

LAB 3: COMBINATIONAL CIRCUITS (DESIGN)

This lab will continue exploring the uses and functions of various key combinational circuit components like encoders and decoders, multiplexers (MUX), and comparators. This time, it will be done in the context of tackling, improving, and upgrading a pre-existing system: a Trigger System for a particle accelerator.

A lot of particle accelerators produce a lot of collisions, decays, and other events, but not all computer systems will be able to store all of the data generated. A Trigger System is therefore necessary to determine whether the event is “interesting” enough for its data to be kept for further analysis.

This particular particle accelerator is having a rough time of it, due to a faulty, flawed, and outdated Trigger System. You are now tasked with debugging and upgrading it to suit the research group’s new needs.

(Logisim-evolution will be used in this lab to load the pre-designed circuits, and to implement upgrades.)

Part 1: Momentum Selector

One of the most important observables is the momentum of the incoming particles, s . The detector looks at 4 levels of momentum:

- Level 0, when $s \leq 0.5 \text{ TeV}$,
- Level 1, when $0.5 \text{ TeV} < s \leq 1.0 \text{ TeV}$,
- Level 2, when $1.0 \text{ TeV} < s \leq 1.5 \text{ TeV}$,
- and Level 3, when $1.5 \text{ TeV} < s \leq 2.0 \text{ TeV}$, etc.,
- All the way to

Correspondingly, every event produces a 4-bit output S from the detector, propagated into the Trigger, with S_0 as the LSB, and S_3 as the MSB, obeying the rule that, if an event

achieves momentum Level j , then $S_j = 1$ for $j = 0, \dots, j$, and $S_k = 0$ for any $k > j$. (E.g., if an event achieves momentum Level 2, then $S_0 = S_1 = S_2 = 1$, but $S_3 = 0$.)

The Momentum Selector takes two 4-bit inputs: the S input provided by the detector, and a 4-bit T input provided by the user. The T-input represents the threshold set by the user, with each T_L associated with Level L. If a user wants the Trigger to only accept events of Level L or above, then T_L is set to 1, while all other T_M are set to 0. The final output of the Momentum Selector must be 1 when an event is accepted (i.e., when the event momentum s is above the threshold set by the user), and 0 otherwise.

The present system is built only for 4 Levels of momentum s . Now, the research group wishes for better resolution, and wants the system upgraded for 8 Levels of momentum s . The group has already upgraded the detector and user interface to now provide 8-bits for inputs S and T.

However, the group budget will not provide for any additional comparators, or comparators with higher bits. You will, however, have access to NOT, AND, OR, and XOR gates.

Upgrade the Momentum Selector for 8 Levels of momentum s , so that the output “Trigger” is 1 if and only if the momentum s is greater than or equal to the threshold provided by the user.

Part 2: Particle Flagger

The particle accelerator’s detector is built to detect all 6 kinds of quarks: up, down, charm, strange, top, and bottom. As such, it also provides a 6-bit input into the Trigger system, Q, where Q_0 is the LSB and Q_5 is the MSB. Each $Q_j = 1$, when the quark associated with it is detected, and 0 if not. The quarks are each assigned to the Q inputs as follows (although you can reassign them, **but if you do so, state this clearly and explicitly**):

Quark	Q input bit
up	Q_0
down	Q_1
charm	Q_2
strange	Q_3
top	Q_4

bottom	Q_5
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Table 1: Assignments of quarks to Q 6-bit inputs

The user will also have access to another interface, allowing them to select for events to be accepted only when the chosen particles are detected. The user interface thus provides a 6-bit input C, where $C_j = 1$ if the user wants events with the associated quark detected.

Each C_j bit is associated with the same quark as each Q_j bit. (E.g., Q_3 is associated with the strange quark, and as such C_3 is also associated with the strange quark)

Design a Particle Flagger upgrade to the Trigger System, so that the output “Trigger” returns 1 if and only if the particles selected by the user are detected, in addition to the condition set in Part 1. *The budget is even tighter this go around, and you are limited to 6 components, only one of which can be an AND gate, and any AND/OR gates available can only take two inputs. Every component above the limit, or use of gates with more than one input will result in a point reduction of 2.*