

D₀

Linear Array.

A linear array is a list of a finite number of homogeneous data elements.

$$\text{Length} = \boxed{UB - LB + 1}$$

upper bond lower bond

$\overbrace{A[K]}$
Subscripted variable
 \uparrow subscripted index

Representation of Linear array in memory

Loc $[A[K]]$ = address of the element $[a[k]]$ of the array $[a]$

$$(d) - d + \text{end} = [sec] \text{ of } \text{do } k$$

first element of the address $[a]$ (Base).

Formula:

$$LOC(LA[K]) = \text{BASE}(la) + w(K - LB)$$

Starting point

words per memory cell

lower bound.

La array $\Rightarrow K$ elementos en orden.

~~$$Exp^{Pdt} =$$~~

Lower bound = 1965

base = 200

w = 4

K = 196532

$$LOC(\text{arr}[1932]) = \text{base} + w(K - LB)$$

$$= 200 + 4(1965 - 1932)$$

= 332 Am

Traversing Linear Array

[Visiting array]

Accessing each element of array once so that it can be processed.

Step 1 : Start

2 : initialize counter.

Set $K = LB$

3. Repeat steps 4th and 5th (while $K \leq UB$).

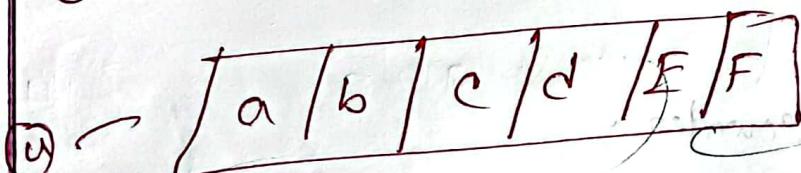
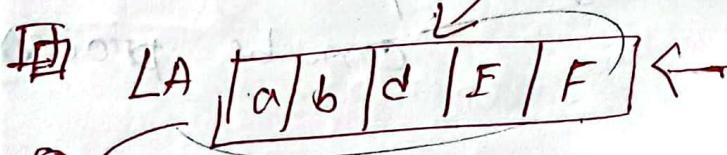
4. Apply process to $LA[K]$.

5. Increment counter

6. Stop [when $K \leq UB$ നാണ്ട്, മാറ്റ് കൂടാൻ
 UB തന്നെ ചുവവ്]

~~Inserting 9 to LA~~

c durabon (insert c)



now algorithm \Rightarrow

J=N

i=1

total element 5 in

Step 1, Set J = N

2. Repeat Steps 3 and 4 while J > 1

3. Set LA [J+1] = LA [J] \rightarrow (ii) 21(07)
907

4. Set J = J - 1 \rightarrow ① 21(07) back (21)
21(07) 21(07) 21(07)

5. Set LA [1] = Item: \rightarrow (1) 21(07) 21(07)
21(07) 21(07) 21(07)

6. Set N = N + 1

7. Exit:

Result 21(07) 21(07) 21(07) 21(07) 21(07)

Deleting Linear array.

1 Set item = LA [K]

2 Repeat for j = K to (N-1)

 Set LA [j] := LA [j+1]

3 Set N := N-1

4 Exit \Rightarrow if N elements.

here, LA is Linear array

of size N elements.

K is primitive integer.

such $K \leq N$ from.
delete (Kth) element of LA.

DATA = SET to end

Data may be organized different way,

logical and mathematical model of particular
organisation of data is ds.

Bubble Sort

• here data is an array N

• Sorts element in Data

■ Repeat steps 2 and 3 for $R=1$ to $n-1$.

■ Set $PTR := 1$.

■ Repeat while $PTR \leq N-R$

■ a) If $Data[PTR] > Data[PTR+1]$, then,

■ Interchange $Data[PTR]$ and $Data[PTR+1]$

■ b) Set $PTR := PTR + 1$

■ Exit.

worst case - $O(n \times n) = O(n^2)$

Best case - $O(n)$

$O(n)$

Searching

Linear Search

A Linear array data with N elements and a specific Item information are given. find location LOC

1. Set LOC = 1 and LOC = 0

2. Repeat steps 3 and 4 while LOC = 0 and $k \leq N$

3. If Item = Data[k] then Set LOC = k.

4. Set K = K + 1.

If LOC = 0 then

print item is not in the array Data.

else,
print Loc is the location of Item.

