HiFT: A Hierarchical Full Parameter Fine-Tuning Strategy

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Abstract

Full-parameter fine-tuning (FPFT) has become the go-to choice for adapting language models (LMs) to downstream tasks due to its excellent performance. As LMs grow in size, fine-tuning the full parameters of LMs requires a prohibitively large amount of GPU memory. Existing approaches utilize zeroth-order optimizer to conserve GPU memory, which potentially compromises the performance of LMs as non-zero order optimizers tend to converge more readily on most downstream tasks. In this paper, we propose a novel optimizer-independent endto-end hierarchical fine-tuning strategy, HiFT, which only updates a subset of parameters at each training step. HiFT significantly reduces the amount of gradients and optimizer state parameters residing in GPU memory at the same time, thereby reducing GPU memory usage. Our results demonstrate that: (1) HiFT achieves comparable performance with parameter-efficient fine-tuning and standard FPFT. (2) Results on six models show that HiFT reduces the number of trainable parameters by about 89.18% on average compared to FPFT. (3) HiFT supports FPFT of 7B models for 24G GPU memory devices under mixed precision without using any memory saving techniques. (4) HiFT supports various optimizers including AdamW, AdaGrad, SGD, etc.

Introduction

Full-Parameter Fine-Tuning (FPFT) Language Models (LMs) has been a successful paradigm in various downstream tasks (Vaswani et al., 2017; Lewis et al., 2020; Liu et al., 2020; Lv et al., 2023). However, as the size of LMs becomes larger, FPFT LMs requires immense memory, which has become an obstacle to conduct research.

One line of research to reduce memory is to use heterogeneous memory (Pudipeddi et al., 2020; Raibhandari et al., 2021) (e.g., GPU, CPU, and NVMe memory) or distributed techniques (e.g., tensor parallelism (Shazeer et al., 2018; Shoeybi et al., 2019; Zhang et al.; Kim et al., 2023; Wu et al., 2023)). These strategies require parameter sharing across diverse devices and thus usually introduce a significant communication burden. Parameter-Efficient Fine-Tuning (PEFT) is another line of strategies for memory reduction, categorized into addition-based, selection-based, and reparametrization-based methods (Lialin et al., 2023). The addition-based methods (e.g., Prefix-Tuning (Li and Liang, 2021), AttentionFusion (Cao et al., 2022)) reduce the number of trainable parameters by only updating newly added parameters and freezing the weights of LMs. Although these methods reduce the number of pa- PEFT 增加额 rameters for fine-tuning, they expand the number 外参数, 加重 of model parameters and increase the burden on forward 负担 forward propagation. The selection-based methods (e.g, BitFit (Zaken et al., 2022), LT-SFT (Ansell et al., 2022), FAR (Vucetic et al., 2022)), on the other hand, fine-tune a subset of model parameters, resulting in a performance gap with FPFT. The reparametrization-based methods (e.g., LoRA (Hu et al., 2022a), KronA (Edalati et al., 2022), S4model (Chen et al., 2023)) leverage low-rank decomposition to minimize the number of trainable parameters. Using low-rank representations inevitably leads to information loss and performance degradation. PEFT involves a trade-off between serving efficiency and quality. According to existing works (Raschka, 2023; Artur et al., 2023; Kourosh and Rehaan, 2023), FPFT still maintains advantages in performance on most benchmarks.

Some works have reduced memory usage for FPFT by removing the momentum state of the optimizer. LOMO (Lv et al., 2023) reduces the memory usage of the optimizer momentum and gradients by integrating gradient calculation and update. However, LOMO requires forward propagation twice. In addition, LOMO forces the model to be 16-bit quantized and uses the gradient checkpointing technique (Chen et al., 2016) to reduce memory usage while LOMO has limited memory savings in real-

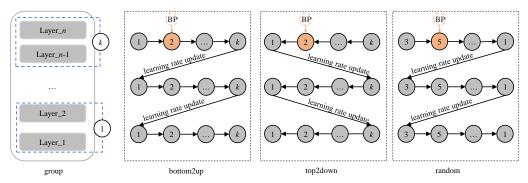


Figure 1: Schematic diagram of our HiFT. **group** represents the grouping operation of the layers. **bottom2up**, **top2down** and **random** are training strategies. Gray indicates that the corresponding parameters are in the frozen state, and brown indicates that the corresponding parameters are in the activated state. k is the number of groups, n is the number of layers of the given model, and BP denotes parameter update through back propagation.

world scenarios. MeZO (Malladi et al., 2023) designs a zeroth-order optimizer to reduce memory usage. However, MeZO is unstable and performs poorly without prompts. These methods make the momentum optimizers unusable, while the momentum optimizers such as AdamW (Loshchilov and Hutter, 2017) have been proven to be superior in improving the performance.

In order to perform FPFT on low-memory devices, we propose a novel end-to-end **Hi**erarchical Fine-Tuning (HiFT) strategy, adopting the idea of layer-by-layer training. HiFT divides the layers of the model into different groups. At each training step, HiFT updates the parameters of one group while freezing the others. Compared to standard FPFT, HiFT leads to different groups of parameters being updated with different learning rates. This causes the model parameters to be updated in an inconsistent amplitude, which leads to a decrease in model performance. To solve this problem, we adopt to delay the learning rate update, which only updates the learning rate once when all layers of model are updated. HiFT is also different from layer-wise training (Bengio et al., 2006), where the layer-wise training incrementally adds new layers to a pre-trained shallow model, only updating the newly added parameters at each training stage until all layers are updated. As a result, layer-wise strategy produces accumulated errors at different training stages due to its pipeline training.

HiFT can significantly reduce the number of trainable parameters per training step. We only keep the momentum and gradients of the parameters that need to be updated on the GPU device due to only a portion of the parameters are updated at each training step. This helps to reduce the GPU memory usage of the optimizer states and gradients.

Assuming we divide the layers of the model into k groups, the average memory usage by gradients and optimizer states is then only 1/k of standard FPFT theoretically. With the batch size being 1 and the sentence length being 512, using the HiFT strategy to full-parameter fine-tuning a 7B model requires about 16.87G, and a 13B model requires about 31G of memory. Given that the memory occupied by forward activations is also related to the input, we discuss the further details in experiments. Another important conclusion is HiFT does not significantly increase the time for fine-tuning. The main reason is that the amount of trainable parameters in a single step is reduced, the training speed of each step is accordingly improved. Although HiFT requires larger epochs (Under the same batch, generally 2 to 3 times and up to 5 times that of standard FPFT. With larger batches, the fine-tuning time gets greatly reduced.), due to the increase in the finetuning speed of a single step, the overall time does not increase significantly. In short, HiFT significantly saves the memory of FPFT at a slight time cost without losing performance.

2 Related Work

Full-Parameter Fine-tuning FPFT fine-tunes the pre-trained LMs on specific tasks by updating all parameters (Sun et al., 2023; Lin et al., 2024; Ma et al., 2024), which requires massive computing power as the parameters of LMs increase. Mixed-precision training enables high-throughput computations by employing half-precision storage for parameters, activations, and gradients (Rajbhandari et al., 2020a; Narayanan et al., 2021). Staged training incrementally increases the amount of compute and reuse the compute from prior stages (Shen et al., 2022). These methods increase the parameter

consumption when training precision or operators. LOMO (Lv et al., 2023) identifies the memory saving of SGD (Robbins and Monro, 1951), fuses the gradient computation and the parameter update in one step. MeZO (Malladi et al., 2023) designs a zeroth-order optimizer to use only two forward passes, which can be used to train a 30B model on a single A100 80GB GPU. These methods waste the superiority of momentum optimizers.

Parameter-Efficient Fine-tuning PEFT minimizes resource utilization from the perspective of parameters with additon, selection or decomposition methods (Lialin et al., 2023). The additionbased methods add and update new parameters with the weights of LMs frozen, such as Prefix-Tuning (Li and Liang, 2021), AttentionFusion (Cao et al., 2022), while the added parameters increase the burden on forward propagation. The selectionbased methods fine-tune a subset of the parameters of LMs, such as BitFit (Zaken et al., 2022), LT-SFT (Ansell et al., 2022), FAR (Vucetic et al., 2022), but has a performance gap with FPFT. The reparametrization-based methods leverage lowrank decomposition to minimize the number of trainable parameters, such as LoRA (Hu et al., 2022a), PHM (Karimi Mahabadi et al., 2021), KronA (Edalati et al., 2022), S4-model (Chen et al., 2023), while using low-rank representations inevitably leads to information loss and performance degradation. PEFT involves a trade-off between serving efficiency and quality.

Memory-Efficient Fine-tuning MEFT minimizes memory usage with heterogeneous memory (e.g., GPU, CPU and NVMe) or parallel methods (e.g., tensor and pipeline parallelism). In a layer-to-layer strategy (Pudipeddi et al., 2020), only the tensors necessary for the computation of a particular layer are transferred to GPU, while the remaining tensors are retained in CPU. ZeRO-Infinity (Rajbhandari et al., 2021) enables the partitioned states and tensors to CPU and NVMe. Tensor parallelism accelerates training by parallelizing tensor computations across different GPUs, but requires multiple global communications during each propagation (Shazeer et al., 2018; Shoeybi et al., 2019). Pipeline parallelism accelerates training by breaking the model into segments or layers and processing them sequentially in a pipeline fashion (Zhang et al.; Kim et al., 2023; Wu et al., 2023). These methods transfer massive memory to heterogeneous devices, although temporarily saving memory, still requires a large number of devices.

