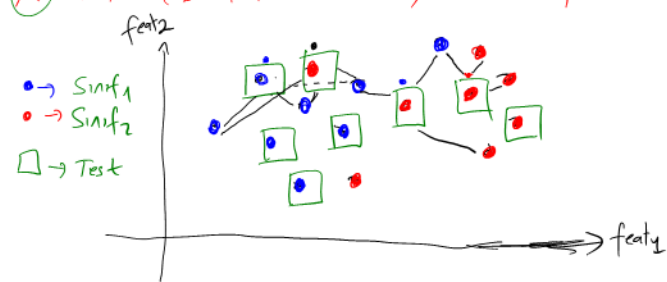
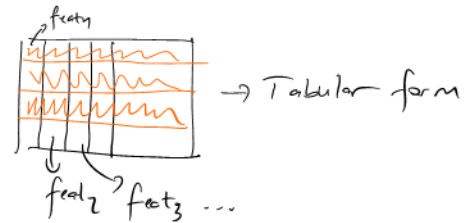
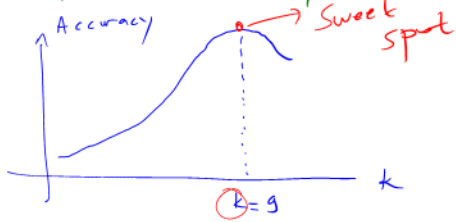


k-NN (Distance based) Classification Supervised (Sınıf / Etiket Var)



k=3

k: En yakın komşu sayısı



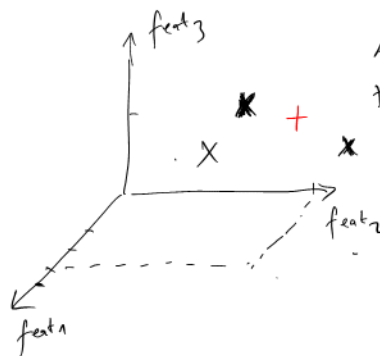
Ayrık (Class)

Tamam	Kolesterol	Şeker	Kırmızı
130	220	110	Yok
140	230	95	Var
120	250	98	Yok
115	165	72	Yok

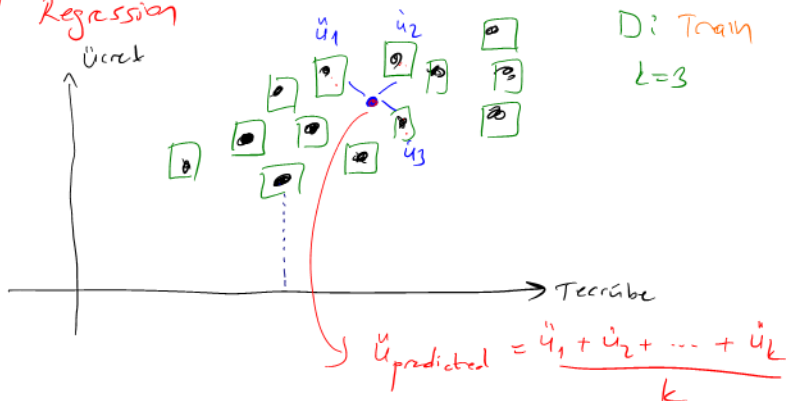
↓ ↓ ↓

feat₁ feat₂ feat₃

Öznitelik



k-NN Regression



D: Train
L=3

Tecrübe	Ücret
25	---
12	---
42	---
30	---
3	---

→ Default
Euclid

(x₁, y₁, z₁)

(x₂, y₂, z₂)

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

- Euclid
- Minkowski
- Cosine
- Jaccard

• Mahalanobis

$$\hat{y}_{predicted} = \frac{\hat{y}_1 + \hat{y}_2 + \dots + \hat{y}_k}{k}$$

Linear Regression → Cont. numerical values

$$y \approx \underbrace{b_0}_{\text{Intercept (bias)}} + \underbrace{b_1 x_1 + b_2 x_2 + b_3 x_3 + b_4 x_4}_{\text{Linear comb.}}$$

coefficients Linear model

	x_1 feat ₁	x_2 feat ₂	x_3 feat ₃	x_4 feat ₄	y
Sample ₁	3.7	4.2	1.3	0.8	0.75
Sample ₂	6.2	6.1	4.4	1.2	0.56
⋮	⋮	⋮	⋮	⋮	⋮

independent variables dependent variable

$y = f(x)$

Amaç: b_0, b_1, \dots, b_4 katsayılarını optimal biçimde bulmak!

