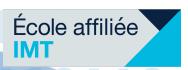




Replicated Data Consistency for Large Scale Distributed Systems

- Operational Transformation Approaches Conflict-free Replicated Data Structures
- Gérald Oster,
 Associate Professor, TELECOM Nancy, Université de Lorraine
 COAST Team, LORIA, Université de Lorraine, Inria, CNRS











CAP Theorem [GL02]

- A system without network partition, can achieve consistency + availability
 - Client and storage system are part of the same environment
- In a large-scale distributed systems, network partitions exist
- Consistency and availability cannot be both achieved
 - Relax consistency, maintain availability
 - Maintain consistency, tolerate unavailability under certain conditions

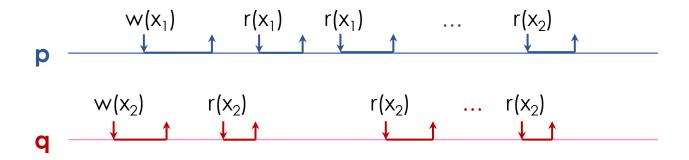
Optimistic Replication

- To sidestep CAP theorem [GL02], a first solution is to avoid synchronizing replicas. Replicas simply reconcile their copies in the background.
- Trade-off between consistency and availability
 - allows replicas to diverge
- This approach is named lazy [LLS90], or optimistic replication [SS05]
- Examples: Bayou, Amazon \$3, etc.

Consistency in Distributed Systems Eventual Consistency

Definition (eventual consistency)

A history h is eventually consistent (EC) when for every object x if there is a bounded amount of write operations on x in h, then eventually all the read operation observer the same state.



Optimistic Replication Strong Eventual Consistency

- Strong Eventual Consistency
 - Eventual delivery: « An update executed at some correct replica eventually executes at all correct replicas »
 - Strong convergence = correct replicas that have executed the same updates have equivalent state
 - No consensus in background, no need to rollback

Operational Transformation (OT) Operation-based approach model

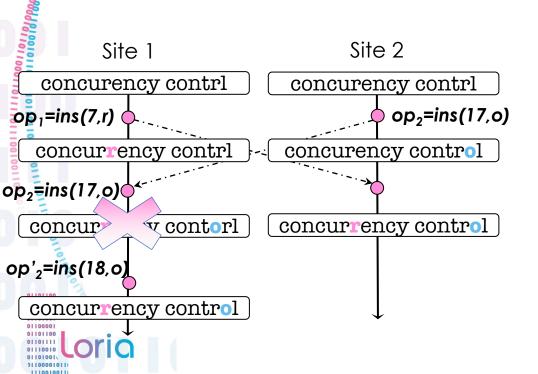
- n copies of an object hosted at n sites
- An object is modified by applying operations
- Each operation is
 - generated at a site (local execution),
 and applied immediately on the local copy
 - broadcasted to other sites
 - integrated at those sites (remote execution)
- System is correct if when it is idle all copies are identical (SEC)

Operational Transformation [EG89] General Architecture

- 2 components:
 - An integration algorithm (diffusion, integration)
 - A set of transformation functions (conflict resolution)
- 3 main issues:
 - Convergence (~ EC)
 - Causality violation
 - (Intention violation)

Operational Transformation Running Example

- Textual document = sequence of characters
- Operations:
 - Ins(p, c) inserts character 'c' at position 'p'
 - Del(p) removes character at position 'p'



T(lns(p1,c1), lns(p2,c2)):
if (p1<p2) return lns(p1,c1)

else return lns(p1+1,c1)

endif

Operational Transformation Example of Transformation Functions

```
T(Ins(p1,c1), Ins(p2,c2)) :-
   if (p1<p2) return lns(p1,c1)
   else return Ins(p1+1,c1)
T(lns(p1,c1), Del(p2)) :-
   if (p1≤p2) return lns(p1,c1)
   else return Ins(p1-1,c1)
   endif
T(Del(p1), Ins(p2,c2)) :-
   if (p1<p2) return Del(p1)
   else return Del(p1+1)
T(Del(p1), Del(p2)):-
   if (p1<p2) return Del(p1)
   else if (p1>p2) return Del(p1-1)
   else return Id()
```

Operational Transformation

Correctness [EG89]

(TP1)
$$op_1 \circ T(op_2, op_1) \equiv op_2 \circ T(op_1, op_2)$$

Site 1
Site 2

op'
op'
op'

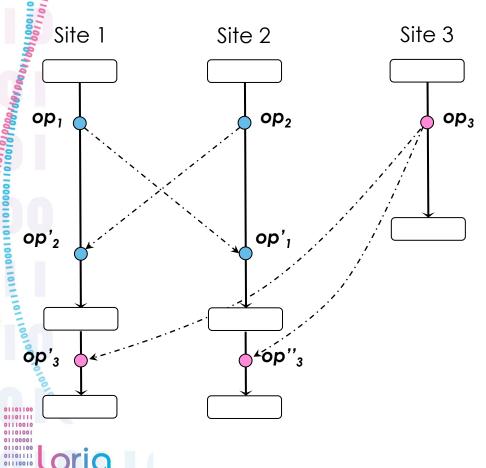
 $T(op_2: operation, op_1: operation) = op'_2$

- op_1 and op_2 concurrent, defined on a state S
- op'₂ same effects as op₂, defined on $S.op_1$

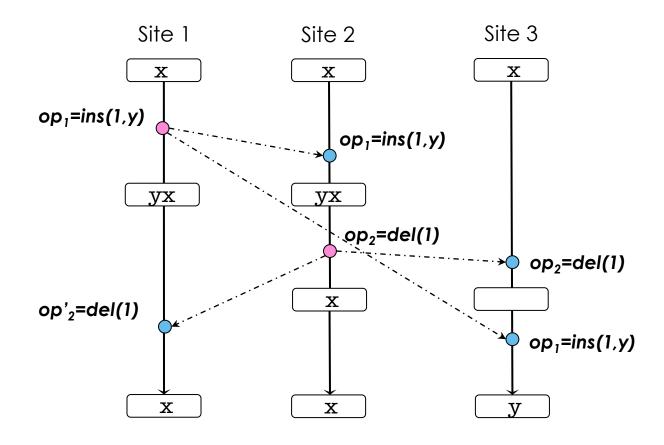
Operational Transformation

Correctness [RNG96]