Different from existing works (Lv et al., 2023; Malladi et al., 2023), HiFT adopts the idea of layer-by-layer training to save memory of FPFT, and can be seamlessly integrated with any optimizer.

3 Approach

The overall training strategy of our **HiFT** is shown in Figure 1. Before elaborating on the details, we first present some necessary notations.

Notation Given the training dataset $\mathcal{D} = \{(x_i,y_i)\}_{i=1}^N$, the goal of the training is to learn a model M with n layers, where N is the number of the training samples, (x_i,y_i) is the labeled data pair. We use P to represent the optimizer, and η_t to represent the learning rate schedule. The number of layers in each group is represented by m and the number of groups is represented by k. If m is divisible by n, then k = n/m, otherwise $k = \lfloor n/m \rfloor + 1$. Queue Q is used to store special identifiers that uniquely identify different layers. $S \in \{\text{"bottom2up","top2down","random"}\}$ represents the adopted update strategy.

Consider a pre-trained LM $f_{\theta_{pre}}$ parameterized by θ_{pre} . Let θ_{fpft} and θ_{hift} denote parameters after full fine-tuning and hierarchical full-parameter fine-tuning after *one training step*, respectively. Let $\mathcal{L}_{\tau}(\mathcal{D};\theta)$ be the objective to minimize during fine-tuning, with \mathcal{D} being the input, θ being updated parameters, and τ being the task in fine-tuning. In the process of full fine-tuning, we optimize the model by adjusting its full parameters:

$$\theta_{fpft} = \operatorname*{argmin}_{\theta_{pre}} \mathcal{L}_{\tau}(\mathcal{D}; \theta_{pre}), \tag{1}$$

where the dimension of θ_{fpft} , $|\theta_{fpft}|$, equals the dimension of θ_{pre} , $|\theta_{pre}|$.

In the process of HiFT, only a subset of parameters are updated at one training step. More formally, with optimizing group $i \in \{1, ..., k\}$, we have:

$$\theta_{hift}^{(i)} = \underset{\beta_i \circ \theta_{hift}^{(i-1)}}{\operatorname{argmin}} \mathcal{L}(\mathcal{D}, \beta_i \circ \theta_{hift}^{(i-1)} + (1 - \beta_i) \circ \theta_{hift}^{(i-1)})$$
(2)

$$\theta_{hift}^{(1)} = \operatorname*{argmin}_{\beta_1 \circ \theta_{pre}} \mathcal{L}(\mathcal{D}, \beta_1 \circ \theta_{pre} + (1 - \beta_1) \circ \theta_{pre}), \quad (3)$$

where β_i denotes a fixed binary mask of parameters, with $\beta_i \in \{0,1\}^{|\theta_{pre}|}$, depending on the training strategy chosen in Figure 1. We simply denote $\theta_{hift}^{(k)}$ as θ_{hift} .

Algorithm 1: HiFT Training Algorithm

```
Require: model M with n layers, number of layers
 per group m, batch size B, step budget T, optimizer
 P, parameter queue Q, update strategy S, learning
 rate schedule \eta_t
Initialize: Initialize queue Q by layer identifier
UpdateStrategy(Q, S)
for t = 1, ..., T do
    a). Freeze all parameters of M;
    b). Sample batch \mathcal{B} \subset \mathcal{D} with random seed s
    Select key features of layers to be updated
    c). E \leftarrow \text{QueueGetAndRemove}(Q, m)
    Removed elements added to tail of queue
    d). QueueAddTail(Q, E)
    e). \theta_s \leftarrow \text{SelectParameters}(M, E)
    f). Set requires_grad = True of parameters \theta_s
    g). UpdateOptimizerParameter(P, \theta_s)
    h). ForwardPropagation(M, \mathcal{B})
    Preserve optimizer state of \theta_s within the GPU
    i). MoveOptimizerState2GPU(P, \theta_s)
    j). Backpropagation(P, \theta_s, M) & Clear
      gradients
     Keep optimizer state within the CPU
    k). MoveOptimizerState2CPU(P, oldsymbol{	heta}_s)
    if IsAllLayerUpdate(t, n, m) then
          Update learning rate \eta_t
     end
    else
          Keep the learning rate \eta_t constant
    end
end
```

3.1 Hierarchical Training

FPFT has been proven to achieve the-state-of-art performance in most downstream tasks (Raschka, 2023; Artur et al., 2023; Kourosh and Rehaan, 2023). Standard FPFT updates all parameters of M at each training step, which requires a large amount of GPU memory to store forward and backward propagation parameters at the same time. Different from standard FPFT, HiFT only updates a part of the model parameters and freezes the remaining parameters at each training step, and achieves fine-tuning of all parameters through layer-by-layer updates. During the BP process, only the parameters that need to be updated will be stored in the GPU memory, which greatly reduces the GPU memory requirements for FPFT.

As shown in Figure 1, we divide the model into k groups and update only one group of parameters in each step. All groups are iterated in sequence until convergence. We provide three update strategies: **bottom2up** (B2U), **top2down** (T2D) and **random** (RAN). Different strategies only represent different order of updates, e.g., bottom2up represents the update from the bottom to top. Note that random strategy only shuffles the grouping order before training, and maintains this order in the training

process, which avoids the instability caused by constant changes in the update order. Here, the embedding layer is regarded as the bottom layer, and the head layer used for classification or generation is the top layer.

The detailed training process is shown in Algorithm 1. The first step is to determine the update strategy. During training, we freeze all parameters. The layers to be updated, denoted by E, are selected from the queue Q based on the parameter m. The selected layer E is removed from head of the queue Q and added to the tail of Q to wait for the next update. We select the parameter θ_s that needs to be updated from M based on E, set the parameter θ_s to a computable gradient state and set the update parameter group of optimizer P to θ_s . Before parameter updates, the states parameters (e.g., the gradient first moment estimation and second moment estimation of AdamW) of optimizer P related to θ_s could be moved to GPU devices. After the completion of weight updates, the corresponding gradients are clean up and optimizer states parameters are moved to CPU. To update the learning rate η_t , we employ a delayed update strategy. Specifically, we adjust the learning rate once after updating all layers, which helps alleviate the instability issue arising from excessively updates in some layers, especially when fine-tuning deep models. By employing the successive update strategy, the number of parameters residing in GPU simultaneously reduces, thus lowering the GPU memory requirements of fine-tuned models.

Note that we provide a theoretical generalization bound for HiFT (Appendix A.1) and memory analysis (Appendix A.2).

4 Experiments

Due to space limitations, please refer to Appendix for datasets (A.3) and experimental setup (A.4).

4.1 Baselines

Language Models include RoBERTa (Liu et al., 2019) with base and large versions, GPT-2 (Radford et al., 2019) with medium and large versions, LLaMA (Touvron et al., 2023) with 7B and 13B versions, and OPT-13B (Zhang et al., 2022).

Fine-Tuning strategies include BitFit (Zaken et al., 2022), Adapter (Houlsby et al., 2019), Prefix (Lester et al., 2021), LoRA (Hu et al., 2022b), MeZO (Malladi et al., 2023), S4 (Chen et al., 2023), Adapter^L (Lin et al., 2020),

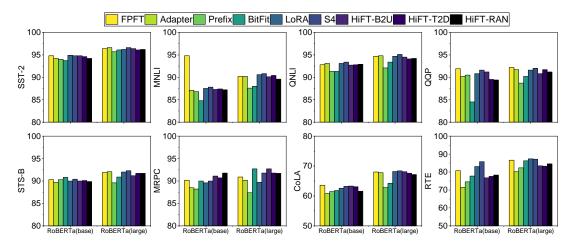


Figure 2: RoBERTa results on different fine-tuning strategies. We report accuracy metrics for the SST-2, QNLI, QQP, MRPC and RTE, mean accuracy for MNLI, spearman coefficient for STS-B and matthews correlation coefficient for CoLA. The m of HiFT is set to 1. B2U, T2D and RAN are bottom2up, top2down and random strategies.

PreLayer (Hu et al., 2022b), and FPFT. Optimizers include AdamW (Loshchilov and Hutter, 2017), SGDM (Qian, 1999), SGD, Adafactor (Shazeer and Stern, 2018), Adagrad (Duchi et al., 2010). Some baselines might only appear in certain experiments.

4.2 Performance Results

No prompt results Figure 2 shows the performance of RoBERTa_{base} and RoBERTa_{large} using different fine-tuning strategies on eight tasks. The HiFT performances of RoBERTa_{base} have competitive advantages with standard FPFT on datasets such as SST-2, MNLI, QNLI and QQP, and HiFT has achieved a weak performance advantage on the MRPC dataset. We observe that HiFT has certain performance advantages on most datasets compared to most PEFT methods such as BitFit, Prefix and Adapter. We get similar conclusions on RoBERTa_{large}. The number of layers of model RoBERTa_{large} is about twice that of RoBERTa_{base}, which reflects to a certain extent that HiFT is not affected by the depth of the model. Table 5 reports the results of GPT-2 including medium and large on the E2E dataset. Compared with standard FPFT, HiFT achieves competitive results on GPT-2 medium and large. Although LoRA has a weak advantage over HiFT in terms of performance, the overall performance of the two is very close.

