## **Dimension reduction**

### Jeff Leek

@jtleek

www.jtleek.com

## **PCA** and SVD

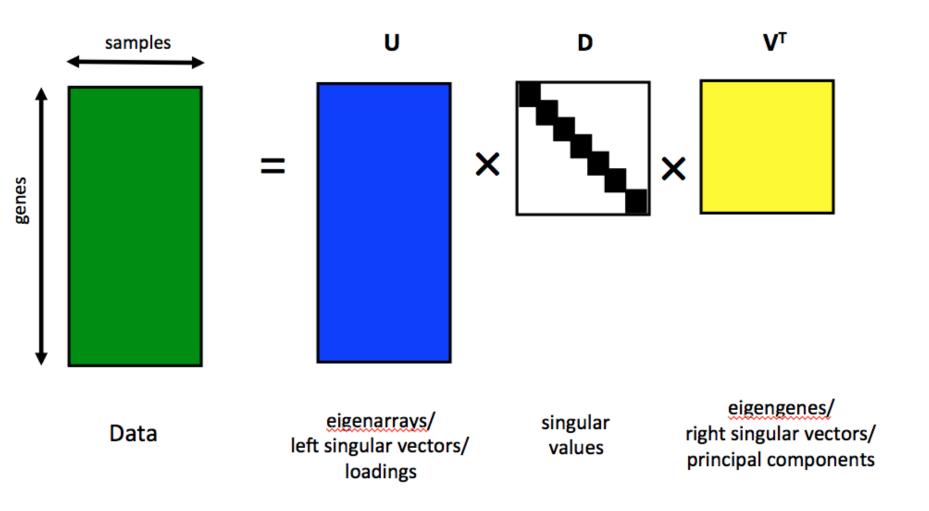
PCA & SVD have different math goals SVD can be used to estimate PCs First proposed in genomics by Alter et al. 2000 PNAS

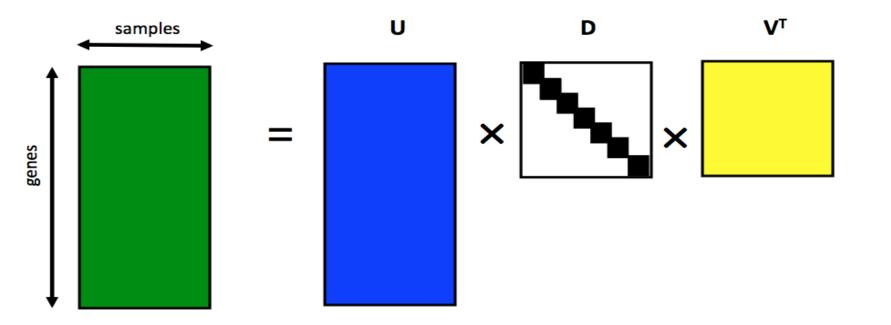
## **Related Problems**

You have multivariate matrix of data X

- Find a new set of multivariate variables that are uncorrelated and explain as much variance across rows as possible.
- Find the best matrix created with fewer variables (lower rank) that explains the original data.

The first goal is statistical and the second goal is data compression.



