

UNIVERSITY OF CALIFORNIA
College of Engineering
Department of Electrical Engineering and Computer Sciences

EE40
Summer 09

SOLUTIONS

Frank Liao

MIDTERM EXAMINATION #2

Time allotted: 100 minutes

NAME: _____
(print) Last First Student ID#

LAB SECTION: _____ / _____
Days / Time

I acknowledge that the UC rules on academic honesty apply. _____
Signature

INSTRUCTIONS:

1. **SHOW YOUR WORK.** Partial credit will be given only if your methods are clear to the grader.
2. Clearly mark (BOX or UNDERLINE) your answers.
3. Specify the units on answers whenever appropriate. Points will be deducted for missing units.
4. Closed book, closed notes. You are allowed ONE 8.5" x 11" sheet of notes. Calculators are allowed.

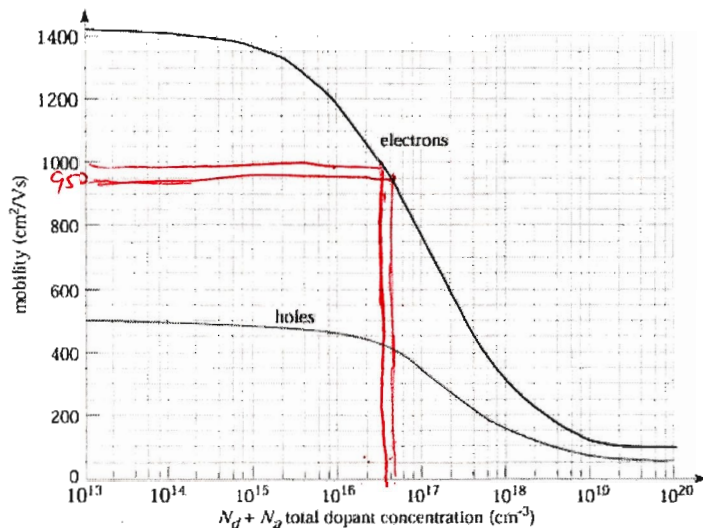
PHYSICAL CONSTANTS

Description	Symbol	Value
Electronic charge	q	1.6×10^{-19} C
Boltzmann's constant	k	8.62×10^{-5} eV/K
Thermal voltage at 300K	$V_T = kT/q$	0.026 V

PROPERTIES OF SILICON AT 300K

Description	Symbol	Value
Intrinsic carrier concentration	n_i	10^{10} cm ⁻³
Dielectric permittivity	ϵ_{Si}	1.0×10^{-12} F/cm

Electron and Hole Mobilities in Silicon at 300K



(Box Prob 4)

SCORE: 1 _____ / 10

2 _____ / 20

3 _____ / 30

4 _____ / 20

5 _____ / 20

TOTAL: _____ / 100

SOLUTIONS

Problem 1 [10 points]: Basic concepts and EE Technology

a) True/False and Multiple Choice. Select only ONE choice. No credit will be given to multiple answers. [2 pts each]

T ☒ F LCD stands for Liquid Capacitance Display.

☒ T F The MEMS accelerometer uses a differential capacitance to detect motion.

☒ T F If an RC circuit has a large time constant, τ , then it takes a long time for the capacitor in that circuit to charge and discharge.

4) What kind of filter is this?