Prompt results MeZO has higher performance under prompt fine-tuning. For a fair comparison, we used prompt templates (see Appendix B.4) of MeZO to perform hierarchical full-parameter fine-tuning. Table 1 reports the prompt-based fine-

tuning results of the RoBERTa_{large}. We clearly observe that HiFT has an absolute performance advantage compared to gradient-free methods including MeZO. Compared with standard FPFT and PEFT methods, HiFT still achieves competitive results. Table 2 reports the performance comparison of OPT-13B using different fine-tuning methods on different tasks. We observe that among the 11 tasks, HiFT enjoys performance advantages in 7 tasks. On different task types, HiFT achieves the same or even better performance than standard FPFT, which fully demonstrates the universal effectiveness of HiFT fine-tuning method.

4.3 Memory Profiling

To evaluate the effectiveness of HiFT in reducing memory, we conduct extensive experiments on different optimizers (i.e., AdamW, SGDM, SGD, Adafactor and Adagrad) based on multiple LMs including RoBERTa_{base}, RoBERTa_{large}, GPT-2_{large}, GPT-Neo (2.7B), LLaMA-2 (7B) and LLaMA-2 (13B). HiFT reduces memory usage from three aspects: gradients, optimizer states, and residual states. Since HiFT only updates a small number of parameters in each step, this directly reduces the amount of trainable parameters in each training step, and the corresponding gradient parameters and optimizer state parameters also be reduced in the same proportion. When only some layer parameters are updated in each step, the amount of parameters tracking gradients in the calculation graph is reduced, including the amount of parameters in the activations, so HiFT also reduces the amount of parameters in residual states. The reduction in

| | SST-2 | SST-5 | SNLI | MNLI | RTE | TREC |
|---------------|------------|------------|-----------------|----------------|-------------|------------|
| Task Type | —— sentime | nt —— | —— natur | al language ii | ıference —— | — topic — |
| Zero-shot† | 79 | 35.5 | 50.2 | 48.8 | 51.4 | 32 |
| | | Gradient | -free methods: | k = 16 | | |
| LP† | 76.0 (2.8) | 40.3 (1.9) | 66.0 (2.7) | 56.5 (2.5) | 59.4 (5.3) | 51.3 (5.5) |
| MeZO† | 90.5 (1.2) | 45.5 (2.0) | 68.5 (3.9) | 58.7 (2.5) | 64.0 (3.3) | 76.9 (2.7) |
| MeZO(LoRA)† | 91.4 (0.9) | 43.0 (1.6) | 69.7 (6.0) | 64.0 (2.5) | 64.9 (3.6) | 73.1 (6.5) |
| MeZO(prefix)† | 90.8 (1.7) | 45.8 (2.0) | 71.6 (2.5) | 63.4 (1.8) | 65.4 (3.9) | 80.3 (3.6) |
| MeZO-Adam† | 90.4 (1.4) | 45.4 (1.5) | 74.1 (2.7) | 64.3 (0.8) | 59.2 (11.1) | 78.3 (1.4) |
| | | Gradient- | based methods: | k = 16 | | |
| FPFT† | 91.9 (1.8) | 47.5 (1.9) | 77.5 (2.6) | 70.0 (2.3) | 66.4 (7.2) | 85.0 (2.5) |
| FPFT(LoRA)† | 91.4 (1.7) | 46.7 (1.1) | 74.9 (4.3) | 67.7 (1.4) | 66.1 (3.5) | 82.7 (4.1) |
| FPFT(prefix)† | 91.9 (1.0) | 47.7 (1.1) | 77.2 (1.3) | 66.5 (2.5) | 66.6 (2.0) | 85.7 (1.3) |
| HiFT | 91.9 (2.3) | 47.8 (2.6) | 76.7 (3.5) | 69.9 (1.9) | 66.3 (4.5) | 84.3 (4.1) |
| | | Gradient- | free methods: k | z = 512 | | |
| LP† | 91.3 (0.5) | 51.7 (0.5) | 80.9 (1.0) | 71.5 (1.1) | 73.1 (1.5) | 89.4 (0.5) |
| MeZO† | 93.3 (0.7) | 53.2 (1.4) | 83.0 (1.0) | 78.3 (0.5) | 78.6 (2.0) | 94.3 (1.3) |
| MeZO(LoRA)† | 93.4 (0.4) | 52.4 (0.8) | 84.0 (0.8) | 77.9 (0.6) | 77.6 (1.3) | 95.0 (0.7) |
| MeZO(prefix)† | 93.3 (0.1) | 53.6 (0.5) | 84.8 (1.1) | 79.8 (1.2) | 77.2 (0.8) | 94.4 (0.7) |
| MeZO-Adam† | 93.3 (0.6) | 53.9 (0.8) | 85.3 (0.8) | 79.6 (0.4) | 79.2 (1.2) | 95.1 (0.3) |
| | | Gradient-b | pased methods: | k = 512 | | |
| FPFT† | 93.9 (0.7) | 55.9 (0.9) | 88.7 (0.8) | 84.4 (0.8) | 82.7 (1.4) | 97.3 (0.2) |
| FPFT(LoRA)† | 94.2 (0.2) | 55.3 (0.7) | 88.3 (0.5) | 83.9 (0.6) | 83.2 (1.3) | 97.0 (0.3) |
| FPFT(prefix)† | 93.7 (0.3) | 54.6 (0.7) | 88.3 (0.7) | 83.3 (0.5) | 82.5 (0.8) | 97.4 (0.2) |
| HiFT | 94.2 (0.6) | 57.2 (0.8) | 88.1 (1.2) | 83.8 (0.8) | 82.6 (0.9) | 96.7 (0.3) |

Table 1: Performance of RoBERTa_{large} based on prompt fine-tuning. LP: Linear probing; MeZO, MeZO(LoRA) and and MeZO(prefix): memory-efficient ZO-SGD with full-parameter tuning, LoRA, and prefix-tuning respectively; FPFT: fine-tuning with AdamW. All reported numbers are averaged accuracy (standard deviation). HiFT uses AdamW and bottom2up strategy. † means the result comes from Malladi et al. (2023)

the number of parameters significantly reduces the GPU memory usage during fine-tuning.

Table 3 reports the memory usage of the parameters, gradients, optimizer states and residual states under FPFT and HiFT for LLaMA-2 (7B). When using the AdamW optimizer and standard mixed precision, HiFT can save about 34.34%-34.46% of memory on RoBERTa_{base}, about 35.34%-36.16% of memory on RoBERTa_{large}, about 26.92%-27.55% of memory on GPT-2_{large}, about 49.65%-54.45% of memory on GPT-Neo and about 57.70%-61.01% of memory on LLaMA compared with FPFT. When using a larger batch size, HiFT is able to save more GPU memory. Please refer to Appendix B for the results of RoBERTa_{base} (Table 6), RoBERTa_{large} (Table 7), GPT-2_{large} (Table 8) and GPT-Neo (2.7B) (Table 9).

Figure 4 shows the percentage of memory used by the parameters of each part when fine-tuning LLaMA (7B) under standard FPFT and HiFT with the AdamW optimizer. Under standard FPFT, the optimizer states occupies the most memory. When fine-tuning 32-bit precision (Figure 4 (a)), the memory occupied by residual states is second only to the

optimizer state. When mixed precision fine-tuning (Figure 4 (c)), the memory used by model parameters exceeds the memory used by residual states is secondary to the optimizer states. The main reason is that in mixed precision training, both 32-bit and half-precision parameters exist at the same time. Therefore, model parameters occupy more memory in mixed precision. HiFT significantly reduces the memory usage of gradients and optimizer states. Therefore, when using HiFT for full-parameter fine-tuning, the main memory-consuming parts are the model parameters and residual states.

We observe an interesting phenomenon when fine-tuning the GPT-Neo (2.7B) (Table 9 in Appendix B) and LLaMA-2 (7B) (Table 3) using mixed precision, the memory usage is higher than FPFT. We find that when using mixed precision fine-tuning, both single-precision and half-precision parameters of the model exist simultaneously. Therefore, the model parameters use more memory in mixed precision than in standard FPFT. Mixed precision mainly focuses on reducing the memory usage of activation states (i.e., residual states). When the model's own parameter size is

| TasK | SST2 | RTE | СВ | BoolQ | WSC | WIC | MultiRC | COPA | ReCoRD | SQuAD | DROP |
|----------------|------|------|------|----------------|-------|------|---------|---------|------------|-------|--------|
| Task type | | | | - classificati | ion — | | | -multip | le choice— | gener | ation— |
| Zero-shot† | 58.8 | 59.6 | 46.4 | 59.0 | 38.5 | 55.0 | 46.9 | 80.0 | 81.2 | 46.2 | 14.6 |
| ICL† | 87.0 | 62.1 | 57.1 | 66.9 | 39.4 | 50.5 | 53.1 | 87.0 | 82.5 | 75.9 | 29.6 |
| LP† | 93.4 | 68.6 | 67.9 | 59.3 | 63.5 | 60.2 | 63.5 | 55.0 | 27.1 | 3.7 | 11.1 |
| MeZO† | 91.4 | 66.1 | 67.9 | 67.6 | 63.5 | 61.1 | 60.1 | 88.0 | 81.7 | 84.7 | 30.9 |
| MeZO (LoRA)† | 89.6 | 67.9 | 66.1 | 73.8 | 64.4 | 59.7 | 61.5 | 84.0 | 81.2 | 83.8 | 31.4 |
| MeZO (prefix)† | 90.7 | 70.8 | 69.6 | 73.1 | 60.6 | 59.9 | 63.7 | 87.0 | 81.4 | 84.2 | 28.9 |
| FPFT† | 92.0 | 70.8 | 83.9 | 77.1 | 63.5 | 70.1 | 71.1 | 79.0 | 74.1 | 84.9 | 31.3 |
| HiFT | 94.4 | 78.7 | 83.1 | 78.1 | 63.6 | 69.4 | 71.9 | 88.0 | 81.4 | 86.1 | 32.7 |

Table 2: Experiments on OPT-13B (with 1000 examples). ICL: in-context learning; LP: linear probing; FPFT: full fine-tuning; Prefix: prefix-tuning. The parameter m of HiFT is set to 1. All experiments use prompts in Appendix B.4. † means the result comes from Malladi et al. (2023)

large, the memory increase of the model parameters may be greater than the memory reduction of mixed precision (when the batch size is not large enough). Therefore, it may appear that the memory usage of mixed precision is greater than standard FPFT. Due to the large number of parameters of LLMs (large language models), it is difficult to use larger batch sizes, so it is difficult to bring out the advantages of mixed precision in the context of large models. HiFT is an optional, more efficient solution that maintains single-precision full-parameter fine-tuning while greatly reducing memory usage. We would like to emphasize that the current mixed precision does not support hierarchical operations, so it cannot take advantage of HiFT.

