## KU LEUVEN

## GENETIC ALGORITHMS

# TSP

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## 1 Experiments

## 2 Implementation

### 2.1 Representation

The original code employed adjacency representation. In adjacency representation a tour is represented as a list of n cities where city j is listed in position i if and only if the tour leads from city i to city j. Thus, the list:

(76853421)

represents the tour:

3-8-1-7-2-6-4-5

1

In our implementation, we have deceided to use path representation. Path representation is the most natural way of representing a tour. This can be easily seen with the following example. The list:

 $(1\ 2\ 7\ 5\ 6\ 3\ 4)$ 

represents the path

1-2-7-5-6-3-4

It was also the simplest representation possible for this problem, and it was easy to implement, as the tour was first encoded in path representation, and then translated to adjancency representation using the function path2adj. Finally, it was translated again to path representation to be used in the plots with the function adj2path.

#### 2.2 Crossover

The new representation required a new crossover operator. The available options were:

- Partially Matched Crossover (PMX)
- Order Crossover (OX)
- Cyclic Crossover (CX)
- Edge Recombination Crossover (ERX)

The one selected is Order Crossover. This crossover exploits a property of the path representation, that the order of the cities (not their positions) are important. It construct an offspring by choosing a subtour of one parent and preserving the relative order of cities of the other parent. Let's consider the following tours:

<sup>&</sup>lt;sup>1</sup>This explanation can be found in the slides about Traveling Salesman Problem

$$\begin{array}{c}
(1\ 2\ 3\ 4\ 5\ 6\ 7\ 8) \\
(2\ 4\ 6\ 8\ 7\ 5\ 3\ 1)
\end{array}$$

If we choose the cut point between the second and the third city, and se second cut point between the fifth and the sixth, we have:

$$(1\ 2 - 3\ 4\ 5 - 6\ 7\ 8)$$
  
 $(2\ 4 - 6\ 8\ 7 - 5\ 3\ 1)$ 

And the offspring is created copying the segments between the cut points, and then, starting from the second cut points of one parent, the rest of the cities are copied in the order in which they appear in the other parent, giving:

$$(87 - 345 - 126)$$
  
 $(45 - 687 - 123)$ 

#### 2.3 Mutation

We were also asked to implement a new mutation operator. For this task, multiple and different options where available, such as Exchange Mutation, Scramble Mutation, Displacement Mutation or Insertion Mutation. As the crossover operator chosen exploits the order property aforementioned, we deceided that the mutation should break this order in some way to avoid reaching a local optima due to the lack of diversity in the order.

The mutation operator selected for this problem is insertion mutation due to its simplicity and effectiveness. This mutation works in the following way. Imagine that we have the path:

Take the 2 out of the sequence,

and reinsert the 2 at a randomly chosen position:

#### 2.4 Fitness Function

The fitness function has been changed as the original one worked with adjacency representation. The simplest way to adapt the old function to the new representation was using path2adj, converting the path to adjacency representation, and then computing the fitness in the same way as it was computed before.

## References

[1] A.E. Eiben, James E Smith. Introduction to Evolutionary Computing. Springer

- [2] P. Larrañaga, C.M.H. Kuijpers, R.H. Murga, I. Inza, S. Dizdarevic Genetic algorithms for the travelling salesman problem: A review of representations and operators. University of the Basque Country
- [3] Dirk Roose Genetic algorithms lectures and slides KU Leuven
- $[4] \ \, {\rm mnemstudio.org} \ \, {\it Genetic} \ \, \, algorithms \ \, \, mutations \ \, \, {\rm http://mnemstudio.org/genetic-algorithmsmutation.htm}$

