

Group - A

- Image compression
- Morphological process

Group - B

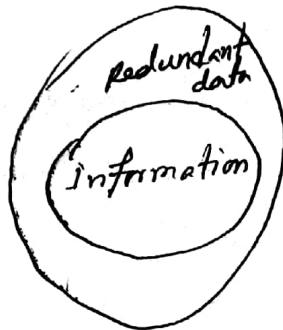
- Segmentation
- Image representation
- Pattern recognition

## Image Compression : (Contents)

- Defn
- fundamental concepts of data compression & image compression.
- Data Redundancy (Def, Type)
- Image compression Model.
- Image compression Type. (Lossy & lossless)
- Fidelity criteria (SNR, RMSE etc.)
- Image compression standards, format etc.

### # Data Compression

- DC is defined as the process of encoding data using a representation that ~~reduces~~ reduces the overall size of data, The reduction is possible when the original dataset contains some type of redundancy.

Information vs Data:

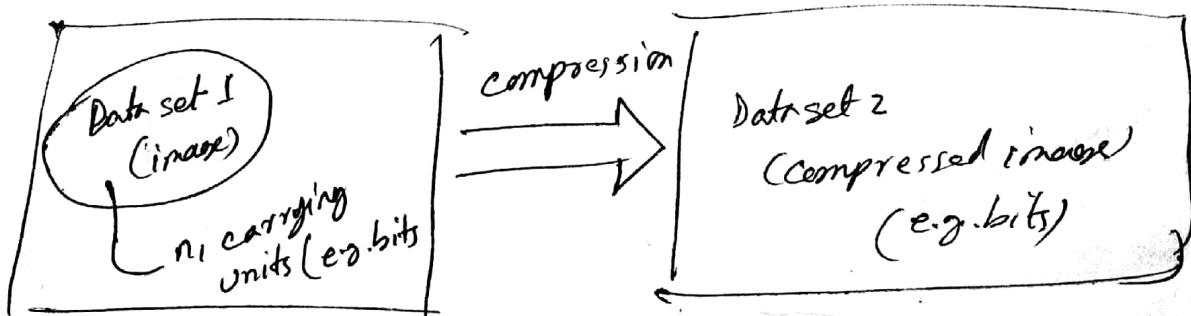
$\text{Data} = \text{Information} + \text{Redundant data}$

Data Redundancy:

- Let  $n_1$  and  $n_2$  denote the number of datum in two different representation of the same image. The relative data redundancy  $R_d$  of the first representation is defined as -

$$R_d = 1 - \left( \frac{1}{C_r} \right) \quad \text{where, } R_d = \text{Relative data redundancy}$$

~~C<sub>r</sub>~~  
C<sub>r</sub> = Compression ratio .



$$\text{Compression ratio: } C_r = \frac{n_1}{n_2}$$

where  $n_1$  = first data  
 $n_2$  = second "

1. if  $n_1 = n_2$   $C_r = 1$  and  $R_d = 0$

2. if  $n_2 < n_1$ , then  $C_r \rightarrow \alpha$

$$R_d = 1$$

3. if  $n_1 < n_2$  then  $C_r \rightarrow 0$

$$R_d \rightarrow -\alpha$$

### Data redundancy

- (i) coding redundancy
- (ii) interpixel "
- (iii) Psycho-visual "

### Coding redundancy:

- \* code: A list of symbols (letters, numbers & bits etc)
- \* code word: A sequence of symbols used to represent a piece of information or an event
- \* code word length: Number of symbols in each code word.

#### Example:

0: 000	4: 100	length = 3
1: 001	5: 101	
2: 010	6: 110	
3: 011	7: 111	

### Mathematical formula of coding redundancy:

$$\text{Average, } \overline{\text{Length}} = \sum_{k=0}^{L-1} (i_k) P(r_k)$$

$N \times M = \text{image}$

$r_k$  =  $\cdot k$ -th gray level ( $0, 1, \dots, L-1$ )

$p(r_k)$ : Probability of  $r_k$

$l(r_k)$ : # of bits for  $r_k$

Total number of bits:  ~~$N \times M \times \text{avg}$~~   $N \times M \times L_{\text{avg}}$

constant length of  $l(r_k)$

#  
Case I

variable length of  $l(r_k)$

Case I:  $l(r_k) = \text{constant length}$

$r_k$	$p(r_k)$	code 1	$l_1(r_k)$
$r_0 = 0$	0.19	000	3
$r_1 = \frac{1}{7}$	0.25	001	3
$r_2 = \frac{2}{7}$	0.21	010	3
$r_3 = \frac{3}{7}$	0.16	011	3
$r_4 = \frac{4}{7}$	0.08	100	3
$r_5 = \frac{5}{7}$	0.06	101	3
$r_6 = \frac{6}{7}$	0.03	110	3
$r_7 = 1$	0.02	111	3

$$L_{\text{avg}} = \sum_{k=0}^7 l(r_k) \cdot p(r_k)$$

$$= 3 \times 0.19 + 3 \times 0.25 + \dots$$

= 3 bits

Total number of bits  $3 \times N^M$ .

Case - II:  $l_2(r_k)$  = Variable Length.

$r_k$	$Pr(r_k)$	Code 1	$l_1(r_k)$	Code 2	$l_2(r_k)$
			11		2
		01		2	
		10		2	
		001		3	
		0001		4	
		00001		5	
		000001		6	
		000000		6	

Lavg = ~~0.19 + 0.25 + 0.21 + 1.6~~

$$\sum_{k=0}^{7} l_2(r_k) \cdot Pr(r_k)$$

$$= 2 \times 0.19 + 2 \times 0.25 + 2 \times 0.21 + 3 \times 1.6 + \dots$$

$$> 2.7 \text{ bits}$$

$$C_F = \frac{3}{2.7} = 1.11$$

$$\text{Therefore } R_d = 1 - \frac{1}{C_F} = 1 - \frac{1}{1.11} = 0.099$$

[Thus 10% of data  
in original 8-bit  
image 2D intensity array is]

## ② Interpixel redundancy:

- If a pixel value can be reasonably predicted from its neighboring pixels the image is said to contain interpixel redundancy.

### # Type of IR:

- Spatial redundancy

→ Local : Pixels at neighboring locations have similar intensity.

→ Global : Recurring patterns.

- Spatial redundancy : Between color planes.

→ Temporal redundancy : Betn consecutive frames,

## ③ Intelli psycho visual redundancy:

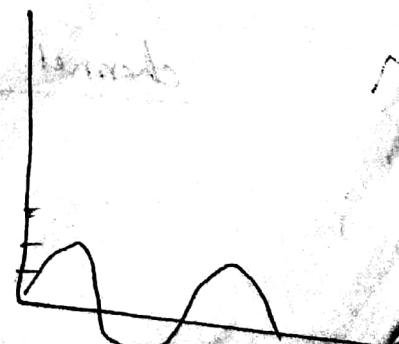
→ It is a redundancy corresponding to different sensitivities

to all image signals by human eyes. Therefore, eliminating some less relative important information in our visual processing maybe acceptable.

→ Psychovisually redundant image information can be identified and removed.

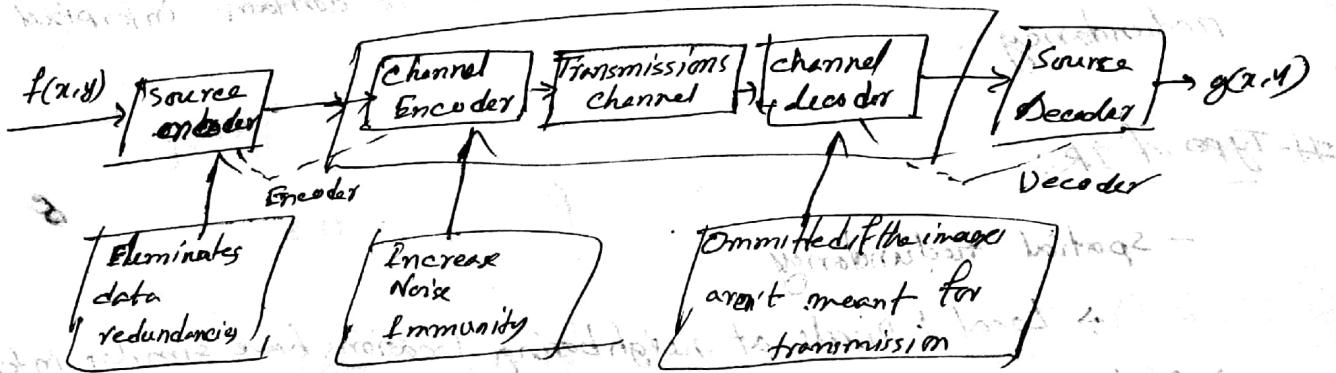
→ a process referred to as quantization.