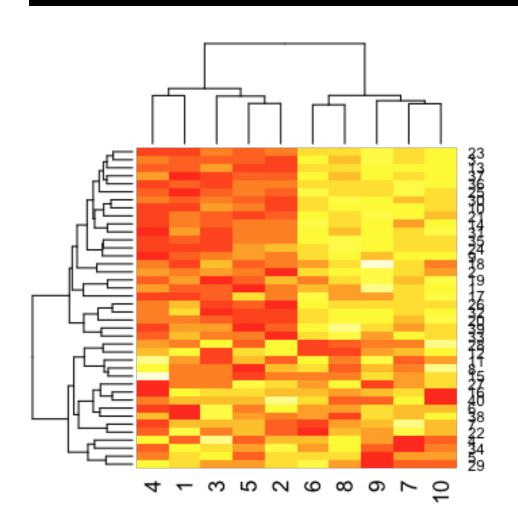


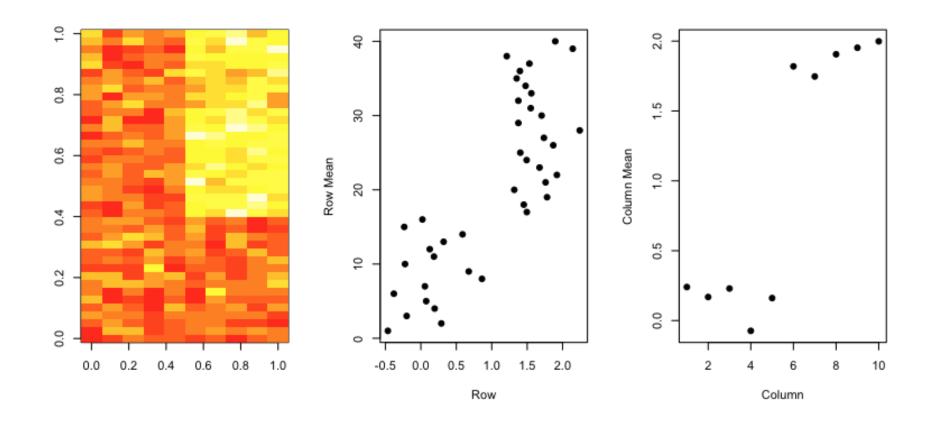
Columns of V<sup>T</sup>/rows of U are orthogonal and calculated one at a time Columns of V<sup>T</sup> describe patterns across genes Columns of U describe patterns across arrays

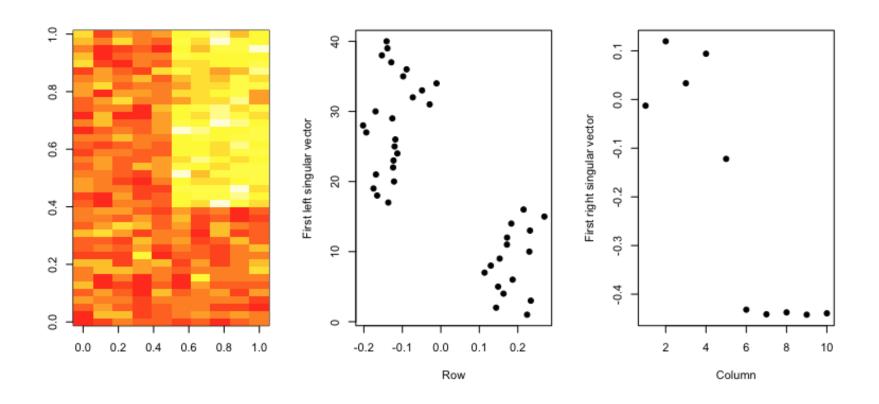
 $d_i^2/\sum_i d_i^2$  is the percent of variation explained by the ith column of V