## 3 Apendix

## 3.1 tsp\_ImprovePopulation.m

```
1 % tsp_ImprovePopulation.m
2 % Author: Mike Matton
4 % This function improves a tsp population by removing local loops
     from
5 % each individual.
6 %
7 | Syntax: improvedPopulation = tsp_ImprovePopulation(popsize,
     ncities, pop, improve, dists)
8 %
9 % Input parameters:
10 %
      popsize
                          - The population size
11 %
      ncities
                          - the number of cities
_{12} \%
                          - the current population (adjacency
      pop
     representation)
_{13} \%
                          - Improve the population (0 = no improvement)
      improve
     <>0 = improvement)
_{14} %
      dists
                          - distance matrix with distances between the
      cities
_{15} \%
16 \% Output parameter:
      improvedPopulation - the new population after loop removal (
     if improve
18 %
                               \Leftrightarrow 0, else the unchanged population).
 function newpop = tsp_ImprovePopulation(popsize, ncities, pop,
     improve, dists)
21
  if (improve)
22
     for i=1:popsize
23
24
       result = improve_path(ncities, pop(i,:), dists);
25
26
       pop(i,:) = path2adj(result);
27
     end
29
 end
30
_{32} newpop = pop;
```

### 3.2 run\_ga.m

```
function run_ga(x, y, NIND, MAXGEN, NVAR, ELITIST, STOP_PERCENTAGE
     , PR_CROSS, PR_MUT, CROSSOVER, LOCALLOOP, ah1, ah2, ah3)
2 % usage: run_ga(x, y,
3 %
                   NIND, MAXGEN, NVAR,
                   ELITIST, STOP_PERCENTAGE,
5 %
                   PR_CROSS, PR_MUT, CROSSOVER,
                   ah1, ah2, ah3)
9 \% x, y: coordinates of the cities
10 % NIND: number of individuals
11 % MAXGEN: maximal number of generations
12 % ELITIST: percentage of elite population
13 % STOP PERCENTAGE: percentage of equal fitness (stop criterium)
14 % PR_CROSS: probability for crossover
15 \% PRMUT: probability for mutation
16 % CROSSOVER: the crossover operator
17/% calculate distance matrix between each pair of cities
18 % ah1, ah2, ah3: axes handles to visualise tsp
 {NIND MAXGEN NVAR ELITIST STOP_PERCENTAGE PR_CROSS PR_MUT
    CROSSOVER LOCALLOOP \;
20
          tic;
21
          GGAP = 1 - ELITIST;
          mean_fits = zeros(1, MAXGEN+1);
          worst=zeros(1,MAXGEN+1);
2.4
          Dist=zeros (NVAR, NVAR);
25
          for i=1:size(x,1)
26
               for j=1:size(y,1)
                   Dist(i,j)=\mathbf{sqrt}((x(i)-x(j))^2+(y(i)-y(j))^2);
28
              end
          end
30
          % initialize population
          Chrom=zeros (NIND, NVAR);
32
          for row=1:NIND
            %Chrom(row,:)=path2adj(randperm(NVAR));
34
              Chrom(row,:) = randperm(NVAR);
35
          end
36
          gen=0;
          % number of individuals of equal fitness needed to stop
          stopN=ceil(STOP_PERCENTAGE*NIND);
39
          % evaluate initial population
          ObjV = tspfun (Chrom, Dist);
41
```

```
best=zeros(1,MAXGEN);
42
          % generational loop
43
          while gen<MAXGEN
44
              sObjV=sort (ObjV);
45
               best (gen+1)=min(ObjV);
            minimum = best (gen + 1);
47
               mean_fits(gen+1)=mean(ObjV);
               worst(gen+1)=max(ObjV);
49
               for t=1:size(ObjV,1)
50
                   if (ObjV(t)=minimum)
                       break;
                   end
              end
              %visualizeTSP(x,y,adj2path(Chrom(t,:)), minimum, ah1,
                  gen, best, mean_fits, worst, ah2, ObjV, NIND, ah3);
               visualizeTSP(x,y,Chrom(t,:), minimum, ah1, gen, best,
                  mean_fits, worst, ah2, ObjV, NIND, ah3);
58
               if (sObjV(stopN)-sObjV(1) \le 1e-15)
                     break;
              end
61
            %assign fitness values to entire population
62
            FitnV=ranking (ObjV);
            %select individuals for breeding
64
            SelCh=select ('sus', Chrom, FitnV, GGAP);
            %recombine individuals (crossover)
               SelCh = recombin (CROSSOVER, SelCh, PR_CROSS);
67
              %SelCh=mutateTSP('inversion', SelCh, PR_MUT);
68
               SelCh=mutateTSP('insertion', SelCh, PR_MUT); % <-- line
69
                  changed, now insertion mutation is used
              %evaluate offspring, call objective function
70
            ObjVSel = tspfun(SelCh, Dist);
71
              %reinsert offspring into population
             [Chrom, ObjV] = reins (Chrom, SelCh, 1, 1, ObjV, ObjVSel);
73
74
              Chrom = tsp_ImprovePopulation(NIND, NVAR, Chrom,
                 LOCALLOOP, Dist);
            %increment generation counter
            gen=gen+1;
          end
          toc;
79
          minimum
 end
```

