

$$a \cdot b \oplus a \cdot c \oplus b \cdot c \rightarrow a \cdot b + a \cdot c + b \cdot c$$

$$a \cdot b \oplus a \cdot c \oplus b \cdot c = (a \cdot b \oplus a \cdot c) \oplus b \cdot c$$

$$= ((a \cdot b \oplus a \cdot c) + b \cdot c) \oplus (a \cdot b \oplus a \cdot c) \cdot b \cdot c$$

$$= ((a \cdot b + a \cdot c) \oplus \overline{a \cdot b \cdot a \cdot c} + b \cdot c) \oplus (a \cdot b \cdot b \cdot c \oplus a \cdot c \cdot b \cdot c)$$

$$= (a \cdot b + a \cdot c) \oplus a \cdot b \cdot c + b \cdot c \oplus (a \cdot b \cdot c \oplus a \cdot b \cdot c) =$$

$$= (a \cdot b + a \cdot c) \oplus a \cdot b \cdot c + b \cdot c =$$

$$(a \cdot b \oplus a \cdot c) + b \cdot c + a \cdot b \cdot c =$$

$$a \cdot (b \oplus c) + a \cdot b \cdot c + b \cdot c =$$

$$= a(b \oplus c + bc) + b \cdot c =$$

$$= a(b\bar{c} + \bar{b}c + bc) + b \cdot c =$$

$$= a(b\bar{c} + bc + \bar{b}c + bc) + b \cdot c =$$

$$= a(\underbrace{b(\bar{c} + c)}_{=1} + \underbrace{(\bar{b} + b)c}_{=1}) + b \cdot c =$$

$$= a(b + c) + b \cdot c = a \cdot b + a \cdot c + b \cdot c$$

$$I_1: (a \oplus b) \cdot c = a \cdot c \oplus b \cdot c$$

$$I_2: a + b = a \oplus b \oplus a \cdot b$$

$$I_2': a \oplus b = (a + b) \oplus a \cdot b$$

$$x \oplus y = x \cdot \bar{y} + \bar{x} \cdot y$$

$$= 0$$

$$b \cdot c + a \cdot b \cdot c =$$

$$= (1 + a) \cdot b \cdot c$$

$$= 1$$

$X, Y = 1888754$. 1-sign; 3-exponent; 4-significant
 $\hookrightarrow \text{bias} = 2^{3-1} - 1 = 3 \hookrightarrow 8\text{-bits for a sign}$

$$X = 0.5625 = +1.001 \times 2^{-1}$$

$$x_E = -1 + \text{bias} = 2$$

$$Y = -3.75 = -1.111 \times 2^{+1}$$

$$y_E = +1 + \text{bias} = 4$$

$$A = 0 \text{ (sign)} \mid 1.001 \text{ (significant)} = 01001_{c_2} \quad E_1 = 2$$

$$M_{sn} = 1 \mid 1.111_{sn} = 10001_{c_2} \quad E_2 = 4$$

$$E := E_1 - E_2 = -2$$

$$A := \text{ARShift}(A)$$

$$A := 0001001$$

$$A + M: \quad \begin{array}{r} A = \overset{\text{carr}}{00010} \mid 01 \\ M = 10001 \mid + \\ \hline A = \overset{\text{carr}}{010011} \mid 01 \end{array}$$

$$E = \max(E_1, E_2) = 4 \quad \rightarrow \text{mantissa is negative}$$

$$A_n = 1 \mid 001101_{c_2} \Rightarrow \overset{\text{sign}}{1} \mid \underbrace{110011}_{\text{mantissa, unsigned}}_{sn}$$

$$\text{Resultat} = \overset{\text{sign}}{1} \mid 1.10011 \times 2^{E-\text{bias}} =$$

$$= -1.10011 \times 2^1 = -11.0011 = -3.1875$$

$$0.0011 = 11_{c_2} \times 2^{-4} = \frac{11_{c_2}}{16} = \frac{3}{16} = 0.1875$$

==

$$0.5625 - 3.75 = -3.1875 \leftarrow$$

$$Y = 0.5625 = +1.001 \times 2^{-1}$$

$$X = +3.75 = +1.111 \times 2^{+1}$$

$$Y_0 = 2$$

$$E_{\max} = 2^3 - 1 = 7$$

$$X_0 = 4$$

$$E_1 = 4$$

$$E_2 = 2$$

$$A_1 = 0.1111$$

$$A_2 = 0.1001$$

$$E = E_1 - E_2 = 2 \rightarrow n \gg 2$$

$$n = 0.001001$$

$$A + n$$

$$A: \begin{array}{c} \text{high} \\ 0.1111 \end{array}$$

$$n: \begin{array}{c} 0.001001 \end{array}$$

$$E = \max(E_1, E_2) = 4$$

$$A = \begin{array}{c} \text{count} \uparrow \\ \text{high} \downarrow \\ 0.1000101 \end{array}$$