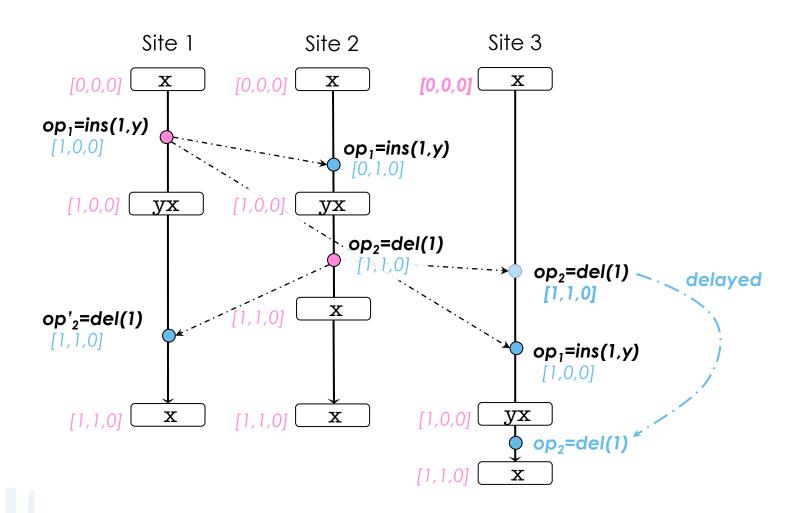
(TP2) $T(op_3, op_1 \circ T(op_2, op_1)) = T(op_3, op_2 \circ T(op_1, op_2))$



Operational Transformation Causality Violation



Operational Transformation Causality Preservation



Operational Transformation (OT) Operation Intention

- Intention of an operation is the observed effect as result of its execution on its generation state
- Passing from an initial state 'ab' to a final state 'aXb' could be observed as:
 - ins(2,x)
 - ins(a < X < b)
 - ins(a < X)
 - ins(X < b)

Operational Transformation (OT) Intention Preservation [SJZYC98]

 For any operation op the effects of executing op at all sites should be the same as the intention of op

• The effect of executing op does not change the effects of independent operations.

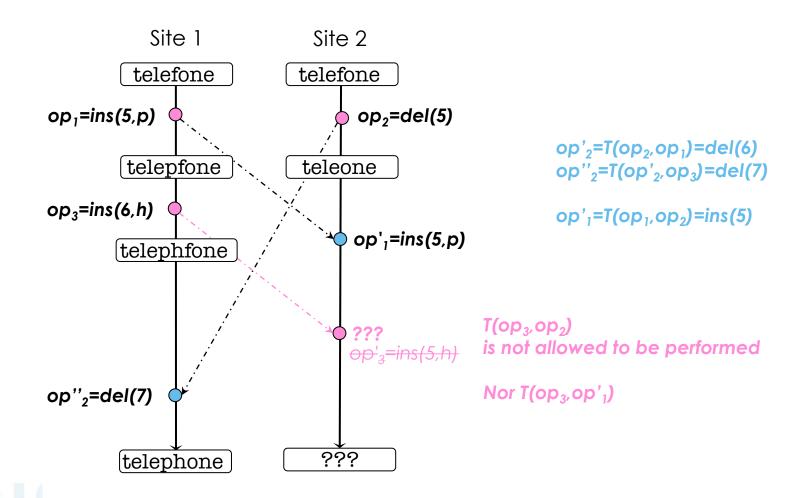
Operational Transformation (OT) Existing Approaches

- Two main families:
 - Transformation functions satisfying both TP1 and TP2
 - Control algorithms avoiding (needs of) TP2

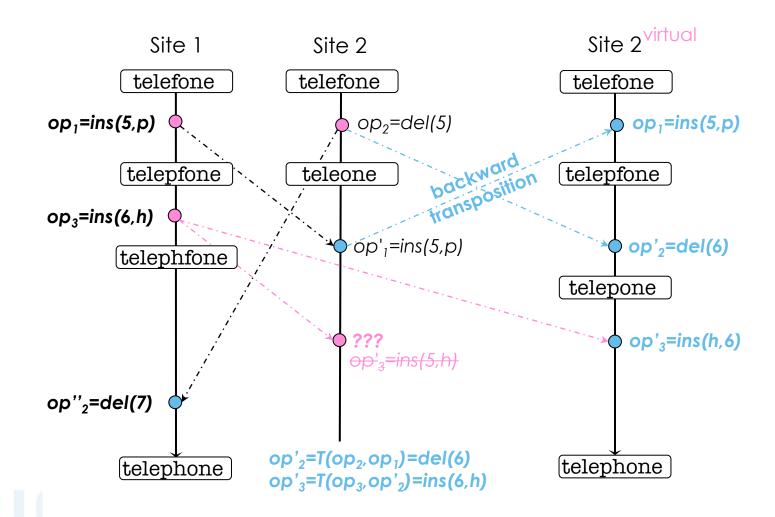
Operational Transformation (OT) Existing Approaches

- Design and verify transformation functions T
- T also known as forward transposition (transpose_fd)
- Verification of conditions TP1 and TP2
 - Combinatorial explosion (>100 cases for a string)
 - Iterative process
 - Repetitive and error prone task

Operational Transformation (OT) Partial Concurrency

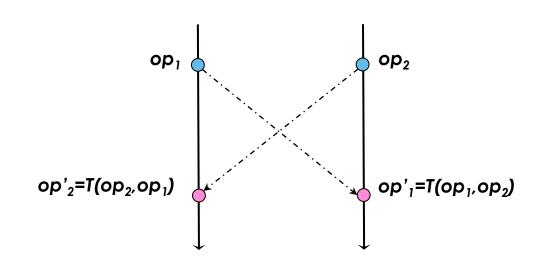


Operational Transformation (OT) Partial Concurrency



Operational Transformation (OT) Backward Transposition [SJZYC98]

- Backward transposition (transpose_bk)
- transpose_bk(op₁, op'₂) = (op₂, op'₁)
 - op'₂ = $T(op_2, op_1)$
 - op'₁ = $T(op_1, op_2)$



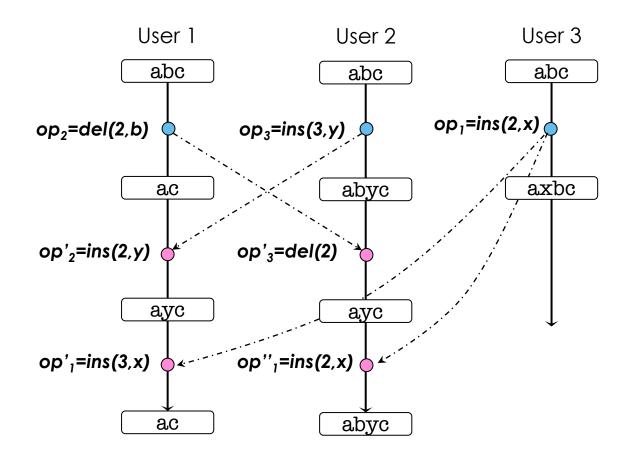
- Note:
 - transpose_bk(op_a, op_b) = $(T^{-1}(op_b,op_a), T(op_a, T^{-1}(op_b,op_a)))$

Operational Transformation **Example of Transformation Functions** [RNG96]