6. Exit

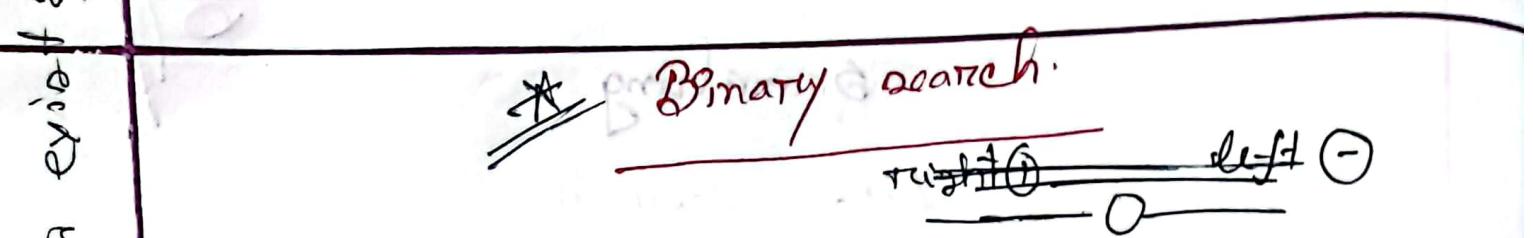
• IM = : 30.1 LOC = [LOC about 30.1]

• LOC = : 30.1

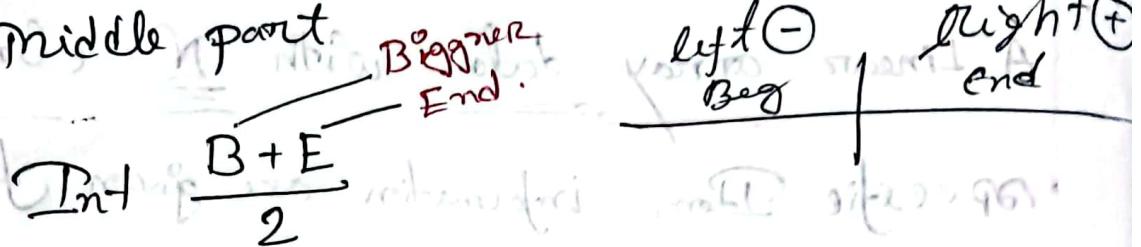
exist 20

2(m)

Beg > End



• Array Middle point



① BEG = LB, END = UB and MID = Int((BEG + END))

② Step 3 and y while BEG ≤ END and
element → Beg end

Data [MID] ≠ Item

③ If Item < Data [mid] then : set END =

Mid - 1. else BEG = mid + 1.

Left 2(m) Right 2(m)

④ Set mid = Int ((BEG + END)/2)

top middle mo.

5. If Data [mid] = Item set LOC := Mid

Else LOC := Null.

efficiency of algorithm

Complexity

Best case analysis
worst " case

Complexity is the function that gives the running time and/or space for some input.

which complexity $f(n)$

Best case: The minimum value. [1st 2ⁿ]

worst case: The maximum value. [last 2ⁿ]

average case: The expected value (half).

$$\log n < n \log n < n^2 < n^3 < 2n \cdot \ln n < n^n$$

$$O(1) < \log n < n \log n < n^3 < 2^n < O(n!)$$

big o notation: It is a way to describe

the speed or complexity of given algorithm

2D Array Memory Representation

Row Major =

$$\text{Loc } A[i][j] = \text{Base}(A) + w[n(i-1) + (j-1)]$$

$$\text{Loc } A[i][j] = \text{Base}(A) + w[n(i-1) + (j-1)]$$

$n = v_2 - l_2 + 1$

Ques: A 2D array is defined, as $A[3:7, -1:4]$ requires 4 words per memory cycle. Find the location ~~A[5,2]~~

$A[5,2]$ if array is implemented in Row major.

order:

$$A[3:7, -1:4] \quad \left| \begin{array}{l} \text{Base}(A) = 200 \\ w = 4 \\ l_1 = 3 \quad v_1 = 7 \\ l_2 = -1 \quad v_2 = 4 \end{array} \right. \quad \left| \begin{array}{l} j = 5, i = 2 \\ n = 4 - (-1) \\ = 6 \end{array} \right.$$

here Row major.

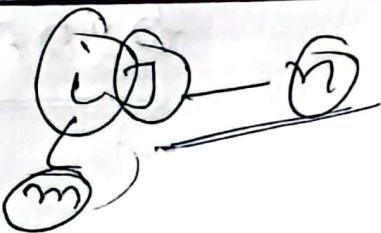
$$\text{Loc } A[i][j] = \text{Base}(A) + w[n(j-1) + (i-1)]$$

$$= 200 + 4[6(5-1) + (2-1)]$$

$$= 200 + 4[6(5-1) + (2-1)]$$

$$= 200 + 4[6(5-1) + (2-1)]$$

~~row~~ Column major.



$$\text{Loc } A[i][j] = \text{Base}(A) + w \left[\frac{(i-1) + m(j-1)}{m} \right]$$

Given defined as $A[20][5]$, 4 words. Find the location $A[12][3]$, are column major.