$$A_{\text{count}} = 1 \text{ (from sign bit)}$$

$$E = 5$$

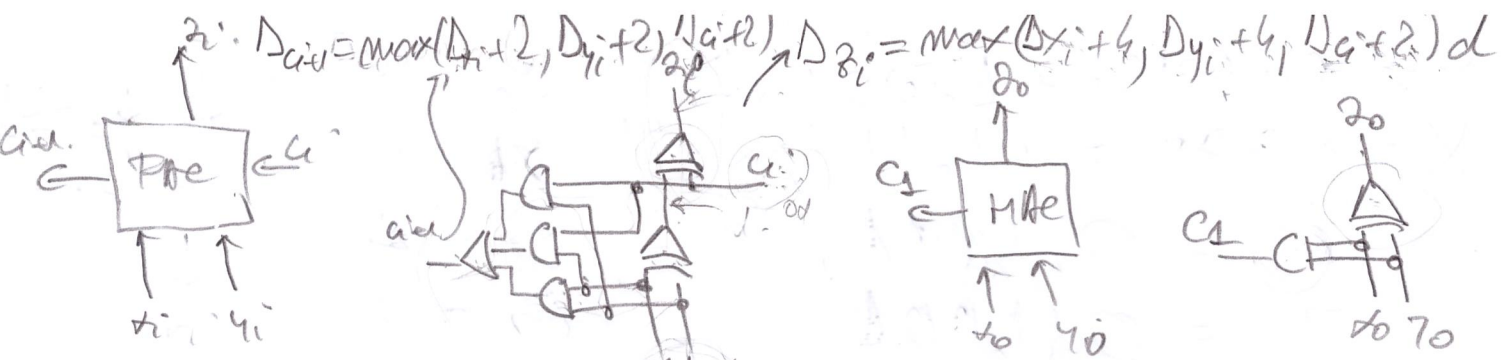
$$\text{Resultat: } +1.000101 \times 2^{E-5} = 0.0101 = \frac{5}{16}$$

$$1.000101 \times 2^2 = 4.001$$

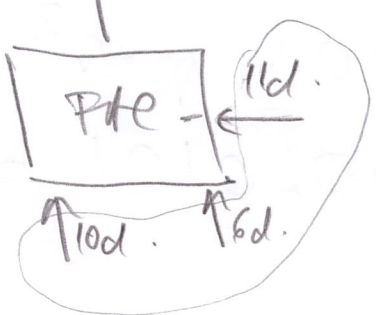
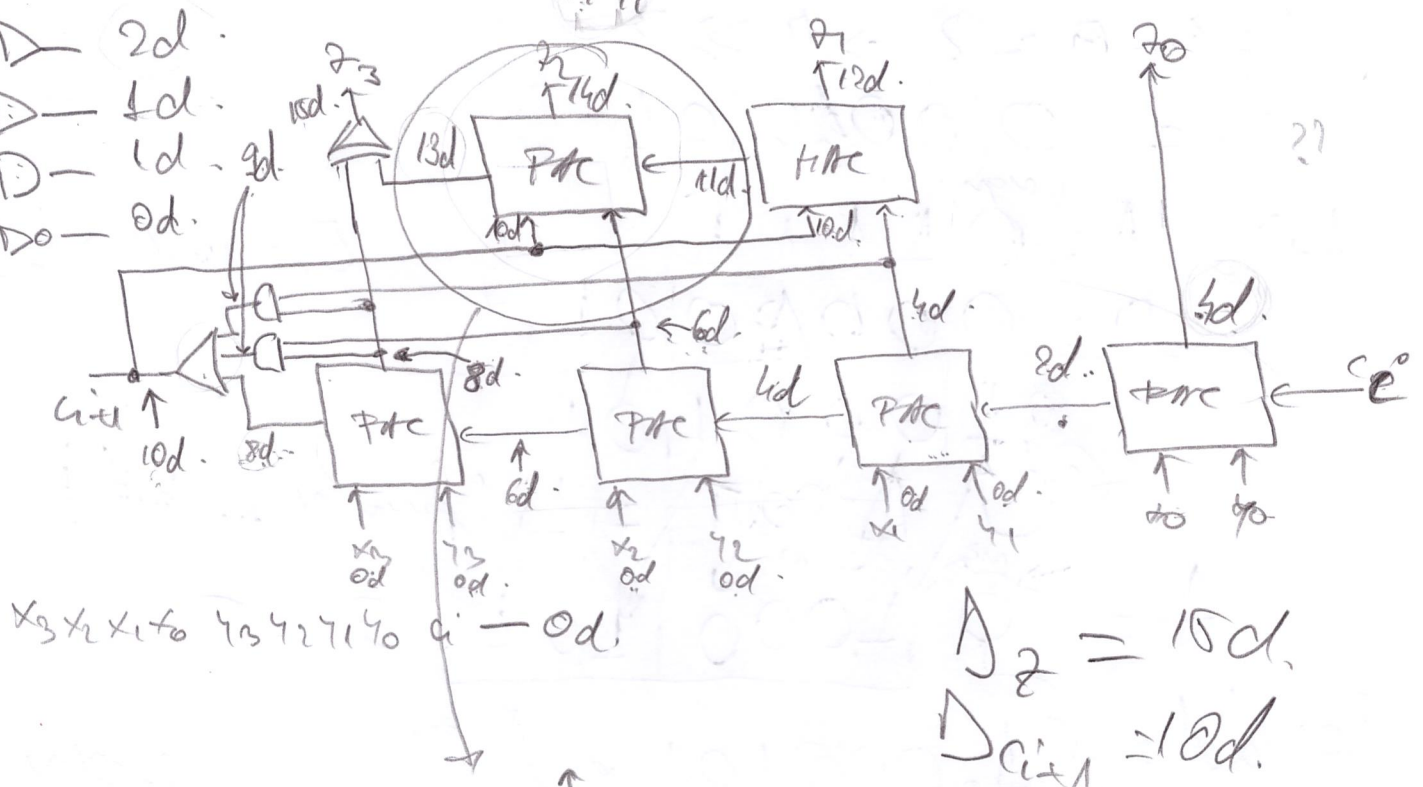
$$= 100.0101 = 4.3125$$