→

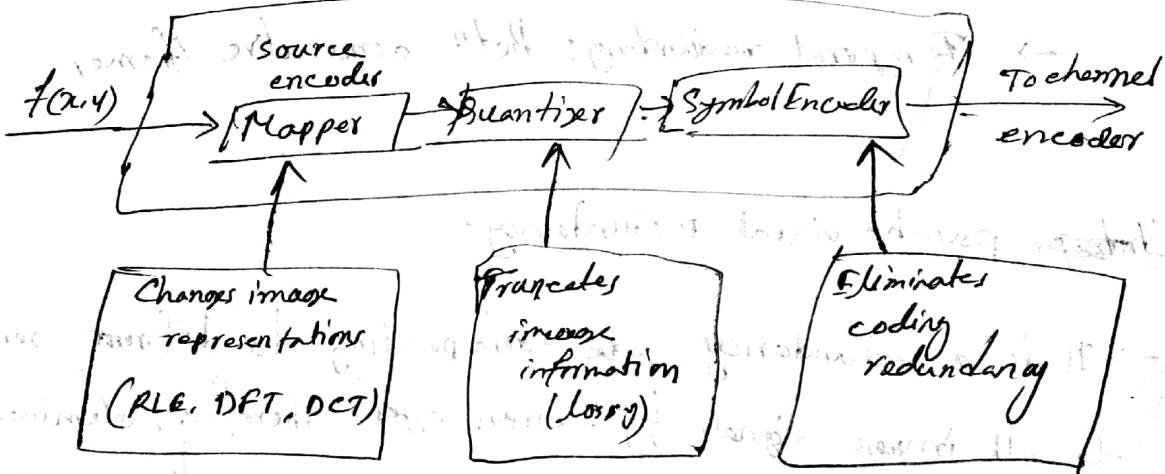


## # Image Compression Model :

→ A compression scheme can generally be modeled as shown -



\* This source encoder is typically modeled as -



### a) Source Encoder Model :



### b) Source decoder model

**Mapper:** transforms the image to a formal design to reduce interpixel redundancies.

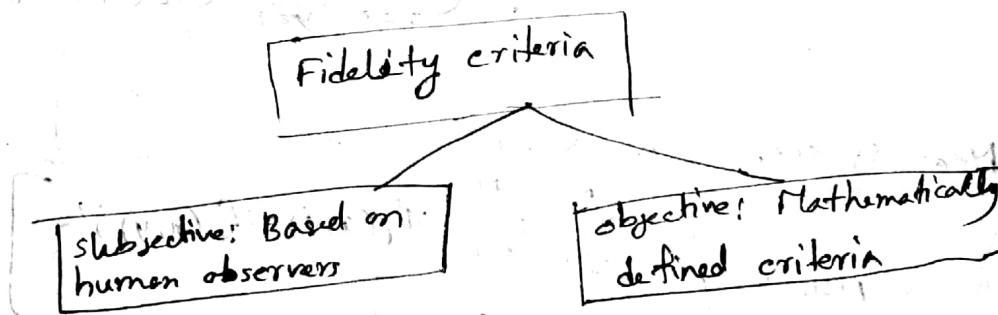
**Quantizer:** Reduces psychovisual redundancies by quantizing deemed less important for visual interpretation.

Symbol encoder:

- codes the data efficiently (typically using some form of variable-length coding scheme) and aims to reduce coding redundancies.

**Error criterion / Fidelity criteria:**

To determine the quality of the image.



① subjective fidelity criteria

Book page - 835  
prob: 8.2

- ① Excellent
- ② fine
- ③ poor
- ④ good

② Objective fidelity criteria

① Mean-square

### ① Mean-square signal-to-noise ratio (SNR<sub>ms</sub>):

$$\text{SNR}_{\text{ms}} = \frac{\left[ \sum_{x=1}^M \sum_{y=1}^N f_2(x,y)^2 \right]}{\left[ \sum_{x=1}^M \sum_{y=1}^N (f_2(x,y) - f_1(x,y))^2 \right]}$$

where,  $f_1$  = original image

$f_2$  = restored image / filtered image

$M \times N$  = size of image

$x \rightarrow$  row       $y \rightarrow$  column

### ② Root mean square of SNR (RMS-SNR)

$$\text{RMS-SNR} = \sqrt{\frac{\sum_{x=1}^M \sum_{y=1}^N f_2(x,y)^2}{\sum_{x=1}^M \sum_{y=1}^N (f_2(x,y) - f_1(x,y))^2}}$$

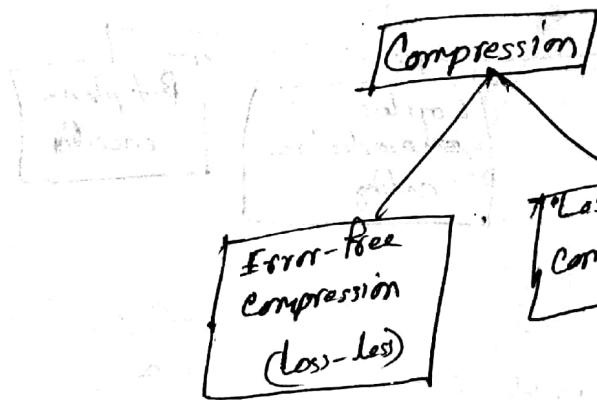
### ③ Mean square error (MSE)

$$\text{MSE} = \frac{\left[ \sum_{x=1}^M \sum_{y=1}^N (f_1(x,y) + f_2(x,y)) \right]^2}{M \times N}$$

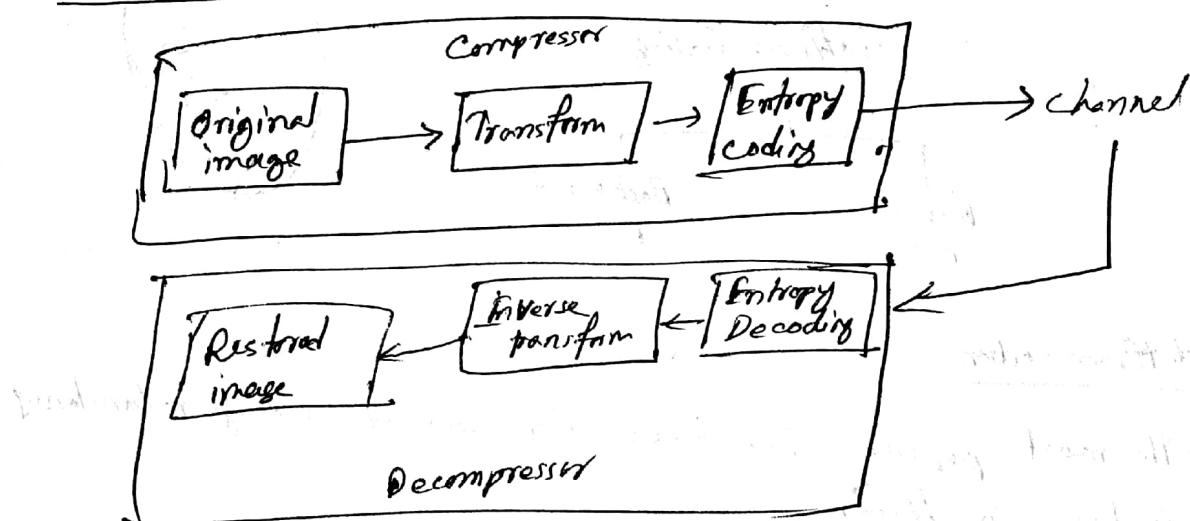
Where Root mean square error (RMSE)