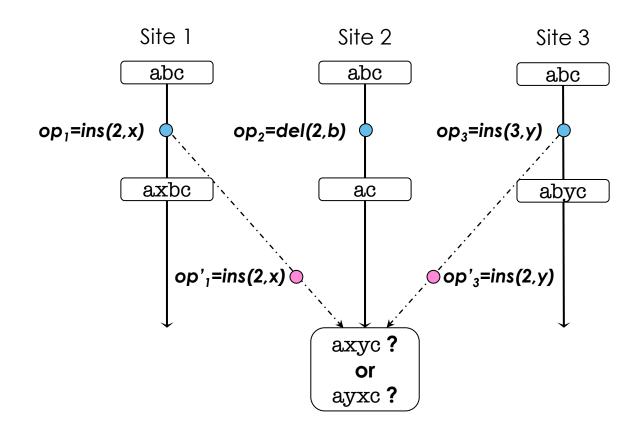
```
T(Ins(p1,c1,u1), Ins(p2,c2,u2)) :-
   if (p1<p2) or (p1=p2 and u1<u2) return lns(p1,c1,u1)
   else return Ins(p1+1,c1,u1)
T(lns(p1,c1,u1), Del(p2,u2)) :-
   if (p1≤p2) return lns(p1,c1,u1)
   else return Ins(p1-1,c1,u1)
   endif
T(Del(p1,u1), Ins(p2,c2,u2)) :-
   if (p1<p2) return Del(p1,u1)
   else return Del(p1+1,u1)
T(Del(p1,u1), Del(p2,u2)):-
   if (p1<p2) return Del(p1,u1)
   else if (p1>p2) return Del(p1-1,u1)
   else return Id()
```

Satisfy TP1 but not TP2!

Operational Transformation Example of Violation of TP2

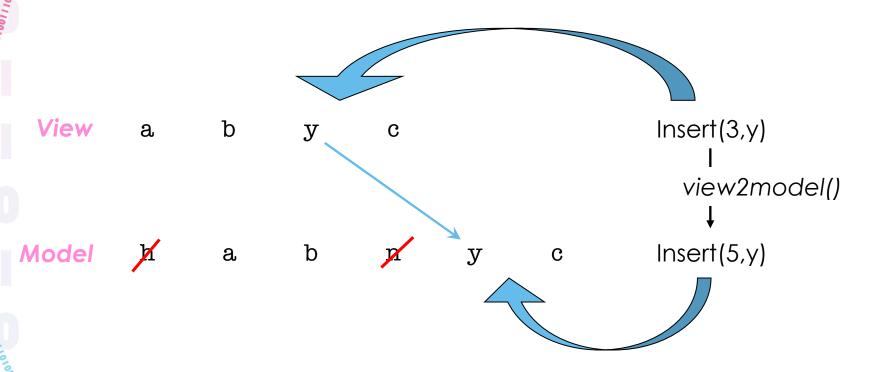


Operational Transformation (OT) False-Tie Problem



Operational Transformation (OT) Tombstone Transformation Functions [OUMI06]

Keep 'tombstones' of deleted elements



Operational Transformation (OT) Tombstone Transformation Functions

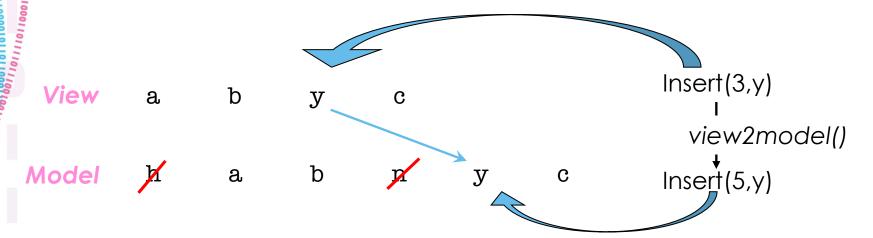
```
T(Ins(p1,c1,s1), Ins(p2,c2,s2)):-
    if (p1<p2) or (p1=p2 and s1<s2) return Ins(p1,c1,s1)
    else return Ins(p1+1,c1,s1)

T(Ins(p1,c1,s1), Del(p2,s2)):-
    return Ins(p1,c1,s1)

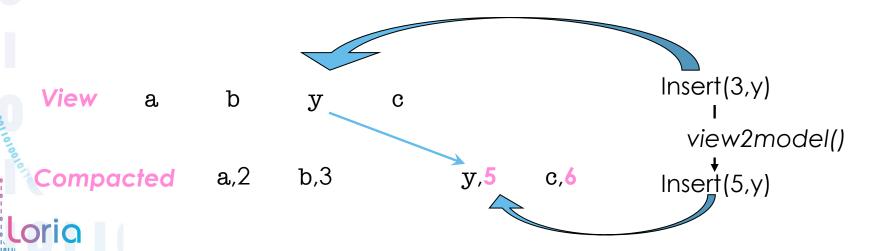
T(Del(p1,s1), Ins(p2,c2,s2)):-
    if (p1<p2) return Del(p1,s1)
    else return Del(p1+1,s1)

T(Del(p1,s1), Del(p2,s2)):-
    return Del(p1,s1)
```

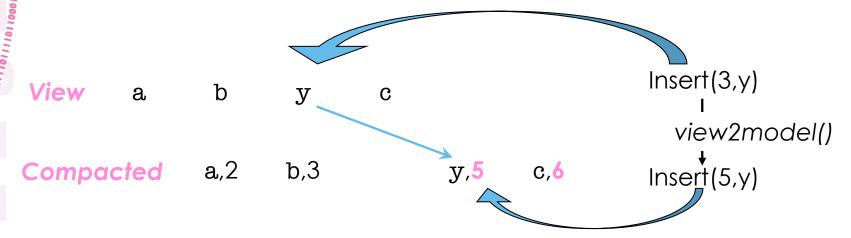
Operational Transformation (OT) Tombstone Transformation Functions – Compact Model



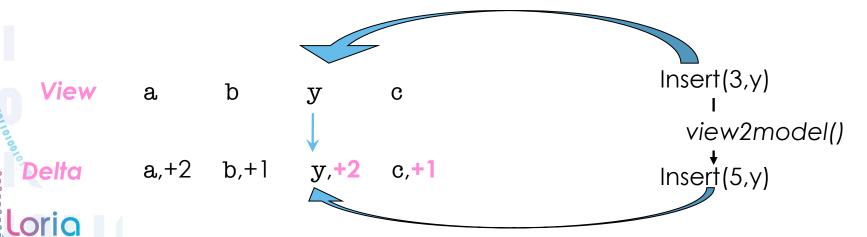
Compacted model = sequence of (character, absolute-position)



Operational Transformation (OT) Tombstone Transformation Functions – Delta Model



Delta model = sequence of (character, offset)



