

# ML course, 2016 fall

## What you should know:

### Week 1, 2 and 3.½: Basic issues in Probabilities and Information theory

**Read:** Chapter 2 from the *Foundations of Statistical Natural Language Processing* book by Christopher Manning and Hinrich Schütze, MIT Press, 2002.<sup>1</sup>

### Week 1: Random events

(slides 3-6 from <https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf>)

#### Concepts/definitions:

- sample space, random event, event space
- probability function
- conditional probabilities
- independent random events (2 forms);  
conditionally independent random events (2 forms)

#### Theoretical results/formulas:

- elementary probability formula:  
 $\frac{\# \text{ favorable cases}}{\# \text{ all possible cases}}$
- the “multiplication” rule; the “chain” rule
- “total probability” formula (2 forms)
- Bayes formula (2 forms)

**Exercises** illustrating the above concepts/definitions and theoretical results/formulas, in particular: proofs for certain properties derived from the *definition of the probability function* for instance:  $P(\emptyset) = 0$ ,  $P(\bar{A}) = 1 - P(A)$ ,  $A \subseteq B \Rightarrow P(A) \leq P(B)$

**Ciortuz et al.’s exercise book:** ch. *Foundations*, ex. 1-5 [6-7], 8, 39-42 [43-45]

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<sup>1</sup>For a more concise / formal introductory text, see *Probability Theory Review for Machine Learning*, Samuel Ieong, November 6, 2006 (<https://see.stanford.edu/materials/aimlcs229/cs229-prob.pdf>) and/or *Review of Probability Theory*, Arian Maleki, Tom Do, Stanford University.

## Week 2: Random variables, and (several) usual probabilistic distributions

(slides 7-9, 13-16, 36-37 [10-12, 17-22, 38-44]  
from <https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf>)

### Concepts/definitions:

- random variables;  
random variables obtained through function composition
- discrete random variables;  
probability mass function (pmf)  
examples: Bernoulli, binomial, geometric, Poisson distributions
- cumulative function distribution
- continuous random variables;  
probability density function (pdf)  
examples: Gaussian, exponential, Gamma, Laplace distributions
- expectation (mean), variance, standard variation; covariance. (**See definitions!**)
- multi-valued random functions;  
joint, marginal, conditional distributions
- independence of random variables;  
conditional independence of random variables

### Advanced issues:

- vector of random variables;  
covariance matrix for a vector of random variables;  
positive [semi-]definite matrices,  
negative [semi-]definite matrices
- the likelihood function (see *Estimating Probabilities*, additional chapter to the *Machine Learning* book by Tom Mitchell, 2016)

**Exercises** illustrating the above concepts/definitions and theoretical results/formulas, concentrating especially on:

- identifying in a given problem's text the underlying probabilistic distribution: either a basic one (e.g., Bernoulli, binomial, categorical, multinomial etc.), or one derived [by function composition or] by summation of identically distributed random variables
- computing probabilities
- computing means / expected values of random variables
- verifying the [conditional] independence of two or more random variables

**Ciortuz et al.'s exercise book:** ch. *Foundations*, ex. 9-16 [17-22], 46-55 [57-63], 64 (additional: ch. *Bayesian classification*, ex. 3)

### Implementation exercises for advanced issues:

1. CMU, 2009 fall, Geoff Gordon, HW3, pr. 3  
Implement *Linear Regression* and apply it to the task of predicting the level of PSA (Prostate Specific Agent) in prostate tissue, using a set of 8 variables (medical test results).<sup>2</sup>

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<sup>2</sup>A somehow simpler exercise, CMU, 2009 spring, Ziv Bar-Joseph, HW1, pr. 4, uses linear regression on the compute the quantity of insulin to be injected into a patient based on his/her blood sugar level.

### Theoretical results/formulas:

- for any discrete variable  $X$ :  
 $\sum_x p(x) = 1$ , where  $p$  is the pmf of  $X$   
for any continuous variable  $X$ :  
 $\int p(x) dx = 1$ , where  $p$  is the pdf of  $X$
- $E[X + Y] = E[X] + E[Y]$   
 $E[aX + b] = aE[X] + b$   
 $E[\sum_{i=1}^n a_i X_i] = \sum_{i=1}^n a_i E[X_i]$   
 $Var[aX] = a^2 Var[X]$   
 $Var[X] = E[X^2] - (E[X])^2$   
 $Cov(X, Y) = E[XY] - E[X]E[Y]$
- $X, Y$  independent variables  $\Rightarrow$   
 $Var[X + Y] = Var[X] + Var[Y]$
- $X, Y$  independent variables  $\Rightarrow$   
 $Cov(X, Y) = 0$ , i.e.  $E[XY] = E[X]E[Y]$

### Advanced issues:

- For any vector of random variables, the covariance matrix is symmetric and positive semi-definite.