#### 3.3 insertion.m

```
1 % low level function for TSP mutation
2 \% Representation is an integer specifying which encoding is used
_{3}|\% 1 : adjacency representation
_{4} % 2 : path representation
  function NewChrom = insertion (OldChrom)
       NewChrom = OldChrom;
       % select two positions in the tour
       rndi = zeros(1,2);
       while \operatorname{rndi}(1) = \operatorname{rndi}(2)
            rndi=rand_int(1,2,[1 \text{ size}(NewChrom},2)]);
       end
       rndi = sort(rndi);
      % get the value of the first random position
17
       temp = NewChrom(rndi(1));
1.8
       % insert this value in the second random position
       NewChrom = insertAt (NewChrom, temp, rndi(2));
20
      % remove the first random position
21
       NewChrom(rndi(1)) = [];
2.5
      % End of function
23
  end
24
  function arrOut = insertAt(arr, val, index)
26
       if index == numel(arr)+1
27
            arrOut = [arr val];
28
       else
            \operatorname{arrOut} = [\operatorname{arr}(1:\operatorname{index}-1) \ \operatorname{val} \ \operatorname{arr}(\operatorname{index}:\operatorname{end})];
30
       end
32 end
```

#### 3.4 order crossover.m

```
% Syntax: NewChrom = order_crossover(OldChrom, XOVR)
% Input parameters:
% OldChrom - Matrix containing the chromosomes of the old population. Each line corresponds to one individual
% (in any form, not necessarily real values).
```

```
7 %
       XOVR
                  - Probability of recombination occurring between
     pairs
8 %
                     of individuals.
% Output parameter:
 %
       NewChrom
                  - Matrix containing the chromosomes of the
     population
_{12} %
                     after mating, ready to be mutated and/or
     evaluated,
 %
                     in the same format as OldChrom.
_{14} %
  function NewChrom = order_crossover(OldChrom, XOVR)
18 if nargin < 2, XOVR = NaN; end
  [rows, \tilde{z}] = size(OldChrom);
2.0
     maxrows=rows;
21
     if rem(rows, 2)^{\sim}=0
       maxrows = maxrows - 1;
     end
24
     for row = 1:2: maxrows
26
      % crossover of the two chromosomes
28
      % results in 2 offsprings
    if rand<XOVR
                        % recombine with a given probability
30
           MatrixChrom = order_low_level([OldChrom(row,:);OldChrom(
31
              row + 1 ...);
      NewChrom(row,:) = MatrixChrom(1,:);
32
      NewChrom(row+1,:) = MatrixChrom(2,:);
33
    else
34
      NewChrom(row,:) = OldChrom(row,:);
35
      NewChrom (row + 1,:) = OldChrom (row + 1,:);
36
    end
37
     end
38
39
     if rem(rows, 2) = 0
40
       NewChrom(rows,:)=OldChrom(rows,:);
     end
42
44 % End of function
```

