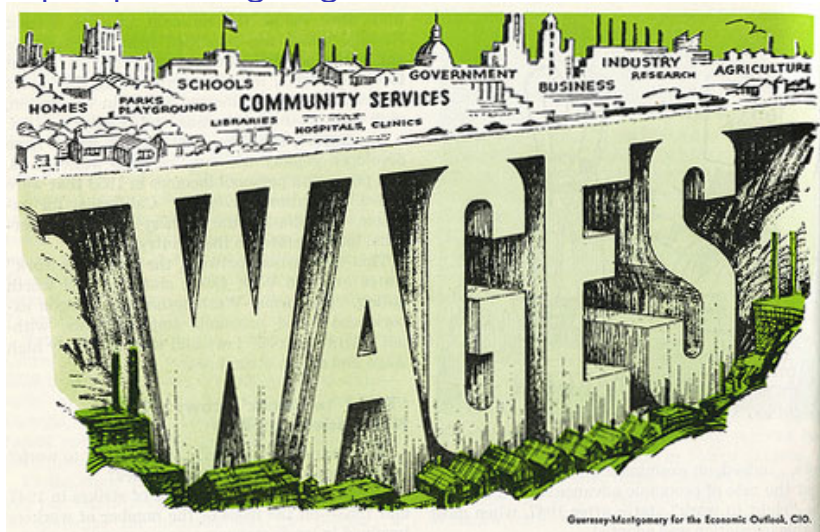


# Predicting with regression, multiple covariates

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## Example: predicting wages



Guernsey-Montgomery for the Economic Outlook, CIO.

Image Credit

<http://www.caahs-media.org/the-high-cost-of-low-wages>

Data from: ISIR package from the book: Introduction to statistical



## Example: Wage data

```
library(ISLR); library(ggplot2); library(caret);
```

```
## Loading required package: lattice
```

```
data(Wage); Wage <- subset(Wage,select=-c(logwage))  
summary(Wage)
```

```
##           year           age           sex  
## Min.      :2003   Min.      :18.00   1. Male    :3000   1. Never  
## 1st Qu.:2004   1st Qu.:33.75   2. Female:    0   2. Married  
## Median :2006   Median :42.00                   3. Widowed  
## Mean    :2006   Mean    :42.41                   4. Divorced  
## 3rd Qu.:2008   3rd Qu.:51.00                   5. Separated  
## Max.      :2009   Max.      :80.00  
##  
##           race           education  
## 1. White:2480   1. < HS Grad      :268   2. Middle Atl  
## 2. Black: 293   2. HS Grad        :971   1. New England
```

## Get training/test sets

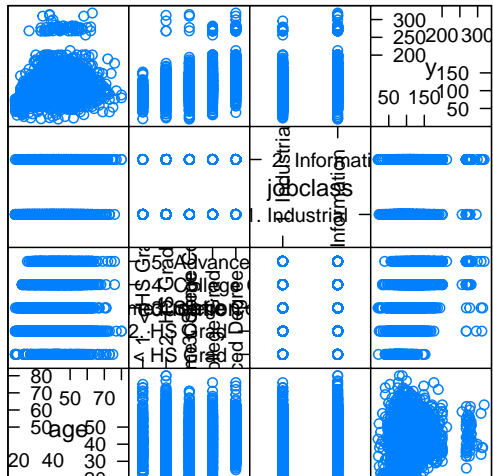
```
inTrain <- createDataPartition(y=Wage$wage,  
                                p=0.7, list=FALSE)  
training <- Wage[inTrain,]; testing <- Wage[-inTrain,]  
dim(training); dim(testing)
```

```
## [1] 2102  11
```

```
## [1] 898  11
```

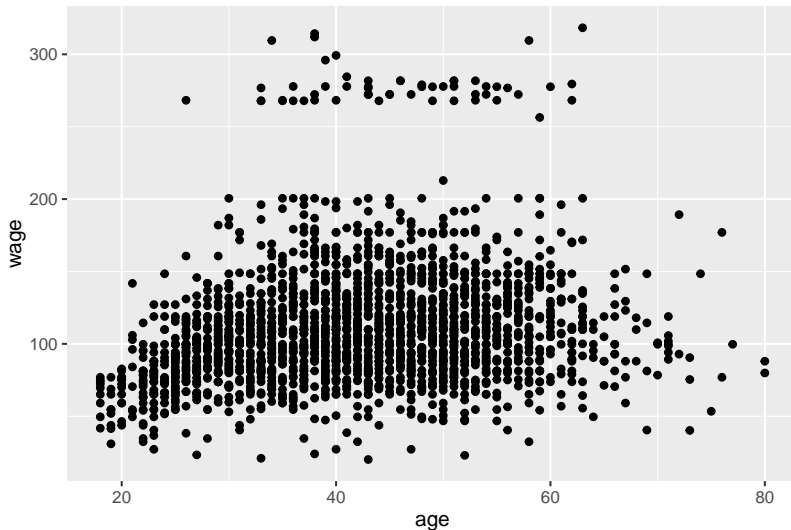
# Feature plot

```
featurePlot(x=training[,c("age", "education", "jobclass")],  
            y = training$wage,  
            plot="pairs")
```