Operational Transformation (OT) Tombstone Transformation Functions – Comparison

- Basic Model
 - Deleted characters are kept
 - Size of the model is growing infinitely
- Compacted Model
 - Update absolute position of all characters located after the effect position
- Delta Model
 - Update the offset of next character
- Observations
 - view2model can be optimized (caret position)
 - Overhead of view2model is not significant

Operational Transformation (OT) General Control Algorithm – SOCT2 [SCF97]



the operation precedes the remote operation

remote operation

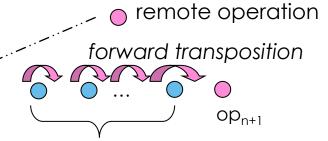
the operation is concurrent with the remote operation

b) principle of integration

equivalent HB



operations preceding the remote operation



operations concurrent with the remote operation

Operational Transformation (OT) Control Algorithms that avoid TP1 and/or TP2

- GOT algorithm [SJZYC98]
 - Does not need to satisfy TP1 and TP2
 - Requires a global serialization order
 - Sum of state vector components
 - If equality, then priority on sites
 - Requires very costly undo/redo mechanism
 - Does not ensure SEC (only EC)

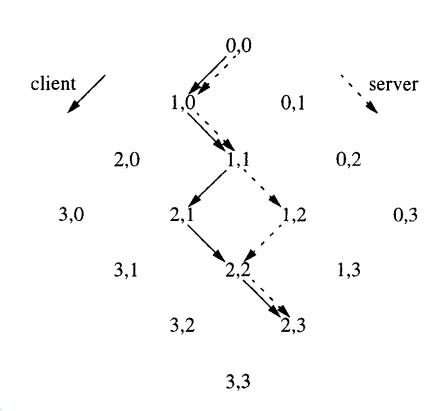
Operational Transformation (OT) Control Algorithms that avoid TP1 and/or TP2

- SOCT4 Algorithm [VCFS00]
 - No undo/redo mechanism, no state vectors
 - Eliminates TP2, but requires TP1
 - Global order of operations according to timestamps generated by a sequencer
 - Local operations executed immediately
 - Assigns a timestamp to the operation and transmits it to the other sites
 - Defers broadcast until execution of all preceding operations
 - Transformations performed by each site

Operational Transformation (OT) Control Algorithms that avoid TP1 and/or TP2

- Jupiter algorithm [NCDL95]
 - Used in GoogleDocs
 - Requires a central server
 - Eliminates TP2, but requires TP1
 - Does not need state vectors
 - Transformations done on the server + client side

Operational Transformation (OT) Jupiter Algorithm



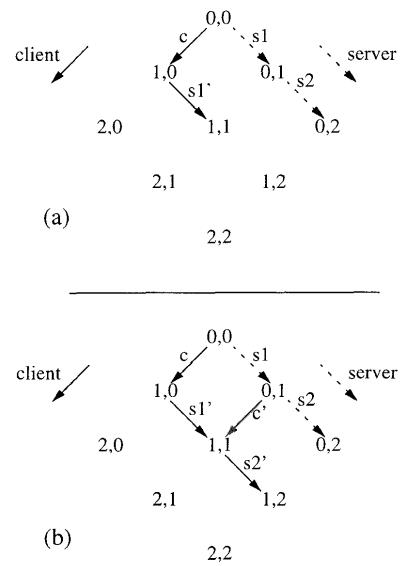
xform(c,s)={c',s'} xform(del x, del y)= {del x-1, del y} if x>y {del x, del y-1} if x<y {no-op, no-op} if x=y

Operational Transformation (OT)

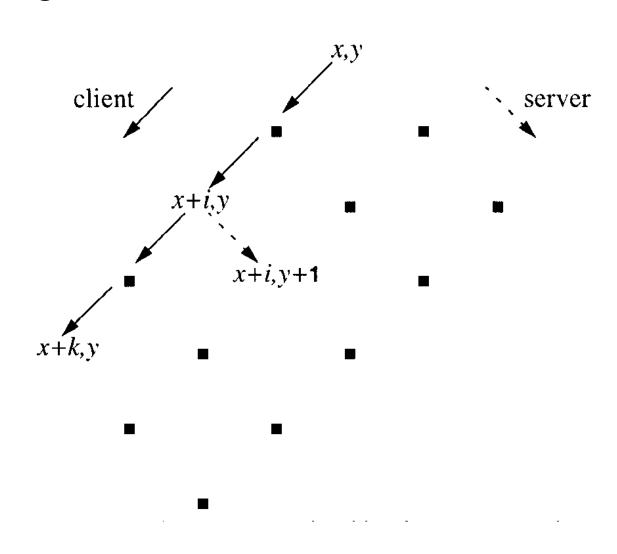
Jupiter Algorithm

01101100

01101100



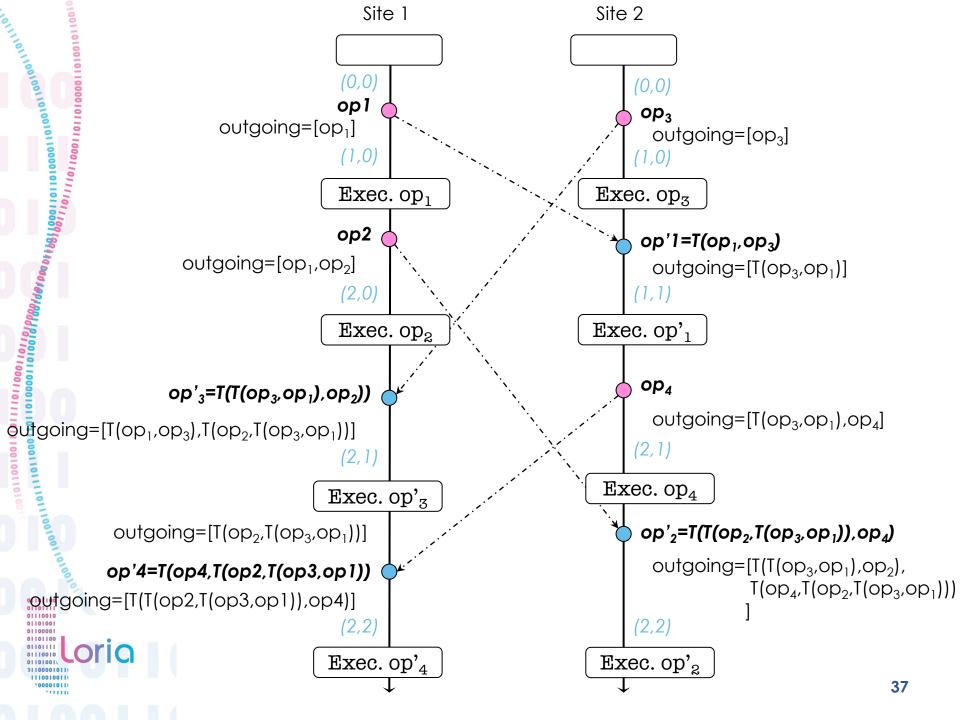
Operational Transformation (OT) Jupiter Algorithm