To fully exploit the advantages of HiFT, we have adapted mixed precision to HiFT. That is, each step only moves the single-precision weight corresponding to the parameter that needs to be updated to the GPU (Mixed precision makes a single-precision backup of the weights of the half-precision model.). Table 3 reports the memory profiling for LLaMA2-7B using adapted mixed precision. When using the AdamW optimizer, the adapted mixed precision for HiFT saves approximately 74.87% of GPU memory. When the batch size is 1, fine-tuning the LLaMA-7B model on the E2E data set requires approximately 16.87G of GPU memory, and finetuning the LLaMA-13B model requires approximately 31G of memory. This means that HiFT supports FPFT of a 7B model on a device with 24G GPU memory. Figure 4 (e) reports the changes in the amount of peak fine-tuning parameters under HiFT at different model sizes. We observe that as the number of model parameters increases, the proportion of peak trainable parameters gradually decreases. When fine-tuning the 13B model, the peak amount of fine-tunable parameters is only 2.44% of the original model parameter amount.

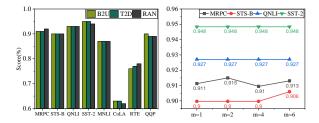


Figure 3: The left shows the performance of HiFT of RoBERTa_{base} under **B2U**, **T2D** and **RAN** strategies, respectively. The right shows the performance of HiFT of RoBERTa_{base} under different grouping settings, where m is the number of layers in each group.

4.4 Wallclock Time Efficiency

Table 10 and Table 11 report the running time of fine-tuning RoBERTa and OPT-13B, respectively. We observe that standard full-parameter fine-tuning has a speed advantage over HiFT on RoBERTa_{base}, while HiFT has a speed advantage over standard full-parameter fine-tuning on RoBERTa_{large}. We believe that the RoBERTa_{base} has a small number of parameters and does not reach the computing bottleneck of the GPU. HiFT requires the CPU and GPU to communicate with a small number of parameters, resulting in a slight speed disadvantage. However, for the larger RoBERTa_{large} model, HiFT has an absolute speed advantage over standard FPFT. On RoBERTa_{large}, the running time of each step of HiFT is in average 1.38 times faster than that of FPFT. Table 11 shows that the average time to fine-tune the OPT-13B on all tasks is approximately 1.32 hours. Under the same batch, the epochs required for hift fine-tuning are generally 2 to 3 times or up to 5 times that of standard FPFT. With larger batches, the fine-tuning time greatly reduces. Compared with the memory advantage brought by HiFT, the weak time disadvantage of our HiFT is acceptable.

| | | | #Trainable | | | | | Residual | |
|-------------|---------------------|--------|-------------------|-----------|----------|----------|----------|------------|-----------|
| Optimizei | #Dtype | #FType | Parameters | #Para(MB) | #Gra(MB) | #Sta(MB) | #PGS(GB) | States(GB) | Total(GB) |
| | FP32 | FPFT | 6738.42M | 25705.04 | 25705.04 | 51410.08 | 100.41 | 41.7 | 142.11 |
| AdamW - | FF32 | HiFT | 202.38M | 25705.04 | 772.03 | 1544.06 | 27.36 | 28.04 | 55.41 |
| Adamw | Mixed | FPFT | 6738.42M | 38557.56 | 25705.04 | 51410.08 | 112.96 | 32.54 | 145.50 |
| _ | MIXCu | HiFT | 202.38M | 38557.56 | 772.03 | 1544.06 | 39.92 | 21.62 | 61.54 |
| | $Mixed^{Hi}$ | HiFT | 202.38M | 13624.53 | 772.03 | 1544.06 | 15.57 | 21.00 | 36.57 |
| | FP32 | FPFT | 6738.42M | 25705.04 | 25705.04 | 25705.04 | 75.31 | 41.71 | 117.01 |
| SGDM - | 1132 | HiFT | 202.38M | 25705.04 | 772.03 | 772.03 | 26.61 | 28.8 | 55.41 |
| SGDM | Mixed | FPFT | 6738.42M | 38557.56 | 25705.04 | 25705.04 | 87.86 | 32.54 | 120.40 |
| _ | WIIACU | HiFT | 202.38M | 38557.56 | 772.03 | 772.03 | 39.16 | 22.37 | 61.54 |
| | MixedHi | HiFT | 202.38M | 13624.53 | 772.03 | 772.03 | 14.81 | 21.75 | 36.57 |
| | FP32 | FPFT | 6738.42M | 25705.04 | 25705.04 | 0.00 | 50.21 | 41.72 | 91.93 |
| SGD - | 1132 | HiFT | 202.38M | 25705.04 | 772.03 | 0.00 | 25.86 | 29.55 | 55.41 |
| SGD | Mixed | FPFT | 6738.42M | 38557.56 | 25705.04 | 0.00 | 62.76 | 32.54 | 95.30 |
| _ | WIIACU | HiFT | 202.38M | 38557.56 | 772.03 | 0.00 | 38.41 | 23.13 | 61.54 |
| | MixedHi | HiFT | 202.38M | 13624.53 | 772.03 | 0.00 | 14.06 | 22.51 | 36.57 |
| | FP32 | FPFT | 6738.42M | 25705.04 | 25705.04 | 10.82 | 50.22 | 41.72 | 91.94 |
| Adafactor - | | HiFT | 202.38M | 25705.04 | 772.03 | 0.33 | 25.86 | 29.55 | 55.41 |
| Adalactor | Mixed | FPFT | 6738.42M | 38557.56 | 25705.04 | 10.82 | 62.77 | 32.54 | 95.31 |
| _ | MIXCU | HiFT | 202.38M | 38557.56 | 772.03 | 0.33 | 38.41 | 23.13 | 61.54 |
| | Mixed ^{Hi} | HiFT | 202.38M | 13624.53 | 772.03 | 0.33 | 14.06 | 22.51 | 36.57 |
| | FP32 | FPFT | 6738.42M | 25705.04 | 25705.04 | 25705.04 | 75.31 | 41.72 | 117.01 |
| | 1132 | HiFT | 202.38M | 25705.04 | 772.03 | 772.03 | 26.61 | 28.80 | 55.41 |
| Adagrad | Mixed | FPFT | 6738.42M | 38557.56 | 25705.04 | 25705.04 | 87.86 | 32.54 | 120.40 |
| _ | | HiFT | 202.38M | 38557.56 | 772.03 | 772.03 | 39.16 | 22.37 | 61.54 |
| Mixed | | HiFT | 202.38M | 13624.53 | 772.03 | 772.03 | 14.81 | 21.75 | 36.57 |

Table 3: The GPU memory usage of fine-tuning LLaMA (7B) on the E2E dataset. The sequence length and batch size are set to 512 and 6, respectively. **#Dtype** represents the data type used for training, where **FP32** represents fully parameter fine-tuning the model with 32-bit precision, **mixed** represents fine-tuning with standard mixed precision and **mixed**^{Hi} represents the mixed precision adapted to HiFT. **#Trainable parameters** represents the maximum number of trainable parameters that appear in a single step during the fine-tuning process. **#Para** represents the memory occupied by the model parameters, **#Gra** represents the memory occupied by the gradient, and **#Sta** represents the memory occupied by the optimizer state. **#PGS** represents the sum of memory occupied by model parameters (i.e., **#Para**), gradients (i.e., **#Gra**) and optimizer state (i.e., **#Sta**). **Residual states** mainly includes activation, temporary buffers and unusable fragmented memory. **Total** represents the total memory used during fine-tuning. The parameter m of HiFT is set to 1.

4.5 Impact of Strategy

The left plot of Figure 3 reports the performance of RoBERTa_{base} using B2U, T2D and RAN strategies. We observe that the order of updates has almost no effect on the performance of the model. It is an interesting phenomenon that the model still achieves competitive results even when updated in a random order. Changing the update order does not affect the position of the corresponding layer in the model, which is the reason why the performance is not affected. We believe that this phenomenon provides support for hierarchical parallel fine-tuning of large-scale models in the future.