$$\text{RMSE} = \sqrt{\text{MSE}}$$

## Types of image compression

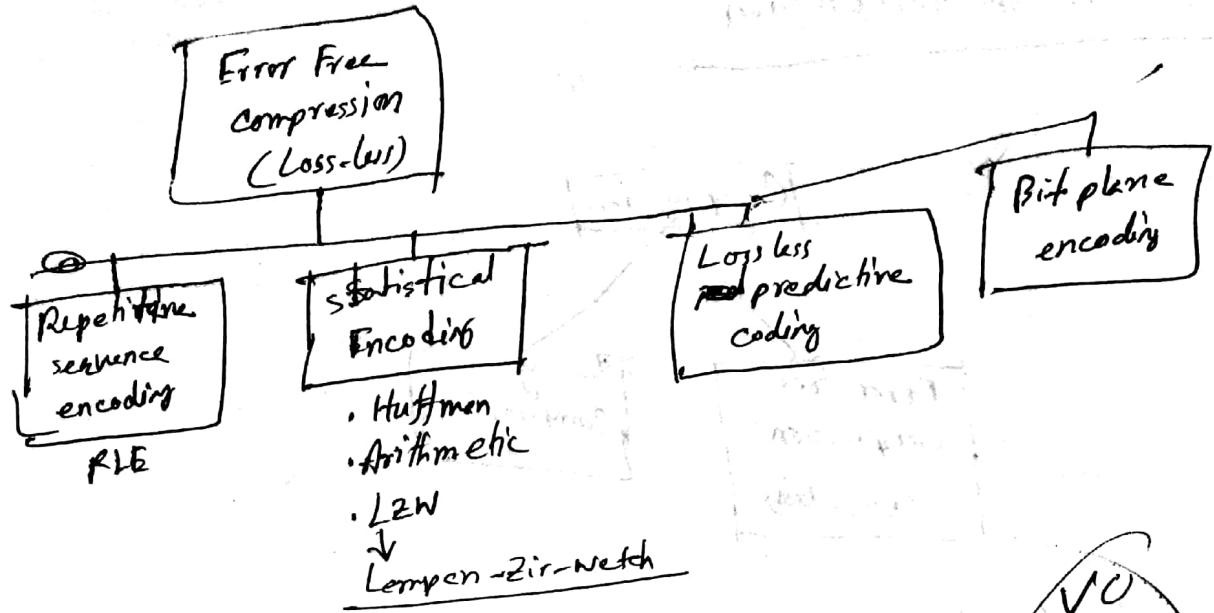


### Error-free (lossless) compression:

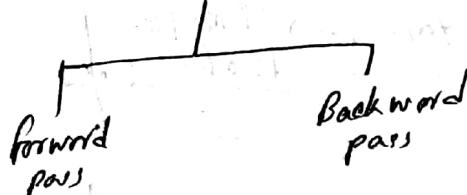


- Lossless compression are usually two-step algorithms.
- # The first step transforms the original image to some other format, in which the interpixel redundancy is reduced.
- # The second step uses an entropy encoder to remove the coding redundancy. The lossless decompressor is a perfect inverse process of the lossless compressor.

Ex: Typically, medical images can be compressed losslessly to about 50% of their original size.



### Huffman Coding



### Huffman coding:

- The most popular technique for removing coding redundancy is due to Huffman

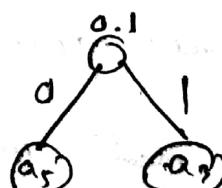
### forward pass:

- ① Sort probabilities per symbol.
- ② Combine the lowest two probabilities
- ③ Repeat step 2 until only two u remain

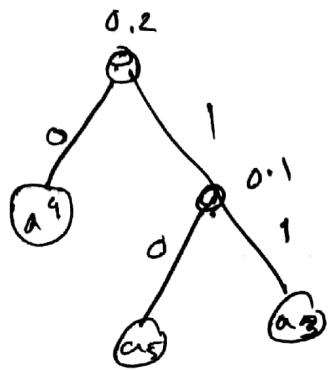
symbol:  $a_2 \ a_6 \ a_1 \ a_4 \ a_3 \ a_5$   
 probability: 0.4 0.3 0.1 0.1 0.06 0.07

### Step-01:

$a_2 \ a_6$        $a_1 \ a_4$   
 0.4 0.3      0.1 0.1

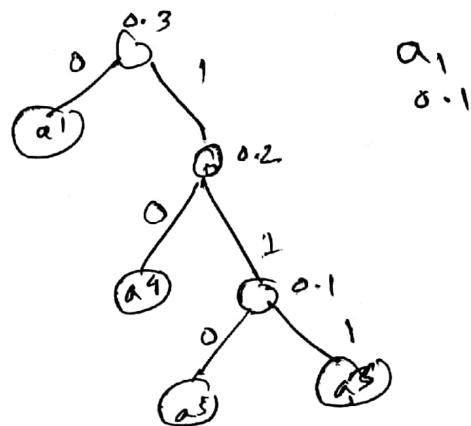


Step-02:     $a_2$      $a_4$   
              0.4    0.3



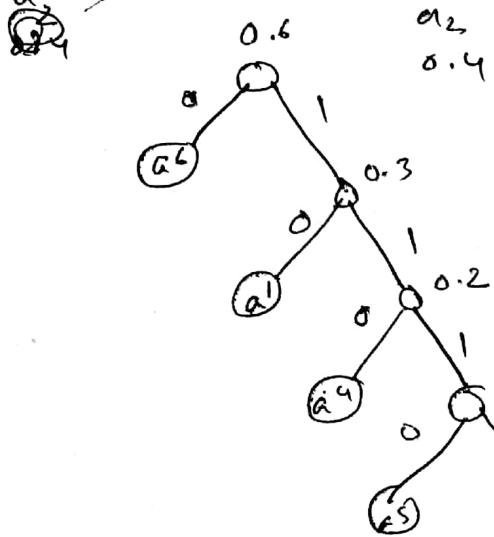
Step-03

$a_2$      $a_6$   
0.4    0.3

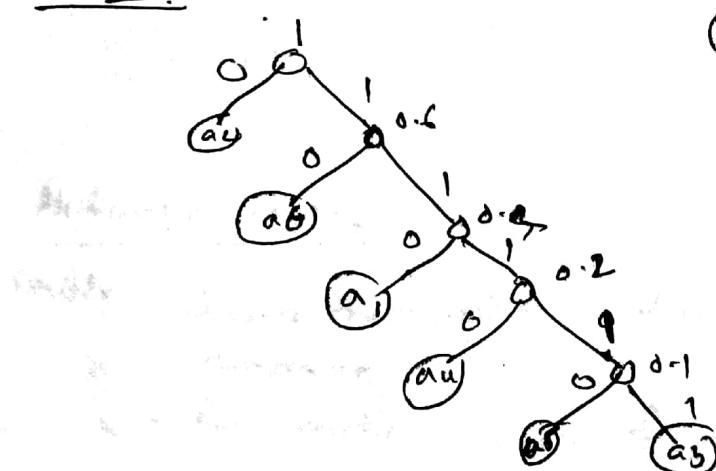


Step-04

1)



Step-05



## Run Length Encoding (RLE)

- RLE is a very simple form of data compression.
- stored as a single data value and count

Ex : AAA BBB CCC AA

Sol = 3A 2B 3C 2A

## Arithmetic Coding:

Adv - Slower than Huffman coding, but typically achieves better compression.

- An entire sequence of source symbols (MSW) is assigned a

Single arithmetic code.

→ Code word defines an integer of real numbers betn 0 and 1.

### Basic Arithmetic coding process

5 symbol message,  $a_1 a_2 a_3 a_4 a_5$  from 9 symbol source is coded.

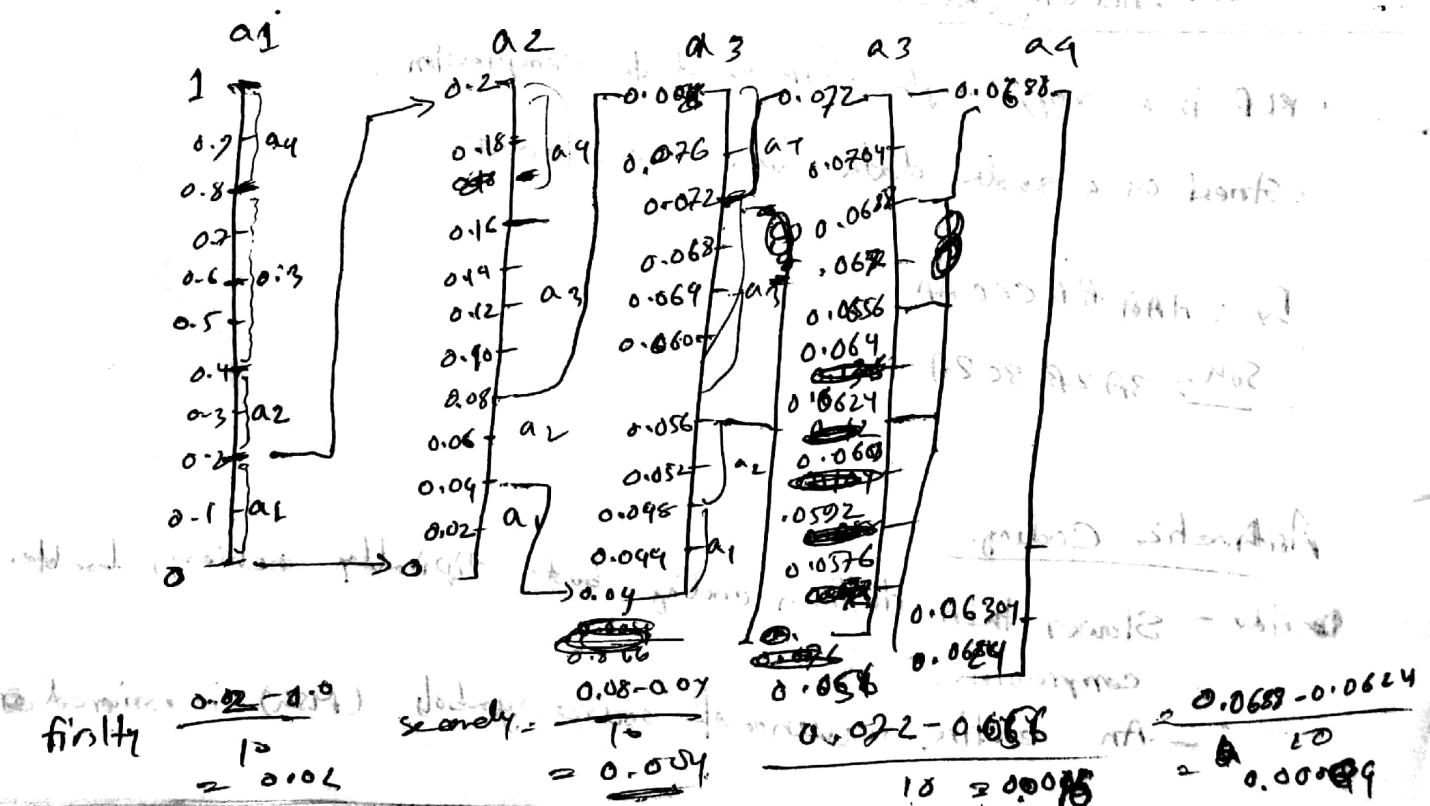
Source symbol	Probability	Initial subinterval
$a_1$	0.2	[0.0 0.2)
$a_2$	0.2	[0.2 0.4)
$a_3$	0.7	[0.4 0.8)
$a_4$	0.2	[0.8 1.0)