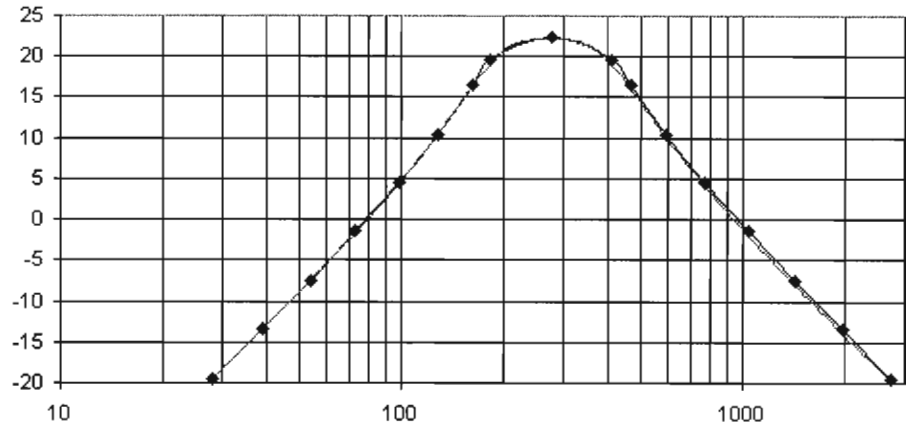
a) Lowpass

b) Highpass

☒ c) Bandpass

d) Bandreject

Bode Plot of a Filter



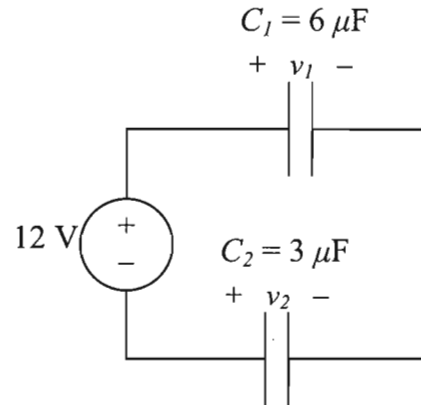
5) What is v_1 , the voltage drop across C_1 ?

☒ a) 4 V

b) 8 V

c) -4 V

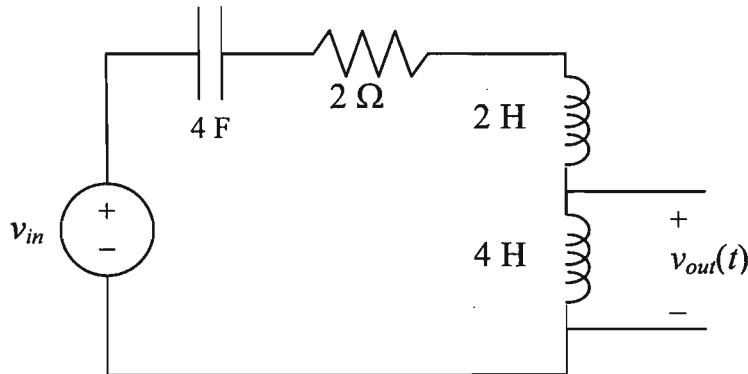
d) -8 V



SOLUTIONS

Problem 2 [20 points]: Phasor Analysis

In the circuit below, $v_{in}(t) = 2 \cos(0.1t + 30^\circ)$.



a.) What is $v_{out}(t)$ in cosine form? [10 pts]

$$V_{out} = V_{in} \left(\frac{Z_{4H}}{Z_{4H} + Z_{2H} + Z_{4F} + Z_{2\Omega}} \right) = V_{in} \left(\frac{j(0.1)(4)}{j(0.1)(6) + \frac{1}{j(0.1)(4)} + 2} \right) = \left(\frac{j0.4}{2 - j1.9} \right) V_{in}$$

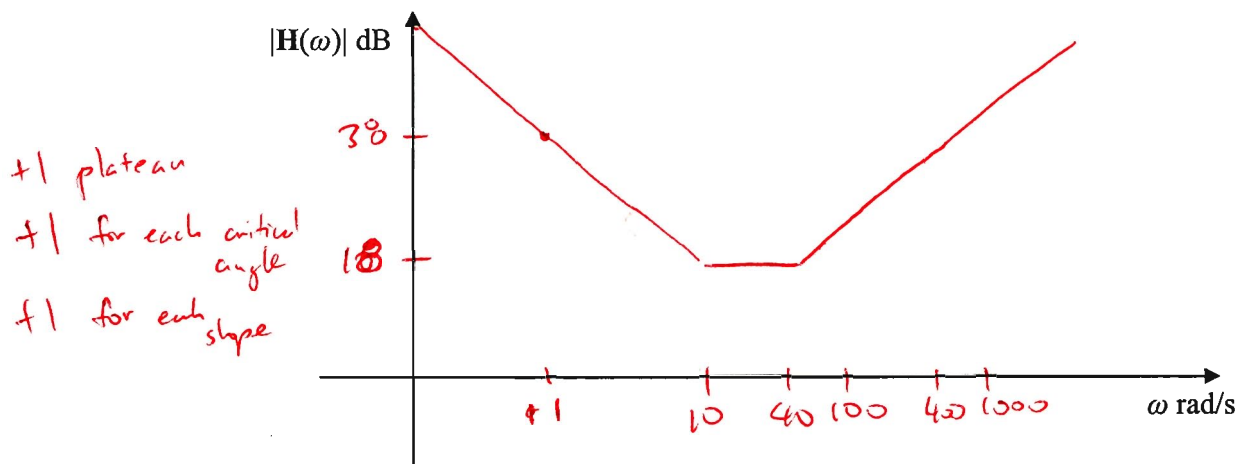
$$= (24.3^\circ) \left(\frac{0.4 \angle 90^\circ}{\sim 2\sqrt{2} \angle -43.5^\circ} \right)$$

$$= 0.29 \angle 163.5^\circ$$

$$\Rightarrow v_{out}(t) = 0.29 \cos(0.1t + 163.5^\circ)$$

b.) If $v_{out}/v_{in} = (20 + j2\omega)(40 + j\omega)/j10\omega$, sketch the bode plot of the magnitude of the transfer function, $H(\omega)$. Label the axes appropriately, denoting critical angles, slopes and plateau values. [10 pts]