**Ciortuz et al.'s exercise book:** ch. *Foundations*, ex. 25

### Week 3.<sup>1</sup>/<sub>2</sub>: Elements of Information Theory

(slides 28-31 [32-33] from <https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf>)

#### Theoretical results/formulas:

##### Concepts/definitions:

- entropy;
- specific conditional entropy;
- average conditional entropy;
- joint entropy;
- information gain (mutual information)

##### Advanced issues:

- relative entropy;
- cross-entropy

- $0 \leq H(X) \leq H(\underbrace{1/n, 1/n, \dots, 1/n}_{n \text{ times}}) = \log_2 n$
- $H(X, Y) = H(X) + H(Y|X) = H(Y) + H(X|Y)$   
(generalisation: the chain rule,  $H(X_1, \dots, X_n) = H(X_1) + H(X_2 | X_1) + \dots + H(X_n | X_1, \dots, X_{n-1})$ )
- $H(X, Y) = H(X) + H(Y)$  iff  $X$  and  $Y$  are indep.
- $IG(X; Y) = H(X) - H(X|Y) = H(Y) - H(Y|X)$
- $IG(X; Y) \geq 0$
- $IG(X; Y) = 0$  iff  $X$  and  $Y$  are independent

**Exercises** illustrating the above concepts/definitions and theoretical results/formulas, concentrating especially on:

- computing different types of entropies (see **Ciortuz et al.’s exercise book**: ch. *Foundations*, ex. 31, 32, 35, 65, 71 [37, 70]);  
(additional: ch. *Bayesian classification*, ex. 3)
- proof of some basic properties (see **Ciortuz et al.’s exercise book**: ch. *Foundations*, ex. 29, 30, [33, 34,] 36, [38], 66-69), including the functional analysis of the entropy of the Bernoulli distribution, as a base for drawing its plot.

## Week 3.<sup>2</sup>/<sub>2</sub>, 4 and 5: Decision Trees

**Read:** Chapter 3 from Tom Mitchell's *Machine Learning* book.

### Important Note:

See the Overview (rom.: “Privire de ansamblu”) document for Ciortuz et al.'s exercise book, chapter *Decision Trees*. It is in fact a “road map” for what we will be doing here. (This *note* applies also to all chapters.)

### Week 3.<sup>2</sup>/<sub>2</sub>, 4:

decision trees and the ID3 algorithm: applications;

properties of decision trees;

analysis of the ID3 algorithm (as an algorithm *per se*):

**Ciortuz et al.'s exercise book**, ch. *Decision trees*, ex. 1-4, 8, 21a, 28-36, 47

- extensions to the ID3 algorithm:

- handling of attributes with many values:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 13

- handling of attributes with costs:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 14

- using other impurity measures as local optimality criterion in ID3:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 15

### Week 5:

- extensions to the ID3 algorithm:

- handling of continuous attributes:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 9-11, 39-41

- decision surfaces, decision boundaries:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 9, 40, and ch. *Instance-based learning*, ex. 11b

- analysis: ID3 as a Machine Learning algorithm;

- *inductive bias* for ID3:

[LC: a hierarchical structure of the model/knowledge, compatibility/consistency with the data, and]

compactness of the resulting decision tree;

- error analysis/computation: training error, validation error, n-fold cross-validation, CVLOO

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 5-7, 21d, 37-38

- ID3 as eager learner:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 16

- ID3 and [non-]robustness to noises, and *overfitting*:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 9, 21bc, 40

- *pruning* strategies for decision trees:

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 19-20, 45-46

- other issues (optional):

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 12, 17-18, 42-44

### Important Note:

Some of the exercises listed above (for weeks 4 and 5) would be done in class (i.e., at seminars) in an easier/nicer way if students would priorily do at home the exercise 31, which asks for the **implementation** of the **information gain** (and also entropy, conditional specific entropy and conditional average entropy), starting from the counts (i.e., data partitions) associated to the leaf nodes of a **decision stump**. This implementation could be later extended to an implementation of ID3 algorithm (the basic form); see ex. 58.

### Implementation exercises:

0. CMU, 2012 fall, T. Mitchell, Z. Bar-Joseph, HW1, pr. 2

Given a Matlab/Octave implementation for ID3, work on synthetic, noisy data, and study the relationship between model complexity, training set size, train and test accuracy;

1. CMU, 2012 spring, Roni Rosenfeld, HW3

Complete a given C (incomplete) implementation for ID3; work on a simple example (Play Tennis from TM's ML book) and on a real dataset (Agaricus-Lepiota Mushrooms); perform *reduced-error* (*top-down vs. bottom-up*) *pruning* to cope with *overfitting*.