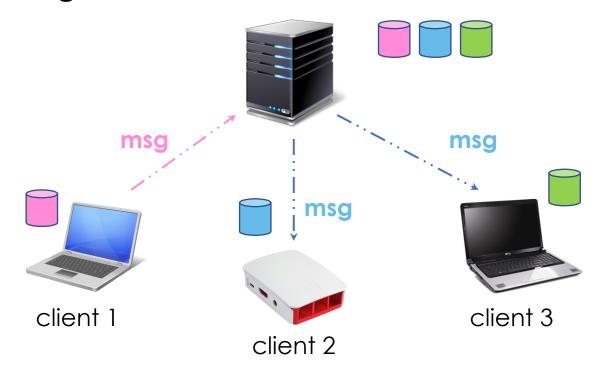
Operational Transformation (OT) Jupiter Algorithm

```
int myMsgs = 0; /* number of messages generated */
int otherMsgs = 0; /*number of messages received */
generate(op) {
 apply op locally;
 send(op, myMsgs, otherMsgs);
 add(op, myMsgs) to outgoing;
 myMsgs = myMsgs + 1;
receive(msg) {
 /* discard acknowledged messages */
 for m in (outgoing) {
   if (m.myMsgs < msg.otherMsgs)</pre>
     remove m from outgoing;
 /* ASSERT: msg.myMsgs == otherMsgs */
 for i in [1..length(outgoing)] {
   /* transform new messages and the ones in the queue */
   { msg, outgoing[i] } = xform(msg, outgoing[i]);
 apply msg.op locally;
 otherMsgs = otherMsgs + 1;
```

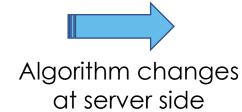
0100191P881d@1000011681



Operational Transformation (OT) Jupiter Algorithm – Generalization to n clients [ZO1]



apply msg.op locally;



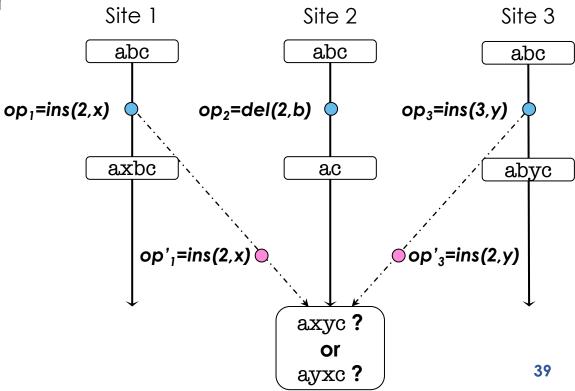
```
apply msg.op locally;
for (c in client list) {
  if (c != client)
    send(c, msg);
}
```

Operational Transformation (OT) Jupiter Algorithm – Summary

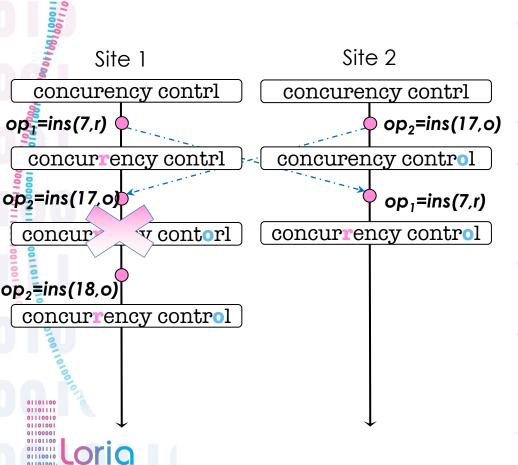
- Requires a server that performs transformations
- Not suitable for P2P environments

False tie scenario gives different results according to

integration order



Operational Transformation (OT) Summary

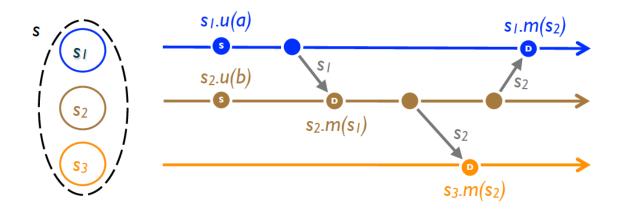


- Transforms non commuting operations to make them commute
- Genericity
- Time complexity
 Average: O(H.c)
 Worst case: O(H²)
- Difficult to write correct transformation functions
- State vectors used for detecting concurrency ⇒ scalability limitations
- Not very suitable for large scale peer-to-peer collaboration

Conflict-free Replicated Data Types (CRDT) [SPBZ09]

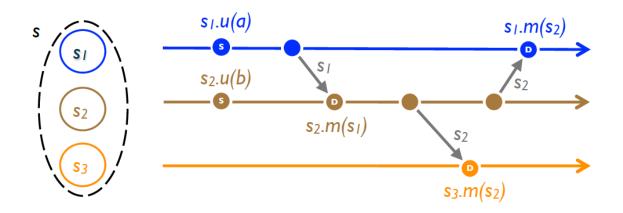
- Data structures
 - Same semantics (w/o concurrency) as classical datastructures
 - Designs operations to be commutative
- Replicated
 - At multiple sites
- Available
 - Replica is updated without coordination
 - Convergence is (formally) guarantee
 - Decentralized / Peer-to-peer
- State-based and Operation-based approaches

Conflict-free Replicated Data Types State-based Replication



- Replicated object: a tuple (S, s₀, q, u, m)
 - S: state domain
 - Replica at process p_i has state $s_i \in S$
 - s₀: initial state
- Each replica can execute one of following commands
 - q: query object's state
 - u: update object's state
- Orion: merge state from a remote replica

Conflict-free Replicated Data Types State-based Replication



- Algorithm
 - Periodically, replica at p_i sends its current state to p_i
 - Replica pi merges received state into its local state by executing m
- After receiving all updates (irrespective of order), each replica will have same state

Conflict-free Replicated Data Types Semi-lattice

- Partial order ≤ set S with a least upper bound (LUB), denoted □
 - m = x \sqcup y is a LUB of { x, y } under \leq if and only if \forall m', x \leq m' \land y \leq m' \Rightarrow x \leq m \land y \leq m \land m \leq m'
- It follows that □ is:
 - commutative: $x \sqcup y = y \sqcup x$
 - idempotent: $x \cup x = x$
 - associative: $(x \cup y) \cup z = x \cup (y \cup z)$

Conflict-free Replicated Data Types Semi-lattice – Example on integers

- Partial order ≤ on set of integers
- Least upper bound □: max (maximum function)
- Therefore, we have:
 - commutative: max(x, y) = max(y, x)
 - idempotent: max(x, x) = x
 - associative: max(max(x, y), z) = max(x, max(y, z))

