Seminar LC 2 - Exerciții

A. Demonstrați, folosind tabelul de adevăr, dacă următoarele identități sunt adevărate:

(1) $(\bar{x}_1 + x_2)(\bar{x}_2 + \bar{x}_3\bar{x}_4) = \bar{x}_1\bar{x}_2 + (\bar{x}_1 + x_2)\bar{x}_3\bar{x}_4.$

(2)
$$\bar{x}_1 x_3 + x_2 (\bar{x}_1 + \bar{x}_4) = \bar{x}_1 x_3 + \bar{x}_1 x_2 + x_2 \bar{x}_4.$$

(3)
$$\overline{x_1}x_4 + \overline{x_2}\overline{x_3} = (x_1 + \overline{x_4})(x_2 + x_3).$$

(4)
$$\overline{x_1 \overline{x}_3 + \overline{x}_1 \overline{x}_2 x_4} = \overline{x}_1 (x_2 + \overline{x}_4) + x_3 (x_1 + x_2 + \overline{x}_4).$$

(5)
$$x_1 \bar{x}_2 x_3 + \bar{x}_2 (\bar{x}_1 \bar{x}_2 x_3 + \bar{x}_4) = \bar{x}_2 x_3 + \bar{x}_2 \bar{x}_4.$$

(6)
$$\overline{x_1 \bar{x}_3 \bar{x}_4 + \bar{x}_1 x_2} = \bar{x}_1 \bar{x}_2 + (x_1 + \bar{x}_2)(x_3 + x_4).$$

B. Să se obțină, pe cale analitică, FCD respectiv FCC pentru funcțiile de mai jos.

FCD

(1)

$$f(x_1, x_2, x_3) = \bar{x}_1 + x_2 \bar{x}_3 + \bar{x}_1 x_3.$$

(2)
$$f(x_1, x_2, x_3) = x_1(\bar{x}_2 + \bar{x}_3) + x_1 x_2 \bar{x}_3.$$

(3)
$$f(x_1, x_2, x_3) = x_1 \bar{x}_2 + x_3 + \bar{x}_1 x_2 \bar{x}_3.$$

(4)
$$f(x_1, x_2, x_3) = x_1(\bar{x}_2 + x_3) + \bar{x}_2\bar{x}_3.$$

(5)

$$f(x_1, x_2, x_3) = \bar{x}_2 x_3 + x_1 + \bar{x}_1 \bar{x}_2 \bar{x}_3.$$

FCC

(1)

$$f(x_1, x_2, x_3) = (\bar{x}_1 + x_2 + x_3)(x_1 + \bar{x}_2).$$

(2)

$$f(x_1, x_2, x_3) = x_1(\bar{x}_2 + \bar{x}_3)(x_1 + \bar{x}_3).$$

(3)

$$f(x_1, x_2, x_3) = (x_1 + \bar{x}_3)(\bar{x}_1 + x_2)\bar{x}_3.$$

(4)

$$f(x_1, x_2, x_3) = (\bar{x}_1 + x_2)(\bar{x}_2 + \bar{x}_3)(\bar{x}_1 + x_3).$$

(5)

$$f(x_1, x_2, x_3) = (x_1 + \bar{x}_2 + x_3)(x_2 + \bar{x}_3)x_2.$$