$$3.75 + 0.5625$$

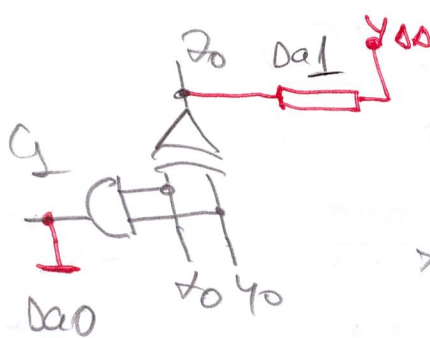
$$\begin{array}{r} 3.7500 \\ + 0.5625 \\ \hline 4.3125 \end{array}$$



- $\Rightarrow \Delta - 2d$
- $\Rightarrow \Delta - 4d$
- $\Rightarrow \Delta - 6d$
- $\Rightarrow \Delta - 8d$
- $\Rightarrow \Delta - 10d$



Here:



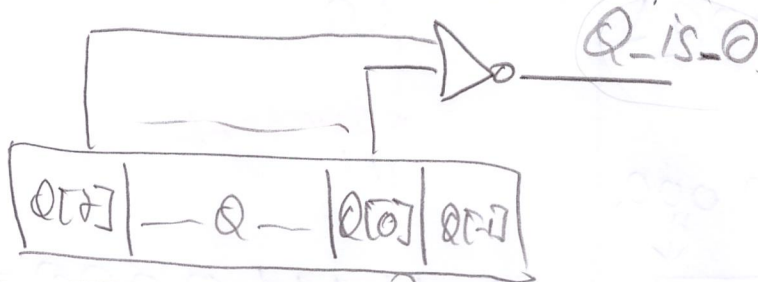
$$x_0, y_0 = 0, 1 \rightarrow z_0 = 1$$

$$\underline{c_1 = 0}$$

$$x_0, y_0 = 1, 1 \rightarrow z_0 = 0, (\bar{1})$$

$$c_1 = \underline{1} (\underline{0})$$

$$X = -3$$



[16; 15]
[4; 3]

INPUT: $P := \text{inBUS}$ } $\rightarrow \{c_0\}$
 $Q[7:0] := \text{inBUS}[7:0], Q[15:8] := 0; \rightarrow \{X\}$

TEST Q IS 0: if $Q\text{-is-}0 == 1$ then go to ...

TEST 4: if $Q[0]Q[1] == 01$ then $P := P + 1$, go to TEST 2; else

Register: $X = 12$
 Integer:

$$Y = -3$$

$$X = 01100c_2$$

$$Y = 111sn = 101c_2$$

F	A	Q	M	COUNT
0	000	000	001	000
	000	01100		
	000	00110		
	000	00011		
+	101			
	101			
+	110	10001		
	101			
	011			
	101	11000		
	110	11100		

COUNT MAX = 4
 COUNT MAX =
 m bits (magnitude
 of X)

$$100$$

$$* \text{COUNT} = 4$$

Integer Arithmetic
 RShift

$$P = 11011100c_2 =$$

$$10100100sn = -(31 + 4) = -36 \checkmark$$

$$X = 0.25 = 0.01010_{sn} = 0.010_{c2}$$

$$Y = -0.5 = 1.100_{sn} = 1.100_{c2}$$

A	Q	n	COUNT
0000	0010	1100	00
0000	0001		01
-1100			
0100			
0010	0000		10
+1100			
1110			
1111	0000		11
1111	0000		

$$\frac{0.25 * (-1.5)}{2}$$

$$= \frac{0.25 * 0.5}{1000} = -\frac{125}{1000} = -0.125$$

$$1001.0000 = 1001$$

$$P = 1.1110000_{c2} = 1.0010000_{sn}$$

$$= -0.001 * 2^{-3} = -\frac{1}{8} = -0.125$$

$$0.25 * (-1.5)$$

$$-1.5 = -1.1_{c2}$$

$$-1.5 = -0.25 * 2$$

$$P = [0.25 * (-0.25)] * 2$$