Conflict-free Replicated Data Types Semi-lattice – Example on sets

- Partial order ⊆ on sets
- Least upper bound □ : ∪ (set union)
- Therefore, we have:
 - commutative: $A \cup B = B \cup A$
 - idempotent: $A \cup A = A$
 - associative: $(A \cup B) \cup C = A \cup (B \cup C)$

Conflict-free Replicated Data Types Monotonic Semi-lattice Object

- A state-based object with partial order \leq , noted (S, \leq , s₀, q, u, m), that has following properties, is called a monotonic semi-lattice:
 - 1. Set S of values forms a semi-lattice ordered by ≤
 - Merging state s with remote state s' computes the LUB of the two states, i.e., s • m(s') = s □ s' (delivery order is not important)
 - 3. State is monotonically non-decreasing across updates, i.e., s ≤ s u
 (updates have effect, no rollback)

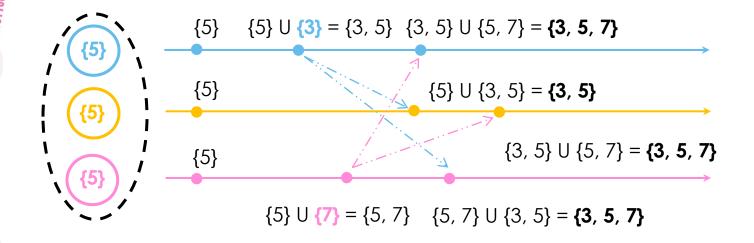
Conflict-free Replicated Data Types Convergent Replicated Data Type (CvRDT)

 Theorem: Assuming eventual delivery and termination, any replicated state-based object that satisfies the monotonic semi-lattice property is SEC

• Since:

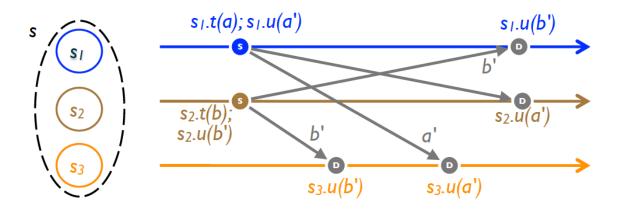
- Merge is both commutative and associative
 - We do not care about order
- Merge is idempotent
 - We do not care about delivering more than once

Convergent Replicated Data Types Example



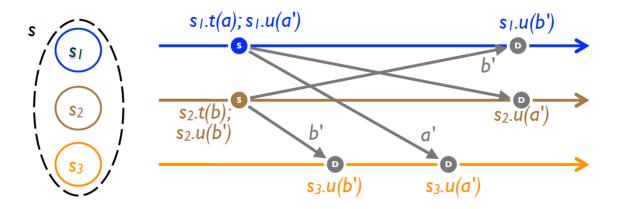
- Each replica can execute one of following commands
 - query q: returns entire set
 - update u: adds new element (e, α)to local set
 - merge m: compute unions between local set and remote set

Conflict-free Replicated Data Types Operation-based Replication



- Replicated object: a tuple (S, s_0 , q, t, u, P).
 - S: state domain
 - Replica at process p_i has state $s_i \in S$
 - s₀: initial state
- Each replica can execute one of following commands
 - q: query object's state
 - t: side-effect-free prepare-update method (at local replica)
 - u: effect-free update method (at all replicas)
 - P: delivery precondition

Conflict-free Replicated Data Types Operation-based Replication



- Algorithm
 - Updates are delivered to all replicas
 - Use causally-ordered broadcast communication protocol, i.e., deliver every message to every node exactly once, w.r.t. happenbefore order
 - Happen-before: updates from same replica are delivered in the order they happened to all recipients (effectively delivery precondition, P)
 - Note: concurrent updates can be delivered in any order

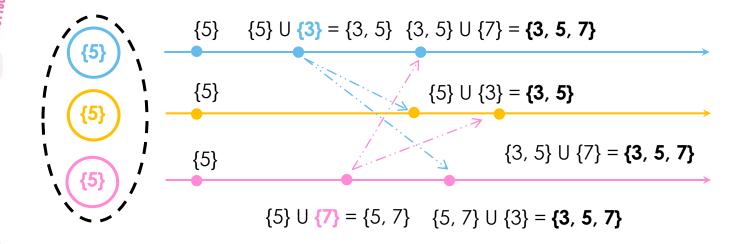
Conflict-free Replicated Data Types Commutativity Property

- Updates (t, u) and (t', u') commute, if and only if for any reachable replica state s where both u and u' are enabled:
 - υ (resp. υ') remains enabled in state s υ' (resp. s υ)
 - $S U U' \equiv S U' U$
- Commutativity holds for concurrent updates

Conflict-free Replicated Data Types Commutative Replicated Data Type (CmRDT)

 Theorem: Assuming causal delivery of updates and method termination, any replicated op-based object that satisfies the commutativity property for all concurrent updates is SEC

Commutative Replicated Data Types Example



- query q: returns entire set
- prepare method t: adds new element (e,α) to local set
- update u: add delta to any remote replica













TRIFORK











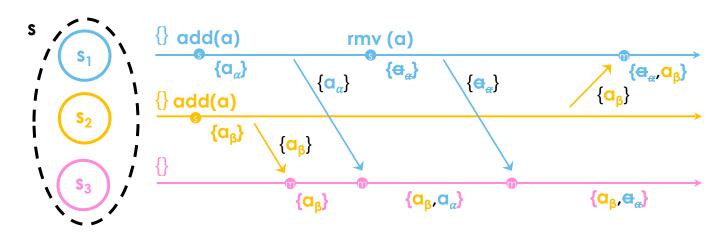


- Register
 - Last-Writer Wins
 - Multi-Value
- Set
 - Grow-Only
 - 2-Phase
 - Observed-Remove
 - Observed-Update-Remove

- Map
- Counter
- Graph
 - Directed
 - Monotonic DAG
 - Edit graph
- Sequence



Conflict-free Replicated Data Types Observed-Remove Set (CvRDT)



- Payload: (A,R) added/removed sets of (element, unique-token)
- Operations:

add(e): $A := A \cup \{(e, \alpha)\}$

remove(e): $R := R \cup \{(e, -) \in A\}$ remove all unique elements observed

 $lookup(e): \exists (e,-) \in A \setminus R$

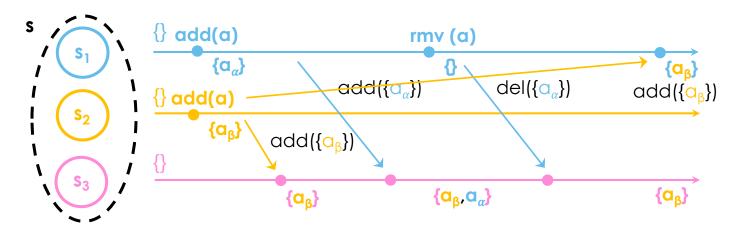
merge(S, S'): (A U A', R U R')

