

Geometric Representation

Planar polygon?

→ It is a polygon in which all vertices lie on the same plane.



polyhedron:

It is a 3D shape made of flat polygons. Faces that enclose a volume.

In modeling polyhedrons are often treated as blocks rather than wireframes.

Curved surface design

It is used in 3D modeling to create more realistic shapes.

Modeling Approaches

- use small ~~ps~~ curved patches joined together
- Build model with solid shapes

Model Construction Method

Additive | Subtractive
Simple shapes to create | remove parts from an object

Wire-frame models (4)

It is a model consist of edges, vertices and polygon here vertices are connected by edge and polygons are sequences of vertices on edges.
It's also called polygonal net/mesh.

Advantage	Disadvantage
• Simple and easy to create	• Lack of detail and realism
provide clear view of the object structure	Complex model can become complex
requires minimal storage space	unsuitable for simulations.

Designer needs little training	Image Causes Confusion
System needs little memory	Can't get required information from this model.
Efficient for visualization	Limited representation Surface and materials.

Representing Polygonal Net model

Different way representing polygonal net model
Some of are →

Vertex List representation: Simplest way. It contains a list of vertices each of which has a position in 3D space.

Explicit vertex list (cont): Vertices $V(P_0, P_1, P_2, \dots, P_n)$ are

Stored in the order they appear

Shared vertices are repeated and edges may be drawn multiple times

Polygon Listing: Each vertex is stored once in a list v_0, \dots, v_N and polygons reference these vertices using indices.

here also shared edges drawn multiple times

→ Explicit Edge Listing

vertex list - Each vertex stored once.

Edge " - each edge is stored once linking 2 vertices

Polygon - Defined as indices pointing to edges

Benefit - Reduces redundancy and each edge drawn only once.

This method is efficient for Wireframe model

→ Glyben are not important

4 problem of Interpolation & Approximation

Interpolation problem

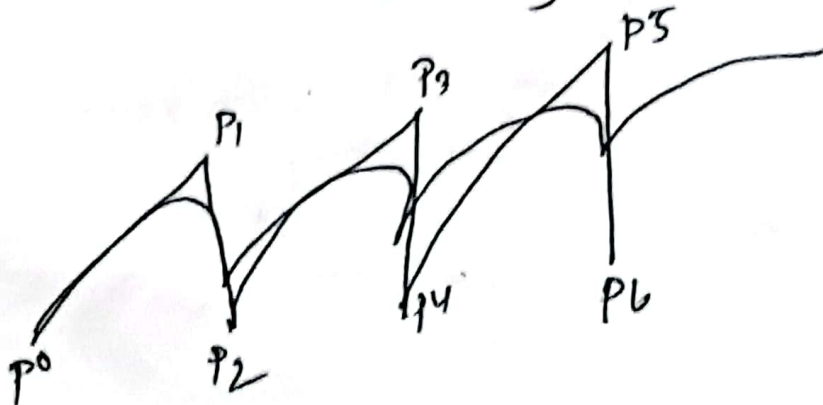
It involves creating a curve or surface that pass through given set of data points.

Challenges are over-fitting, irregular data and high computation — large dataset is expensive.

Approximation Problem

Definition: It creates a curve on surface that closely follows the data points without necessarily passing through them.

Challenges are ⇒ loss of precision, Balancing accuracy, Bias



Seg 7 (chp 10)

Hidden Surface

Hidden Surface is a parts of object that are not visible from a particular viewpoint because they are blocked by other objects in the scene.

* In Overlap 2 point lie on the same projection line they are said to overlap in the projection

* If 2 point overlap a depth Comparison is performed to determine which point is in front of the other

Depth Comparison \rightarrow In the same projection line.

$$\underline{x_1 = x_2} \quad \text{and} \quad \underline{y_1 = y_2} \quad \text{2D depth.}$$

Comparison of z

Hidden Surface algorithm, used for which objects and surface will obscure (dark) ~~to~~ determine for

Z buffer Algorithm

The Z buffer Algorithm is used for hidden surface removal in 3D graphics. It works by sorting the depth of each pixel to determine which surface are visible.

when the surface is drawn, its depth at each pixel is compared with the depth value already sorted in the Z-buffer for pixel.

- If the new depth smaller (close to camera) than the sorted depth, the surface visible.

- If the new depth is larger, the surface hidden and the Z buffer stays remain unchanged.

Z buffer ensures that only the closest surfaces are visible in each pixel.

Steps in Z buffer Algorithm.

• Initialize the Z buffer :

① Set the screen background colour (black.)