## Plot age versus wage

```
qplot(age,wage,data=training)
```



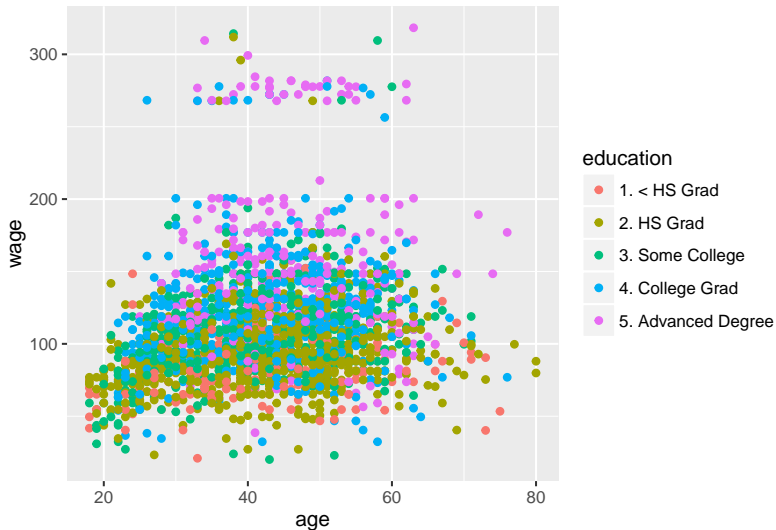
# Plot age versus wage colour by jobclass

```
qplot(age,wage,colour=jobclass,data=training)
```



# Plot age versus wage colour by education

```
qplot(age,wage,colour=education,data=training)
```





## Fit a linear model

$$ED_i = b_0 + b_1 age + b_2 I(\text{Jobclass}_i = \text{"Information"}) + \sum_{k=1}^4 \gamma_k I(\text{education}_i = \text{"Education"}_k)$$

```
modFit<- train(wage ~ age + jobclass + education,  
               method = "lm",data=training)  
finMod <- modFit$finalModel  
print(modFit)
```

```
## Linear Regression
```

```
##
```

```
## 2102 samples
```

```
## 10 predictor
```

```
##
```

```
## No pre-processing
```

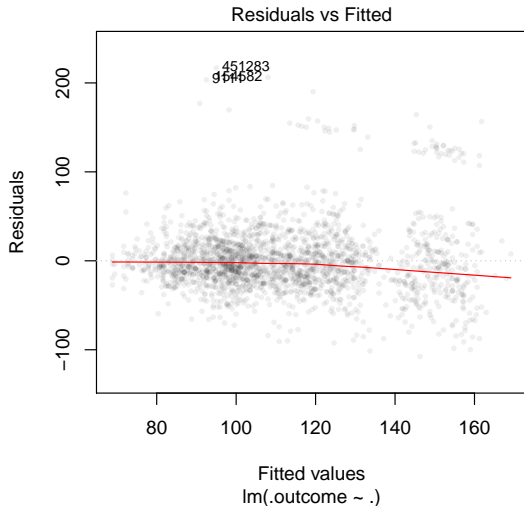
```
## Resampling: Bootstrapped (25 reps)
```

```
## Summary of sample sizes: 2102, 2102, 2102, 2102, 2102, 2102
```

```
## Resampling results:
```