4.6 Impact of Grouping

The right plot of Figure 3 reports the impact of different grouping settings on model performance. Although different grouping settings can cause fluctuations in model performance, the overall impact is negligible. We use the learning rate delayed update strategy, which updates the learning rate

only after all layers are updated once. This strategy ensures that the learning rate used to update the parameters of each layer is the same in each training step, which helps to prevent the model performance from decreasing due to the update of some parameters being too fast in the hierarchical update process.

Conclusion

In this paper, we propose an end-to-end hierarchical full-parameter fine-tuning strategy, HiFT, which groups the model parameters and updates a single group of parameters per training step. The number of trainable parameters per training step greatly reduce, which lowers the GPU memory usage of the corresponding gradients, optimizer state parameters, and activations. HiFT lowers the barrier of full-parameter fine-tuning of language models and supports full-parameter fine-tuning of a 7B model on a 24G memory device.

Limitations

Although HiFT achieves the performance of standard full-parameter fine-tuning at a lower GPU memory cost, there are still some shortcomings. HiFT divides the model by layers, and the maximum division limit is the number of layers of the model. Due to the limitation of the number of layers, HiFT cannot break through the number of model layers for finer-grained division. When the model width is large, it limits HiFT's capabilities. On the other hand, after dividing the model, the number of parameters in each group is different, and the GPU memory usage fluctuates during the fine-tuning process. The peak memory occupied by the fine-tuned model is the decisive factor that determines whether the model is able to be fine-tuned on a certain device. This fluctuation in memory usage during fine-tuning prevents us from fully utilizing resources.

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Appendix

Generalization Bound for HiFT

In this section, we establish the generalization bound for HiFT, first building upon a quantization assumption as in Panigrahi et al. (2023). It is important to note that quantization is a common practical consideration; for instance, in our work, we implement a 32-bit quantization precision.

Assumption 1. (Quantization bound) Given model parameters θ , we denote $\bar{q}(\theta)$ to be the parameter that quantizes every parameter into the q given values. Then there exist $\varepsilon > 0$ s.t. for any sample x_i with label y_i at any training step, we have

$$|\mathcal{L}((x_i, y_i); \bar{q}(\theta)) - \mathcal{L}((x_i, y_i); \theta)| \le \varepsilon. \tag{4}$$

Assumption 2. (Uniform convergence generalization bound for subset parameter fine-tuning) Following Panigrahi et al. (2023), we deviate from the classical uniform convergence generalization bound (Nagarajan and Kolter, 2019) to get a tighter uniform convergence generalization bound for HiFT:

$$\mathcal{L}_{test}(\theta_{hift}^{(i)}) - \mathcal{L}_{train}(\theta_{hift}^{(i)})$$

$$\leq \sup_{\widetilde{\theta}_{hift}^{(i)} \in \Theta} |\mathcal{L}_{test}(\widetilde{\theta}_{hift}^{(i)}) - \mathcal{L}_{train}(\widetilde{\theta}_{hift}^{(i)})|,$$
(5)

where Θ denotes the subset of parameter space, $\theta_{hift}^{(i)}$ being the parameter after i-th optimizing step at one training step.

Theorem 3. (HiFT generalization bound) *Under* Assumption 1 and 2, we have the following generalization bound for HiFT:

$$\mathcal{L}_{test}(\theta_{hift}^{(k)}) - \mathcal{L}_{test}(\theta^*) \\
\leq 4k\epsilon + 2\sum_{i=1}^{k} \sup_{\widetilde{\theta}^{(i)}} |\mathcal{L}_{test}(\overline{q}(\widetilde{\theta}^{(i)})) - \mathcal{L}_{train}(\overline{q}(\widetilde{\theta}^{(i)}))| \\
+ \mathcal{L}_{test}(\theta^{(k)*}) - \mathcal{L}_{test}(\theta^*), \tag{6}$$

where θ^* denotes the parameter with the best test performance, $\widetilde{\theta}^{(i)}$ is in the space of $\beta_i \circ \theta_{pre}$ and $\theta^{(i)*}$ denotes the parameter with the best test performance when only changing the subset parameter $\beta_i \circ \theta_{pre}$. With probability at least $1 - \delta$, the second term $2 \sum_{i=1}^k \sup_{\widetilde{\theta}^{(i)}} |\mathcal{L}_{test}(\overline{q}(\widetilde{\theta}^{(i)}))|$ $\mathcal{L}_{train}(\bar{q}(\widetilde{\theta}^{(i)}))$ can be further bounded:

$$2\sum_{i=1}^{k} \sup_{\widetilde{\theta}^{(i)}} |\mathcal{L}_{test}(\overline{q}(\widetilde{\theta}^{(i)})) - \mathcal{L}_{train}(\overline{q}(\widetilde{\theta}^{(i)}))|$$

$$\leq 2\sum_{i=1}^{k} \sqrt{\frac{s_{i} \log q + \log(1/\delta)}{N}},$$
(7)

where s_i denotes the number of parameters in each optimizing group i.

Proof. We first derive HiFT generalization bound between the objective with parameters after a first step of optimization at one training step $\mathcal{L}_{test}(heta_{hift}^{(1)})$ and the objective with parameters that has the best test performance $\mathcal{L}_{test}(\theta^*)$:

$$\mathcal{L}_{test}(\theta_{hift}^{(1)}) - \mathcal{L}_{test}(\theta^*) \\
\leq 4\epsilon \\
+ 2 \sup_{\widetilde{\theta}^{(1)}} |\mathcal{L}_{test}(\overline{q}(\widetilde{\theta}^{(1)})) - \mathcal{L}_{train}(\overline{q}(\widetilde{\theta}^{(1)}))| \\
+ \mathcal{L}_{test}(\theta^{(1)*}) - \mathcal{L}_{test}(\theta^*),$$
(8)

with probability at least $1 - \delta$, the second term can be bounded:

$$2 \sup_{\widetilde{\theta}^{(1)}} |\mathcal{L}_{test}(\overline{q}(\widetilde{\theta}^{(1)})) - \mathcal{L}_{train}(\overline{q}(\widetilde{\theta}^{(1)}))|$$

$$\leq 2\sqrt{\frac{s_1 \log q + \log(1/\delta)}{N}}$$
(9)

The above inequality can be shown by considering Theorem D.2 in Panigrahi et al. (2023) and taking $\Theta_N = 1$. Similarly, we can have:

$$\mathcal{L}_{test}(\theta_{hift}^{(i)}) - \mathcal{L}_{test}(\theta_{hift}^{(i-1)}) \\
\leq 4\epsilon \\
+ 2 \sup_{\widetilde{\theta}^{(i)}} |\mathcal{L}_{test}(\overline{q}(\widetilde{\theta}^{(i)})) - \mathcal{L}_{train}(\overline{q}(\widetilde{\theta}^{(i)}))| \\
+ \mathcal{L}_{test}(\theta^{(i)*}) - \mathcal{L}_{test}(\theta_{hift}^{(i-1)})$$
(10)

Summing over the above terms with $i = \{1, ..., k\}$ completes the proof of this theorem.

A.2 Memory Analysis

According to previous work (Lv et al., 2023; Malladi et al., 2023), the main components that consume GPU memory during the fine-tuning process include the weight parameter, optimizer states, gradients, and calculation of residual states (i.e, activations, temporary buffers and fragmented memory) (Rajbhandari et al., 2020b). In this section, we give theoretical analysis on the GPU memory advantages of HiFT strategy from the perspectives of weight parameter, optimizer states and gra**dients** ¹. Assuming the model is fine-tuned using the AdamW optimizer with 32-bit precision, we employ W_1 , W_2 , W_3 to represent weight parameter, optimizer states and gradients respectively.

¹Since the GPU memory occupied by forward activations is related to the model implementation, batch size and sentence length, we analyze the GPU memory requirements of internal variables through experiments.

AdamW optimizer stores the gradient first moment estimation and second moment estimation, which means that the optimizer state parameter W_2 is two times larger than weight parameter W_1 (i.e., $W_2 = 2 * W_1$). The gradient parameters typically correspond to the parameters updated in the model (i.e., $W_3 = W_1$). Therefore, the number of gradient parameters W_3 is the same as the number of parameters W_1 that need to be updated in the model. Therefore, for standard FPFT, the GPU memory required for these parameters is as follows:

$$W_{fpft} = W_1 + W_2 + W_3$$

$$= W_1 + 2W_1 + W_1$$

$$= 4W_1$$
(11)

Taking the fine-tuning of LLaMA-7B at 32 precision using the AdamW optimizer as an example, the W_1 parameter is about 26.08G. Theoretically, the GPU memory required for fine-tuning these three parts of the 7B model is approximately 104.32 GB. If considering GPU memory occupied by forward activations and the impact of batch size and sentence length (Lv et al., 2023), the actual scenario FPFT requires more GPU memory than 104.32 GB. Under the HiFT training strategy, since only one group of parameters is updated for each training step, only the gradients of the updated parameters and the corresponding optimizer states are stored in the GPU according to Algorithm 1. The weight parameter need to reside in the GPU memory for forward propagation. Therefore, the average GPU memory required for each training step is as follows:

$$W_{hift} = W_1 + \frac{W_2}{k} + \frac{W_3}{k}$$

$$= \frac{k+3}{k} * W_1$$
(12)

Compared with FPFT, the memory saved by HiFT in model parameters, gradients and optimizer states is:

$$\Delta W = W_{peft} - W_{hift}$$

$$= \frac{3k - 3}{k} * W_1$$
(13)

In addition to these computable fixed parameters, HiFT can reduce the number of activation-related parameters that simultaneously reside in memory, which is discussed in the experimental section. Considering the embedding layer, task-related head layer and 32 hidden layers, LLaMA-7B has n=34

layers. When m=1, it can be deduced that k=34, and the required GPU memory can be inferred to be $\mathcal{W}_{hift} \approx 31.13G$, the GPU memory saving is about 73.19G compared with FPFT.

