Fintech Homework 6, BlockChain and CryptoCurrency

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Use the elliptic curve "secp256k1" as Bitcoin and Ethereum. Let G be the base point in the standard. Let d be the last 6 digits of your student ID number.

Module prequisities pycoin ecdsa secp256k1 --> https://pycoin.readthedocs.io/en/latest/api.html) pip3 install pycoin ecdsa

1.

In [1]:

```
import numpy as np
from pycoin.ecdsa.secp256k1 import secp256k1_generator as g

STU_ID = 922024

x, y = 4 * g
print('x = %s \ny = %s' %(hex(x), hex(y)))
```

x = 0xe493dbf1c10d80f3581e4904930b1404cc6c13900ee0758474fa94abe8c4cd13y = 0x51ed993ea0d455b75642e2098ea51448d967ae33bfbdfe40cfe97bdc47739922

2.

In [2]:

```
1 x, y = 5 * g
2 print('x = %s \ny = %s' %(hex(x), hex(y)))
```

x = 0x2f8bde4d1a07209355b4a7250a5c5128e88b84bddc619ab7cba8d569b240efe4y = 0xd8ac222636e5e3d6d4dba9dda6c9c426f788271bab0d6840dca87d3aa6ac62d6

3.

In [3]:

```
1 x, y = STU_ID * g
2 print('x = %s \ny = %s' %(hex(x), hex(y)))
```

x = 0x4eb5558d3cefbc3aa76064f8a529e1992b6a2eae9c955d0869fc284fc6216db9y = 0xb6a6a2108b1be93f13588bd3a41393ac88deb0e6f6ef9cb81ef00368cd7da92c

In [4]:

```
list operations = []
 2 STU_ID = 922024
   num = STU_ID
 5
   while num > 1:
 6
        if num & 0x1 == 1:
 7
            list_operations.append('a')
 8
            num -= 1
 9
       else:
            list operations.append('d')
10
11
            num >>= 1
12
   print('binary representation of 922024: ', bin(STU_ID))
13
    print('add %d times ' % (list_operations.count('a')))
    print('double %d times ' % (list_operations.count('d')))
15
   print('total %d times' % (len(list_operations)))
16
    print('datailed steps ', list_operations)
17
18
```

5. (My STU_ID represented in binary form does not contain continuous 1's more than 3 times in the middle part of string, so I use 961533 instead for performance comparison)

dada --> adds (no improvent for performance) dadada --> addds equivalent to 111 = (0 + 1) << 3 and then subtract 1 dadadada ---> adddds equivalent to 1111 = (0 + 1) << 4 then subtract 1

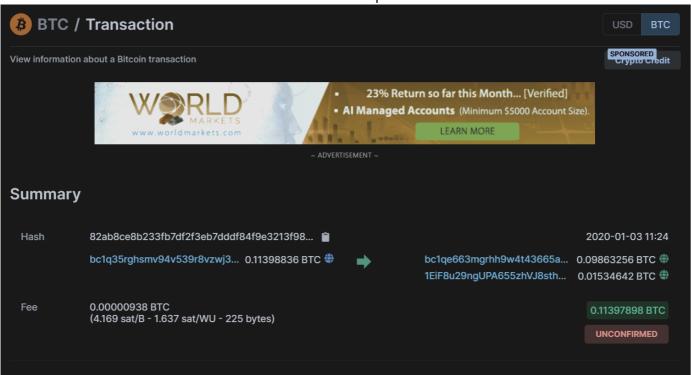
such method can be done in a greedy manner

```
In [5]:
```

```
list operations = []
   binary_str = ''
 2
 3
   num = 961533
 4
 5
   while num > 1:
 6
       if num & 0x1 == 1:
 7
           list_operations.append('a')
 8
           binary_str += '1'
 9
           num -= 1
10
       else:
           list_operations.append('d')
11
12
           binary_str += '0'
13
           num >>= 1
14
15
    print(list_operations)
16
    print('binary representation of 961533: ', bin(961533))
    print('add %d times ' % (list_operations.count('a')))
17
   print('double %d times ' % (list_operations.count('d')))
18
    print('total %d times' % (len(list_operations)))
19
   print('datailed steps ', list_operations)
20
21
22
   #-----#
23
   # build a replace list, dadada --> addds, dadadada ---> adddds
24
25
   print('\n-----\n')
26 | replace_pair = []
27
   half = len(binary_str) >> 1
   if half % 2:
28
       half -= 1
29
30
31
   # greedy approach
32
   for i in range(3, half + 1):
       replace_pair.append(('da' * i, 'a' + 'd' * i + 's'))
33
34
   str_operations = ''.join(list_operations)
35
36
    for each_pair in reversed(replace_pair):
37
       target_str, new_str = each_pair
38
       str_operations = str_operations.replace(target_str, new_str)
39
40
   list_operations = list(str_operations)
41
42
   print('binary representation of 961533: ', bin(961533))
43
   print('add %d times ' % (list_operations.count('a')))
   print('double %d times ' % (list_operations.count('d')))
44
    print('subtract %d times ' % (list_operations.count('s')))
45
46 print('total %d times' % (len(list operations)))
   print('datailed steps ', list_operations)
['a', 'd', 'a', 'd', 'a', 'd', 'a', 'd', 'a', 'd', 'a', 'd', 'a',
    'a', 'd', 'a', 'd']
```

