

We will use the following simple algorithm. Consider triples of  $T$  in any order, and add them if they do not conflict with previously added triples. Let  $M$  denote the set returned by this algorithm and  $M^*$  be the optimal three-dimensional matching.

(1) *The size of  $M$  is at least  $1/3$  of the size of  $M^*$ .*

*Proof.* Each triple  $(a, b, c)$  in  $M^*$  must intersect at least one triple in our matching  $M$  (or else we could extend  $M$  greedily with  $(a, b, c)$ ). One triple in  $M$  can only be in conflict with at most 3 triples in  $M^*$  as edges in  $M^*$  are disjoint. So  $M^*$  can have at most 3 times as many edges as  $M$  has. ■