A.3 Datasets

We conduct experiments on the following datasets: **GLUE** (Wang et al., 2018) (SST-2 (Socher et al., 2013), CoLA (Warstadt et al., 2019), MNLI (Williams et al., 2018), MRPC (Warstadt et al., 2019), QNLI (Rajpurkar et al., 2018), QQP², RTE and STS-B (Cer et al., 2017)); **SuperGLUE** (CB (De Marneffe et al., 2019), BoolQ (Clark et al., 2019), COPA (Roemmele et al., 2011), MultiRC (Khashabi et al., 2018), RTE, WiC (Pilehvar and Camacho-Collados, 2019), WSC (Levesque et al., 2012), ReCoRD (Zhang et al., 2018)), **SQuAD** (Rajpurkar et al., 2016), **E2E** (Novikova et al., 2017) and **DROP** (Dua et al., 2019). We conduct memory profiling using CoLA and E2E datasets as examples.

A.4 Implementation Details

The performance results of the experiment are based on training with the AdamW optimizer. For RoBERTa_{base} and RoBERTa_{large} models, we follow Chen et al. (2023) for the hyperparameter setting of no-prompt fine-tuning such as batch size and learning rate. For GPT-2_{medium} and GPT-2_{large}, we follow Hu et al. (2022b) for the hyperparameter setting for no-prompt fine-tuning such as batch size and learning rate. For RoBERTalarge model, we follow Malladi et al. (2023) for the hyperparameter setting of prompt fine-tuning such as prompt template, batch size and learning rate. The specific model layering principle is that all embedding layers are treated as a single layer including position coding, all head layer parameters are treated as a single layer, and the remaining layers are divided according to the construction structure of the model. For example, RoBERTabase has 12 hidden layers, thus are divided into 12 layer units. Then we group them according to the divided layers. Table 4 reports hyperparameter used for HiFT.

B More Experiment Results

Table 5 reports the results of GPT-2 including medium and large on the E2E dataset. We use the same evaluation metrics as Hu et al. (2022a).

²https://quoradata.quora.com/First-Quora-Dataset-Release-Question-Pairs

B.1 Proportion of Parameters

Figure 4 (a, b, c, d) shows the percentage of memory used by the parameters of each part when fine-tuning LLaMA-2 (7B) under standard FPFT and HiFT with the AdamW optimizer. Figure 4 (e) repotrs the changes in the amount of peak fine-tuning parameters under HiFT at different model sizes.

B.2 Results of Memory Profiling

This part of the experiment mainly reports the memory usage of different models fine-tuned with different optimizes. Table 6 and Table 7 report the memory profiling of RoBERTa_{base} and RoBERTa_{large} fine-tuned on CoLA respectively. Table 8 and Table 9 report the memory profiling of GPT-2_{large} and GPT-Neo fine-tuned on E2E respectively.

B.3 Time Profiling

This part mainly provides the time results of the fine-tuning process of the RoBERTa_{base} 10, RoBERTa_{large} 10, and OPT-13B 11 models.

B.4 Prompts

Tables 12 and 13 gives detailed prompts of different datasets.

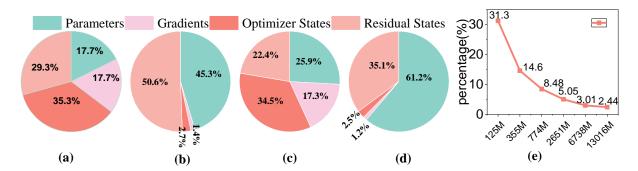


Figure 4: (a), (b), (c) and (d) represent the proportion of parameters occupied by different parts when fine-tuning LLaMA-2 (7B). The sequence length and batch size are set to 512 and 6. (a): 32-bit precision FPFT; (b): 32-bit precision HiFT; (c) mixed precision FPFT; (d): mixed precision HiFT. Fine-tuning uses the AdamW optimizer. The m is set to 1 for HiFT. (e) represents the change in the proportion of the peak trainable parameters to the total model parameters during the HiFT training under different size models.

| | | *** |
|---------------|------------------------|------------------------------|
| Experiment | Hyperparameters | Values |
| RoBERTa-base | Total Batch size | 64 |
| | Learning rate | $\{1e-5, 2e-5, 3e-5\}$ |
| | warmup | {0.0, 0.02, 0.06} |
| | Epochs | {50, 100} |
| | Device | 8*GTX 1080Ti (11G) |
| | Weight Decay | 0 |
| RoBERTa-large | Total Batch size | 32 |
| | Learning rate | $\{1e-5, 2e-5, 3e-5\}$ |
| | warmup | $\{0.0, 0.02, 0.06\}$ |
| | Epochs | {50, 100} |
| | Device | 8*GTX 1080Ti (11G) |
| | Weight Decay | 0 |
| GPT-2 (M) | Batch size | 32 |
| | Learning rate | $\{5e-5\}$ |
| | warmup | $\{0.0\}$ |
| | Epochs | {20 } |
| | Device | RTX A6000 (48G) |
| | Temperature | 0.8 |
| | Beam size | 10 |
| | repetition penalty | 4 |
| | length penalty | 0.9 |
| GPT-2 (L) | Batch size | 32 |
| | Learning rate | $\{5e-5\}$ |
| | warmup | $\{0.0\}$ |
| | Epochs | {20} |
| | Device | RTX A6000 (48G) |
| | Temperature | 0.8 |
| | Beam size | 10 |
| | repetition penalty | 4 |
| | length penalty | 0.9 |
| RoBERTa-large | Batch size $(k = 16)$ | {2,4,8} |
| | Batch size $(k = 512)$ | $\{8, 16, 32\}$ |
| | Learning Rates | $\{1e-5, 3e-5, 5e-5, 8e-5\}$ |
| | Device | 8*GTX 1080Ti (11G) |
| | Weight Decay | 0 |
| | Steps $(k=16)$ | 2,000 |
| | Steps $(k = 512)$ | 4,000 |
| OPT-13B | Batch size | {2,4,8} |
| | Learning Rates | $\{1e-5, 2e-5, 5e-5, 8e-5\}$ |
| | Epochs | 5 |
| | Device | A100 (80G) |
| | Weight Decay | 0 |
| | | |

Table 4: The hyperparameter grids used for HiFT experiments.

| | | E2E | NLG C | hallenge | |
|----------------------------------|-------|------|-------|----------|-------|
| Model & Method | BLUE | NIST | MET | ROUGE-L | CIDEr |
| GPT-2 M (FPFT)† | 68.20 | 8.62 | 46.20 | 71.00 | 2.47 |
| GPT-2 M (Adapter ^L)† | 66.30 | 8.41 | 45.00 | 69.80 | 2.40 |
| GPT-2 M (Adapter ^H)† | 67.30 | 8.50 | 46.00 | 70.70 | 2.44 |
| GPT-2 M (FPFT ^{Top2})† | 68.10 | 8.59 | 46.00 | 70.80 | 2.41 |
| GPT-2 M (PreLayer)† | 69.70 | 8.81 | 46.10 | 71.40 | 2.49 |
| GPT-2 M (LoRA)† | 70.40 | 8.85 | 46.80 | 71.80 | 2.53 |
| HiFT | 69.40 | 8.67 | 46.77 | 71.26 | 2.46 |
| | | | | | |
| GPT-2 L (FPFT)† | 68.50 | 8.78 | 46.00 | 69.90 | 2.45 |
| GPT-2 L (Adapter ^L)† | 69.10 | 8.68 | 46.30 | 71.40 | 2.49 |
| GPT-2 L (PreLayer)† | 70.30 | 8.85 | 46.20 | 71.70 | 2.47 |
| GPT-2 L (LoRA)† | 70.40 | 8.89 | 46.80 | 72.00 | 2.47 |
| HiFT | 70.30 | 8.86 | 46.64 | 72.22 | 2.48 |
| | | | | | |

