

Assignment 1

4. FastText Embeddings

4.1 a) 40'000
b) 2e6

doesn't
depend on u_c

4.2 a) i) $\frac{\partial \mathcal{L}}{\partial u_c} = \frac{\partial}{\partial u_c} \left(-\log(\sigma(s(w_e, w_c))) - \dots \right)$

$$= \frac{\partial}{\partial u_c} -\log \left(\sigma \left(\sum_g z_g^T u_c \right) \right)$$

$$= -\frac{1}{\sigma \left(\sum_g z_g^T u_c \right)} \frac{\partial}{\partial u_c} \sigma \left(\sum_g z_g^T u_c \right)$$

$$= -\frac{1}{\sigma \left(\sum_g z_g^T u_c \right)} (1 - \sigma \left(\sum_g z_g^T u_c \right)) \sigma \left(\sum_g z_g^T u_c \right) \sum_g z_g$$

$$= \cancel{(-1)} (\sigma \left(\sum_g z_g^T u_c \right) - 1) \sum_g z_g$$

$$a) ii) \frac{\partial L}{\partial u_n} = \underbrace{\frac{\partial}{\partial u_n} - \log(\dots)}_{=0} - \sum_{u \in N_n} \log(\sigma(-s(w_+, w_n)))$$

$$= \frac{\partial L}{\partial u_n} - \sum_{u \in N_n} \log(\sigma(-s(w_+, w_n)))$$

same as i) but with a negative sign

$$\Rightarrow \frac{\partial L}{\partial u_n} = (1 - \sigma(-s(w_+, w_n))) \sum_g z_g$$

$$b) \frac{\partial L}{\partial z_g} = \frac{\partial L}{\partial u_c} + \sum_{u \in N_c} (1 - \sigma(-s(w_+, w_n))) u_n$$

sorry for the mess

$$= \sum_{u \in N_c} (1 - \sigma(-s(w_+, w_n))) u_n + (\sigma(s(w_+, w_c)) - 1) u_c$$

□