

An Event-B Specification of CoffeeClub

This Event-B system is based on a model that appeared in the book: System Modelling & Design Using Event-B by Ken Robinson.

It illustrates how a an abstract machine describes the consistency of a single bank account. The refinement then add multiple membership accounts while still maintaining the single bank account.

It also illustrates the use of a witness to drop (or replace) a variable when refining an event.

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CONTEXT CoffeeClubCtx

1

SETS

1.1

MEMBER

AXIOMS

ax0: finite(MEMBER)

END

VARIABLES

2.1

piggybank The coffe club has a single bank account storing all its money.

INVARIANTS

inv1: *piggybank* $\in \mathbb{N}$ The bank account can be positive or zero, but not negative.

EVENT *INITIALISATION*

THEN

init_0: *piggybank* := 0

END

EVENT *FeedBank*

2.2

When money is put into the bank account we feed it.

ANY

amount_feed

WHERE

grd_1: *amount_feed* $\in 1..100$

THEN

act_1: *piggybank* := *piggybank* + *amount_feed*

END

EVENT *RobBank*

2.3

Likewise, when taking money, we rob it.

ANY

amount_rob

WHERE

grd_1: *amount_rob* $\in 1..50$ The cost of a coffe is 1 up to 50.

grd_2: *amount_rob* \leq *piggybank*

THEN

act_1: *piggybank* := *piggybank* − *amount_rob*

END

We now introduce the concept of member accounts, the sum of the member accounts should be the total piggy bank account.

REFINES *CoffeeClubMch*
SEES *CoffeeClubCtx*

VARIABLES

members
accounts
coffeeprice

INVARIANTS

inv1_1: $members \subseteq \text{MEMBER}$
inv1_2: $accounts \in members \rightarrow \mathbb{N}$
inv1_3: $coffeeprice \in 1..30$

3.1

EVENT *INITIALISATION*
EXTENDS *INITIALISATION*
THEN

init1_1: $members := \emptyset$
init1_2: $accounts := \emptyset$
init1_3: $coffeeprice := 1$

END

EVENT *SetPrice*
ANY

new_price

WHERE

grd0: $new_price \in 1..30$

THEN

act0: $coffeeprice := new_price$

END

3.2

EVENT *NewMember*
ANY

new_member

WHERE

grd0: $new_member \in \text{MEMBER}$
grd1: $new_member \notin members$

THEN

act0: $accounts(new_member) := 0$
act1: $members := members \cup \{new_member\}$

END

3.3

EVENT *Contribute*
REFINES *FeedBank*
ANY

3.4

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    contribution
    member
WHERE
    grd0:    contribution  $\in$  1..70
    grd1:    member  $\in$  members
    grd2:    member  $\in$  dom(accounts)
WITH
    amount_feed:    amount_feed = contribution
THEN
    act0:    accounts(member) := accounts(member) + contribution
    act1:    piggybank := piggybank + contribution
END

EVENT BuyCoffee
REFINES RobBank
ANY
    member_buy
WHERE
    grd1_1:    member_buy  $\in$  dom(accounts)
    grd1_2:    accounts(member_buy)  $\geq$  coffeeprice
    grd1_3:    coffeeprice  $\leq$  piggybank
WITH
    amount_rob:    amount_rob = coffeeprice
    The amount is replaced with the coffee price. Note that proof for amount_rob
     $\in$  1..50 is easily proven since the coffeeprice is defined as coffeeprice  $\in$  1..30
THEN
    act1_1:    accounts(member_buy) := accounts(member_buy) - coffeeprice
    act1_2:    piggybank := piggybank - coffeeprice
END

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3.5

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