## Computation of main coefficients

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## Computation of coefficients for Theorem 1 and 2

## Computation of $e_1(\varepsilon)$

```
# Definition of the functions
e_1n = function(eps, hasSkewness = TRUE) {

P_1n = ( 144 + 48*eps + 4*eps^2 ) / 576
if (hasSkewness){
   P_1n = P_1n + ( 96*sqrt(2*eps) + 32*eps + 16*sqrt(2)*eps^(3/2) ) / 576
}
b = eps^2*( 1/6 + 2 * P_1n / (1-3*eps)^2 )
   return(exp(b))
}

# print(e_1n(eps = 0.1))
# print(e_1n(eps = 0.1, hasSkewness = FALSE))

th1_coeff_K4n <- function(eps) {0.327 * (1/12 + 1 / (4 * (1-3*eps)^2 ) )}
th1_coeff_lambda3n_2 <- function (eps) {0.037 * e_1n(eps = eps)}

# Changes for theorem 2
e_3n = function(eps) { exp( eps^2 / 6 + eps^2 / (2 * (1-3*eps)^2) ) }
th2_coeff_lambda3n_2 <- function(eps) {0.037 * e_3n(eps = eps)}</pre>
```

## Computation of the corresponding coefficients

```
eps = c(0.2, 0.1, 0.05, 0.02)
df_coefficients = data.frame(
    eps = eps,
    Coef.K4n = th1_coeff_K4n(eps),
    Coef.lambda3n.2.in.th1 = th1_coeff_lambda3n_2(eps),
    Coef.lambda3n.2.in.th2 = th2_coeff_lambda3n_2(eps)
)

df_coefficients
```

```
## eps Coef.K4n Coef.lambda3n.2.in.th1 Coef.lambda3n.2.in.th2

## 1 0.20 0.5381875 0.04519895 0.04220694

## 2 0.10 0.1940867 0.03757922 0.03744183

## 3 0.05 0.1403988 0.03709494 0.03707952

## 4 0.02 0.1197692 0.03701206 0.03701084
```