

Appendix B: Fractal Terminology and Notation

Vocabulary:

A fractal is a never-ending pattern. Fractals are infinitely complex patterns that are self-similar across different scales. They are created by repeating a simple process over and over in an ongoing feedback loop. Driven by recursion, fractals are images of dynamic systems – the pictures of Chaos.

Equations used:

Complex Point:

Let $c = a + bi$

$$i^2 = -1$$

Formula $Z_{n+1} = Z_n^2 + c$

$$Z_0 = 0$$

The Modulus is the distance to the origin (much like the Pythagorean theorem for complex numbers):

$$Z = x + yi$$

$$|z| = |x + yi| = \sqrt{x^2 + y^2}$$

Let $c = c_r + c_i$

Let $z = z_r + z_i$

$$z' = z^2 + c$$

$$\begin{aligned} &= (z_r + z_i)(z_r + z_i) + c_r + c_i \\ &= z_r^2 + 2*z_r*z_i - z_i^2 + c_r + c_i \end{aligned}$$

$$z_r' = z_r^2 - z_i^2 + c_r$$

$$z_i' = 2*z_i*z_r + c_i$$