Singular vectors/principal components

Method to identify patterns in the data

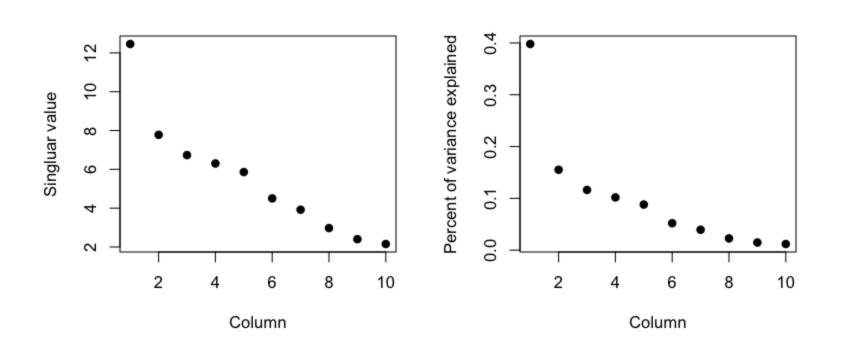


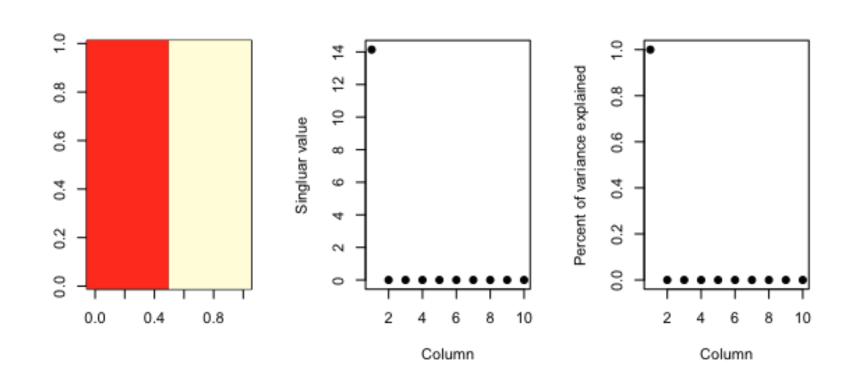




# Singular values

D is a diagonal matrix  $d_{ii} = \text{ith singular value}$   $d_{ii}^{2} / \sum d_{jj}^{2} = \text{percent variance}$  explained by ith singular vectors



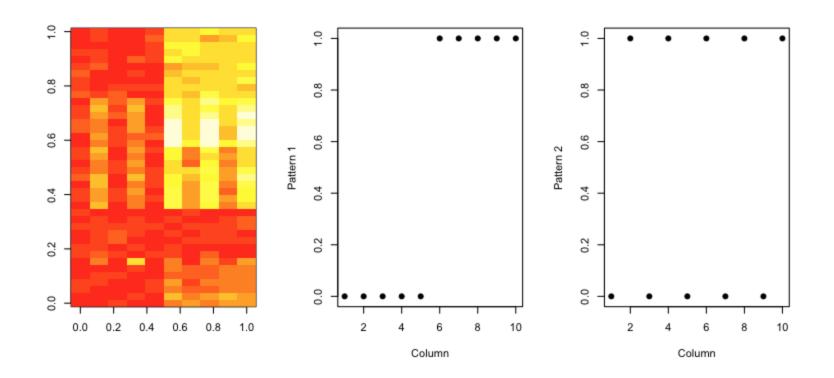


More than one pattern

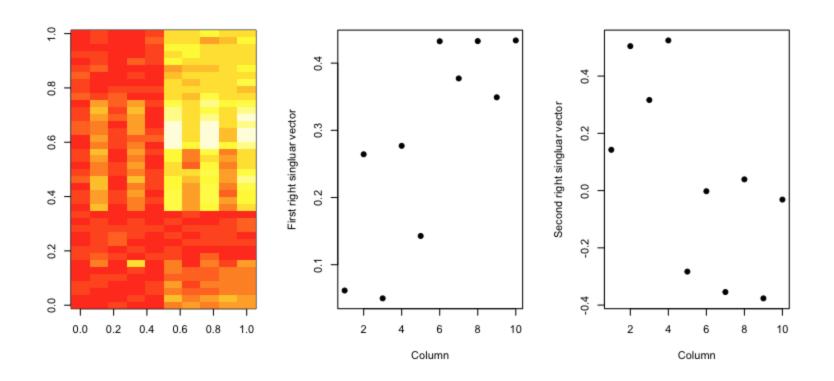
One PC/SV may not equal one "variable"

