

hypothesis test formula sheet

One sample tests

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
one sample z-test	μ unknown, σ^2 known	$H_0 : \mu = \mu_0$	$Z_{\text{obs}} = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}})$
one sample z-test for a proportion	π unknown	$H_0 : \pi = \pi_0$	$Z_{\text{obs}} = \frac{\hat{\pi} - \pi_0}{\sqrt{\frac{\pi_0(1-\pi_0)}{n}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}})$
one sample t-test	μ, σ^2 unknown	$H_0 : \mu = \mu_0$	$T_{\text{obs}} = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$	t_{n-1}	$2 \cdot P(t_{n-1} < - T_{\text{obs}})$
chi-square test for variance	μ, σ^2 unknown	$H_0 : \sigma^2 = \sigma_0^2$	$T = \frac{(n-1) \cdot s^2}{\sigma_0^2}$	χ_{n-1}^2	TODO
sign test	none	$H_0 : m = m_0$	$B_{\text{obs}} = \sum_i I_{x_i > m_0}$	$\text{Binomial}(\sum_i I_{x_i \neq m_0}, \frac{1}{2})$	$2 \cdot \min(P(B \geq B_{\text{obs}}), P(B \leq B_{\text{obs}}))$

Two sample tests

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
two sample z-test	μ_1, μ_2 unknown σ_1^2, σ_2^2 known	$H_0 : \mu_1 - \mu_2 = \delta_0$	$Z_{\text{obs}} = \frac{(\bar{x} - \bar{y}) - \delta_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}})$
two sample z-test for a proportion	π_1, π_2 unknown	$H_0 : \pi_1 = \pi_2$	$Z_{\text{obs}} = \frac{\hat{\pi}_1 - \hat{\pi}_2}{\sqrt{\hat{\pi}(1 - \hat{\pi}) \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}})$
equal variance t-test	$\sigma_1^2 = \sigma_2^2$ unknown	$H_0 : \mu_1 - \mu_2 = \delta_0$	$T_{\text{obs}} = \frac{(\bar{x} - \bar{y}) - \delta_0}{s_{\text{pooled}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$	t_{n-1}	$2 \cdot P(t_{n_1+n_2-2} < - T_{\text{obs}})$
welch's t-test	$\sigma_1^2 \neq \sigma_2^2$ unknown	$H_0 : \mu_1 - \mu_2 = \delta_0$	$T_{\text{obs}} = \frac{(\bar{x} - \bar{y}) - \delta_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$	t_ν	$2 \cdot P(t_\nu < - T_{\text{obs}})$
F-test for equal variance	σ_1^2, σ_2^2 unknown	$H_0 : \sigma_1^2 = \sigma_2^2$	$F_{\text{obs}} = \frac{s_1^2}{s_2^2}$	F_{n_1-1, n_2-1}	TODO

where

$$s_{\text{pooled}} = \sqrt{\frac{(n_1 - 1) \cdot s_1^2 + (n_2 - 1) \cdot s_2^2}{n_1 + n_2 - 2}} \quad \nu = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right)^2}{\frac{\left(\frac{s_1^2}{n_1} \right)^2}{n_1 - 1} + \frac{\left(\frac{s_2^2}{n_2} \right)^2}{n_2 - 1}} \quad \hat{\pi} = \frac{n_1 \hat{\pi}_1 + n_2 \hat{\pi}_2}{n_1 + n_2} \quad (1)$$

Paired two-sample tests (incomplete, don't trust these yet)

Suppose x_i is paired with y_i . Then let $d_i = x_i - y_i$.

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
paired z-test	μ unknown, σ^2 known	$H_0 : \mu_1 - \mu_2 = \delta_0$	$Z_{\text{obs}} = \frac{\bar{d} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$	$N(0, 1)$	$2 \cdot P(Z < - Z_{\text{obs}})$
paired t-test	μ, σ^2 unknown	$H_0 : \mu_1 - \mu_2 = \delta_0$	$T_{\text{obs}} = \frac{\bar{d} - \mu_0}{\frac{s_d}{\sqrt{n}}}$	t_{n-1}	$2 \cdot P(t_{n-1} < - T_{\text{obs}})$
paired sign test	none	$H_0 : m_1 - m_2 = \delta_0$	$B_{\text{obs}} = \sum_i I_{d_i > \delta_0}$	$\text{Binomial}(\sum_i I_{d_i \neq \delta_0}, \frac{1}{2})$	$2 \cdot \min(P(B \geq B_{\text{obs}}), P(B \leq B_{\text{obs}}))$

Related to linear regression and ANOVA

The tests for β_0 and β_1 are for simple linear regression only.

name	known parameters	null hypothesis	test statistic	null distribution	p-value (two sided)
one-way anova / F-tests	TODO	TODO	TODO	TODO	TODO
tukey's honestly significant differences	TODO	TODO	TODO	TODO	TODO
T-test for β_0	TODO	TODO	TODO	TODO	TODO
T-test for β_1	TODO	TODO	TODO	TODO	TODO
overall F-test for linear model	TODO	TODO	TODO	TODO	TODO

Nonparametric tests

- Kruskal-Wallis
- Rank-Sum
- Signed-Rank

Bootstrap and permutation (parametric, one and two sample, paired)