision

REFINES m4_timeout

SEES c2_speed_limit

VARIABLES

current_speed

INVARIANTS

inv2 : $(\text{driver_acknowledge_brake} = \text{TRUE} \wedge$
 $f_speed_exceeds(\text{current_speed} \mapsto c_OS_speed_limit) = \text{TRUE} \wedge$
 $\text{driver_responded_brake_ack} = \text{TRUE}) \Rightarrow$
 $\text{service_brake_active} = \text{TRUE}$
 PROPERTY_5.9_03 driver acknowledge does not deactivate
 service brake if train speed exceeds OS speed limit

inv10 : $\text{transition_and_ack} = \text{TRUE} \Rightarrow$
 $((f_speed_exceeds(\text{current_speed} \mapsto c_OS_speed_limit) = \text{TRUE} \wedge$
 $\text{current_mode} = c_OS) \Rightarrow$
 $\text{service_brake_active} = \text{TRUE})$
 PROPERTY_5.9_01, brake is activated if mode is OS and current speed exceeds limit

EVENTS

Event deactivate_service_brake $\hat{=}$

extends deactivate_service_brake

when

grd1 : $\text{service_brake_active} = \text{TRUE}$
isin_driver_acknowledge_brake : $\text{driver_acknowledge_brake} = \text{TRUE}$
grd2 : $f_speed_exceeds(\text{current_speed} \mapsto c_OS_speed_limit) = \text{FALSE}$

then

enter_deactivated_brake : $\text{deactivated_brake} := \text{TRUE}$
act2 : $\text{service_brake_active} := \text{FALSE}$
act3 : $\text{driver_responded_brake_ack} := \text{FALSE}$
leave_driver_acknowledge_brake : $\text{driver_acknowledge_brake} := \text{FALSE}$

end

Event update_train_speed_brake $\hat{=}$

if brake is on new speed cannot exceed current speed

any

l_speed

where

grd1 : $l_speed \in t_speed$
grd2 : $\text{service_brake_active} = \text{TRUE}$
grd3 : $f_speed_exceeds(l_speed \mapsto \text{current_speed}) = \text{FALSE}$
grd4 : $\text{init_OS_procedure} = \text{TRUE} \vee \text{OS_mode} = \text{TRUE}$

then

act1 : $\text{current_speed} := l_speed$

end

Event update_train_speed_no_brake $\hat{=}$

any

l_speed

```

where
    grd1 : service_brake_active = FALSE
    grd2 : l_speed ∈ t_speed
    grd3 : driver_acknowledge_brake = FALSE
    grd4 : init_OS_procedure = TRUE ∨ OS_mode = TRUE
then
    act1 : current_speed := l_speed
end
END

```

At this refinement stage, it is possible to prove the two remaining safety properties from the D2.5 document: If the train is in the *driver_responded_brake_ack* state, then even if the driver has acknowledged the service brake activation, the service brake will not be deactivated if the *current_speed* exceeds the OS speed limit. And, if the train is in OS mode and the *current_speed* exceeds the speed limit, then the service brake is active.

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