• {true} add(e) || remove(e) {e∈S}

Optimised OR-set

- summarise received adds in a vector
- check vector during merge

Conflict-free Replicated Data Types Observed-Remove Set (CmRDT)



• Payload:

 $S = \{(e, \alpha), (e, \beta), (e, Y), ...\}$ where $\alpha, \beta, Y, ...$ are unique token

Operations:

add(e): $S := S \cup \{(e, \alpha)\}$ where α is a fresh unique token

lookup(e): $\exists \alpha$: (e, α) \in S

remove(e): $R := \{(e, \alpha) \mid \exists \alpha \ (e, \alpha) \in S\}$ (at source) no tombstones

 $S := S \setminus R$

 $\{true\}\ add(e)\ \|\ remove(e)\ \{e \in S\}$

Conflict-free Replicated Data Types P-Counter (CvRDT)

- Payload:
 - P = [int, int, ...]
- Operations:
 - value(): $\sum_{i} P[i]$
 - increment(): P[MyID]++
 - merge(S,S'): $S \sqcup S' = [...,max(s.P[i],s'.P[i]),...]_i$
- Positive

Conflict-free Replicated Data Types PN-Counter (CvRDT)

- Payload:
 - P = [int, int, ...],N = [int, int, ...]
- Operations:
 - value(): $\sum_{i} P[i] \sum_{i} N[i]$
 - increment(): P[MyID]++
 - decrement(): N[MyID]++
 - merge(S,S'): $S \sqcup S' = ([...,max(s.P[i],s'.P[i]),...]_{i,s})$
 - $[...,max(s.N[i],s'.N[i]),...]_{i}$
- Positive or negative

Conflict-free Replicated Data Types CVRDT vs. CmRDT

- Both approaches are equivalent
 - A state-based object can emulate an operation-based object, and vice-versa
- Operation-based:
 - More efficient since you only ship small updates
 - But require causally-ordered broadcast
- State-based:
 - Only require reliable broadcast

CRDT Examples (cont'd)

- Integer vector (virtual clock):
 - u: increment value at corresponding index by one
 - m: maximum across all values, e.g., m([1, 2, 4], [3, 1, 2]) = [3, 2, 4]
- Counter: use an integer vector, with query operation
 - q: returns sum of all vector values (1-norm), e.g., q([1, 2, 4]) = 7
- Counter that decrements as well:
 - Use two integer vectors:
 - Lupdated when incrementing
 - D updated when decrementing
 - q: returns difference between 1-norms of I and D

Conflict-free Replicated Data Types (CRDT) (Text) Sequence [PMSL09] [WUM09]

- Document = linear sequence of elements
 - Each element has a unique identifier
 - Identifier constant for the lifetime of the document
 - Dense total order of identifiers consistent with element order:
 - $\forall id_x$, id_y : $id_x < id_y \Rightarrow \exists id_z$: $id_x < id_z < id_y$
- Different approaches for generating identifiers:
 - TreeDoc, Logoot, LogootSplit, ...

Conflict-free Replicated Data Types (CRDT) Logoot [WUM09]

n

С

u

r

е

0

n

t

Logoot identifiers: $\langle p_1, s_1, h_1 \rangle \langle p_2, s_2, h_2 \rangle \cdots \langle p_k, s_k, h_k \rangle$

<1,2,1>

p_i integer s_i site identifier h_i logical clock at site s_i

<1.2.2> <2,1,2> <3,1,3> <3,1,3><8,4,5> <3.2.5> <4,1,7>

<4,1,7><9,2,6> n

<7,2,8> С <9.1.7>

<10,2,8>

<12,3,1> <12,3,1><6,5,1>

<12,3,1><7,8,2>

<12,3,1><7,8,2><12,3,5>

<12,3,1><7,8,2><13,3,6>

<12,3,1><7,8,2><14,3,7>

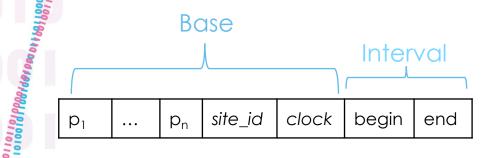
Time complexity

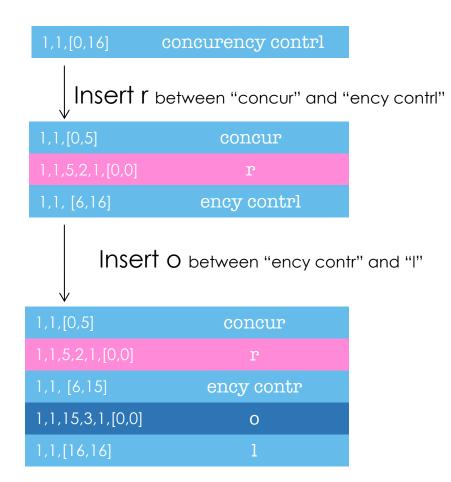
Average: O(k.log(n))

Worst case: O(H.log(H))

- No need for concurrency detection
- Identifiers storage cost
- New design for each data type
- Suitable for large-scale collaboration