x_1	x_2	x_3	x_4	y
$x_1^{(1)}$	$x_2^{(1)}$	$x_3^{(1)}$	$x_4^{(1)}$	$y^{(1)}$
$x_1^{(2)}$	$x_2^{(2)}$	$x_3^{(2)}$	$x_4^{(2)}$	$y^{(2)}$
⋮	⋮	⋮	⋮	⋮
$x_1^{(n)}$	$x_2^{(n)}$	$x_3^{(n)}$	$x_4^{(n)}$	$y^{(n)}$

$$\Rightarrow y^{(1)} \approx b_0 + b_1 x_1^{(1)} + \dots + b_4 x_4^{(1)}$$

$$\Rightarrow y^{(2)} \approx b_0 + b_1 x_1^{(2)} + \dots + b_4 x_4^{(2)}$$

$$\vdots$$

$$\Rightarrow y^{(n)} \approx b_0 + b_1 x_1^{(n)} + \dots + b_4 x_4^{(n)}$$

$\left. \begin{matrix} b_0 \\ b_1 \\ b_2 \\ b_3 \\ b_4 \end{matrix} \right\} = ?$

$$\begin{bmatrix} 1 & x_1^{(1)} & x_2^{(1)} & x_3^{(1)} & x_4^{(1)} \\ 1 & x_1^{(2)} & x_2^{(2)} & x_3^{(2)} & x_4^{(2)} \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & x_1^{(n)} & x_2^{(n)} & x_3^{(n)} & x_4^{(n)} \end{bmatrix} \begin{bmatrix} b_0 \\ b_1 \\ b_2 \\ b_3 \\ b_4 \end{bmatrix} \approx \begin{bmatrix} y^{(1)} \\ y^{(2)} \\ \vdots \\ y^{(n)} \end{bmatrix}$$

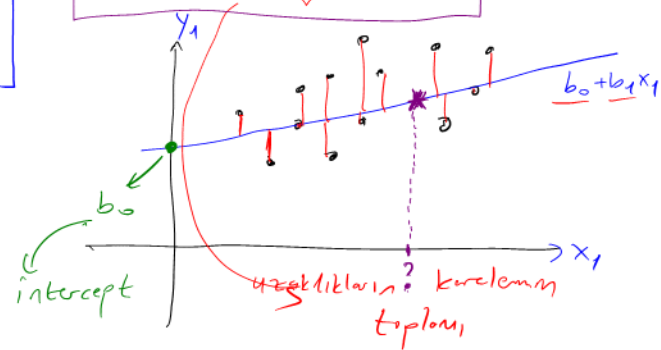
5 bilinmeyen

X \vec{b} \vec{y}

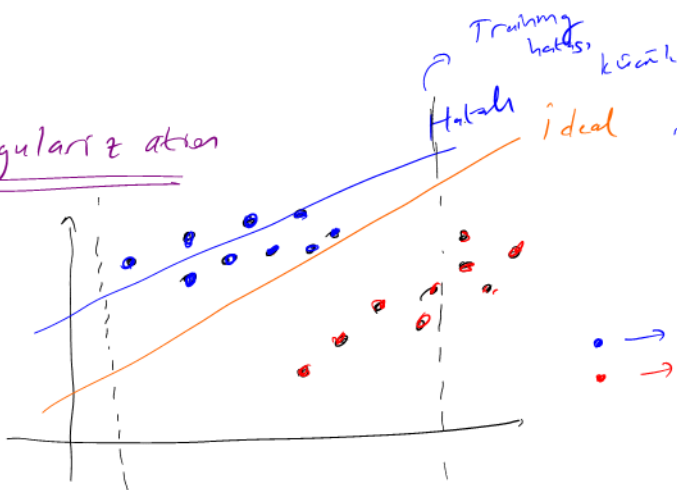
Dikdörtgen $n \times 5$

$$X \vec{b} \approx \vec{y} \Rightarrow \vec{b} = ?$$

$$\min \| X \vec{b} - \vec{y} \|_2^2$$

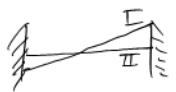


Regularization



Overfitting

• → Train
• → Test



RIDGE

$$\min_{\vec{b}} \underbrace{\|X\vec{b} - \vec{y}\|_2^2}_{\text{RSS}} + \underbrace{\alpha \|\vec{b}\|_2^2}_{\text{Penalty term}}$$

$b_0^2 + b_1^2 + \dots + b_n^2$

LASSO

$$\min_{\vec{b}} \underbrace{\|X\vec{b} - \vec{y}\|_2^2}_{\text{RSS}} + \underbrace{\beta \|\vec{b}\|_1}_{\text{Penalty norm}}$$

$|b_0| + |b_1| + \dots + |b_n|$

$$\min_{\vec{b}} \underbrace{\|X\vec{b} - \vec{y}\|_2^2 + \alpha \|\vec{b}\|_2 + (1-\alpha) \|\vec{b}\|_1}_{\text{Elastic-Net problem}}$$

$\alpha = [0.1, 0.01, \boxed{0.001}, 0.0001] \Rightarrow \text{grid-search}$

$\nearrow R^2 \quad \nearrow R^2 \quad \nearrow R^2 \quad \nearrow R^2$