$\Rightarrow \text{Base} = 200, w=4, i=12, j=3$

$m = \text{number of rows}$

here

$$\text{Loc } A[i][j] = \text{Base}(A) + w[(i-1) + m(j-1)]$$

$$\text{Loc } A[12][3] = 200 + 4 + [(12-1) + 20(3-1)]$$

$$[(12-1) + (3-1)] \times 4 = 488$$

~~$(12-1) + (3-1) = 14$~~

col $\text{Loc } A[j][k] = \text{Base}(A) + w[M(k-1) + (j-1)]$.

row $\text{Loc } A[j][k] = \text{Base}(A) + w[m(j-1) + (k-1)]$

Matrix

Matrix multiplication.

let

$$A [M \times P] \Rightarrow C [M \times N]$$

$$B [P \times N]$$

row column.

a \Rightarrow row b \Rightarrow column \Rightarrow same width

$$\begin{cases} m = \text{row} \\ n = \text{column} \end{cases}$$

Algorithm

1. Repeat step 2 to 4 for $I = 1$ to m .
2. Repeat step 3 and 4 for $J = 1$ to n
3. Set $C[i, j] := 0$
initialize zero matrix.
4. Repeat for $k = 1$ to P :

$$C[i, j] := C[i, j] + A[i, k] * B[k, j]$$

minimum cost plan last 3 digits remain.

no swap bill no obtain one by

Sparse matrix

array representation.

	0	1	2	3	4
0	0	0	4	0	8
1	0	0	0	3	6
2	0	0	0	2	0
3	0	2	3	0	0

"(2) ~~on~~ ~~with~~ 0 ~~by~~ 0
value ~~on~~ ~~with~~
Row ~~on~~ ~~with~~ 0 value

Row	0	0	1	1	2	3	3
column	2	4	3	4	3	1	2
value	4	5	3	6	0	2	-3

SM

- Matrix with a relatively high proportion of zero entries are called sparse matrix

Mathematical and function

• Exponents and logarithm.

- common logarithm (base 10), natural logarithm (base e)
Binary " (base 2)

• algorithmic notation:

- step, control, exit

- comments $\boxed{[\dots]}$ for

- variable - upper case for

- assignment statements $(:=)$

- input and output

$$\# \lfloor 3.14 \rfloor = 3$$

$$\lfloor -8.5 \rfloor = -9$$

flock

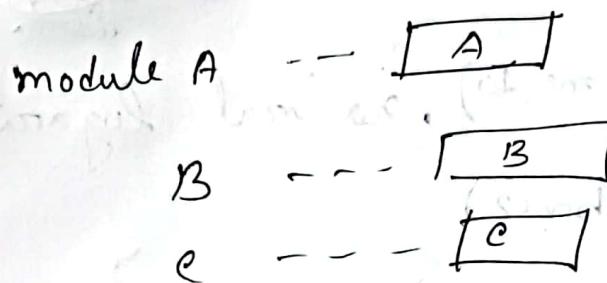
$$\lceil 8.5 \rceil = 9$$

$$\lceil 3.4 \rceil = 4$$

ceiling

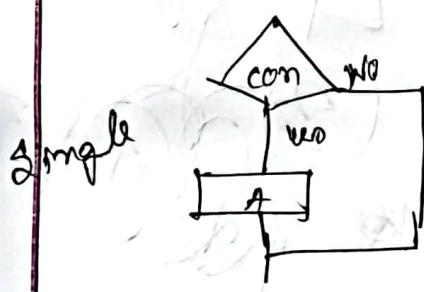
Control Structure

Sequential flow:



Searily

Conditional flow:



multiple

if (1)

A₁

Else if

A₂

Else if A₁, A₂

else B

• Quadratic equation.

① read A, B, C

② set $D := B^2 - 4AC$

3. if $D > 0$ then

a) set $n_1 := (-B + \sqrt{D})/2A$ and $n_2 := (-B - \sqrt{D})/2A$.

b. write: n_1, n_2

else if $D = 0$

set $x := -B/2A$.

write: 'unique solution', x .

else

write: 'no real solution'

Ex:

Matrix

$$B[1] = a_{11} \\ i \quad j$$

$$B[2] = a_{23} = 3 \times 1 + 3 \times 3$$

last acc HC = 5

∴ column index শুরু হলে 3

$$L = \frac{\partial (J-1)}{2} + N.$$

like:

$$3,2 \Rightarrow L = \frac{\cancel{3}(3-1)}{2} + 2 \quad [3-1]$$

$$= 3 + 2 = 5$$

$$\therefore B[5]_{32}.$$

Multidimensional array:

⇒ It's a array more than one level or dimension.