Table 5: GPT-2 medium (M) and large (L) with different fine-tuning methods on the E2E NLG Challenge. For all metrics, higher is better. m of HiFT is set to 1. \dagger means the result comes from Hu et al. (2022a)

| _ | | | #Trainable | | | | | Residual | |
|-----------|---------|-------------|-------------------|-----------|----------|----------|----------|------------|-----------|
| Optimizer | #Dtype | #FType | Parameters | #Para(MB) | #Gra(MB) | #Sta(MB) | #PGS(GB) | States(GB) | Total(GB) |
| | fp32 | FPFT | 124.65M | 475.49 | 475.49 | 950.98 | 1.86 | 5.02 | 6.88 |
| AdamW | 1p32 | HiFT | 39.00M | 475.49 | 148.77 | 297.54 | 0.90 | 3.61 | 4.52 |
| Adamv | mixed | FPFT | 124.65M | 713.25 | 475.49 | 950.98 | 2.09 | 3.58 | 5.67 |
| | IIIIACU | HiFT | 39.00M | 713.25 | 148.77 | 297.54 | 1.13 | 2.58 | 3.71 |
| | fp32 | FPFT | 124.65M | 475.49 | 475.49 | 475.49 | 1.39 | 5.00 | 6.39 |
| SGDM | 1p32 | HiFT | 39.00M | 475.49 | 148.77 | 148.77 | 0.75 | 3.76 | 4.52 |
| SODM | mixed | FPFT | 124.65M | 713.25 | 475.49 | 475.49 | 1.63 | 3.57 | 5.20 |
| | IIIIXCU | HiFT | 39.00M | 713.25 | 148.77 | 148.77 | 0.99 | 2.71 | 3.69 |
| | fp32 | FPFT | 124.65M | 475.49 | 475.49 | 0.00 | 0.93 | 4.97 | 5.90 |
| SGD | 1p32 | HiFT | 39.00M | 475.49 | 148.77 | 0.00 | 0.61 | 3.91 | 4.52 |
| 300 | mixed | FPFT | 124.65M | 713.25 | 475.49 | 0.00 | 1.16 | 3.57 | 4.73 |
| | IIIIXCU | HiFT | 39.00M | 713.25 | 148.77 | 0.00 | 0.84 | 2.88 | 3.72 |
| | fp32 | FPFT | 124.65M | 475.49 | 475.49 | 0.98 | 0.93 | 4.98 | 5.91 |
| Adafactor | 1032 | HiFT | 39.00M | 475.49 | 148.77 | 0.19 | 0.61 | 3.91 | 4.52 |
| Adaractor | mixed | FPFT | 124.65M | 713.25 | 475.49 | 0.98 | 1.16 | 3.57 | 4.73 |
| | IIIIXCU | HiFT | 39.00M | 713.25 | 148.77 | 0.19 | 0.84 | 2.87 | 3.71 |
| | fp32 | FPFT | 124.65M | 475.49 | 475.49 | 475.49 | 1.39 | 5.00 | 6.39 |
| Adamad | 1p32 | HiFT | 39.00M | 475.49 | 148.77 | 148.77 | 0.75 | 3.76 | 4.52 |
| Adagrad | mived | FPFT | 124.65M | 713.25 | 475.49 | 475.49 | 1.63 | 3.57 | 5.20 |
| | mixed | HiFT | 39.00M | 713.25 | 148.77 | 148.77 | 0.99 | 2.71 | 3.69 |

Table 6: The GPU memory usage of fine-tuning RoBERTa_{base} on the CoLA dataset. The sequence length and batch size are set to 512 and 8, respectively. **#Dtype** represents the data type used for training, where **FP32** represents fully parameter fine-tuning the model with 32-bit precision, and **mixed** represents fine-tuning with mixed precision. **#Trainable parameters** represents the maximum number of trainable parameters that appear in a single step during the fine-tuning process. **#Para** represents the memory occupied by the model parameters, **#Gra** represents the memory occupied by the optimizer state. **#PGS** represents the sum of memory occupied by model parameters (i.e., **#Para**), gradients (i.e., **#Gra**) and optimizer state (i.e., **#Sta**). **Residual states** mainly includes activation, temporary buffers and unusable fragmented memory. **Total** represents the total memory used during fine-tuning. The parameter m of HiFT is set to 1.

| | | | #Trainable | | Residual | | | | |
|-----------|---------|-------------|-------------------|-----------|----------|----------|----------|------------|-----------|
| Optimizer | #Dtype | #FType | Parameters | #Para(MB) | #Gra(MB) | #Sta(MB) | #PGS(GB) | States(GB) | Total(GB) |
| | fp32 | FPFT | 355.36M | 1355.60 | 1355.60 | 2711.20 | 5.30 | 13.08 | 18.38 |
| AdamW | 1p32 | HiFT | 52.00M | 1355.60 | 198.38 | 396.73 | 1.90 | 9.97 | 11.88 |
| Adamw | mixed | FPFT | 355.36M | 2033.40 | 1355.60 | 2711.20 | 5.96 | 9.30 | 15.25 |
| | IIIIXeu | HiFT | 52.00M | 2033.40 | 198.38 | 396.73 | 2.57 | 7.17 | 9.74 |
| | fp32 | FPFT | 355.36M | 1355.60 | 1355.60 | 1355.60 | 3.97 | 13.08 | 17.05 |
| SGDM | 1p32 | HiFT | 52.00M | 1355.60 | 198.38 | 198.38 | 1.71 | 10.20 | 11.91 |
| SODM | mixed | FPFT | 355.36M | 2033.40 | 1355.60 | 1355.60 | 4.63 | 9.30 | 13.93 |
| | | HiFT | 52.00M | 2033.40 | 198.38 | 198.38 | 2.37 | 7.36 | 9.74 |
| | fp32 | FPFT | 355.36M | 1355.60 | 1355.60 | 0.00 | 2.65 | 13.08 | 15.73 |
| SGD | | HiFT | 52.00M | 1355.60 | 198.38 | 0.00 | 1.52 | 10.36 | 11.88 |
| SGD | mixed | FPFT | 355.36M | 2033.40 | 1355.60 | 0.00 | 3.31 | 9.30 | 12.60 |
| | | HiFT | 52.00M | 2033.40 | 198.38 | 0.00 | 2.18 | 7.56 | 9.74 |
| | fp32 | FPFT | 355.36M | 1355.60 | 1355.60 | 3.14 | 2.65 | 13.08 | 15.73 |
| Adafactor | 1p32 | HiFT | 52.00M | 1355.60 | 198.38 | 0.21 | 1.52 | 10.36 | 11.88 |
| Adaracion | mixed | FPFT | 355.36M | 2033.40 | 1355.60 | 3.14 | 3.31 | 9.30 | 12.61 |
| | IIIIXCU | HiFT | 52.00M | 2033.40 | 198.38 | 0.21 | 2.18 | 7.51 | 9.69 |
| | fp32 | FPFT | 355.36M | 1355.60 | 1355.60 | 1355.60 | 3.97 | 13.08 | 17.05 |
| A doored | 1p32 | HiFT | 52.00M | 1355.60 | 198.38 | 198.38 | 1.71 | 10.20 | 11.91 |
| Adagrad | mixed | FPFT | 355.36M | 2033.40 | 1355.60 | 1355.60 | 4.63 | 9.30 | 13.93 |
| | mixed | HiFT | 52.00M | 2033.40 | 198.38 | 198.38 | 2.37 | 7.36 | 9.74 |

Table 7: The GPU memory usage of fine-tuning RoBERTa_{large} on the CoLA dataset. The sequence length and batch size are set to 512 and 8, respectively.

| | | | #Trainable | | | | | Residual | |
|------------|---------|-------------|-------------------|-----------|----------|----------|----------|------------|-----------|
| Optimizer | #Dtype | #FType | Parameters | #Para(MB) | #Gra(MB) | #Sta(MB) | #PGS(GB) | States(GB) | Total(GB) |
| | fp32 | FPFT | 774.03M | 2952.69 | 2952.69 | 5905.39 | 11.53 | 37.26 | 48.79 |
| AdamW | 1p32 | HiFT | 65.64M | 2952.69 | 250.40 | 500.79 | 3.62 | 31.73 | 35.35 |
| Adamw | mixed | FPFT | 774.03M | 4429.05 | 2952.69 | 5905.39 | 12.98 | 28.13 | 41.11 |
| | IIIIXeu | HiFT | 65.64M | 4429.05 | 250.40 | 500.79 | 5.06 | 24.97 | 30.03 |
| | fp32 | FPFT | 774.03M | 2952.69 | 2952.69 | 2952.69 | 8.65 | 37.26 | 45.91 |
| SGDM | 1032 | HiFT | 65.64M | 2952.69 | 250.40 | 250.40 | 3.37 | 31.98 | 35.35 |
| SODM | mixad | FPFT | 774.03M | 4429.05 | 2952.69 | 2952.69 | 10.09 | 28.14 | 38.23 |
| | mixed | HiFT | 65.64M | 4429.05 | 250.40 | 250.40 | 4.81 | 25.22 | 30.03 |
| | fp32 | FPFT | 774.03M | 2952.69 | 2952.69 | 0.00 | 5.77 | 37.25 | 43.02 |
| SGD | | HiFT | 65.64M | 2952.69 | 250.40 | 0.00 | 3.13 | 32.22 | 35.35 |
| SOD | mixad | FPFT | 774.03M | 4429.05 | 2952.69 | 0.00 | 7.21 | 28.12 | 35.33 |
| | mixed | HiFT | 65.64M | 4429.05 | 250.40 | 0.00 | 4.57 | 25.46 | 30.03 |
| | fp32 | FPFT | 774.03M | 2952.69 | 2952.69 | 5.31 | 5.77 | 37.26 | 43.03 |
| Adafactor | 1p32 | HiFT | 65.64M | 2952.69 | 250.40 | 0.21 | 3.13 | 32.22 | 35.35 |
| Adaracion | mixad | FPFT | 774.03M | 4429.05 | 2952.69 | 5.31 | 7.21 | 28.12 | 35.33 |
| | mixed | HiFT | 65.64M | 4429.05 | 250.40 | 0.21 | 4.57 | 25.46 | 30.03 |
| | fn22 | FPFT | 774.03M | 2952.69 | 2952.69 | 2952.69 | 8.65 | 37.26 | 45.91 |
| A do amo d | fp32 | HiFT | 65.64M | 2952.69 | 250.40 | 250.40 | 3.37 | 31.98 | 35.35 |
| Adagrad | mixad | FPFT | 774.03M | 4429.05 | 2952.69 | 2952.69 | 10.09 | 28.13 | 38.22 |
| | mixed | HiFT | 65.64M | 4429.05 | 250.40 | 250.40 | 4.81 | 25.22 | 30.03 |

