class Monad m where

```
return :: a -> m a (>>=) :: m a -> (a -> m b) -> m b
```

unde:

- `m` este un constructor de tipuri
 `m a` tipul computatiilor care produc rezultate de tip a
- tipul `a -> m b` este tipul continuarilor
 Continuare: O functie care foloses,te un rezultat de tip `a` pentru a produce o computatie de tip `b`
- `(>>=)` este operatia de "secventiere" a computatiilor
- `return` este continuarea triviala

Pentru un `v` dat, produce computatia care va avea ca rezultat acel `v`.

Deci un monad in cod arata cam asa:

```
instance Monad Parser where  \begin{array}{lll} \text{return } x = \text{Parser } (\s \rightarrow [(x,s)]) \\ \text{m} >>= k &= \text{Parser } (\s \rightarrow [(y,u)] \\ & (x,\ t) \leftarrow \text{apply m s,} \\ & (y,\ u) \leftarrow \text{apply } (k\ x)\ t\ ] \\ \end{array}
```

Monadul maybe

```
instance Monad Maybe where
  Just x >>= k = k x
  Nothing >>= k = Nothing
  return x = Just x
```

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MyIO

```
module MyIO(MyIO, myPutChar, myGetChar, convert)
where
type Input
               = String
type Remainder = String
type Output
               = String
data MyIO a
             = MyIO (Input -> (a, Remainder,
                                          Output))
apply :: MyIO a -> Input -> (a, Remainder, Output)
apply (MyIO f) inp = f inp
myPutChar :: Char -> MyIO ()
myPutChar ch = MyIO ( inp -> ((), inp, [ch]))
myGetChar :: MyIO Char
myGetChar = MyIO (\ch:rem) \rightarrow (ch, rem, []))
instance Monad MyIO where
return x = MyIO (\langle inp - \langle x, inp, "" \rangle)
m \rightarrow>= k = MyIO (\np ->
                    let (x, rem1, out1) = apply m
                      inp in
                    let (y, rem2, out2) = apply (k
                      x) rem1 in
                    (y, rem2, out1++out2))
convert :: MyIO () -> IO ()
convert m = interact (\inp ->
                let (x, rem, out) = apply m inp
                in out)
```

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```
Parser
                                                               instance Monad Parser where
                                                                 return x = Parser (\s \rightarrow [(x,s)])
                                                                 m \rightarrow >= k = Parser (\s ->
                                                                                  [ (y, u) |
module Parser(Parser,apply,parse,char,spot,
                                                                                    (x, t) \leftarrow apply m s,
 token, star, plus, parseInt) where
                                                                                    (y, u) \leftarrow apply (k x) t 
import Data.Char
                                                               -- Parsers form a monad with sums
import Control.Monad
                                                                    class MonadPlus m where
-- The type of parsers
                                                                      mzero :: m a
newtype Parser a = Parser (String -> [(a, String)])
                                                                      mplus :: m a \rightarrow m a \rightarrow m a
-- Apply a parser
                                                               instance MonadPlus Parser where
apply :: Parser a -> String -> [(a, String)]
                                                                             = Parser (\s \rightarrow \])
apply (Parser f) s = f s
                                                                 mplus m n = Parser (\s \rightarrow apply m s ++ apply n
                                                               s)
-- Return parsed value, assuming at least one
successful parse
                                                               -- Parse one character
parse :: Parser a -> String -> a
                                                               char :: Parser Char
parse m s = one [x | (x,t) \leftarrow apply m s, t ==
                                                               char = Parser f
"" ]
                                                                 where
                 where
                                                                 f [] = []
                 one []
                                           = error "no
                                                                 f(c:s) = [(c,s)]
parse"
                 one [x]
                                           = x
                                                               -- guard :: MonadPlus m => Bool -> m ()
                 one xs | length xs \rightarrow 1 = error
                                                               -- quard False = mzero
"ambiguous parse"
                                                               -- quard True = return ()
-- Parsers form a monad
                                                               -- Parse a character satisfying a predicate (e.g.,
                                                               isDigit)
     class Monad m where
                                                               spot :: (Char -> Bool) -> Parser Char
       return :: a -> m a
                                                               spot p = do { c <- char; quard (p c); return c }</pre>
      ( >> = ) :: ma \rightarrow (a \rightarrow mb) \rightarrow mb
```

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```
-- Match a given character
token :: Char -> Parser Char
token c = spot (== c)
-- Perform a list of commands, returning a list of
values
-- sequence :: Monad m \Rightarrow [m \ a] \rightarrow m \ [a]
-- sequence []
-- sequence (m:ms) = do {
                          x \leftarrow m;
                          xs <- sequence ms;</pre>
                          return (x:xs)
-- match a given string (defined two ways)
match :: String -> Parser String
match []
           = return []
match(x:xs) = do {
                    y \leftarrow token x;
                   ys <- match xs;
                    return (y:ys)
match' :: String -> Parser String
match' xs = sequence (map token xs)
-- match zero or more occurrences
star :: Parser a -> Parser [a]
star p = plus p `mplus` return []
-- match one or more occurrences
plus :: Parser a -> Parser [a]
plus p = do x \leftarrow p
              xs <- star p
              return (x:xs)
```

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Parser folosit in evaluare de expresii

```
module Exp where
import Control.Monad
import Parser
data Exp = Lit Int
        | Exp :+: Exp
        | Exp :*: Exp
        deriving (Eq.Show)
evalExp :: Exp -> Int
evalExp(Lit n) = n
evalExp(e:+: f) = evalExp(e + evalExp(f))
evalExp(e:*:f) = evalExp(e:*)
parseExp :: Parser Exp
parseExp = parseLit `mplus` parseAdd `mplus`
parseMul
  where
  parseLit = do { n <- parseInt;</pre>
                 return (Lit n) }
  parseAdd = do { token '(';
                  d <− parseExp;</pre>
                 token '+';
                  e <- parseExp;
                 token ')';
                 return (d :+: e) }
 parseMul = do { token '(';
                  d <- parseExp;</pre>
                 token '*';
                  e <- parseExp;
```

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