6, 7

Take this transaction from bitcoin official website as an example.



Link of this transaction

(https://www.blockchain.com/btc/tx/82ab8ce8b233fb7df2f3eb7dddf84f9e3213f98ed48a7548051573858d6df1ab)

```
import hashlib
 2
 3
   STU_ID = 922024
 4
 5
    def exgcd(a, b, x, y):
 6
        if a == 0:
 7
           x = 0
 8
           y = 1
 9
           return x, y, b
10
       x1 = 0
11
       y1 = 0
12
13
       x1, y1, gcd = exgcd(b % a, a, x1, y1)
14
       x = y1 - (b // a) * x1
15
       y = x1
16
17
       return x, y, gcd
18
19
    def modinv(a, m):
20
       x, y, gcd = exgcd(a, m, 0, 0)
21
        assert gcd == 1, 'Modular inverse does not exist'
22
23
       return (x \% m + m) \% m
24
25
   # step referencing to ECDSA signing in blockchain ppt - 3
26
27
    def signing():
28
        print('\n-----\n')
29
       # 1. calculate msg_hashed = HASH(msg)
       msg = 'R08922024'
30
31
       hash_func = hashlib.sha256()
32
       hash_func.update(msg.encode('utf-8'))
       msg_hashed = hash_func.hexdigest()
33
34
       print('msg_hashed = ', msg_hashed)
35
36
        # 2\sim4. Random k and calculate (x1, y1) = k * G
        dA = STU_ID # use as private key
37
       QA = dA * g # QA = dA * G
38
39
       n_order = g.order()
40
       print('order of G = ', n_order)
41
       k = 2 # select k [1, n - 1], this is the ephemeral key
42
       x1, y1 = k * g
43
44
       # 5. calculate r = x1 mod n, k and n_order should be co-prime, otherwise no
45
       # modinv exists.
46
       k_modinv = modinv(k, n_order)
47
        r = x1 \% n \text{ order}
48
49
        # 6, calculate s = k ^ -1 (z + rdA) \mod n
       msg_hashed = 0x82ab8ce8b233fb7df2f3eb7dddf84f9e3213f98ed48a7548051573858d6df1ab
50
51
        s = k_modinv * (msg_hashed + r * dA) % n_order
        print('r = %s \setminus ns = %s' % (hex(r), hex(s)))
52
53
54
        return n_order, r, s, msg_hashed, QA
55
56
   # step referencing to ECDSA signing in blockchain ppt - 3
57
    def verifying(n_order, r, s, msg_hashed, QA):
58
        print('\n-----\n')
59
```

```
n_order
60
61
        if r < 1 or r > n_order:
            print('verifying failed, error code 2')
62
63
            exit(2)
        elif s < 1 or s > n_order:
64
            print('verifying failed, error code 3')
65
            exit(3)
66
67
        # calculate w = s ^ -1 \mod n
68
        w = modinv(s, n_order)
69
        u1 = msg_hashed * w % n_order
70
71
        u2 = r * w % n_order
       x1, y1 = (u1 * g + u2 * QA)
72
73
74
       if r % n_order == x1:
            print('signature verified successfully')
75
76
77
78 | n_order, r, s, msg_hashed, QA= signing()
79 verifying(n_order, r, s, msg_hashed, QA)
```

signature verified successfully