CMU, 2011 spring, T. Mitchell, A. Singh, HW1, pr. 3

Similar to the above one, except that *pruning* a node is conditioned on getting at least an  $\epsilon$  increase in accuracy; dataset: mushrooms.<sup>3</sup>

◦ CMU, 2008 spring, T. Mitchell, HW1, pr. 2

Asked for doing an ID3 implementation, including *reduced-error pruning* and *rule-based pruning*; work on a real dataset: German Credit Approval.

See the interesting Note at the end of the 'german-description.txt' file!

◦ CMU, 2009 spring, Tom Mitchell, HW1

Do an ID3 implementation, including *rule post-pruning*; work on a real dataset: predicting the votes in the US House of Representatives.

2. CMU, 2011 fall, T. Mitchell, A. Singh, HW1, pr. 2

Working with continuous attributes, complete a given a Matlab/Octave implementation for ID3, perform *reduced-error pruning*; implement another splitting criterion: the *weighted misclassification rate*; work on a real dataset: Breast Cancer.

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<sup>3</sup>A similar exercise — CMU, 2011 spring, Roni Rosenfeld, HW3 — uses a chess dataset.

## Week 6 and 7: Bayesian Classifiers

**Read:** Chapter 6 from Tom Mitchell's *Machine Learning* book (except subsections 6.11 and 6.12.2).

### Week 6:

Bayes' theorem:

Ciortuz et al.'s exercise book, ch. *Foundations*, ex. 6-7, 43-45;

classes of machine learning hypotheses: MAP hypotheses vs. ML hypotheses:

Ciortuz et al.'s exercise book, ch. *Bayesian classification*, ex. 1-3, 12-13, 21, 32

application of Naive Bayes and Joint Bayes algorithms:

Ciortuz et al.'s exercise book, ch. *Bayesian classification*, ex. 4-7, 22-26

### Week 7:

computation of the [training] error rate of Naive Bayes:

Ciortuz et al.'s exercise book, ch. *Bayesian classification*, ex. 8-10, 27-29;

some properties of Naive Bayes and Joint Bayes algorithms:

Ciortuz et al.'s exercise book, ch. *Bayesian classification*, ex. 11, 33;

comparisons with other classifiers:

Ciortuz et al.'s exercise book, ch. *Bayesian classification*, ex. 30-31.

### Implementation exercises:

0. CMU, 2010 fall, Ziv Bar-Joseph, HW2, pr. 4

Implement the Naive Bayes classification algorithm,  
and perform CVLOO on a toy ("weather prediction") dataset;  
do *feature selection* based on CVLOO.

1. Stanford, 2012 spring, Andrew Ng, pr. 6

Implement the Naive Bayes (train and test) algorithm;  
use it as a spam filter on a subset of the Ling-Spam dataset.

2. CMU, 2011 spring, Tom Mitchell, HW2, pr. 3

Implement the Naive Bayes classification algorithm and perform  $n$ -ary classification on the *20 Newsgroups* dataset;

for the  $P(X_i|Y)$  parameters, do MAP estimation (instead of MLE) using as prior the Dirichlet distribution;<sup>4</sup>

identify the *key words* (for classification) using *conditional entropy*; analyse its effectiveness relative to the *information gain*.

## Week 8: midterm EXAM

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<sup>4</sup>An earlier exercise, CMU, 2009 spring, T. Mitchell, HW3, pr. 2, centered on Naive Bayes and the MAP estimation with Dirichlet prior, but instead of asking the student to perform  $n$ -ary classification (on the 20 newsgroups dataset), it limited itself to binary classification on a much simpler dataset: hokey vs. baseball newsgroups. A similar exercise — CMU, 2014f, W. Cohen and Z. Bar-Joseph, HW2, pr. 6 — uses a simple measure for feature (i.e. keyword) selection, and classifies texts from The Economist and The Onion.

