

Mid-term Exam – 1, Part I (75%)

15-points

ECE3040

Please submit on Canvas, before 4:30AM, June 9, 2021

Name: _____ ID: _____ .

1. Write a MATLAB script to represent the following matrix, and identify element in (second row - third column), and element in (third row - second column). PTS: 10

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

Solution:

```
>>A= [1 2 3; 4 5 6; 7 8 9]
```

Ans =

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

```
>>A(2,3)
```

ans =

6

```
>>A(3,2)
```

ans =

8

2. Write MATLAB script to calculate, $\mathbf{A}^2 + \mathbf{B}^2 - \mathbf{AB}$, and $\mathbf{A} \cdot \mathbf{A}^T / \log(\mathbf{B}^2)$ in format short.

$$\mathbf{A} = \begin{bmatrix} 1 & 0 & 1 \\ 2 & 3 & 4 \\ -1 & 6 & 7 \end{bmatrix} \quad \mathbf{B} = \begin{bmatrix} 7 & 4 & 2 \\ 2 & 5 & 6 \\ -1 & 2 & 1 \end{bmatrix}$$

PTS: 10 points

Solution:

```
>>format short;
>>A = [1 0 1; 2 3 4; -1 6 7];
>>B = [7 4 2; 2 5 6; -1 2 1];
>>S1 = (A^2 + B^2 - A*B)

>>S2 = A*A'/log10(B^2)
```

3. Write MATLAB script to solve the following system of equation.

$$\begin{aligned} P + x + 4y + 3z &= 5 \\ 2P + 3x + y - 2z &= 1 \\ P + 2x - 5y + 4z &= 3 \\ P - 3z &= 9 \end{aligned}$$

PTS: 15 points

Solution:

```
>> eq1 = P + x + 4y + 3z = 5;
>>eq2 = 2P + 3x + y - 2z = 1;
>>eq3 = P + 2x - 5y + 4z = 3;
>>eq4 = P - 3z = 9;

>> s = solve(eq1, eq2, eq3, eq4);

>>p = s.p
    P =
    1404.127

>>x = s.x
```

```

X =
-818/127
>>y = s.y
Y =
-53/127
>>z = s.z
Z =
87/127

```

4. Solve the following second order differential equation and plot the solution for $-50 < x < 50$

$$\frac{d^2 f}{dx^2} - \frac{\sin x}{x} \left(1 - \frac{2}{x^2}\right) - \frac{2 \cos x}{x^2} = 0, \quad \text{for } f(0) = 2 \text{ and } f'(0) = 0$$

PTS: 10 points

Solution:

```
>>g = desolve('D2f - sin(x)/x - 2*cos(x)/x^2 + 2*sin(x)/x^2 = 0', 'f(0) = 2', 'Df(0) = 0', 'x')
```

```

g =
-sin(x)/x + 3

```

```
>>ezplot(g, [-50, 50])
```

5. What is the area under the curve $f(x) = x^2 \cos(x)$ for $-6 < x < 6$, and plot the function in red, with labels x and y, title $x^2 \cos(x)$ and legend 'Area integration'. PTS: 10 points

Solution

```

>>f= x^2*cs(x);
>>a = int(f, -6, 6)

ans =
68*sin(6) +24*cos(6)

>>double(a)

ans =
4.0438

>> plot(f, 'r', xlabel('x'), ylabel('y'), title('x^2 cos(x)'), legend('Area integration'))

```

6. Solve the following integration,

$$\int_0^{\pi} \int_0^{\sin x} (x^2 + y^2) dy dx$$

PTS: 10-points

Solution:

```
>>int(int(x^2+y^2)dydx, y, 0, sin(x)), 0, pi)
```

```
ans =
```

```
Pi^2 - 32/9
```

7. Plot the 3-D function

PTS: 15 points

```
X = (a+b*cosv)*cosu  
Y = (a + b*cosv)*sinu  
Z = b*sinv
```

```
0<u<2π, and 0<v<2π, and a=5, b= 1
```

Solution:

```
>>a=5, b=1;  
>>u = linspace(0, 2*pi, 40);  
>>v = u;  
>>x = (a+b*cos(v)).*cos(u);  
>>y= (a+b*cos(v))*sinu;  
>>z=b*sin(v);  
Surf(x,y,z, 'face color', 'interp', 'facelighting', axis equal, axis off, view (150, 20),...  
title ('Torus.')
```

8. Plot function f1 in dotted and f2 in solid lines on the same plot with legend F1, and _____ F2, and x between 0 to 5 with 0.1 divisions, title: Multiple Function Plot, x-label, X, and y-label Y, and with grid. PTS: 10 points

$$F1 = x^2 - 3x + 2$$

$$F2 = 2x^2 + x - 3$$

Solution:

```
>> x = 0:0.1:5;
>> f(:, 1) = x.^2 - 3*x + 2;
>> f2(:, 2) = 2*x.^2 + x - 3;
>> plot(x, f)
>> title('Multiple Function Plot'), xlabel('X'), ylabel('Y'), grid on, legend('F1', 'F2')
```

If students write scripts in one line or multiple lines, they get full mark.

9. Find the **Laplace transform** of

$$v(t) = 3e^{-2t} \sin 5t + 4e^{-2t} \cos 5t$$

and **invers Laplace transform** of.

$$F(s) = \frac{25}{s+3} + \frac{48}{(s+2)(s^2+16)}$$

10-points

Solution:

% Laplace transform

```
>> v = 3*exp(-2*t)*sin(5*t) + 4*exp(-2*t)*cos(5*t);
```

```
>> V = laplace(v)
```

% Inverse Laplace transform

```
>> F = 25/(s+3) + 48/((s+2)*(s^2+16));
```

```
>> f = ilaplace(F)
```