K-means Clustering

Roger D. Peng, Associate Professor of Biostatistics

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Can we find things that are close together?

- How do we define close?
- How do we group things?
- How do we visualize the grouping?
- ▶ How do we interpret the grouping?

How do we define close?

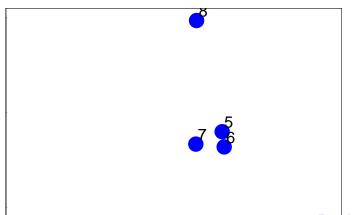
- Most important step
- ▶ Garbage in → garbage out
- Distance or similarity
- Continuous euclidean distance
- Continous correlation similarity
- Binary manhattan distance
- ▶ Pick a distance/similarity that makes sense for your problem

K-means clustering

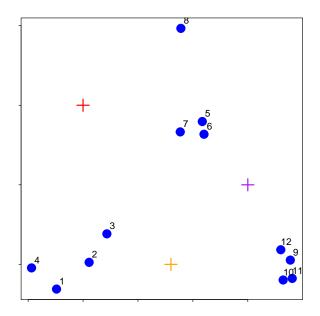
- A partioning approach
- ► Fix a number of clusters
- ▶ Get "centroids" of each cluster
- Assign things to closest centroid
- Reclaculate centroids
- Requires
- A defined distance metric
- A number of clusters
- An initial guess as to cluster centroids
- Produces
- Final estimate of cluster centroids
- An assignment of each point to clusters

K-means clustering - example

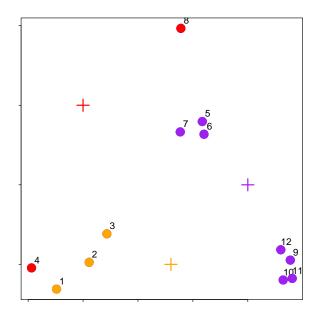
```
set.seed(1234); par(mar=c(0,0,0,0))
x <- rnorm(12,mean=rep(1:3,each=4),sd=0.2)
y <- rnorm(12,mean=rep(c(1,2,1),each=4),sd=0.2)
plot(x,y,col="blue",pch=19,cex=2)
text(x+0.05,y+0.05,labels=as.character(1:12))</pre>
```



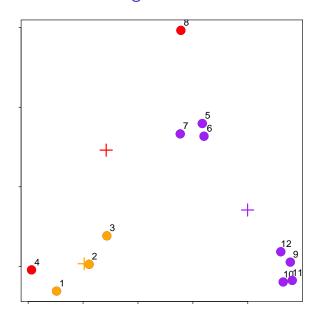
K-means clustering - starting centroids



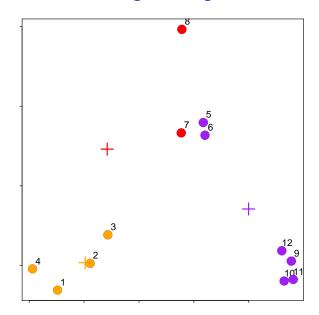
K-means clustering - assign to closest centroid



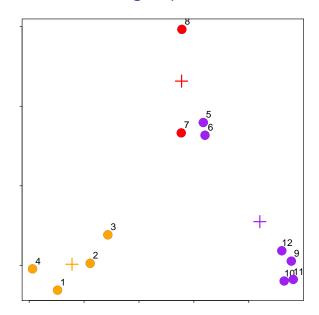
K-means clustering - recalculate centroids



K-means clustering - reassign values



K-means clustering - update centroids



kmeans()

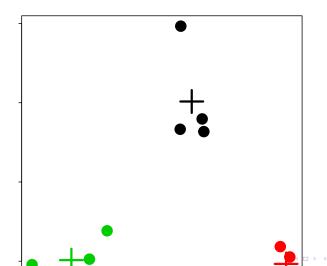
▶ Important parameters: *x*, *centers*, *iter.max*, *nstart*

[1] 3 3 3 3 1 1 1 1 2 2 2 2

```
dataFrame <- data.frame(x,y)</pre>
kmeansObj <- kmeans(dataFrame,centers=3)</pre>
names(kmeansObj)
## [1] "cluster" "centers"
                                   "totss"
                                                     "withi
## [5] "tot.withinss" "betweenss" "size"
                                                     "iter"
## [9] "ifault"
kmeansObj$cluster
```

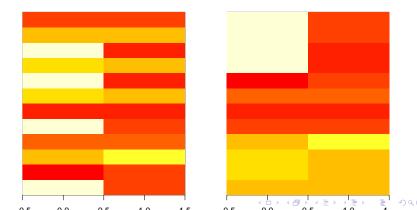
kmeans()

```
par(mar=rep(0.2,4))
plot(x,y,col=kmeansObj$cluster,pch=19,cex=2)
points(kmeansObj$centers,col=1:3,pch=3,cex=3,lwd=3)
```



Heatmaps

```
set.seed(1234)
dataMatrix <- as.matrix(dataFrame)[sample(1:12),]
kmeansObj <- kmeans(dataMatrix,centers=3)
par(mfrow=c(1,2), mar = c(2, 4, 0.1, 0.1))
image(t(dataMatrix)[,nrow(dataMatrix):1],yaxt="n")
image(t(dataMatrix)[,order(kmeansObj$cluster)],yaxt="n")</pre>
```



Notes and further resources

- K-means requires a number of clusters
- ▶ Pick by eye/intuition
- ▶ Pick by cross validation/information theory, etc.
- Determining the number of clusters
- K-means is not deterministic
- ▶ Different # of clusters
- Different number of iterations
- Rafael Irizarry's Distances and Clustering Video
- Elements of statistical learning