

# hypothesis test formula sheet

## One sample tests

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
one sample z-test	$\mu$ unknown, $\sigma^2$ known	$H_0 : \mu = \mu_0$	$Z_{\text{obs}} = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}} )$
one sample t-test	$\mu, \sigma^2$ unknown	$H_0 : \mu = \mu_0$	$T_{\text{obs}} = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$	$t_{n-1}$	$2 \cdot P(t_{n-1} < - T_{\text{obs}} )$
TODO	$\mu, \sigma^2$ unknown	$H_0 : \sigma^2 = \sigma_0^2$	$TODO = \frac{(n-1) \cdot s^2}{\sigma_0^2}$	$\chi_{n-1}^2$	TODO
sign test	none	$H_0 : m = m_0$	$B_{\text{obs}} = \sum_i I_{X_i > m_0}$	$\text{Binomial}(\sum_i I_{X_i \neq m_0}, \frac{1}{2})$	$2 \cdot \min(P(B \geq B_{\text{obs}}), P(B \leq B_{\text{obs}}))$

## Two sample tests

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
two sample z-test	$\mu_1, \mu_2$ unknown $\sigma_1^2, \sigma_2^2$ known	$H_0 : \mu_1 - \mu_2 = \delta_0$	$Z_{\text{obs}} = \frac{(\bar{x} - \bar{y}) - \delta_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}} )$
equal variance t-test	$\sigma_1^2 = \sigma_2^2$ $\mu_1, \mu_2$ unknown	$H_0 : \mu_1 - \mu_2 = \delta_0$	$T_{\text{obs}} = \frac{(\bar{x} - \bar{y}) - \delta_0}{s_{\text{pooled}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$	$t_{n-1}$	$2 \cdot P(t_{n_1+n_2-2} < - T_{\text{obs}} )$
welch's t-test	$\sigma_1^2 \neq \sigma_2^2$ $\mu_1, \mu_2$ unknown	$H_0 : \mu_1 - \mu_2 = \delta_0$	$T_{\text{obs}} = \frac{(\bar{x} - \bar{y}) - \delta_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$	$t_\nu$	$2 \cdot P(t_\nu < - T_{\text{obs}} )$
F-test for equal variance	$\sigma_1^2, \sigma_2^2$ $\mu_1, \mu_2$ unknown	$H_0 : \sigma_1^2 = \sigma_2^2$	$F_{\text{obs}} = \frac{s_1^2}{s_2^2}$	$F_{n_1-1, n_2-1}$	TODO

where

$$s_{\text{pooled}} = \sqrt{\frac{(n_1 - 1) \cdot s_1^2 + (n_2 - 1) \cdot s_2^2}{n_1 + n_2 - 2}} \quad (1)$$

$$\nu = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\frac{\left(\frac{s_1^2}{n_1}\right)^2}{n_1 - 1} + \frac{\left(\frac{s_2^2}{n_2}\right)^2}{n_2 - 1}} \quad (2)$$

### Paired two-sample tests (incomplete, don't trust these yet)

Suppose  $x_i$  is paired with  $y_i$ . Then let  $d_i = x_i - y_i$ .

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
paired z-test	$\mu$ unknown, $\sigma^2$ known	$H_0 : \mu_1 - \mu_2 = \delta_0$	$Z_{\text{obs}} = \frac{\bar{d} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}} )$
paired t-test	$\mu, \sigma^2$ unknown	$H_0 : \mu_1 - \mu_2 = \delta_0$	$T_{\text{obs}} = \frac{\bar{d} - \mu_0}{\frac{s}{\sqrt{n}}}$	$t_{n-1}$	$2 \cdot P(t_{n-1} < - T_{\text{obs}} )$
paired sign test	none	$H_0 : m_1 - m_2 = \delta_0$	TODO	TODO	TODO

### Related to linear regression and ANOVA

The tests for  $\beta_0$  and  $\beta_1$  are for simple linear regression only.

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
one-way anova / F-tests	TODO	TODO	TODO	TODO	TODO
tukey's honestly significant differences	TODO	TODO	TODO	TODO	TODO
T-test for $\beta_0$	TODO	TODO	TODO	TODO	TODO
T-test for $\beta_1$	TODO	TODO	TODO	TODO	TODO
overall F-test for linear model	TODO	TODO	TODO	TODO	TODO

### Nonparametric tests

- Kruskal-Wallis
- Rank-Sum
- Signed-Rank

Bootstrap and permutation (parametric, one and two sample, paired)