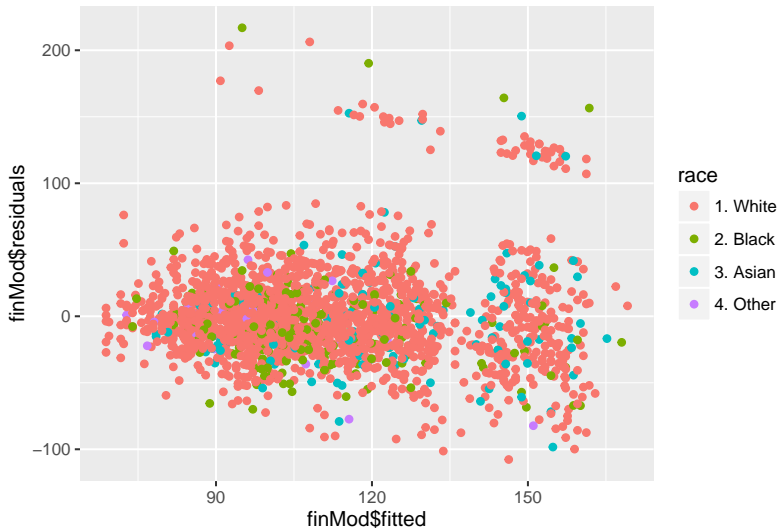
# Diagnostics

```
plot(finMod,1,pch=19,cex=0.5,col="#00000010")
```



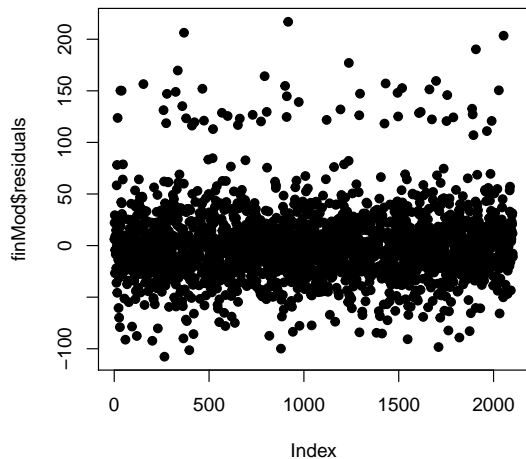
## Color by variables not used in the model

```
qplot(finMod$fitted,finMod$residuals,colour=race,data=train
```



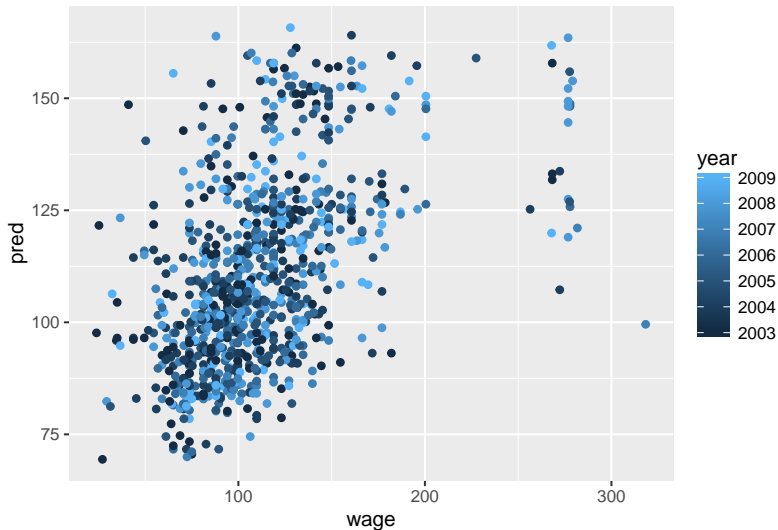
## Plot by index

```
plot(finMod$residuals,pch=19)
```



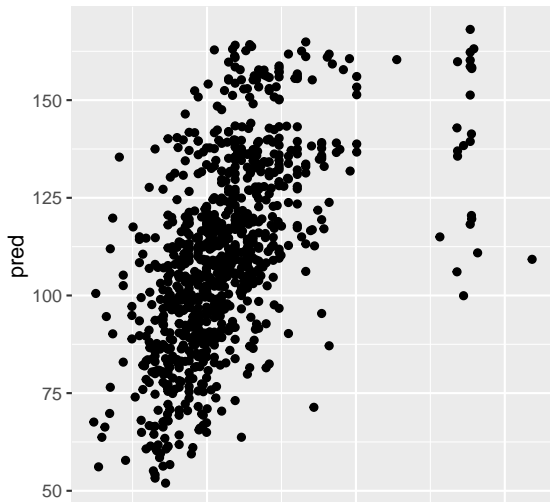
## Predicted versus truth in test set

```
pred <- predict(modFit, testing)
qplot(wage, pred, colour=year, data=testing)
```



## If you want to use all covariates

```
modFitAll<- train(wage ~ .,data=training,method="lm")  
pred <- predict(modFitAll, testing)  
qplot(wage,pred,data=testing)
```



# Notes and further reading

- ▶ Often useful in combination with other models
- ▶ Elements of statistical learning
- ▶ Modern applied statistics with S
- ▶ Introduction to statistical learning