$[0, 1)$   
half open  
 $0 \text{ to } 1$

$$\frac{0.08 - 0.07}{10} = 0.001$$

Encoding sequence:

(0.08) with min. Abundance



$$[0.06752, 0.0688] \rightarrow 0.068$$

Therefore 3 decimal digits are used to represent the first 5

symbol message.

Problem 8.17 / 8.18

Given a 4 Symbol

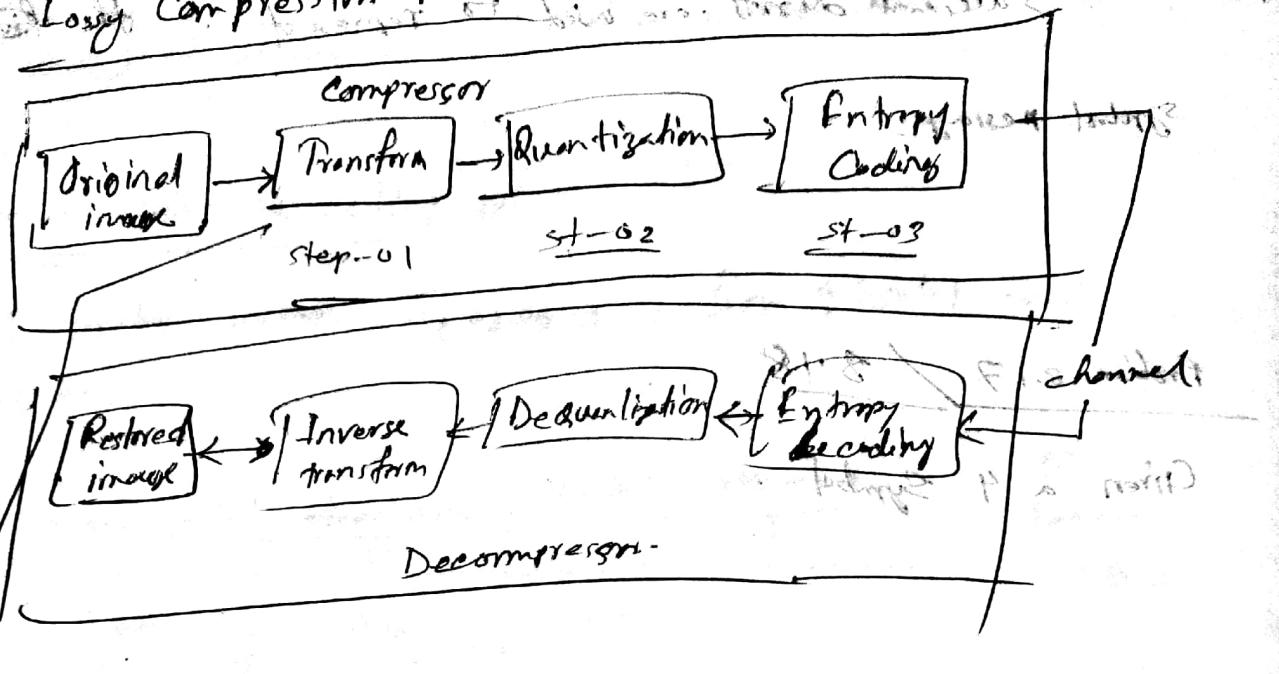
15-01-18

## Presentation topic

- 1. Lempel - Ziv - Welch (LZW) Coding
- 2. Quad tree Coding
- 3. Lossless Predictive Coding.

→ fundamentals of DCT by Anil K. Jain

## Lossy Compression Methods



removes  
interpixel  
redundancy

Significant  
information

### Lossy compression

- ① Transform Coding
- ② Block Truncation Compression
- ③ Vector Quantization "
- ④ Lossy Predictive coding
- ⑤ Wavelet Coding

① Transform Coding: Transform Coding is a general scheme

for lossy image compression. It uses a reversible  
and linear transform to decorrelate the original  
image into a set of coefficients in transform domain.

The coefficients are then quantized and coded sequentially in transform domain.

Eg: DFT, FFT, DCT, etc.

## ② Block Truncation Compression:

- BTC is a type of lossy image compression technique for gray scale images. It divides the original image into blocks and then uses a quantizer to reduce the number of gray levels in each block whilst maintaining the same mean and standard deviation.

Figure 8.6 Pg - 8 538

Image compression standard format

Percentage compression standards:

## What is JPEG?

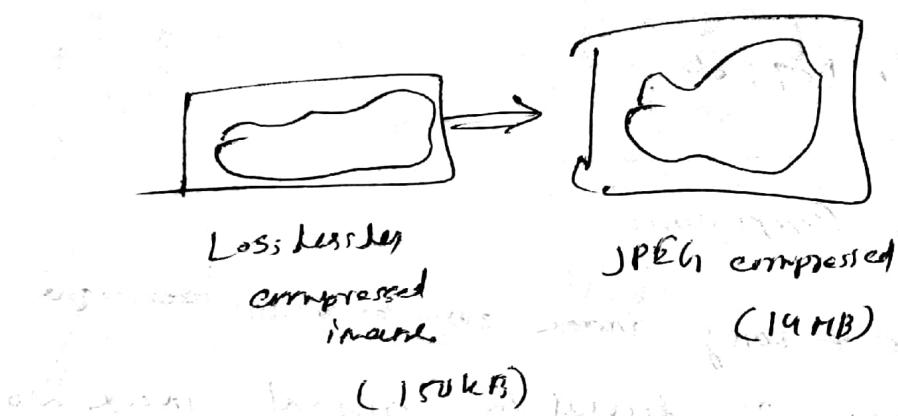
- Joint photographic Expert Group

Voted as international standard in 1992

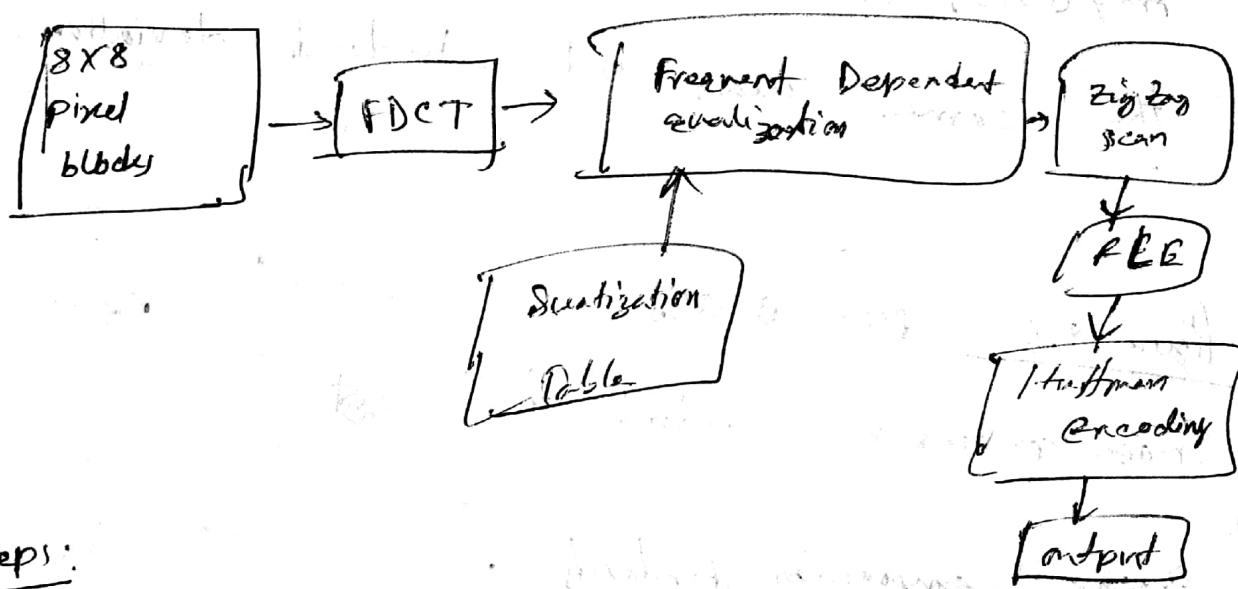
- Works with color and gray scale images

e.g. satellite, Medical

- Lossy and loss-less compression method



### JPEG Algo:



### steps:

- ① Divide image 8x8 pixel blocks .
- ② Apply 2D Fourier Discrete Cosine Transform (FDCT) transform
- ③ Apply coarse quantization for high spatial frequency component .
- ④ Compress resulting data losslessly and store .

