

# ML course, 2016 fall

## What you should know:

### Week 1, 2 and 3. $\frac{1}{2}$ : Basic issues in Probabilities and Information theory

**Read:** Chapter 2 from the *Foundations of Statistical Natural Language Processing* book by Christopher Manning and Hinrich Schütze, MIT Press, 2002, and/or *Probability Theory Review for Machine Learning*, Samuel Ieong, November 6, 2006 (<https://see.stanford.edu/materials/aimlcs229/cs229-prob.pdf>).

### Week 1: Random events

(slides #3-#6 from <https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf>)

#### Concepts/definitions:

- event/sample space, random event
- probability function
- conditional probabilities
- independent random events (2 forms);  
conditionally independent random events (2 forms)

#### Theoretical results/formulas:

- elementary probability formula:  
 $\frac{\# \text{ favorable cases}}{\# \text{ all possible cases}}$
- the “multiplication” rule; the “chain” rule
- “total probability” formula (2 forms)
- Bayes formula (2 forms)

**Exercises** illustrating the above concepts/definitions and theoretical results/formulas, in particular: proofs for certain properties derived from the *definition of the probability function* for instance:  $P(\emptyset) = 0$ ,  $P(\bar{A}) = 1 - P(A)$ ,  $A \subseteq B \Rightarrow P(A) \leq P(B)$

**Ciortuz et al.’s exercise book:** ch. 1, ex. 1-5 [6-7], 8, 39-42 [43-45]

## Week 2: Random variables

(slides #7-#16 [#35-#44] from <https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf>)

### Concepts/definitions:

- random variables;  
random variables obtained through function composition
- discrete random variables;  
probability mass function (pmf)  
examples: Bernoulli, binomial, geometric, Poisson distributions
- cumulative function distribution
- continuous random variables;  
probability density function (pdf)  
examples: Gaussian, exponential, Gamma distributions
- expectation (mean), variance, standard variation; covariance. (**See definitions!**)
- multi-valued random functions;  
joint, marginal, conditional distributions
- independence of random variables;  
conditional independence of random variables

### Advanced issues:

- the likelihood function (see also Week 12)
- vector of random variables;  
covariance matrix for a vector of random variables;  
positive [semi-]definite matrices,  
negative [semi-]definite matrices

**Exercises** illustrating the above concepts/definitions and theoretical results/formulas, concentrating especially on:

- identifying in a given problem's text the underlying probabilistic distribution: either a basic one (e.g., Bernoulli, binomial, categorical, multinomial etc.), or one derived [by function composition or] by summation of identically distributed random variables
- computing probabilities
- computing means / expected values of random variables
- verifying the [conditional] independence of two or more random variables

**Ciortuz et al.'s exercise book:** ch. 1, ex. 9-16 [17-22], 46-55 [57-63], 64

### Implementation exercises for advanced issues:

1. CMU, 2009 fall, Geoff Gordon, HW3, pr. 3  
Implement *Linear Regression* and apply it to the task of predicting the level of PSA (Prostate Specific Agent) in prostate tissue, using a set of 8 variables (medical test results).<sup>1</sup>
2. CMU, 2014 fall, William Cohen, Ziv Bar-Joseph, HW3, pr. 1  
Implement *Logistic Regression* and apply it to the task of hand-written character recognition.<sup>2</sup>

<sup>1</sup>A somehow simpler exercise, CMU, 2009 spring, Ziv Bar-Joseph, HW1, pr. 4, uses linear regression on the compute the quantity of insulin to be injected into a patient based on his/her blood sugar level.

<sup>2</sup>A similar exercise, CMU, 2009 spring, Ziv Bar-Joseph, HW2, pr. 4.1-2, applies logistic regression (LR) on the *Breast Cancer* dataset [while pr. 4.3-4 compares LR with the Rosenblatt *perceptron* on this dataset].

### Theoretical results/formulas:

- for any discrete variable  $X$ :  
 $\sum_x p(x) = 1$ , where  $p$  is the pmf of  $X$   
for any continuous variable  $X$ :  
 $\int p(x) dx = 1$ , where  $p$  is the pdf of  $X$
- $E[X + Y] = E[X] + E[Y]$   
 $E[aX + b] = aE[X] + b$   
 $Var[aX] = a^2 Var[X]$   
 $Var[X] = E[X^2] - (E[X])^2$   
 $Cov(X, Y) = E[XY] - E[X]E[Y]$
- $X, Y$  independent variables  $\Rightarrow$   
 $Var[X + Y] = Var[X] + Var[Y]$
- $X, Y$  independent variables  $\Rightarrow$   
 $Cov(X, Y) = 0$ , i.e.  $E[XY] = E[X]E[Y]$

### Advanced issues:

- For any vector of random variables, the covariance matrix is symmetric and positive semi-definite.

**Ciortuz et al.'s exercise book:** ch. 1, ex. 25

◦ CMU, 2014 fall, W. Cohen, Z. Bar-Joseph, HW3, pr. 1.4-6

Implement *Multinomial Logistic Regression* and apply it to the *ORL Faces* dataset [while pr. 1.1-3,7 compares (M)LR with *K*-NN, Gaussian Naive Bayes and Gaussian Joint Bayes on this dataset].

3. CMU, 2010 fall, Ziv Bar-Joseph, HW2, pr. 4

Study the regularization effect for logistic regression, using L2 and (especially) L1 norm, especially for *feature selection*. Work on the *communities and crime* dataset.