#### 3.5 order\_low\_level.m

```
1 % low level function for calculating an offspring
2 % given 2 parent in the Parents – agrument
3 Parents is a matrix with 2 rows, each row
4 % represent the genocode of the parent
6 % Returns a matrix containing the offspring
  function Offspring=order_low_level(Parents)
10
      cols = size(Parents, 2);
11
      Offspring=zeros (2, cols);
13
      start_index = rand_int(1, 1, [1, cols - 1]);
15
      end\_index = rand\_int(1, 1, [start\_index + 1, cols]);
16
17
      Offspring(1, start_index:end_index) = Parents(2, start_index:
18
         end_index);
      Offspring(2, start_index:end_index) = Parents(1, start_index:
         end_index);
20
21
      for off = 1:2
           Buff = Parents (off,:);
23
           Buff = [Buff(end\_index + 1:end), Buff(1:end\_index)];
2.4
25
           members = ismember(Buff, Offspring(off, :));
26
           Buff (members == 1) = 0;
28
           ii = 1;
          X = find(Buff);
30
           for jj=1:start\_index - 1
              \mathbf{if} \ \mathrm{Buff}(\mathrm{X}(\mathrm{ii})) = 0
32
                  Offspring (off, jj) = Buff (X(ii));
                  Buff(X(ii)) = 0;
34
                  ii = mod(ii, cols) + 1;
35
              end
36
          end
37
           ii = 1;
39
          X = find(Buff);
           for jj=end_index + 1:cols
```

```
if Buff(X(ii)) \tilde{}=0
42
                  Offspring (off, jj) = Buff(X(ii));
43
                  Buff(X(ii)) = 0;
44
                  ii = mod(ii, cols) + 1;
45
              end
           end
47
          %Offspring(off, end_index+1:end) = Buff(start_index:end);
          \%Offspring(off, 1:start\_index - 1) = Buff(1:start\_index - 1)
49
              1);
      end
 |\%| end function
```

### 3.6 tspgui.m

```
CROSSOVER = 'order_crossover';

crossover = uicontrol(ph, 'Style', 'popupmenu', 'String', {'
order_crossover'}, 'Value', 1, 'Position', [10 50 130 20], '
Callback', @crossover_Callback);
```

### 3.7 tspfun.m

```
1 %
2 % ObjVal = tspfun (Phen, Dist)
3 % Implementation of the TSP fitness function
4 % Phen contains the phenocode of the matrix coded in path
5 % representation
6 % Dist is the matrix with precalculated distances between each
    pair of cities
7 % ObjVal is a vector with the fitness values for each candidate
    tour
8 %
     (=each row of Phen)
9 %
 function ObjVal = tspfun(Phen, Dist)
11
     % the objective function works with adjacency representation.
         In this
     % version, path representation is used, so the fitness
13
         function should
     \% be adapted. Now, the phenotype is converted to adjacency
     % representation first, and then, the Objective Value is
        computed as it
     % was computed in the original version.
16
      adj = zeros(size(Phen));
```

```
for row=1:size(Phen)
    adj(row,:) = path2adj(Phen(row,:));
end

ObjVal = Dist(adj(:,1), 1);
for t=2:size(adj,2)
    ObjVal=ObjVal + Dist(adj(:,t), t);
end

End

End

End

End

The path2adj(Phen(row,:));

end

ObjVal = Dist(adj(:,1), 1);

for t=2:size(adj,2)

ObjVal=ObjVal + Dist(adj(:,t), t);

end

End

End

End

The path2adj(Phen(row,:));

The path2adj(Phen(row
```

#### 3.8 mutateTSP.m.

```
1 % MUTATETSP.M.
                       (MUTATion for TSP high-level function)
2 %
3 % This function takes a matrix OldChrom containing the
4 % representation of the individuals in the current population,
_{5} mutates the individuals and returns the resulting population.
7 Syntax: NewChrom = mutate(MUT.F, OldChrom, MutOpt)
8 %
9 % Input parameter:
       MUT<sub>F</sub>
                  - String containing the name of the mutation
     function
11 %
       OldChrom - Matrix containing the chromosomes of the old
12 %
                    population. Each line corresponds to one
     individual.
13 %
       MutOpt
                  - mutation rate
14 % Output parameter:
_{15} \%
       NewChrom - Matrix containing the chromosomes of the
     population
 %
                    after mutation in the same format as OldChrom.
16
17
 function NewChrom = mutateTSP(MUT_F, OldChrom, MutOpt)
19
20
 % Check parameter consistency
21
     if nargin < 2, error ('Not_enough_input_parameters'); end
22
  [rows, \tilde{z}] = size(OldChrom);
 NewChrom=OldChrom;
25
 for r=1:rows
27
    if rand<MutOpt
```

```
NewChrom(r,:) = feval(MUT.F, OldChrom(r,:));
end
end
% End of function
```