## ④ Video compression standards.

### ① Video teleconferencing standards.

→ H.261 (Px64)

→ H.261

→ H.263 (10 to 30 kbit/s)

→ H.320 (7500 bandwidth)

### ② Multimedia standards

→ MPEG-1 (1.5 MB/s)

→ MPEG-2 (2-10 MB/s)

→ MPEG-4 (5 to 40 kbit/s)

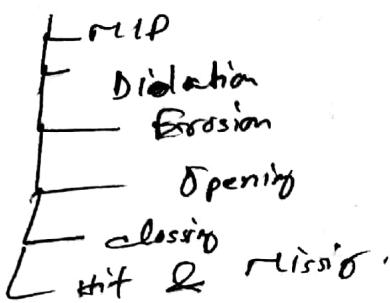
~~information theory~~ [half忘却] information theory is the basis of

- It studies the generation, storage and communication of info

- To find fundamental limits of signal processing and communication operations such as data compression

why need?

## Morphological Image processing



MID: A Branch in biology that deals with the form or shape & structure of animals and plants.

## mathematical morphology:

- As a tool for extracting image components that are useful in the representation & description of region shape.
- The language of mathematical morphology is -

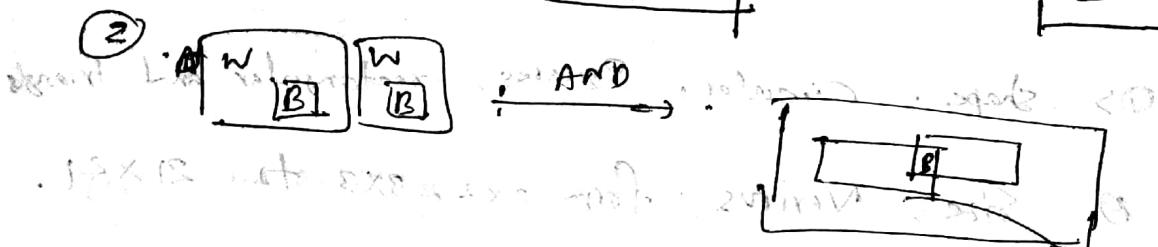
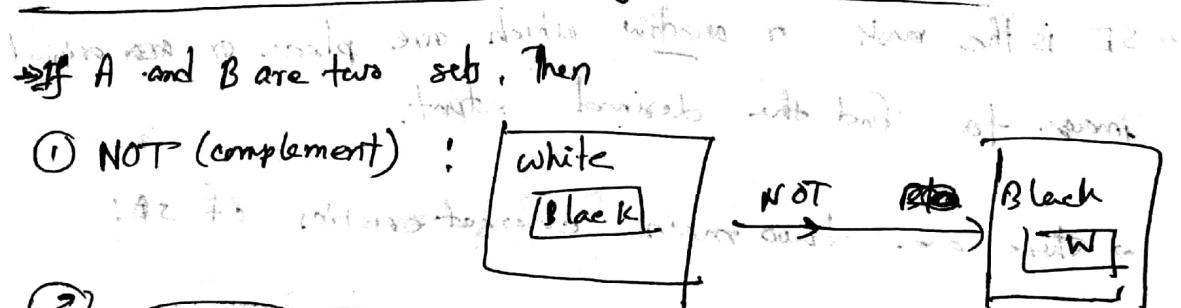
set theory:

$A \rightarrow A^C$	$\rightarrow$ Reflection: $B = \{w   w = -b, b \in B\}$
$A \rightarrow \hat{A}$	$\rightarrow$ Translation ( $A)_z = \{c   c = a + z, a \in A\}$

### • Basic concepts in set theory:

- Subset :  $A \subseteq B$
- Union :  $A \cup B$  (or  $\cup$ )
- Intersection :  $A \cap B$  (And  $\cap$ )
- Complement :  $(A)^C \rightarrow \{w | w \notin A\}$  [NOT  $\neg$ ]
- Difference :  $A - B = \{w | w \in A, w \notin B\} = A \cap B^C$

## \* Implementation of set theory by using image:



(a) And (B) only visualizing  
the common  
portion from  
both images  
(A  $\cap$  B)

## \* Application of Morphology :

① Common usages include

- Edge detection
- Noise removal

② about the • Image enhancement  
• Segmentation

③ facing shapes with region edges.

④ To count regions

⑤ To estimate sizes of regions.

- \* Structural element (SE):
- SE is the mask or window which we place over original image to find the desired output.
- There are two main characteristics of SE:

- ① Shape: Circular, Squares, Rectangular and Triangles.
- ② Size: Various form  $2 \times 2$ ,  $3 \times 3$  to  $21 \times 21$ .

MATLAB

```
Se = strel('shape', parameters)
where,
    shape
```

1	1	1	1
1	1	0	
1	1	1	

SE-01

1	1	1
1	1	0
0	1	0

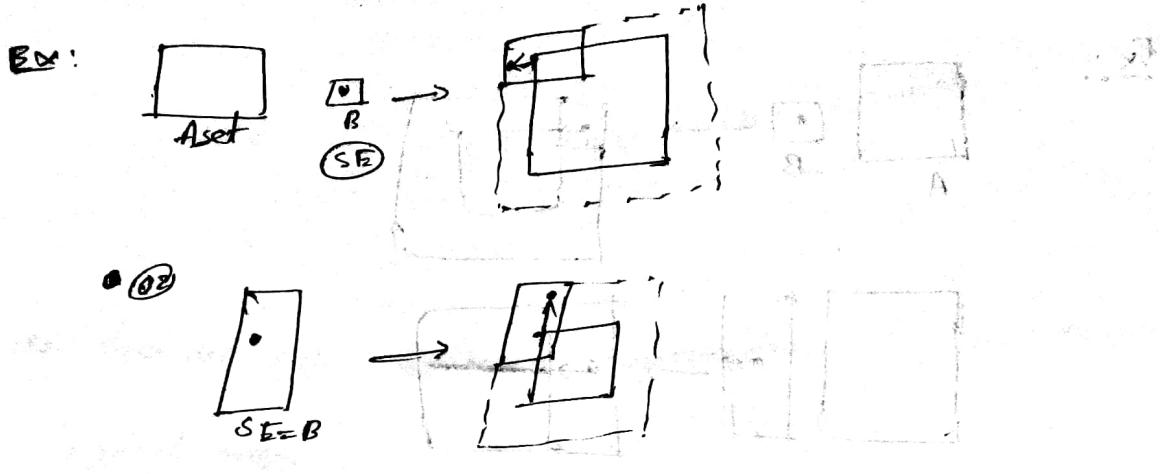
SE-02

## Basic Morphological operations:

- ① Dilation
- ② Erosion

### Dilation:

- Dilation adds pixels to the borders of objects in an image.
- Dilation is used for ~~expanding~~ expanding an element A by using SE B.



