

STA457TUT6

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```
set.seed(111)
ar1 = c()
ma1 = c()
sigma2 = c()
for (i in 1:10){
  z <- arima.sim(model = list(ar = c(-0.5), ma = c(-0.9)),
    n = 500)
  AR <- arima(z, order = c(1,0,1))
  ar1[i] = coef(AR)[1]
  ma1[i] = coef(AR)[2]
  sigma2[i] = AR$sigma2
}

ar1_ = matrix(ar1)
colnames(ar1_) <- c("estimated_phi" )
true_phi <- c(-0.5)
ar_1 <- rbind(true_phi,ar1_)
rownames(ar_1) <- c("true_phi","sim1","sim2","sim3","sim4","sim5","sim6","sim7","sim8","sim9","sim10")

ar1_ = matrix(ar1)
colnames(ar1_) <- c("estimated_phi" )
true_parameter <- c(-0.5)
ar_1 <- rbind(true_parameter,ar1_)
rownames(ar_1) <- c("true_parameter","sim1","sim2","sim3","sim4","sim5","sim6","sim7","sim8","sim9","sim10")

ma1_ = matrix(ma1)
colnames(ma1_) <- c("estimated_theta" )
true_parameter <- c(-0.9)
ma_1 <- rbind(true_parameter,ma1_)
rownames(ma_1) <- c("true_parameter","sim1","sim2","sim3","sim4","sim5","sim6","sim7","sim8","sim9","sim10")

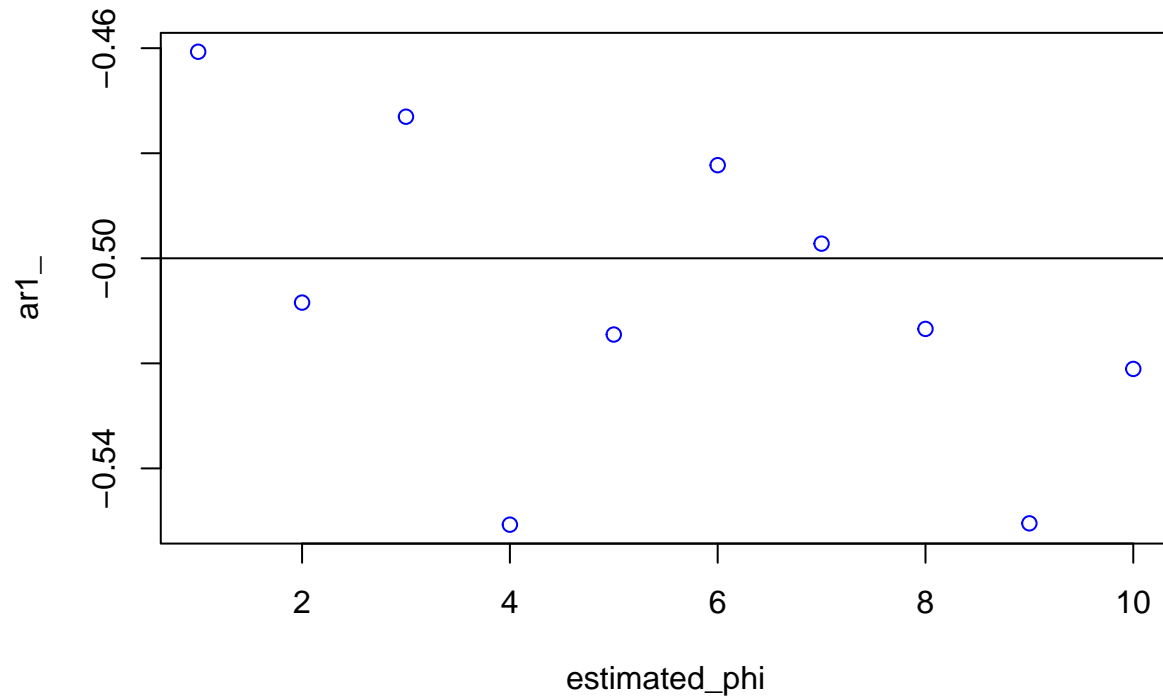
sigma2_ = matrix(sigma2)
colnames(sigma2_) <- c("estimated_sigma2" )
true_parameter <- c(1)
sigma_2 <- rbind(true_parameter,sigma2_)
rownames(sigma_2) <- c("true_parameter","sim1","sim2","sim3","sim4","sim5","sim6","sim7","sim8","sim9","sim10")

do.call(cbind, list(ar_1, ma_1,sigma_2))