↓

General multidimensional Array

Index or range $LB = 1$ to UB

Range $(2:8)$, $(-4:1)$, $(6:16)$
 LB UB $[UB - LB + 1]$.

length
of dimension

$= 8 - 2 + 1$ $b_2 = 8 - 2 + 1$ $b_3 = 6 - 10 + 1$
 $= 7$ M N B $= 7$ $= 5$
 $\equiv [7, 6]$

So have $\frac{7 \times 6 \times 5}{= 210}$ elements total.

math

now Base 200, $w = 4$ [23rd one]

$(5, -1, 8)$

effective index.

$E_1 5 - 2 = 3$ $E_2 = \frac{-1 - 4}{-1 - 4} = 0$ $E_3 = 8 - 6 = 2$

↑ 2nd row 2nd col (-) Lower bound.

now major order.

$$E_1 L_2 = 3 \cdot 6 = 18$$

$$E_1 \cdot L_2 + E_2 = 18 + 3 = 21$$

$$(E_1 L_2 + E_2) L_3 = 21 \cdot 5 = 105$$

$$(E_1 L_2 + E_2) L_3 + E_3 = 105 + 2$$

$$= 107$$

therefore

Loc (maze [5, 1, 8])

$$= \text{Bone} + w [\quad]$$

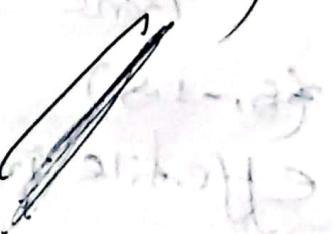
$$= 200 + 4(107) =$$

$$= 628$$

$$E_1 L_2$$

$$E_1 L_2 + E_2$$

$$(E_1 L_2 + E_2) L_3 + E_3$$



broad search ⊂ broad search

④

String

mitting parts

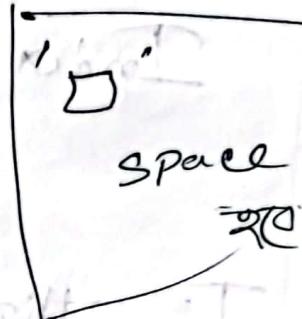
concatenation

~~A + The man!~~

~~A → The man!~~

All B

[Add or



Space

substring

order

The ~~end~~ substring The end
and its substring.

initial \Rightarrow start

(string, initial, length)

The man, $\frac{5}{start}$, $\frac{02}{end}$

\Rightarrow 'man'

String Operation

Index (text, pattern)

T = ~~the~~ father in the program

Index (T, 'The') = 7.

Index (T, 'hum') = 0

~~Index (T)~~

word processing

Insert (text, position, string)

Ex

Insert (A B C D E F G, 3, xyz)

3 no position add xyz

= A B C xyz D E F G //

slack

- * A stack is a list of elements in which an element may be inserted or deleted only one end called the top of stack.

- Stack means portion of last element
 - Top probably set 0 of portion stored with 1 .

- Push = insert element } operation of stack.
 - pop = delete }

Array representation.

-10P

~~#~~

- How to push. algorithm

- 1. If $\text{top} = \text{MaxSTK}$ then : print :

overflow and return.

full error in.

2. Set $\text{TOP} := \text{TOP} + 1$

3. Set $\text{STACK}[\text{TOP}] = \text{item}$

insert new item.

4. return

~~#~~

- How to POP

1. If $\text{top} = 0$ then : print : underflow

and return.

→ ~~item~~ → ~~return~~ delete ~~20~~ ~~in~~

2. Set $\text{ITEM} := \text{STACK}[\text{TOP}]$

3. Set $\text{TOP} = \text{TOP} - 1$.

→ ~~top~~ ~~in~~ ~~not~~ ~~item~~ ~~delete~~

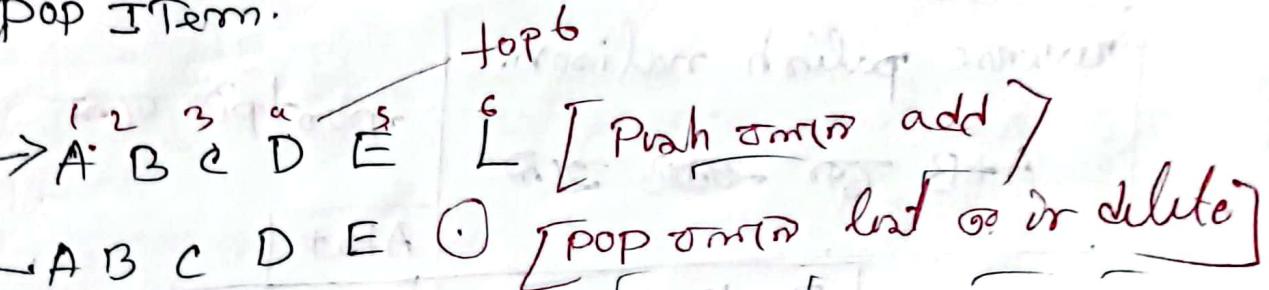
4. return.