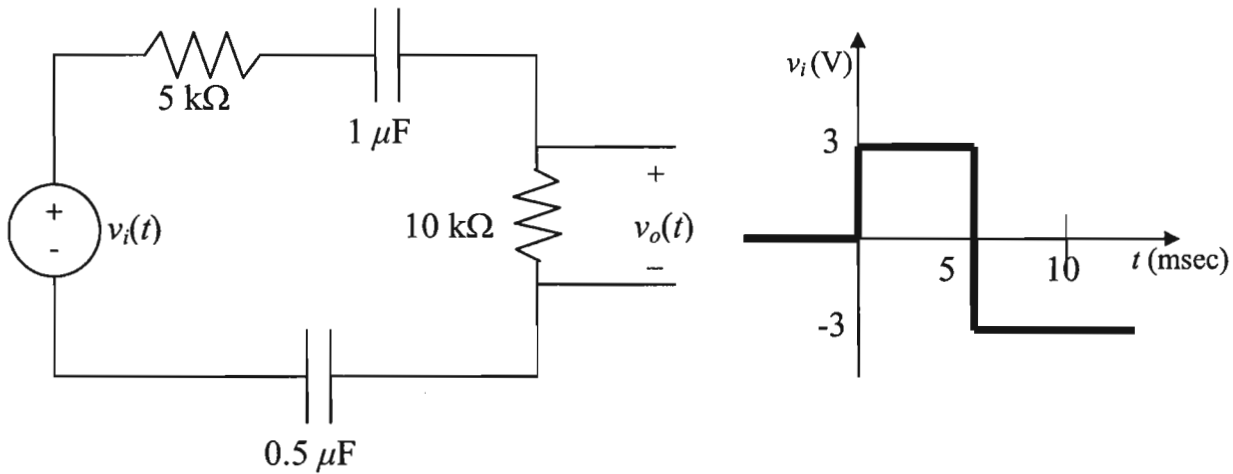
$$|H(\omega)| = 80 \frac{(1 + \frac{j\omega}{10})(1 + \frac{j\omega}{40})}{j\omega} \Rightarrow 20 \log 80 = 20(1.9) = 38$$



SOLUTIONS

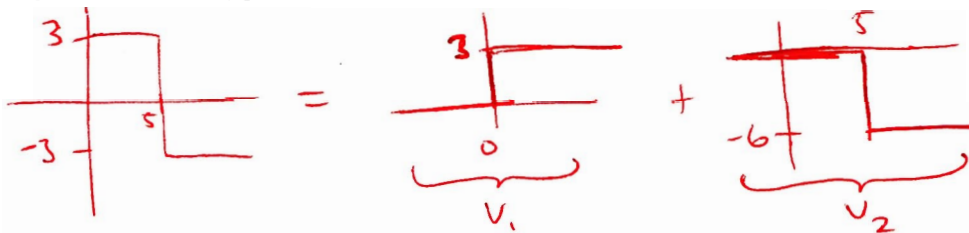
Problem 3 [30 points]: First-Order Transients

Consider the circuit below:

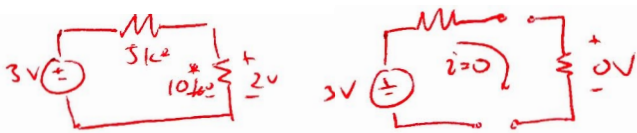


a.) Find the expression for $v_o(t)$ (piecewise expressions are acceptable) and plot $v_o(t)$ for $0 \text{ msec} \leq t \leq 10 \text{ msec}$. Label the values of $v_o(0^+)$, $v_o(5^-)$, and $v_o(5^+)$. [20 pts]

Show your work below. (Space for your answer is on the next page)



For V_1 :



$$V(0^+) = 2V$$

$$V(\infty) = 0V$$

$$\tau = (5+10)k \times \left(\frac{0.5\mu}{1.5\mu} \right) = 5ms$$

$$\Rightarrow 0 \leq t < 5ms$$

$$v_o(t) = 2e^{-t/5ms} = 2e^{-200t}$$

- +2 for initial value
- +2 for final value
- +2 for constant τ
- +1 for expression