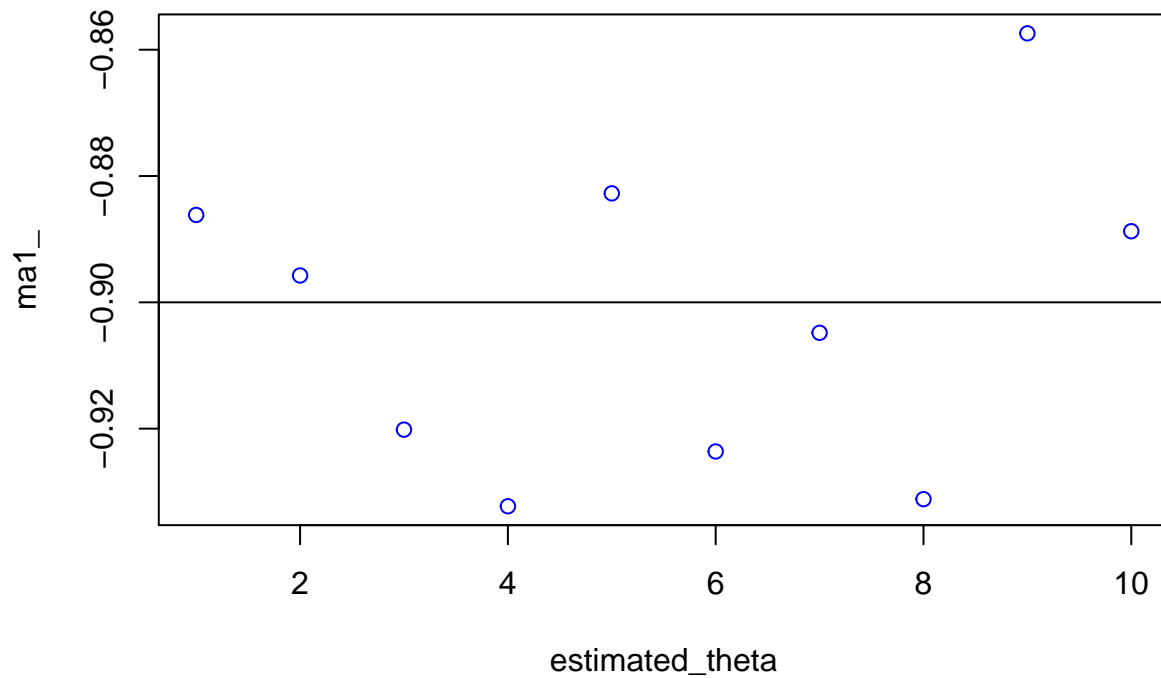
##           estimated_phi estimated_theta estimated_sigma2
## true_parameter    -0.5000000    -0.9000000         1.0000000
## sim1             -0.4606816    -0.8861621         1.0066656
## sim2             -0.5084295    -0.8957472         0.9545764
```

```
## sim3      -0.4730468    -0.9201530    0.9389484
## sim4      -0.5507091    -0.9322839    0.9242786
## sim5      -0.5145113    -0.8827459    0.9709722
## sim6      -0.4822710    -0.9236083    1.1460721
## sim7      -0.4972073    -0.9048256    1.0309401
## sim8      -0.5134424    -0.9311640    0.8993930
## sim9      -0.5504592    -0.8574106    0.9380856
## sim10     -0.5210618    -0.8887411    1.1221034
```

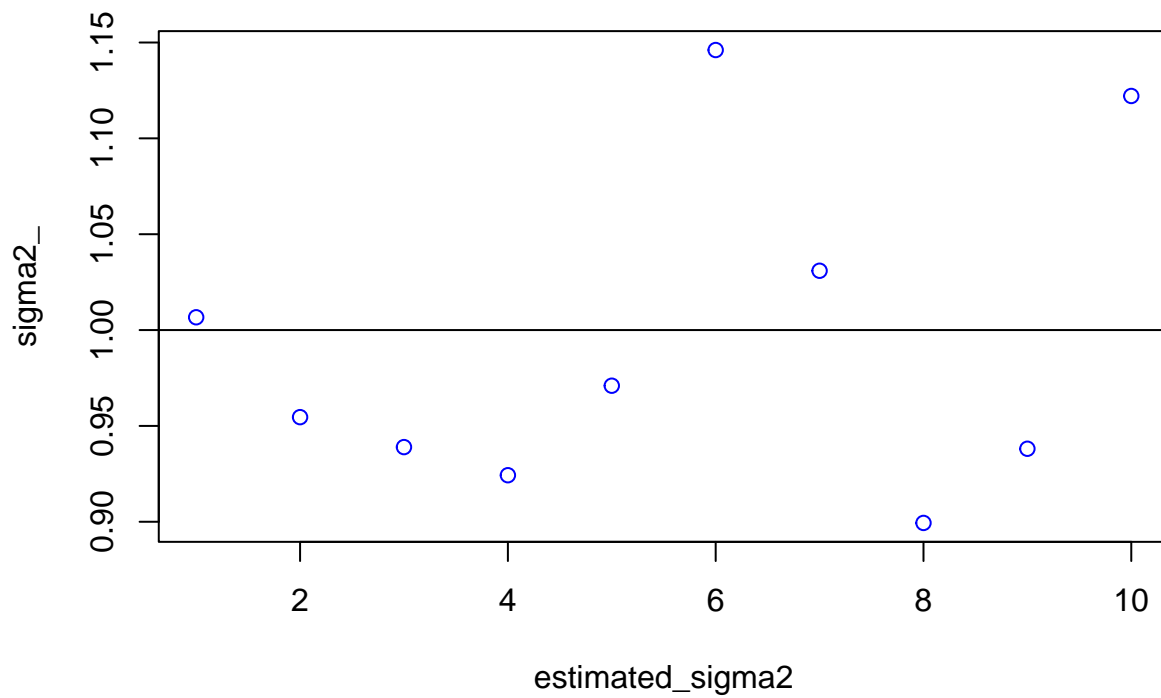
```
plot(ar1_,xlab = "estimated_phi",col = "blue")
abline(h = -0.5)
```



```
plot(ma1_,xlab = "estimated_theta",col = "blue")
abline(h = -0.9)
```



```
plot(sigma2_,xlab = "estimated_sigma2",col = "blue")
abline(h = 1)
```



The conclusion is that the estimated values are randomly distributed around the true parameters taken($\phi = -0.5, \theta = -0.9, \sigma^2 = 1$). There's no pattern of relationship between the estimates, which indicates that the observations taken are identical and independent distribution.