### Dilation in MATLAB:

Syntax :  $y = \text{imdilate}(A, B)$

where

simple program of Dilation :

$BW = \text{zeros}(9, 9)$

$(BW@)(4:6, 4:7) = 1$

$SE = \text{strel}('square', 3)$

$BW2 = \text{imdilate}(BW, SE)$



$A \rightarrow \text{input img}$

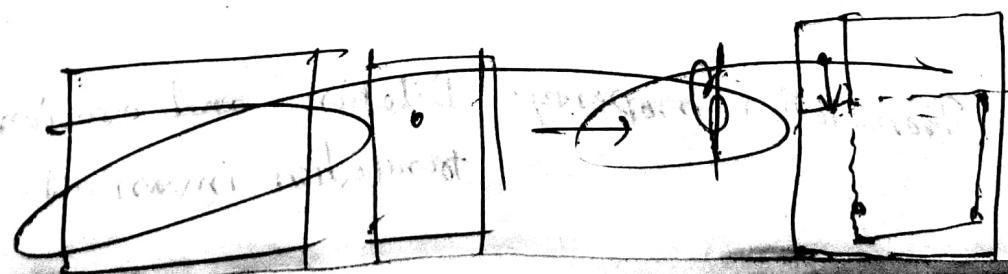
$B \rightarrow \text{SE}$

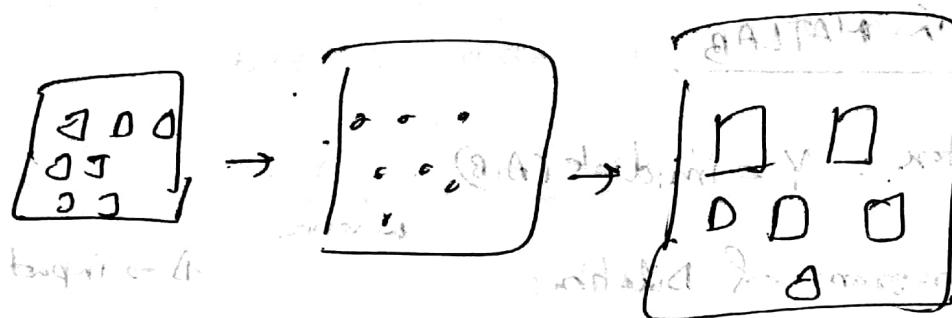
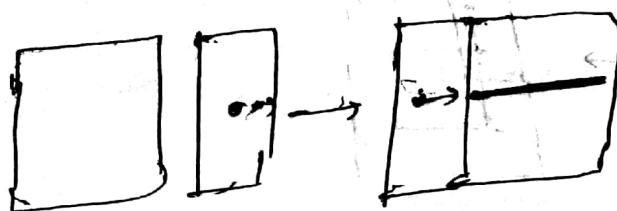
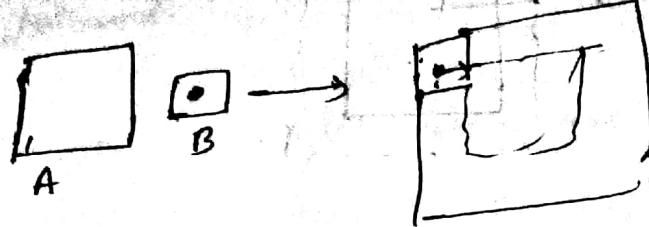
$\cdot Y - \text{Dilated img.}$

### Erosion :

- Erosion - removes pixels on object boundaries

- Erosion is used for shrinking of element A by using element B.





$$\psi = \text{imode}(A, B)$$

(or dilation by structuring element)

Properties of 'Dilation' and 'erosion' - 18/09

① Commutative property:

$$A \oplus B = B \oplus A$$

$$A \ominus B = B \ominus A$$

② Associative property:

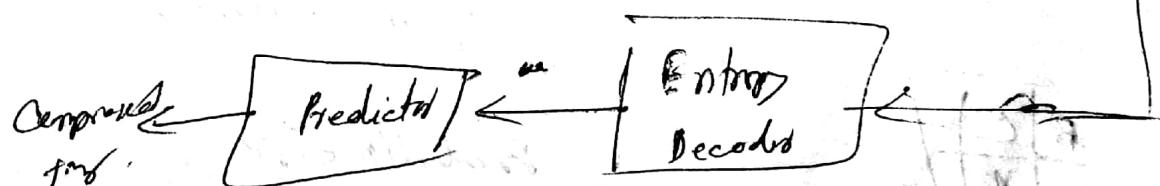
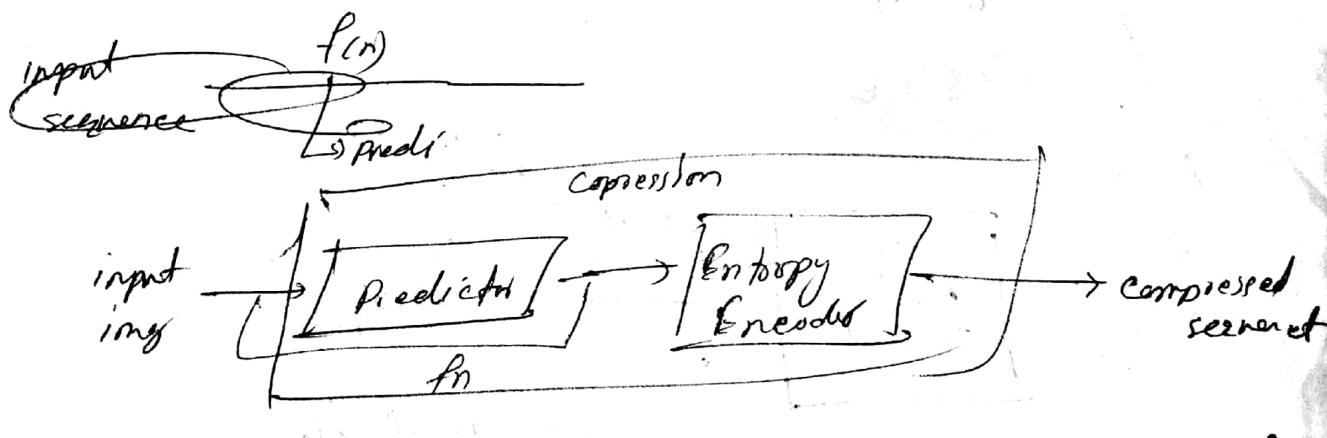
$$(A \oplus B) \oplus C = A \oplus (B \oplus C)$$

$$(A \ominus B) \ominus C \neq A \ominus (B \ominus C)$$

③ Translation property: Dilation and erosion are translation invariant.

## Lossless predictive coding

- The decoder renders an exact reproduction of the original digital image.
- Image processing & quantization use a predictive technique instead of transforming encoding technique.



## Predictors

0 No prediction

$$1 f(i,j) = f(i-1,j)$$

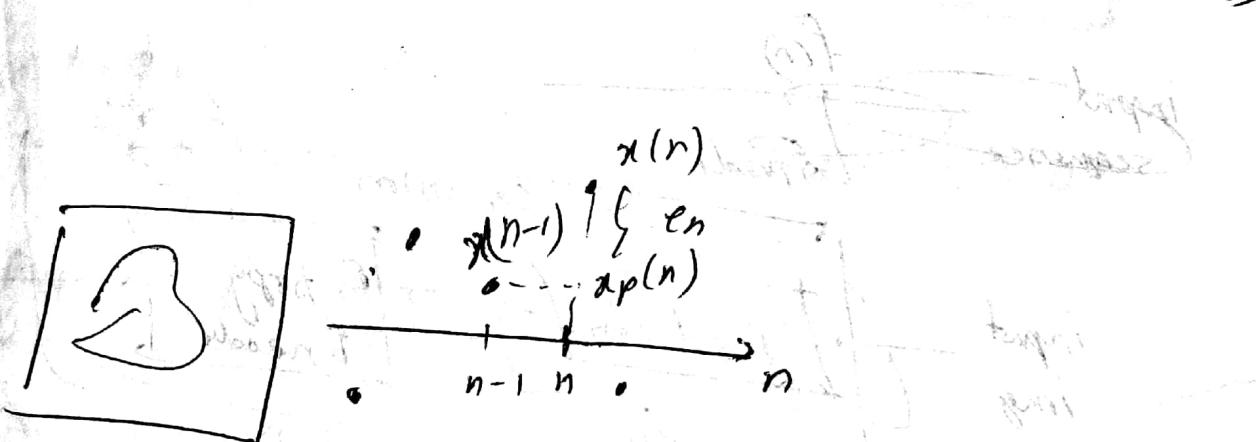
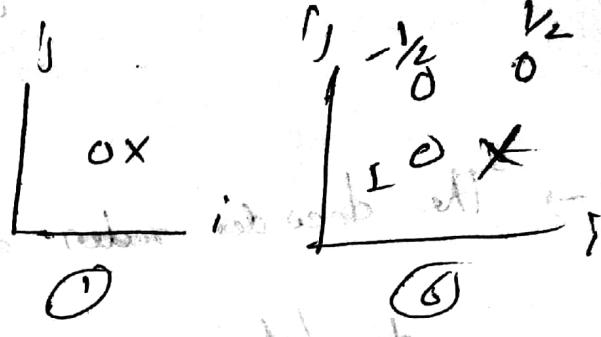
$$2 \hat{f}(i,j) = f(i,j-1)$$

$$3 \tilde{f}(i,j) = f(i-1,j-1)$$

$$4 \hat{f}(i,j) = f(i,j-1) + f(i-1,j) - f(i-1,j-1)$$

$$5 \hat{f}(i,j) = f(i,j-1) + (f(i-1,j) - f(i-1,j-1))/2$$

$$6. \hat{f}(i,j) = f(i-1,j) + (f(i,j-1) - f(i-1,j-1))/2$$



Predicted value of  $x(n)$

$$x_p(n) = x(n-1)$$

Prediction error

$$e_n = x(n) - x_p(n)$$

$$= x(n) - x(n-1)$$

Selection value / Prediction

0	No prediction
1	$x = A$
2	$x = B$
3	$x = C$
4	$x = A + B + C$
5	$x = AF(B - C)/2$
6	$x = B + (A - C)/2$
7	$x = (A + B)/2$

23-01-18

### Dilation:

- Mathematically expressed as-

$$x \oplus B = \{ p \in \mathbb{Z}^2 \mid p = x + b, x \in X, b \in B \}$$

origin      stretched pixel gray

To perform dilation there are two method.