90%

STACK , A B C D E - - -

Push L

Pop Item.



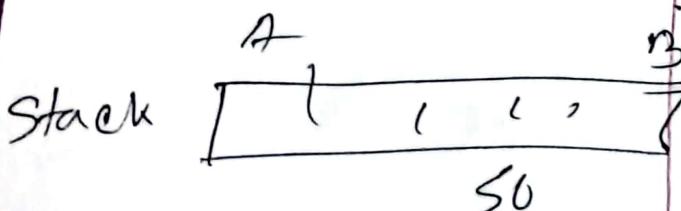
Minimizing overflow

Application of Stack.

A
20

B
30

$$\underline{A + B = 50}$$



- Evaluation of Arithmetic

- Backtracking

- Delimiter Checking

- Reverse of Data.

- Processing a function call.

polish notation

(before placed operands)

$A+B$ $\xrightarrow{\text{PreFix}}$ $+AB$ $\xrightarrow{\text{PostFix}}$ polish notation.

reverse polish notation.

$A+B$ $\xrightarrow{\text{PostFix}}$ ~~AB~~ $\xrightarrow{\text{PostFix}}$

$AB+$

Prefix + AB, Postfix AB+

#

① $(A+B)*C$

$\Rightarrow [+AB]*C$

$\Rightarrow *+[AB]C$

3rd grad rule then

(* 2nd

#

② $A+B*C$

$\Rightarrow A+[*BC]$

$\Rightarrow +A[*BC]$

(*) $\xrightarrow{\text{PostFix}}$ $\xrightarrow{\text{PostFix}}$

(*) $\xrightarrow{\text{PostFix}}$ $\xrightarrow{\text{PostFix}}$

$$\# (A+B) \cdot / (C-D)$$

↑ or ↑ right to left
*, / left to right

$$= [\underline{+AB}] / [\underline{-CD}]$$

$$= \underline{\underline{/ + \underline{AB} - CD}}$$

Reverse / postfix notation

post of reverse
+ / m/s

$$\begin{aligned} \textcircled{1} & (A+B) * C \\ = & \underline{\underline{AB + C *}} \end{aligned}$$

$$\begin{aligned} \textcircled{2} & \underline{\underline{ABC * +}} \\ \textcircled{3} & \underline{\underline{AB + CD - /}} \end{aligned}$$

infix	postfix	prefix / polish
$A+B$	$\underline{\underline{AB +}}$ $A * B + C / D$ $= AB * + CD /$ $= AB * CD / +$	$\underline{\underline{+ AB}}$ $A * B + C / D$ $\Rightarrow * AB + C / D$ $= * AB + CD /$ $= * AB / CD$

Evaluation of a postfix notation:

- postfix & infix are same!

let given postfix P

Step

① Add a right parenthesis ")" at the end of P

$P')$ লাই কাষ কোড

② Scan P from left to right and repeat
step 3 and 4 for each element until ")" is found

$P')$ নি পার্স করা হচ্ছে 3, 4

③ If an operand, put on stack.

④ If an operator $\boxed{\otimes}$ is encountered.

যেমন operator \otimes ।

a. Remove the two elements of stack.

where A is the top B is the next top.

⑤ b. Evaluate $B \otimes A$

$B \otimes A$ formal term

• place the result of (b) back stack.

Stack push top first

[End of if]

[end of step 2 loop] Step 2 ~~middle~~ (2nd)

5. Set value equal to the top element on.

Stack.

6. Exit.

~~84~~
5 6 2 + * 12 4 / -)
1 2 3 4 5 6 7 8 9 10
our turn and

5 * (6+2) - 12/4.

= 37

$$\# \textcircled{5} * (6+2) - 12/4 \textcircled{1} \textcircled{6}$$

Symbol www.symbol.com Stack www.stack.com

$$\textcircled{1} \textcircled{6} 5 \longrightarrow \underline{5}$$

$$\textcircled{2} 6 \longrightarrow \underline{5, 6}$$

$$\textcircled{3} 2 \longrightarrow \underline{5, 6, 2}$$

$$\textcircled{4} + \longrightarrow \textcircled{5} (6+2) \\ = \underline{5, 8}$$

$$\textcircled{5} * \longrightarrow 5 * 8 \\ = 40$$

$$\textcircled{6} 12 \longrightarrow \underline{40, 12} \quad \underline{(12-4)} \\ = \underline{-8}$$

$$\textcircled{7} 4 \longrightarrow \underline{40, 12, 4} \quad \underline{-} \\ = \underline{-12}$$