② Initialize the Z buffer to the minimum depth for each pixel.

Process Each object

• Each object calculate its depth each pixel.

• If the new depth smaller, update Z buffer changed pixel color

• If the new depth larger, keep pixel unchanged.

Final Image

Display the pixels in the frame buffer, using depth values in the Z buffer to determine which surfaces are visible, hidden surfaces are removed.

Example (Z buffer)

Consider Looking at a 3D scene with a
~~Cube and sphere.~~

tree, house, Car in 7, 5, 3, depth.

Steps

- Initialize background clr black.
- " Z buffer minimum depth (10)
- Compare depth value 10, in tree) smaller than 10.

So update clr pixel is tree clr

- Compare update (7 tree) depth value. here
(5 house) smaller than (7 tree).

So update clr pixel to house clr

Same Car (3) use than (5 house)

Final Image

Car front \rightarrow house \rightarrow tree

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Subdivision & Warrens Algo

It is a recursive method that subdivides the screen into smaller quadrants until each quadrant can be easily classified as either visible or hidden.

Steps

- Set the viewing area to the whole screen
- In PVL sort polygons by depth (Z Value)

Closely polygons

- Complete inside the viewing area.
- " outside.
- Surrounding the area.
- Partially overlap

Various polygons

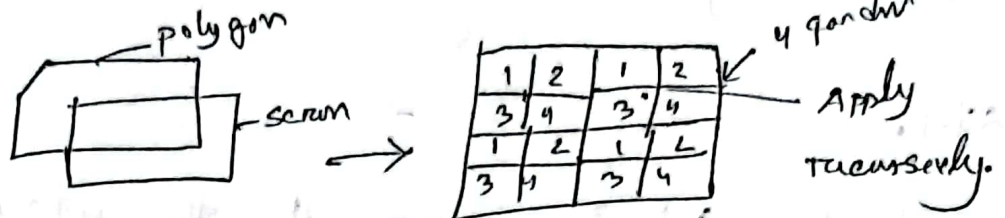
- Various outside polygons
- " polygons surrounded by others.
- " disjoint polygons.

Check PVL → If empty area hidden.

If one polygon remain - It visible

• If multiple polygons remain, subdivide 4 quadrants.

• Apply recursively each quadrant.



$$\frac{\text{Math}}{10.4} \text{ (which point observe)}$$

Given points.

$$C \begin{pmatrix} 0, 0, -10 \\ x_0, y_0, z_0 \end{pmatrix}$$

$$P_1 \begin{pmatrix} 1, 2, 0 \\ x_1, y_1, z_1 \end{pmatrix}$$

$$P_2 \begin{pmatrix} 3, 6, 20 \\ x_2, y_2, z_2 \end{pmatrix}$$

$$P_3 \begin{pmatrix} 2, 4, 6 \\ x_3, y_3, z_3 \end{pmatrix}$$

Sol $P_0(x_0, y_0, z_0) \& P_1(x_1, y_1, z_1)$

$$x = x_0 + (x_1 - x_0) t$$

$$y = y_0 + (y_1 - y_0) t$$

$$z = z_0 + (z_1 - z_0) t$$

now eq for $C(x_0, y_0, z_0)$ and $P_1(x_1, y_1, z_1)$

$$x = x_0 + (x_1 - x_0)t$$

$$= 0 + (1 - 0)t = t$$

$$y = y_0 + (y_1 - y_0)t$$

$$= 0 + (2 - 0)t = 2t$$

$$z = z_0 + (z_1 - z_0)t$$

$$= -10 + (0 - (-10))t$$

So put values on $P_2(3)$ and $P_3(2)$

$$x = t$$

$$y = 2t$$

$$z = -10 + 10t$$

$$\Rightarrow x = 3$$

$$y = 6$$

$$z = 20$$

$$\Rightarrow x = 2$$

$$y = 4$$

$$z = 10$$

put values $P_1(1)$

$$x = 1$$

$$y = 2$$

$$z_1 = 0$$

but P_3 does not obscure

and $z = 10$ and $P_3 z = 10$ (Given)

here P_1, P_2 takes P_3 and

$z_1 < z_2$ so P_1 in front of P_2 .

$$0 < 20$$

P_1 obscures P_2

10.5

Steps of weather any given point obscure

other point :

① weather 2 point lie same projection line

② If they do, which point in front of the other



10.10

Basic Scan Line Method for hidden surface

Scan line method process the screen row by row to determine which surface are visible or hidden.

Algorithm looks all polygon intersect ($y=a$) line for each pixel on the line & compares Z value for each polygon

with smallest Z value set the color