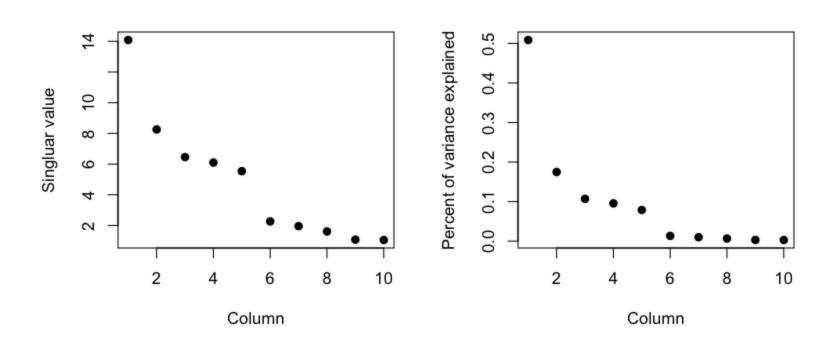
Patterns are orthogonal

#### https://github.com/jtleek/dataanalysis/tree/master/week3/006dimensionReduction



#### https://github.com/jtleek/dataanalysis/tree/master/week3/006dimensionReduction

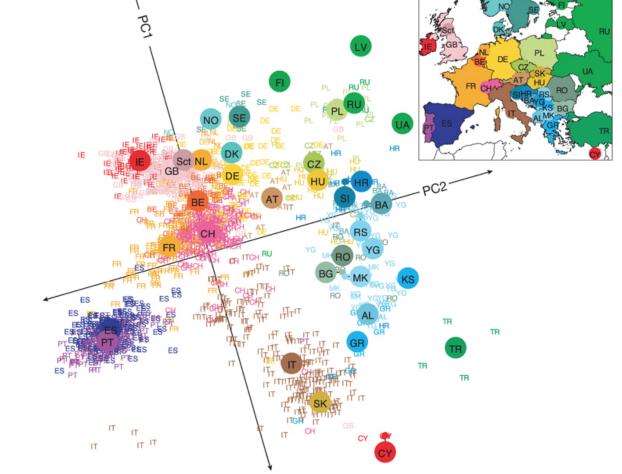




# How this is used Identify meaningful patterns

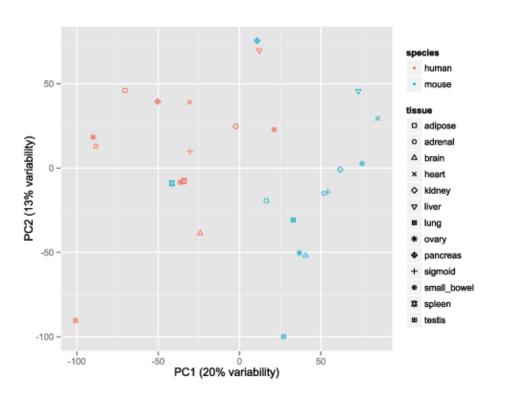
Find batch effects

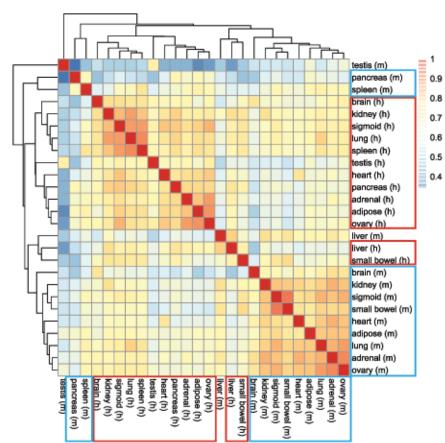
## http://www.nature.com/nature/journal/v456/n7218/full/nature07331.html



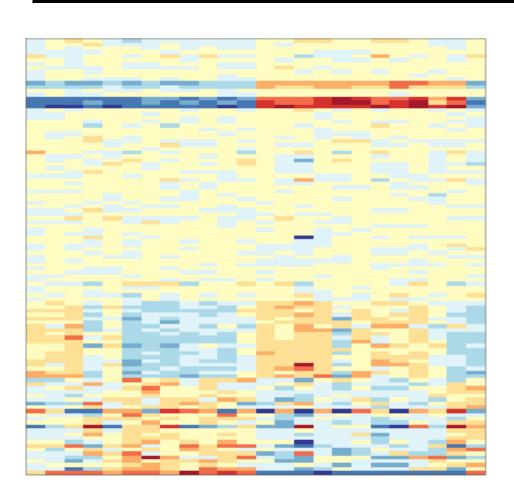
a

b





#### http://genomicsclass.github.io/book/pages/svacombat.html



#### http://genomicsclass.github.io/book/pages/svacombat.html