① Substitution method

② Addition

① Sub. met

$$A = \begin{array}{|c|c|c|} \hline & 0 & 1 \\ \hline 0 & & 1 \\ \hline 1 & 0 & 0 \\ \hline 0 & 0 & 0 \\ \hline \end{array}$$

origin      Image

$$B = \begin{array}{|c|c|} \hline 1 & 0 \\ \hline 0 & 1 \\ \hline \end{array}$$

minn

Step 1 - Match the strel with the image value.

2 - if origin of strel matched then

1	1	
0	0	

0	1	0
1	0	0
0	0	0

→ No match

0	1	1	0
1	0	1	0
0	0	0	0

→ Yes  
replace it  
by the strel

0	1	1	0
1	0	0	0
0	0	0	0

→ Yes

0	1	1	1	1	1
1	0	0	0	0	0
0	0	0	0	0	0

→ Yes

0	1	1	1
1	1	0	0
0	0	0	0

0	1	1	1	1	1
1	1	1	1	0	0
0	0	0	0	0	0

0	1	1	1
1	1	1	1
0	0	1	0

## ② Vector Add:

A <sub>2</sub>	0	1	2
0	0	1	0
1	1	0	0
2	0	0	0

B	0	1
0	1	1
1	0	0

SE

Now position of 1's:

$$A_2 = \{(0,1), (1,0)\}$$

$$B = \{(0,0), (0,1)\}$$

0	1	1	1	1	1
1	1	1	1	0	0
0	0	1	0	0	0
1	1	1	1	1	1

$$(0,0) + (0,1) = (0,1)$$

$$(0,0) + (1,0) = (1,0)$$

$$(0,1) + (0,1) = (0,2)$$

$$(0,0) + (1,0) = (1,0)$$

$$A \oplus B = \{(0,1), (1,0), (0,2), (1,1)\}$$

	0	1	2
0	0	1	1
1	1	1	0
2	0	0	0

Finally we can say that:

→ Connect 'area' that are separated.

→ In gray scale image dilation increase the brightness of the object.



778

→ Segmentation & Segmentation

representation & Description.

RLE.

Shape factor (math)

Signature & skeleton - define

Convex hull -

thinnest ~~thick~~ skeleton

~~object~~

syntactic rule statistical model

decision theoretic approach (math)

pattern recognition cycle / syntactic model

supervise vs

Minimum distance classifier.

Artificial Neural net - define (layer, class)

Boundary reblocked mesh.

boundary set.

Diffusion  
reaction

Advection

Convection - boundary conditions

Convection - boundary conditions

Convection

Convection - boundary conditions

Convection - boundary conditions

Convection

Convection - boundary conditions

Convection - boundary conditions

Convection

Convection - boundary conditions

Convection - boundary conditions

Convection

Convection - boundary conditions

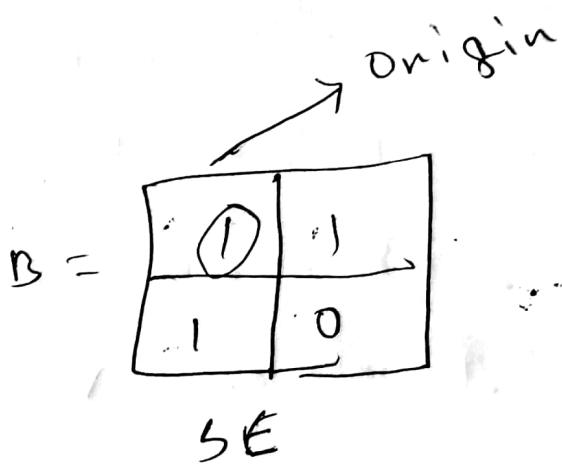
Image

Erosion

- Completely opposite of dilation
- Denoted by  $A \ominus B$

lef

1	1	1	1
1	1	0	1
0	1	1	1
0	1	0	0



Original input image

1	1	1	1
1	1	0	1
0	1	1	1
0	1	0	0

no match

0	1	1	1
1	1	0	1
0	1	1	1
0	1	0	0

after

0	1	1	1
1	1	0	1
0	1	1	1
0	1	0	0

Not  
match

0	1	0	1
1	1	0	1
0	1	0	1
0	1	0	0

last step

0	1	0	0
0	0	0	0
0	1	0	0
0	0	0	0

Output image

## Opening and closing

- can be performed by performing combinations of erosions and dilations.

Combine to keep general shape but smooth with respect to

opening — object

closing — background

opening - An erosion followed by a dilation  
closing - A dilation followed by an erosion.

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opening - Opening of set A by  $\text{SE}_B$ , denoted  $A^\circ B$ , is defined as —

$$A^\circ B = (A \ominus B) \oplus B.$$

Thus, opening A by B is a function  
of erosion A by B, followed by a

dilation of the result by B.

Closing

The closing of set A by set B,

denoted  $A \cdot B$  is defined as

$$A \cdot B = (A \oplus B) \ominus B$$

which says the closing of A by B  
is simply the dilation of A by B,

followed by the erosion of the result  
by B.

$$A^* B = (A \ominus B) \oplus B \quad (\text{opening})$$

$$A = \begin{array}{|c|c|c|c|c|c|c|} \hline & 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline \end{array}$$

$$B = \begin{array}{|c|c|c|c|} \hline 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 \\ \hline \end{array}$$

original. Tang SE

B 50 min  
but end 25% centre value change 25

$$A \ominus B = \begin{array}{|c|c|c|c|c|c|c|} \hline 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 0 & 1 & 0 & 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline \end{array}$$

$$(A \ominus B) \oplus B = \begin{array}{|c|c|c|c|c|c|c|} \hline 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ \hline \end{array}$$

## The - Hit or Miss Transformation:

- It is a morphological operation where we mainly focus on finding patterns of foreground and background object.
- For this we use two conditions.
- Hit condition:  
 → If the foreground and background pixels in the SEs exactly matches with the foreground and background pixels in the img then it is hit condition and pixel below the origin of SE is set to the foreground colour.
- Miss condition:  
 → if foreground and background pixels in element doesn't match exactly .it is miss condition .

## ② Mathematically defined as :

$$A \otimes = (A \ominus B) \cap (A^C \ominus B_2)$$

$$\begin{matrix} 1 & 1 & 1 \\ 0 & 0 & 0 \end{matrix} \xrightarrow{\text{complement}} \begin{matrix} 0 & 0 \\ 1 & 1 \end{matrix}$$

(A)

Let  $w = \begin{matrix} 1 & 1 \\ 1 & 1 \end{matrix}$  and  $B_2 = \begin{matrix} 0 & 1 \\ 1 & 0 \end{matrix}$

$$B_2 = w - B = \begin{matrix} 1 & 1 \\ 1 & 1 \end{matrix} - \begin{matrix} 0 & 1 \\ 1 & 0 \end{matrix} = \begin{matrix} 1 & 0 \\ 0 & 1 \end{matrix}$$

1	0	1
1	0	1
1	1	1

1 - represent foreground  
 0 - represent -  
 Background

Now,

$$\begin{array}{|c|c|} \hline 1 & 0 \\ \hline 0 & 1 \\ \hline \end{array} \cap \begin{array}{|c|c|} \hline 1 & 1 \\ \hline 0 & 0 \\ \hline \end{array} = \begin{array}{|c|c|} \hline 1 & 0 \\ \hline 0 & 0 \\ \hline \end{array}$$

Let,

$$A = \begin{array}{|c|c|c|c|} \hline 1 & 1 & 1 & 0 \\ \hline 1 & 1 & 0 & 1 \\ \hline 1 & 1 & 0 & 0 \\ \hline \end{array}$$

org. img

$$\begin{array}{|c|c|} \hline 1 & 0 \\ \hline 0 & 1 \\ \hline \end{array}$$

centre

$$A \ominus B = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

$$A^c = \begin{array}{|c|c|c|c|} \hline 0 & 1 & 0 & 1 \\ \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 1 & 1 \\ \hline \end{array}$$

Let,

$$w_2 = \begin{array}{|c|c|} \hline 1 & 1 \\ \hline 1 & 1 \\ \hline \end{array}$$

$$B_2 = w - B = \begin{array}{|c|c|} \hline 1 & 1 \\ \hline 1 & 1 \\ \hline \end{array} - \begin{array}{|c|c|} \hline 1 & 0 \\ \hline 0 & 1 \\ \hline \end{array} = \begin{array}{|c|c|} \hline 0 & 1 \\ \hline 1 & 0 \\ \hline \end{array}$$

$$A^c \ominus B_2 = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 0 & 1 \\ \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 1 & 1 \\ \hline \end{array} \ominus \begin{array}{|c|c|} \hline 0 & 1 \\ \hline 1 & 0 \\ \hline \end{array} = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

Therefore,

$$A \otimes B = (A \ominus B) \cap (A^c \ominus B_2)$$

$$= (A \ominus B) \cap (A^c \ominus (w - B))$$

$$= \begin{array}{|c|c|c|c|} \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array} \cap \begin{array}{|c|c|c|c|} \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array}$$

$$A \otimes B = \begin{array}{|c|c|c|c|} \hline 0 & 0 & 1 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 0 & 0 & 0 & 0 \\ \hline \end{array} \rightarrow \text{output is } \text{Hif.}$$

Ch-10 - Image segmentation (Non-trivial)Image Segmentation:

- Image segmentation is the process of partitioning a digital image into multiple segments (sets of pixels, also known as super-pixels).
- Segmentation subdivides an image into its ~~constant~~ <sup>constituent</sup> regions or objects.