Table 8: The GPU memory usage of fine-tuning GPT-2_{large} on the E2E dataset. The sequence length and batch size are set to 512 and 8, respectively.

| | | | #Trainable | | | | | Residual | |
|-----------|---------|--------|-------------------|-----------|----------|----------|----------|------------|-----------|
| Optimizer | #Dtype | #FType | Parameters | #Para(MB) | #Gra(MB) | #Sta(MB) | #PGS(GB) | States(GB) | Total(GB) |
| | fp32 | FPFT | 2651.31M | 10113.95 | 10113.95 | 20227.89 | 39.51 | 22.69 | 62.20 |
| AdamW | 1p32 | HiFT | 133.9M | 10113.95 | 510.79 | 1021.58 | 11.37 | 16.95 | 28.33 |
| Addiliw | mixed | FPFT | 2651.31M | 15170.93 | 10113.95 | 20227.89 | 44.45 | 19.57 | 64.01 |
| | IIIIXCu | HiFT | 133.9M | 15170.93 | 510.79 | 1021.58 | 16.31 | 15.92 | 32.23 |
| | fp32 | FPFT | 2651.31M | 10113.95 | 10113.95 | 10113.95 | 29.63 | 22.69 | 52.32 |
| SGDM | 1p32 | HiFT | 133.9M | 10113.95 | 510.79 | 510.79 | 10.87 | 17.45 | 28.33 |
| SODM | mixed | FPFT | 2651.31M | 15170.93 | 10113.95 | 10113.95 | 34.57 | 19.57 | 54.13 |
| | IIIIXCu | HiFT | 133.9M | 15170.93 | 510.79 | 510.79 | 15.81 | 16.33 | 32.14 |
| | fp32 | FPFT | 2651.31M | 10113.95 | 10113.95 | 0.00 | 19.75 | 22.69 | 42.44 |
| SGD | 1p32 | HiFT | 133.9M | 10113.95 | 510.79 | 0.00 | 10.38 | 17.95 | 28.33 |
| SOD | mixed | FPFT | 2651.31M | 15170.93 | 10113.95 | 0.00 | 24.69 | 19.56 | 44.26 |
| | IIIIXCu | HiFT | 133.9M | 15170.93 | 510.79 | 0.00 | 15.31 | 16.83 | 32.14 |
| | fp32 | FPFT | 2651.31M | 10113.95 | 10113.95 | 8.99 | 19.76 | 22.69 | 42.45 |
| Adafactor | 1p32 | HiFT | 133.9M | 10113.95 | 510.79 | 0.22 | 10.38 | 17.95 | 28.33 |
| Adatactor | mixed | FPFT | 2651.31M | 15170.93 | 10113.95 | 8.99 | 24.70 | 19.56 | 44.26 |
| | IIIIXCu | HiFT | 133.9M | 15170.93 | 510.79 | 0.22 | 15.31 | 16.83 | 32.14 |
| | fn22 | FPFT | 2651.31M | 10113.95 | 10113.95 | 10113.95 | 29.63 | 22.69 | 52.32 |
| Adagrad | fp32 | HiFT | 133.9M | 10113.95 | 510.79 | 510.79 | 10.87 | 17.45 | 28.33 |
| Adagrad | mixed | FPFT | 2651.31M | 15170.93 | 10113.95 | 10113.95 | 34.57 | 19.57 | 54.14 |
| | mixed | HiFT | 133.9M | 15170.93 | 510.79 | 510.79 | 15.81 | 16.33 | 32.14 |

Table 9: The GPU memory usage of fine-tuning GPT-Neo on the E2E dataset. The sequence length and batch size are set to 512 and 8, respectively.

| | | SS | T-2 | MN | NLI | QN | NLI | Q | OP . | R | ГЕ | ST | S-B | MR | PC. | Co. | LA |
|--------------------------|--------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| Models | FTType | steps/sec | sec/steps |
| | HiFT | 1.42 | 0.71 | 1.53 | 0.70 | 1.41 | 0.71 | 1.40 | 0.72 | 1.06 | 0.94 | 1.15 | 0.87 | 1.12 | 0.89 | 1.26 | 0.79 |
| RoBERTa _{base} | FPFT | 1.76 | 0.57 | 1.78 | 0.56 | 1.75 | 0.57 | 1.75 | 0.57 | 1.10 | 0.91 | 1.36 | 0.73 | 1.26 | 0.80 | 1.48 | 0.68 |
| | HiFT | 1.20 | 0.83 | 1.18 | 0.85 | 1.18 | 0.85 | 1.14 | 0.88 | 1.09 | 0.92 | 1.05 | 0.95 | 1.08 | 0.93 | 1.14 | 0.88 |
| RoBERTa _{large} | FPFT | 0.86 | 1.17 | 0.86 | 1.16 | 0.84 | 1.19 | 0.84 | 1.19 | 0.78 | 1.28 | 0.77 | 1.29 | 0.79 | 1.26 | 0.82 | 1.22 |

Table 10: Running time statistics of RoBERTa on different tasks. The steps/sec indicates how many steps are run per second, and sec/steps indicates how long it takes to run each step.

| Time | SST2 | RTE | CB | BoolQ | WSC | WIC | MultiRC | COPA | ReCoRD | SQuAD | DROP |
|------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| Sec/steps | 8.16 | 5.47 | 29.47 | 5.48 | 11.55 | 7.81 | 5.21 | 14.46 | 7.45 | 4.57 | 4.13 |
| Total(sec) | 5102.21 | 6841.42 | 2800.05 | 6853.32 | 1022.23 | 4883.62 | 6518.04 | 2747.39 | 4658.79 | 5706.37 | 5166.14 |

Table 11: Running time statistics of OPT-13B on different tasks. The sec/steps indicates how long it takes to run each step, and total represents the time required to run 5 epochs, including evaluation time.

| Dataset | C | Type | Prompt | Label words |
|------------------------|-------------|--|--|--|
| SST-2 SST-5 TREC | 2 5 6 | sentiment cls. sentiment cls. topic cls. | $< S_1 >$ It was <code>[MASK]</code> . $< S_1 >$ It was <code>[MASK]</code> . <code>[MASK]</code> : $< S_1 >$ | {great, terrible} {great, good, okay, bad, terrible} {Description, Expression, Entity, |
| MNLI SNLI RTE | 3 3 2 | NLI NLI NLI | $ \begin{array}{c} \ ?\ [{\rm MASK}]\ , < S_2> \\ \ ?\ [{\rm MASK}]\ , < S_2> \\ \ ?\ [{\rm MASK}]\ , < S_2> \end{array} $ | Human, Location, Number} {Yes, Maybe, No} {Yes, Maybe, No} {Yes, No} |

Table 12: The prompts of the datasets we used in our RoBERTa-large experiments (i.e., Table 1). The prompts are adapted from (Gao et al., 2021) and include a template and a set of label words that can fill in the [MASK]token. $\langle S_1 \rangle$ and $\langle S_2 \rangle$ refer to the first and the second (if any) input sentence.

| Dataset | Type | Prompt |
|---------|------|---|
| SST-2 | cls. | <text> It was terrible/great</text> |
| RTE | cls. | <pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre> |
| | | Does this mean that " <hypothesis>" is true? Yes or No?</hypothesis> |
| | | Yes/No |
| СВ | cls. | Suppose <pre><pre>Suppose <pre><pre>Suppose <pre><pre>Suppose <pre><pre><pre>Suppose <pre><pre>Suppose <pre><pre><pre>Suppose <pre><pre><pre>Suppose <pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre></pre> |
| BoolQ | cls. | <pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre> |
| WSC | cls. | <text></text> |
| | | In the previous sentence, does the pronoun " <span2>" refer to <span1>? Yes or No? Yes/No</span1></span2> |
| WIC | cls. | Does the word " <word>" have the same meaning in these two sentences? Yes, No?</word> |
| | | <pre><sent1></sent1></pre> |
| | | <sent2></sent2> |
| | | Yes/No |
| MultiRC | cls. | <pre><paragraph></paragraph></pre> |
| | | Question: <question></question> |
| | | I found this answer " <answer". correct?="" is="" no?<="" or="" td="" that="" yes=""></answer".> |
| | | Yes/No |
| COPA | mch. | <pre><premise> so/because <candidate></candidate></premise></pre> |
| ReCoRD | mch. | <pre><passage></passage></pre> |
| | | <pre><query>.replace("@placeholder", <candidate>)</candidate></query></pre> |
| SQuAD | QA | Title: <title></td></tr><tr><td></td><td></td><td>Context: <context></td></tr><tr><td></td><td></td><td>Question: <question></td></tr><tr><td>DDOD</td><td>0.4</td><td>Answer:</td></tr><tr><td>DROP</td><td>QA</td><td>Passage: <context></td></tr><tr><td></td><td></td><td>Question: <question></td></tr><tr><td></td><td></td><td>Answer:</td></tr></tbody></table></title> |

Table 13: The prompts of the datasets we used in our OPT experiments. There are three types of tasks: classification (cls.), multiple-choice (mch.), and question answering (QA). <text> represents input from the dataset and Yes represents label words. For inference on multiple choice tasks, we put in different candidates in the prompt and calculate the average log-likelihood for each candidate, and choose the candidate with the highest score. For inference on QA tasks, we use greedy decoding to generate the answer. All prompts configurations are consistent with Malladi et al. (2023)