For V_2 :



$$V(5^+) = -4V$$

$$V(\infty) = 0V$$

$$\tau = 15k \times \frac{1}{3}\mu = 5ms$$

$$\text{For } V_2: v_o(t) = -4e^{-t/5ms}$$

$$\Rightarrow 5ms \leq t \leq 10ms$$

$$v_o(t) = 2e^{-t/5ms} - 4e^{-(t-5)/5ms}$$

- +2 for initial value
- +2 for final value
- +1 for constant τ
- +3 expression (and use of superposition)

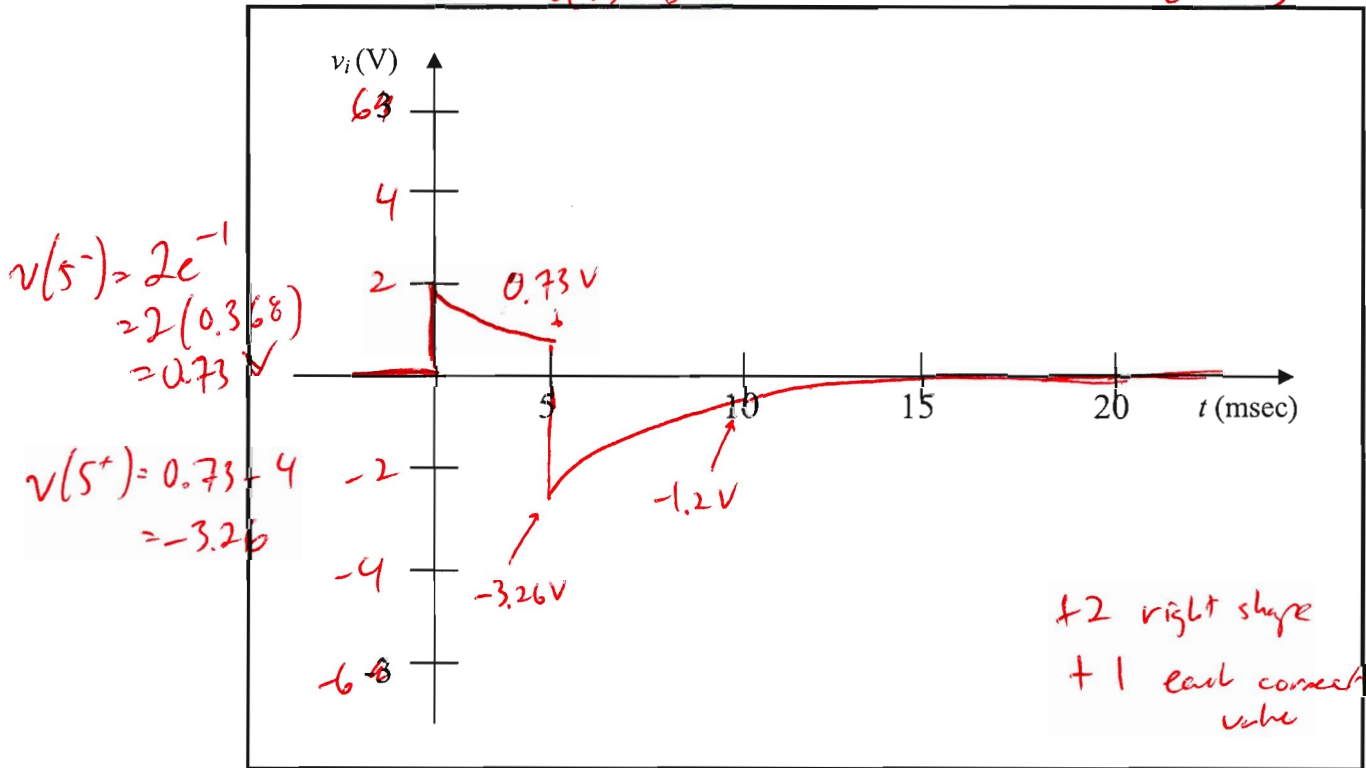
Answer:

Expression for $v_o(t)$:

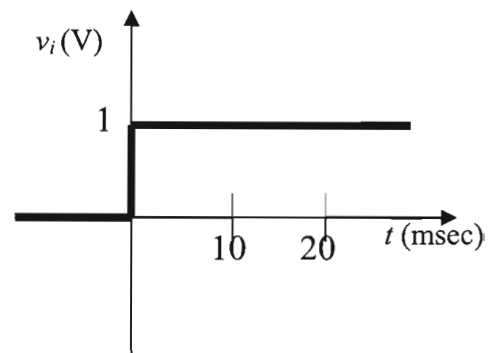
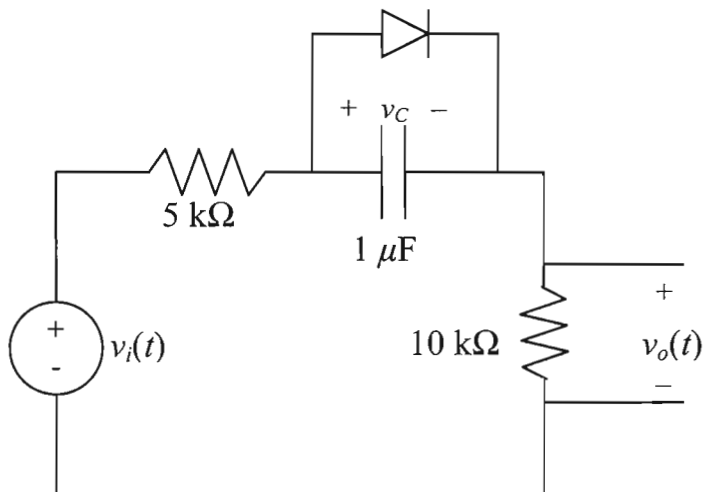
$$\begin{cases} 2e^{-t/5\text{ms}} & 0 \leq t < 5\text{ms} \\ 2e^{-t/5\text{ms}} - 4e^{-(t-5)/5\text{ms}} & t \geq 5\text{ms} \end{cases}$$

$3.26e^{-200t}$

or $v_o(t) = 2e^{-200t} - 4e^{-200(t-5)} \cdot u(t-5)$



b.) Suppose we modify the circuit and apply a different input voltage.



SOLUTIONS

On the axes below, plot for $v_C(t)$ and $v_o(t)$. Use the large signal model for the diode with a turn-on voltage, $V_D=0.7$ V. Label the following values: (1) the final voltage of v_C , (2) the time, t , when v_C reaches its final voltage, (3) the final voltage of v_o , and (4) the time, t , when v_o reaches its final voltage. [10 points]

Space for work:

For v_C : $v_C(0^-) = v_C(0^+) = 0$ V $v_C(\infty) = 1$ V

$$\tau = 15k \times 1\mu = 15 \text{ ms}$$

$$\Rightarrow v_C(t) = 1 - e^{-t/15\text{ms}}$$

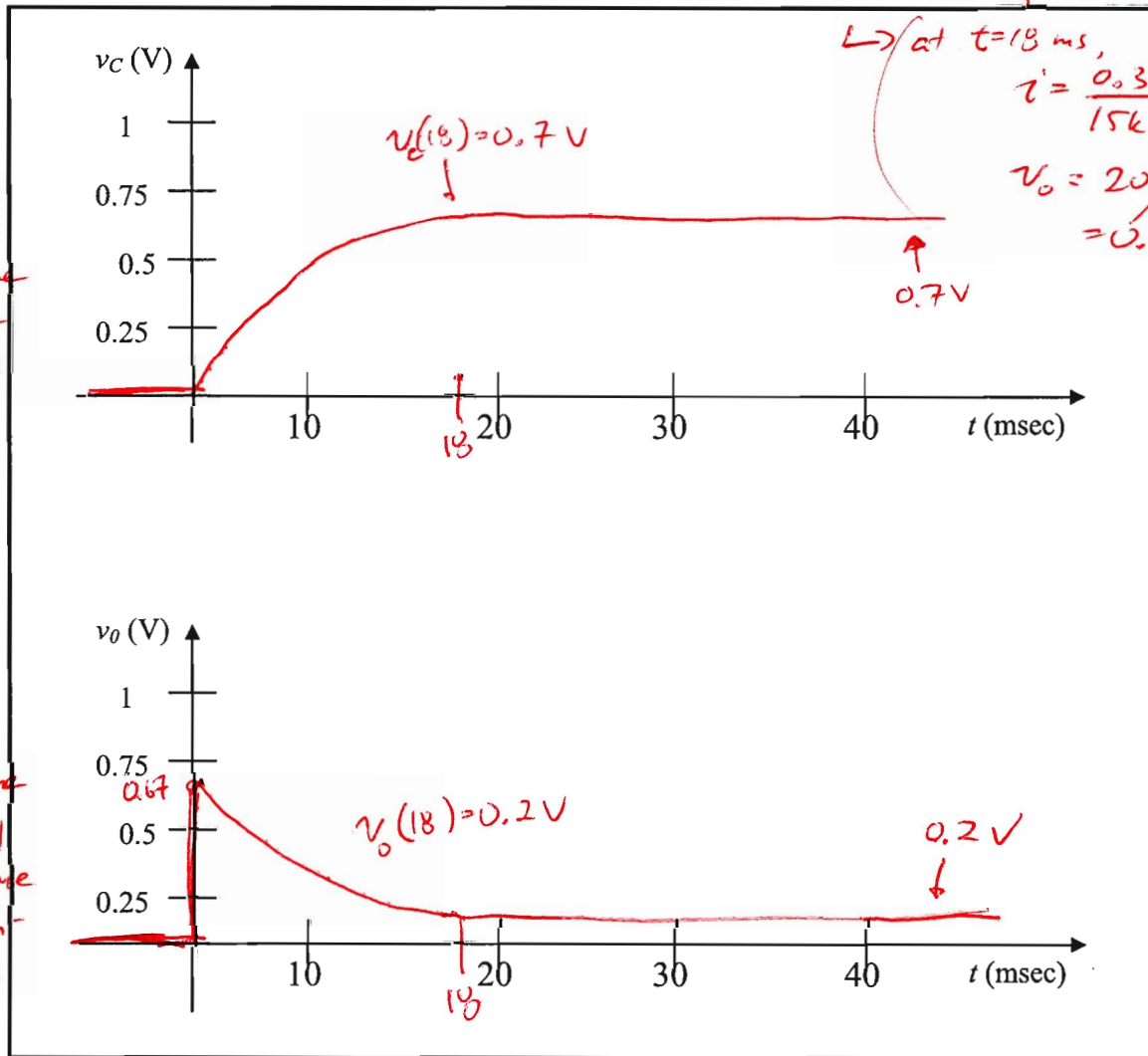
at $v_C = 0.7$ V the diode will turn on and fix v_C at 0.7 V