Goal of segmentation:

- (1) - The purpose of image segmentation is to partition an image into meaningful regions with respect to a particular application.
- (2) - The segmentation is based on measurements taken from the image and might be grey level, colour, texture, depth or motion.
- (3) - Image segmentation is to reduce the number of columns in the input reference image and then group neighbouring pixels of similar colour together to form bounded segments.

## Types of segmentation:

### ① Discontinuity

- ① point detection
- ② line detection
- ③ Edge
- ④ Edge linking algo

### ② Similarity

- ① Local processing
- ② Regional processing
- ③ Global processing using transform
- ④ and group theory approach

### ③ Similarity

- ④ Region extraction
  - Region based approach
    - Region growing
    - Region splitting and merging
- ⑤ Pixel based approach.

### ⑥ Thresholding

Point detection:

-1	-1	-1
-1	8	-1
-1	-1	-1

A point is detected at a location where the mask is centered, if  $|R| > T$ , where  $R$  = response of the point detection mask at the point,  
 $T$  = non negative threshold

$$R = w_1 z_1 + w_2 z_2 + \dots + w_k z_k$$

$$= \sum_{k=1}^K w_k z_k$$

$z_k$  is the intensity of  $k$ th pixel

Line detection:

-1	-1	-1
2	2	2
-1	-1	-1

Horizontal  
line

-1	2	-1
-1	2	-1
-1	2	-1

Vertical  
line

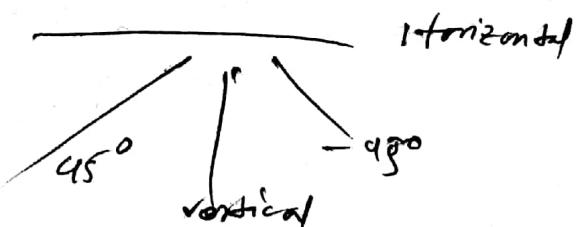
-1	-1	2
-1	2	-1
2	-1	-1

45° line

1	2	-1	1
-1	2	-1	-1
-1	-1	2	-1

-45° line

Let  $R_1, R_2, R_3, R_4$  be the responses of the mask. If at a certain point in the image  $|R_i| > |R_j|$  for all  $i < j$  then that point is said to be associated with line in the direction of mask  $i$ .



$$\begin{aligned} R_1 &> R_2 \\ R_3 &> R_4 \\ R_i &\neq R_j \end{aligned}$$

## Discontinuity.

To partition an image based on abrupt changes in intensity (such as edges).

The principal areas of interest within this category are detection of isolated points, lines and edges in an image.

⇒ Edge detection.

⇒ Edge linking:

{ Local processing.  
Regional processing.

### Local processing:

Step 01: Apply edge detection

Step 02: Analyze the characteristic of pixels in a small neighborhood ( $3 \times 3, 5 \times 5$ ) for every point in the image.

Step 03: Link the similar points.

(a) Strength of response of gradient.

$$|\alpha(x_0, y_0) - \alpha(x_0 + i, y_0 + j)| \leq E.$$

(a) The direction of the gradient vector.

$$|\alpha(x_0, y_0) - \alpha(x_0 + i, y_0 + j)| < A.$$

Local processing:

~~for~~ if the distance of a point is lesser than the threshold value, then ~~it~~ it must be connected, otherwise ~~not~~ not.

first connect two points, and find the distance of other pixels from the line and the count will be clockwise.

## # Similarity

### Region extraction

#### Region based approach

Region growing

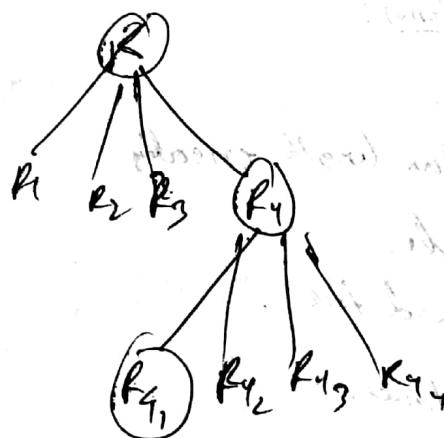
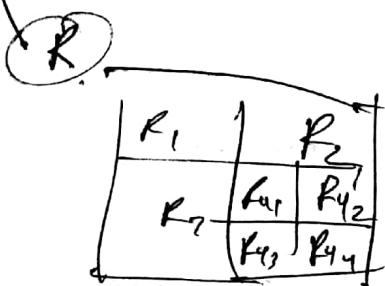
Region splitting and merging

Region growing is a procedure that groups pixels or sub regions into large regions based on predefined criteria.

Basic approach is to start with a set of seed points and from there grow regions by appending to each ~~data~~ those neighbouring pixels have properties similar to the seed.

# Region splitting and merging

- Subdivide an image initially into a set of arbitrary, disjointed regions and then merge and/or split the regions in an attempt to satisfy the conditions stated earlier.



Pixel based approach

- Thresholding
- Use of motion in segmentation

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## Chapters - II

### Representation and Description

→ Identification of inherent characteristic (features) of objects found in an image

Features → Perimeter, area,  $x_{\text{max}}$ ,  $x_{\text{min}}$ ,  $y_{\text{max}}$ ,  $y_{\text{min}}$ , shape factor, etc.



If Representation can be one of two choices:

- Represent the region in terms of external characteristics (boundary):
  - primary focus on shape characteristics.
- Represent the region in terms of its internal char (pixels of the region).
  - primary focus on regional properties. Like color, texture etc.

### Representation schemes:

① Run code:

RLE - Run length encoding

② Chain code.

③ Quad tree.

④ Signatures.

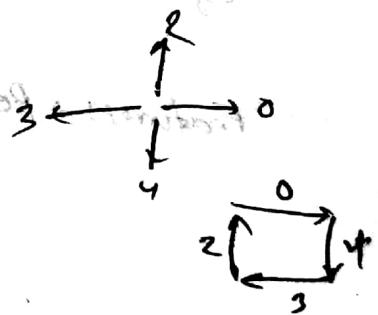
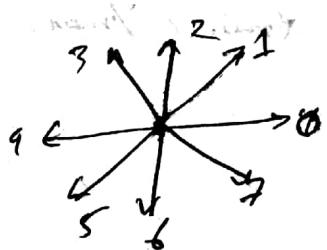
⑤ Skeleton.

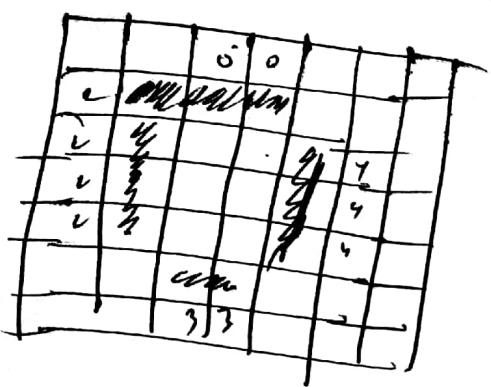
⑥ Convex hull

⑦ Thinning.



Chain code: Chain code is used to represent a boundary by a connected sequence of straight line segments of specified length and boundary





using 1st code : 0044473 2222

using 2nd code : 002665813222

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$$\begin{aligned} \text{Perimeter} ; P &= \text{even count} + \sqrt{2} \text{ odd count} \\ &= 8 + \sqrt{2} \times 3 \\ &= 8 + 3\sqrt{2} \rightarrow \end{aligned}$$

$$\text{shape factor} = (\text{perimeter})^2 / \text{area}$$

Area :

code	Area	New Y <sub>0</sub> value
0	$A = A + Y$	$Y = Y$
1	$A = A + (Y_1 \text{ or } 0)$	$Y = Y + 1$
2		
3		
4		
5		
6		
7		