## Errata la

### *Exerciții de învățare automată, versiunea septembrie 2017*

1. cap. *Fundamente*, ex. 2, pag. 23, rândul 12 de jos:  
orice  $p \in (0, 1) \longrightarrow p = 1/2$
2. cap. *Fundamente*, ex. 33, pag. 66, rândul 6 de sus:  
d. Similar,  $\longrightarrow$  Similar,
3. cap. *Fundamente*, ex. 34, pag. 69, rândul 8 de jos:  
 $-\sum_x p(x) \log \frac{p(x)}{q(x)} \longrightarrow -\sum_x p(x) \log \frac{q(x)}{p(x)}$
4. cap. *Fundamente*, ex. 34, pag. 69, rândul 6 de jos:  
 $KL(p||q) \geq 0 \longrightarrow KL(p||q) = 0$
5. cap. *Fundamente*, ex. 70, pag. 87, rândul 3 de sus:  
 $CH(P_{true}, P_A), CH(P_{true}, P_A) \longrightarrow CH(P_{true}, P_A), CH(P_{true}, P_B)$
6. cap. *Arbori de decizie*, ex. 11, pag. 155, la al treilea compas de decizie, eticheta de pe ramura din dreapta:  
 $T \longrightarrow N$
7. cap. *Arbori de decizie*, ex. 11, pag. 155, în primul desen (mai precis, arborele de decizie cu două niveluri de test), la al treilea nod de decizie:  
 $- \longrightarrow +$   
(Alexandra Minghel, studentă FII, anul III)
8. cap. *Arbori de decizie*, ex. 11, pag. 156, nota de subsol 57:  
 $322.5 \longrightarrow 232.5$  (la toate cele 4 apariții)
9. cap. *Arbori de decizie*, ex. 11, pag. 157, rândul 1 de sus:  
Confrom  $\longrightarrow$  Conform
10. cap. *Arbori de decizie*, ex. 22, pag. 181, rândul 15 de jos:  
cu sunt  $\longrightarrow$  cum sunt
11. cap. *Arbori de decizie*, ex. 22, pag. 181, rândul 1 de jos:  
deciât  $\longrightarrow$  decât
12. cap. *Arbori de decizie*, ex. 22, pag. 182, rândul 2 de sus:  
diminueaza probabilitatea alocată instanțelor incorect clasificate  $\longrightarrow$  diminueaza probabilitatea alocată instanțelor corect clasificate  
(Lucian Nevoe, student FII, master)
13. cap. *Arbori de decizie*, ex. 22, pag. 184, rândul 4 de jos:  
 $\frac{\partial}{\partial \alpha_m} \longrightarrow \frac{\partial}{\partial \alpha_t}$
14. cap. *Arbori de decizie*, ex. 23, pag. 185, în tabelul din dreapta jos:  
eticheta (adică  $y_i$ ) pentru  $x_7$  trebuie să fie  $-1$  (în loc de  $+1$ )
15. cap. *Arbori de decizie*, ex. 23, pag. 186, rândul 5 de jos, exceptând notele de subsol:  
perchi  $\longrightarrow$  perechi
16. cap. *Arbori de decizie*, ex. 23, pag. 187, în primul tabel, linia din mijloc, ultima coloană:  
 $\frac{2}{9} + \frac{2}{9} = \frac{2}{3} \longrightarrow \frac{4}{9} + \frac{2}{9} = \frac{2}{3}$

17. cap. *Arbori de decizie*, ex. 23, pag. 187, în al doilea tabel, linia din mijloc, penultima și ultima coloană:  

$$\frac{1}{9} + \frac{2}{9} = \frac{2}{9} \longrightarrow \frac{2}{9} + \frac{1}{9} = \frac{1}{3}$$
și respectiv  

$$\frac{1}{3} \longrightarrow \frac{2}{9}$$
18. cap. *Arbori de decizie*, ex. 23, pag. 188, rândul 14 de jos:  
 $h1 \longrightarrow h_1$
19. cap. *Arbori de decizie*, ex. 23, pag. 189, rândul 1 de jos, exceptând formulele:  
distribuții  $\longrightarrow$  distribuții
20. cap. *Arbori de decizie*, ex. 23, pag. 189, rândul 2 de sus (din *Observația 2*):  
 $X_2 \geq 7/2 \longrightarrow X_2 < 7/2$
21. cap. *Arbori de decizie*, ex. 23, pag. 190, rândul 1 de jos:  
 $X_1 \geq 5/2 \longrightarrow X_1 < 5/2$
22. cap. *Arbori de decizie*, ex. 2, pag. 231, rândul 24 de jos:  
„...ușă!”  $\longrightarrow$  „...ușă!”
23. cap. *Arbori de decizie*, ex. 2, pag. 231, rândul 14 de jos:  
„...inițial!”  $\longrightarrow$  „...inițial?”
24. cap. *Învățare bazată pe memorare*, ex. 5, pag. 294, rândul 9 de sus:  
sunt prezentate  $\longrightarrow$  este prezentată
25. cap. *Învățare bazată pe memorare*, ex. 9, pag. 303, rândul 14 de sus:  
aplicațiile practice care  $\longrightarrow$  aplicațiile practice în care
26. cap. *Clusterizare*, ex. 11, pag. 348, rândul 6 de jos:  
instanțele  $\longrightarrow$  instanțele
27. cap. *Clusterizare*, ex. 11, pag. 362, rândurile 2 și 4 de jos:  
distribuții  $\longrightarrow$  distribuții
28. cap. *Clusterizare*, ex. 11, pag. 362, rândul 3 de jos:  
fiindcă funcția  $\longrightarrow$  fiindcă funcția
29. cap. *Clusterizare*, ex. 30, pag. 390, rândul 19 de jos:  
sunt situate  $\longrightarrow$  sunt situați