LogootSplit identifiers

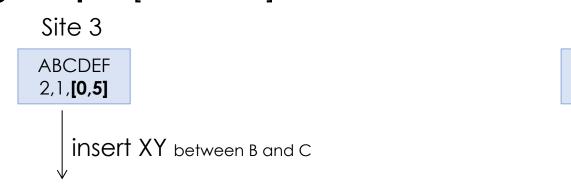


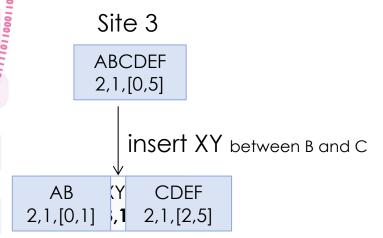


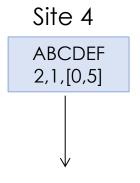
Site 4

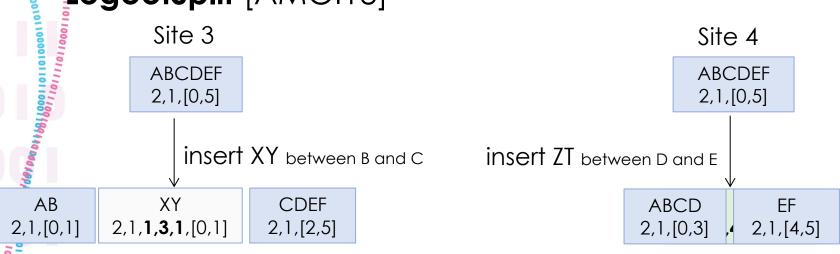
ABCDEF

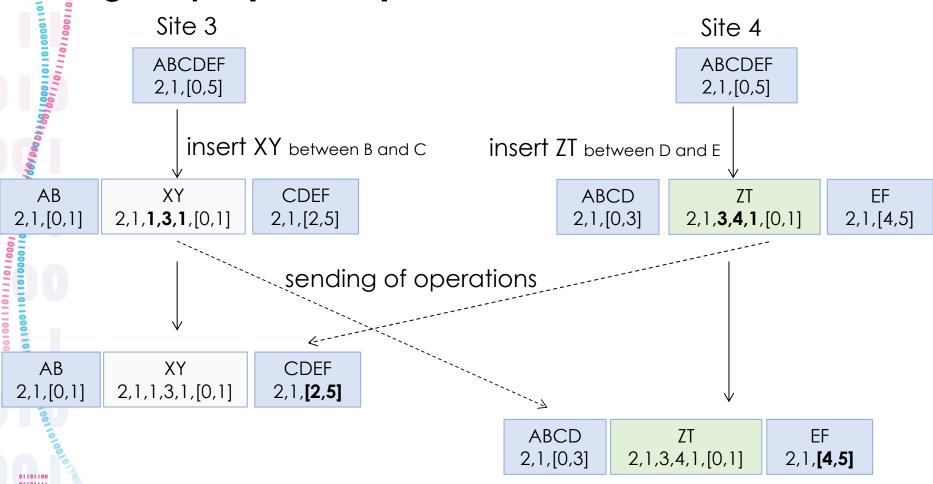
2,1,[0,5]

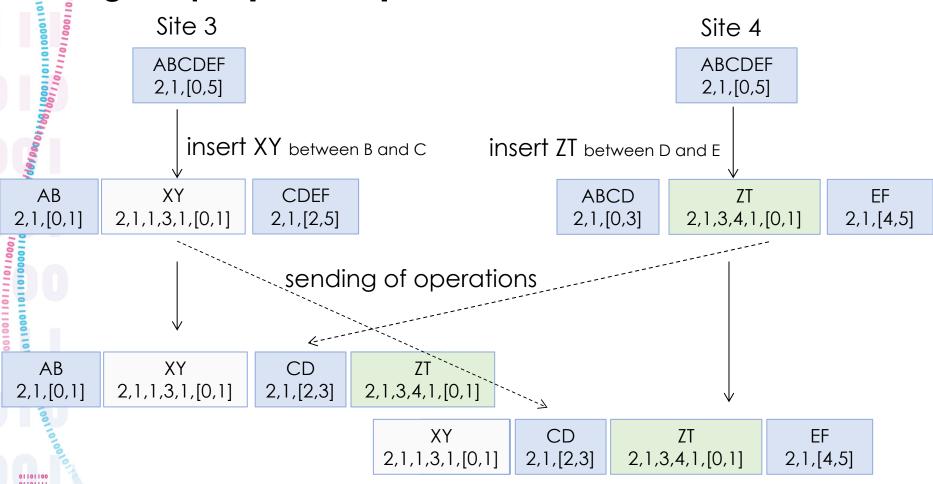












Conflict-free Replicated Data Types (CRDT) Take away

- Strong eventual consistency
 - Parallel and unsynchronized updates
 - Deterministic merge
- State-based approach (CvRDT):
 - Monotonic semi-lattice
 - Reliable broadcast (epidemic propagation)
- Operation-based approach (CmRDT):
 - Commutative concurrent updates
 - Causally-ordered broadcast

References

- **[GL02]** Brewer's conjecture and the feasibility of consistent, available, partition-tolerant web services, S. Gilbert and N. Lynch, ACM SIGACT news, 2002.
- **[SS05]** Optimistic replication. Y. Saito and M. Shapiro. ACM Computing Surveys. 37(1), 2005.
- [LLS90] Lazy replication: exploiting the semantics of distributed services, R. Ladin, B. Liskov, L. Shrira, ACM SIGOPS european workshop, 1990.
- **[EG89]** Concurrency Control in GroupWare Systems, C.A. Ellis and S.J. Gibbs. ACM SIGMOD Record 18(2), 1989.
- [RNG96] An integrating, transformation-oriented approach to concurrency control and undo in group editors, M. Ressel, D. Nitsche-Ruhland, and R. Gunzenhäuser. CSCW 1996.

References

- **[SJZYC98]** Achieving convergence, causality preservation, and intention preservation in real-time cooperative editing systems, C. Sun, X. Jia, Y. Zhang, Y. Yang, and D. Chen. ACM Transactions on Computer-Human Interaction. 5(1), 1998.
- [OUMI06] Tombstone transformation functions for ensuring consistency in collaborative editing systems, G. Oster, P. Urso, P. Molli, and A. Imine. CollaborateCom 2006.
- [SCF97] Serialization of concurrent operations in a distributed collaborative environment, M. Suleiman, M. Cart, and J. Ferrié. GROUP 1997.
- [VCFS00] Copies convergence in a distributed real-time collaborative environment. N. Vidot, M. Cart, J. Ferrié, and M. Suleiman. CSCW 2000.
- [NCDL95] High-latency, low-bandwidth windowing in the Jupiter collaboration system, D. A. Nichols, P. Curtis, M. Dixon, and J. Lamping. UIST 1995.

References

- **[Z01]** AA. Zafer, NetEdit: A Collaborative Editor. Master's Thesis, VirginiaPolytechnic Institute and State University. 2001.
- [SPBZ09] CRDTs: Consistency without concurrency control, M. Shapiro, N. Preguica, C. Baquero, M. Zawirski Research Report, RR-6956, INRIA, 2009
- [PMSL09] A commutative replicated data type for cooperative editing, N. Preguica, M. Joan, M. Shapiro, and M. Letia. ICDCS 2009.
- **[WUM09]** Logoot: a Scalable Optimistic Replication Algorithm for Collaborative Editing on P2P Networks, S. Weiss, P. Urso and P. Molli. ICDCS 2009.
- [AMOI13] Supporting Adaptable Granularity of Changes for Massive Scale Collaborative Editing, L. André, S. Martin and G. Oster C.-L. Ignat. CollaborateCom 2013.

Materials

Some of the presented materials are coming from:

 "Conflict-free Replicated Data Types (CRDTs) for collaborative environments", Marc Shapiro, Nuno Preguiça, Carlos Baquero and Marek Zawirski. Keynote WETICE 2011

http://events.telecom-sudparis.eu/wetice/invited_speakers/ShapiroKeyNote.pdf

 "Data Replication and Consistency", Claudia-Lavinia Ignat. Lectures at Université de Lorraine

https://members.loria.fr/Clgnat/replication/

Thank you

COAST Team

http://team.inria.fr/coast/

01101100

developmen WOPK granularity

authenticating

 ${
m framework}_{
m priva}$

performance inter-document co-authoring