$$\text{this happens at } 0.7 = 1 - e^{-t/15\text{ms}}$$

$$\Rightarrow t = 18 \text{ ms}$$

For v_o : $v_o(0^+) = 0.67$ V $v_o(\infty) = 0$ V $\tau = 15 \text{ ms}$

$$\Rightarrow v_o(t) = 0.67 e^{-t/15\text{ms}} \text{ and at } t = 18 \text{ ms, } v_o = 0.2 \text{ V}$$



+3 for shape
+1 for final value
+1 for right time

+2 for shape
+2 for final value
+1 for right time

SOLUTIONS

Problem 4 [20 points]: Doping and Carrier Concentrations

Consider a Si sample maintained under thermal equilibrium conditions at $T = 300\text{K}$, doped with phosphorous at a concentration of $2 \times 10^{16} \text{ cm}^{-3}$.

a.) Is this material n-type or p-type? What are the majority and minority carrier concentrations? [6 pts]

phosphorous = donor \Rightarrow n-type
majority - ~~holes~~ electrons
minority - ~~electrons~~ holes

$$n = N_D = 2 \times 10^{16} \text{ cm}^{-3}$$

$$p = \frac{n_i^2}{N_D} = \frac{10^{20}}{2 \times 10^{16}} = 5 \times 10^3 \text{ cm}^{-3}$$

Write your answers here:

type:	n-type	+2
majority concentration:	$2 \times 10^{16} \text{ cm}^{-3}$	+2
minority carrier concentration:	$5 \times 10^3 \text{ cm}^{-3}$	+2

b.) Suppose this sample is additionally doped with boron at a concentration of 10^{16} cm^{-3} . How will the carrier concentrations change? [3 pts]

boron is acceptor

but b/c $N_A < N_D$, material is still n-type \Rightarrow majority = electrons
minority = holes

$$n = N_D - N_A = 10^{16} \text{ cm}^{-3}$$

$$p = \frac{n_i^2}{n} = \frac{10^{20}}{10^{16}} = 10^4 \text{ cm}^{-3}$$

Write your answers here:

new majority concentration:	10^{16} cm^{-3}	+1
new minority carrier concentration:	10^4 cm^{-3}	+1

c.) Find the resistivity of this sample (with the boron doping). [4 pts]

$$\rho = \frac{1}{q n \mu_n + q p \mu_p} \approx \frac{1}{q n \mu_n}$$

From the chart, using $N_D + N_A = 3 \times 10^{16} \text{ cm}^{-3}$,

$$\mu_n \approx 950 \text{ cm}^2/\text{V}\cdot\text{s}$$

+7 for formula
+1 correct conc.
+3 for mobility
+1 for correct value

$$\Rightarrow \rho = \frac{1}{(1.6 \times 10^{-19} \text{ C})(10^{16} \text{ cm}^{-3})(950 \text{ cm}^2/\text{V}\cdot\text{s})} = 0.66 \text{ } \Omega\text{-cm}$$