$$\textcircled{8} / \longrightarrow 40 (12 \div 4) \\ = \underline{40, 3}$$

$$\textcircled{9} - \longrightarrow (40-3) \quad \cancel{12} \cancel{4} \\ = \cancel{37} \quad \cancel{2} \cancel{8}$$

$$\textcircled{10}) \quad \cancel{12} \cancel{4} - (37) \quad \cancel{2} \cancel{8}$$

operator ~~also~~ operand ~~not~~ operator

Transforming infix to postfix

• S infix, P postfix

1. push "(" onto stack, and add ")" to the end of S.
2. Scan S from left to right repeat step (3-6) for each element of S until the stack empty
3. If an operand is encountered, add it to P
operand ~~from S~~ ~~to P~~ to push .
4. If a left parenthesis is encountered, push it into stack.
5. If an operator \otimes is encountered then.
 - a. Repeatedly pop from STACK and add to P each operation (on the top stack) which

has the same precedence and or higher
precedence than \otimes . until left parenthesis is encountered

- \otimes ক্ষমান এই higher \otimes^2 -এরে in Stack
then pop এর P to Push এর
+ এর higher \otimes , /

b. add \otimes to stack

for \otimes stack দখিবো

6. If parenthesis is encountered then:

a. Repeatedly pop from stack and

to P each operation (on the top of
stack) until a left parenthesis is encountered

(Stack তের Left parenthesis এর সব প্রক্রিয়া
-এর পরে control, then P এর সময়)

b. remove the left parenthesis,

c. left parenthesis এর পরের, the parenthesis
সর্বান্তর

7. exit (got all no) .

Infix to Postfix

Example - () - left parenthesis

Infix: A + B * C - (D / E + F) * G) * H

$$A + B * C - (D / E + F) * G) * H$$

$$A + B * C - (D / E + F) * G) * H$$

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20

Symbol	Stack	Expression P
(1) A	(A
(2) +	(+	A - left
(3) ((+(stack
(4) B	(+(B	AB
(5) *	(+(B*	AB
(6) C	(+(B*C	ABC
(7) -	(+(B*-	ABC*
(8))	(+(B*-)	ABC*D
(9) D.	(+(B*-D	ABC*D
10. /	(+(B*-D/	ABC*DEF
11. E	(+(B*-D/F	
12. ^	(+(B*-D/F^	ABC*DEF
13. F		

higher
order
of 2nd
order

TGS T ~~DATA~~ (1) ~~FCGQO 2020~~
P (G DATA) and
(1) IR remove and

(14)

C + (-)

A B C * DEF 4/

(15) *

C + (- *)

A B C * DEF 4/1

(16) G₂

C + (- *)

A B C * DEF 4/2

(17) J

C + (+)

A B C * DEF 4/2 *

(18) *

C + (*)
→ higher just 2020
just 2020

A B C * DEF 4/2 *

(19) H

C + (*)

A B C * D F F 4/2 * - H

(20) J

A B C * D E F 4/2 * - H * +

TGS Pranthisio DATA (1) FCGQO 2020

TGS Q (1) P (G 2020)

higher wise.

(1) IR remove

ABCD EFGH

+ (1) - (2) +

ABCD EFGH

+ (1) - (2) +

Introduction.

Data : Data means ^{simple} values or set of values.

Entity : Each patient is an entity.

Attributes : The properties - Name, N.I.D., Room etc are attributes.

Entity set : The collection of patients is the entity set.

Information : It is processed, organized and restructured data.

- Data, process and information
- Data types

Build data type (char, double, int)

Abstract data type

User defined data type

5, 4, 8, 5

5, 4, 8, 5

5, 2, 3

5, 7, 8,

Abstract data type.

It is a type of objects whose behaviour
is defined by a set of values and set of
operations.