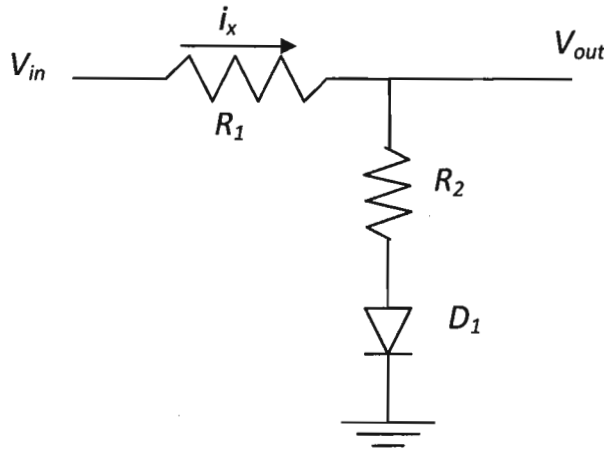
$$\left(\mu_n = 1000 \text{ cm}^2/\text{V}\cdot\text{s} \text{ is acceptable ALSO} \right)$$

$$\rho = 0.625 \text{ } \Omega\text{-cm}$$

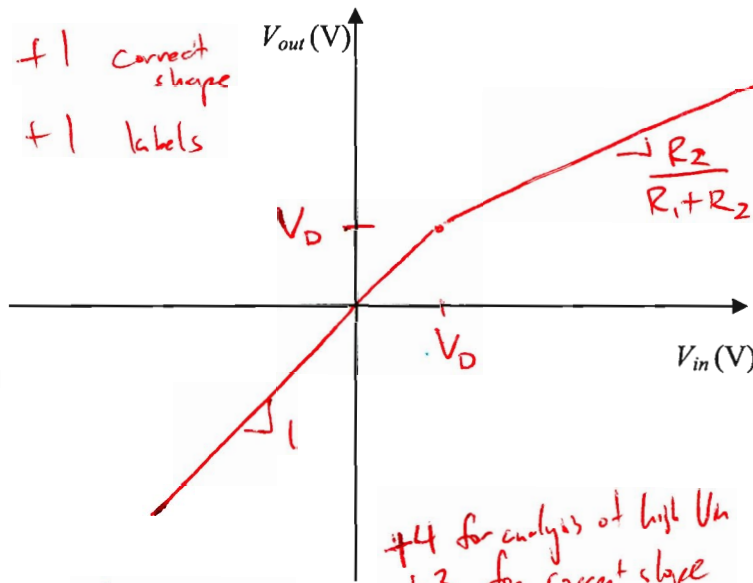
SOLUTIONS

Problem 5 [20 points]: Diode Circuits

Consider the following diode circuit:

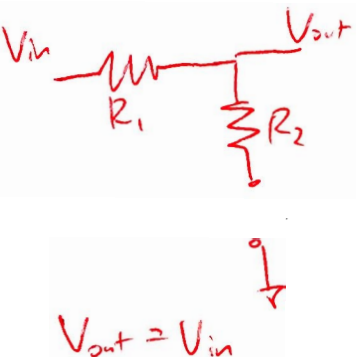


a.) Using the large-signal model, plot V_{out} as function of V_{in} of the circuit below. Remember, a diode about to turn on carries zero current but sustains V_D . For full credit, you must label all important points on the graph (e.g. slope or cross-over points).

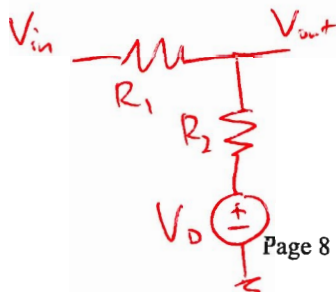


+2 for analysis of low V_{in}
+1 for correct slope

For low V_{in} ,
 D_1 is off:



For high V_{in}
 D_1 is on:



+2 for correct
cross-over
Cross-over point:
 $V_{in} = V_{out} = V_D$

KCL:

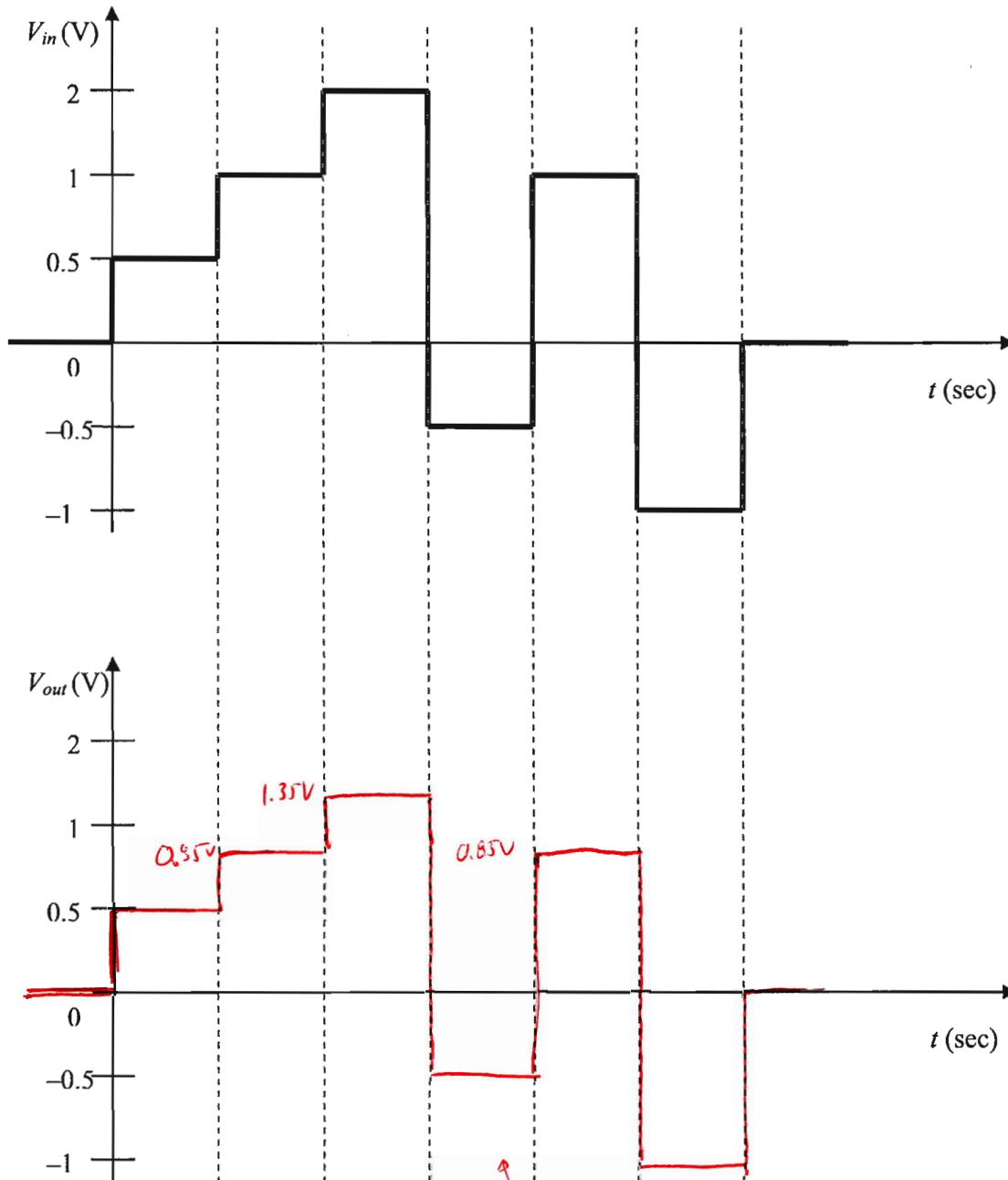
$$\frac{V_{in} - V_{out}}{R_1} = \frac{V_{out} - V_D}{R_2}$$

$$\left(\frac{1}{R_1} + \frac{1}{R_2}\right) V_{out} = \frac{V_{in}}{R_1} + \frac{V_D}{R_2}$$

$$\Rightarrow V_{out} = \underbrace{\left(\frac{R_2}{R_1 + R_2}\right)}_{\text{slope}} V_{in} + \left(\frac{R_1}{R_1 + R_2}\right) V_D$$

SOLUTIONS

b.) Suppose $R_1 = 2 \text{ k}\Omega$, $R_2 = 2 \text{ k}\Omega$, and $V_D = 0.7 \text{ V}$ and V_{in} is given by the waveform shown below. Plot V_{out} on the given axes.



For $V_{in} < 0.7 \text{ V}$

$$V_{out} = V_{in}$$

For $V_{in} \geq 0.7 \text{ V}$

$$V_{out} = \frac{1}{2} V_{in} + \frac{1}{2} (0.7)$$

$$= 0.5 V_{in} + 0.35$$

+1 correct plot

+2 correct analysis

+3 correct analysis