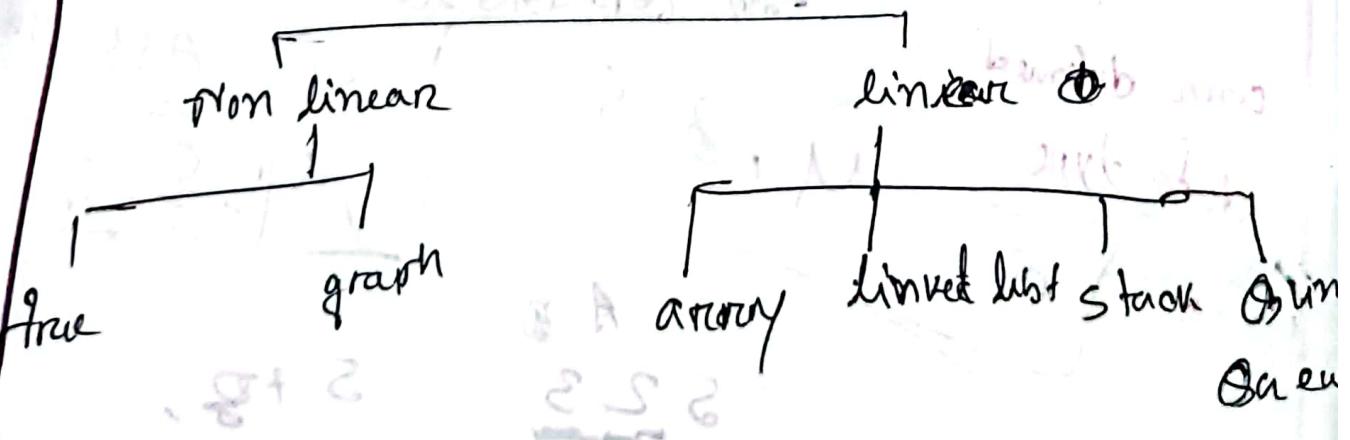
- Some abilites (built in data
to ansav)
calculus defined data type

Data structure



The mathematical and logical model
of particular organization of data is
called a data structure.

Data structure



Array

- collection of some type of data.

Linked List

It is an ordered collection of finite, homogeneous data elements, called nodes, where, the linear order is maintained by means of links or pointers.

- Our books are finite collection containing address
of our address of room

Stack

One item is lost on first out

Push item

LIFO

last one, withdrawn

Queue

Push item

FIFO

first one, withdrawn

First in first out

Free

Contain hierarchical, hierarchical relationship between various elements

-symmetric → true -2(6n) Octrap

Brachistion n. n. n. n. n.

↓ conected Simplus size
2cm green

D's operation.

- Traversing - Processing each element in the list
 - Search - find the exact element given value
 - Insertion - Adding new element in the list.
 - Deletion - Removing an element from the list
 - Sorting - Arranging elements in some type of order
 - Merging - Combining two sorted list in the single list (2nd term end)

~~diff~~ difference

Data

It means value or set of values.

It has individual figures, numbers or groups.

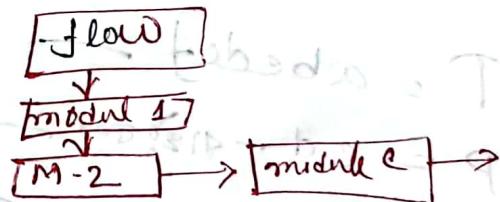
Information

Data with attributes is called information.

Information is processed data.

Control structure:

(i) Sequential logic: unless the introduction are given to traverse, the modules are executed in obvious sequence.



(ii) Selection logic: The structures which implement this logic are called conditional structure or if structures.

If condition

[module A]

else

[module B]

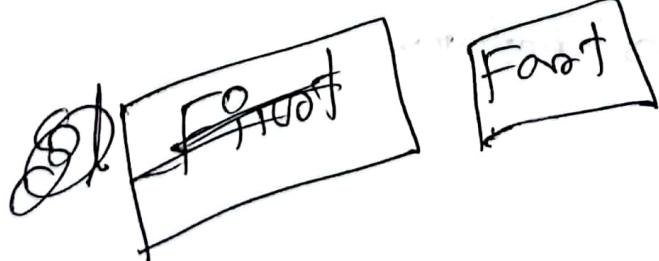
3. Iteration logic: It starts with a repeat statement and ends followed by a module.

multidimensional Array

① length of dimension and element
 $(UB-LB+1)$ program ends Q

Pattern matching

$T = abcde \rightarrow$ length - ⑥
 $P = cd \rightarrow$ for mode 2 - ② R
max = $S-R+1$



format

1. Set $K := 1$ and $\max := S - R + 1$

$\Rightarrow K=1$ तक, \max तक कम्प्लेक्सिटी $\Theta(6)$

2. Repeat steps 3 to 5 while $K \leq \max$

3. Repeat for $L = 1$ to R .

pattern G?

length

if $P[L] \neq T$

$\boxed{[K+L-1]}$

$\boxed{[1, 2, 3, 4]}$

गढ़िया कर करो

4. Set $\text{index} = K$ and $\text{exit} = 1$

5. Set $K := K + 1$

① (प्रारंभिक)

6. $\text{index} = 0$ Set

7. Exit

Example

$P = \text{xxxxy}$

$Q_0 = \epsilon$, $Q_1 = x$, $Q_2 = xx$, $Q_3 = xxx$, $Q_4 = xxxx$

$Q_5 = xxxxxy \in P$

Table:

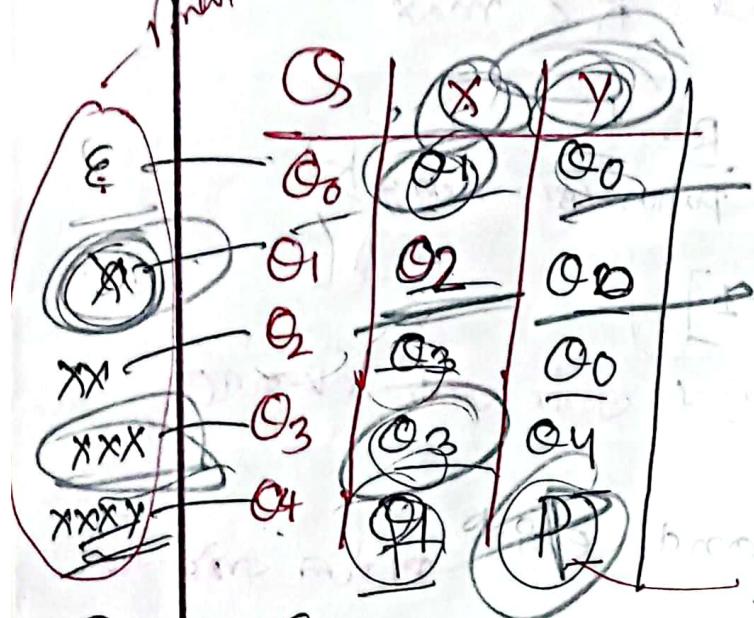
Final mem

~~Ex O1~~

new ex arr?

$E_{in} \rightarrow x \text{ arr} \Rightarrow O_1$

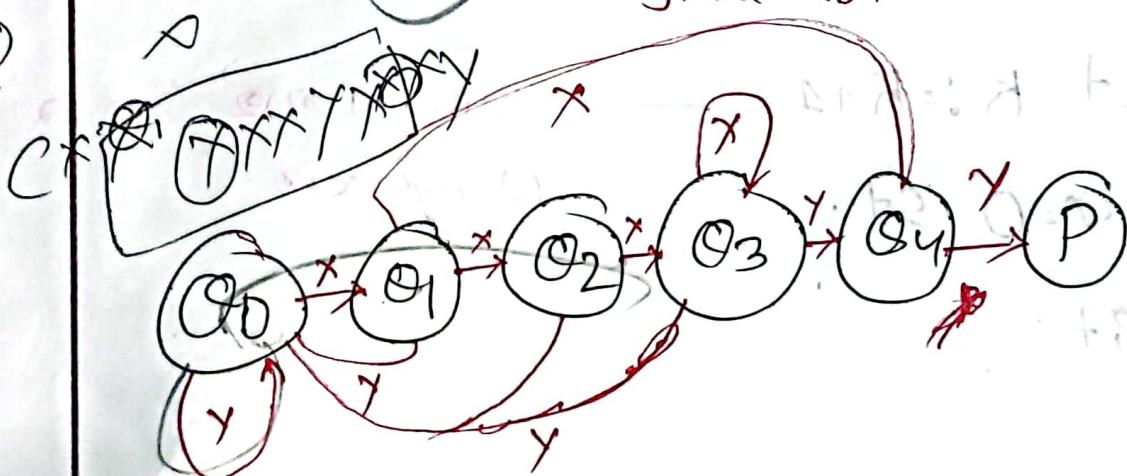
Final mem O_0



$(\overbrace{x \ x \ x \ x}^{\text{---}}) \rightarrow O_3$

$\overbrace{xxxxy}^{\text{---}} \rightarrow$

final state O_1



$x \ x \ x \ y \ x \ x$

=

$x \ x \ x \ y \ x \ x$

#Slow pattern matching

$$\text{Length}(T) - \text{Length}(P) + 1$$

$$T = (ab)^5 \quad P = abc$$

$$T = ababababab = \text{Length}(T) = 10$$

$$P = abc \rightarrow \text{Length}(P) = 3$$

$$\rightarrow 10 - 3 + 1$$

$$\rightarrow 8.$$

~~Find~~ ③ by P ~~in T~~ in T (with 3 \rightarrow)

and

abc ~~in T~~ in T

$$1) \underline{aba} = abc \rightarrow 3$$

$$2) \underline{bab} = abc \rightarrow 1 \quad 6 \cdot \underline{bab} = abc \rightarrow 1$$

$$3) \underline{aba} = abc \rightarrow 3 \quad 7 \cdot \underline{aba} = abc \rightarrow 3$$

$$4) \underline{bab} = abc \rightarrow 1$$

$$5) \underline{aba} = abc \rightarrow 3$$

$$C = 3 + 1 + 3 + 1 + 3 + 1 + 3 + 1$$

$$= 16.$$