

- **N:** Natural numbers (e.g., 1, 2, 3, ...).
- **Z:** Integers (e.g., ..., -3, -2, -1, 0, 1, 2, 3, ...).
- **Q:** Rational numbers (e.g., fractions like $1/2$, $-3/4$, $7/5$, ...).
- **R:** Real numbers (e.g., integers, fractions, decimals, and irrational numbers).

Now, instead of writing “x is a natural number”, we write “ $x \in \mathbb{N}$ ” so therefore $A = \{x \mid x \text{ is a natural number that is a multiple of } 3\}$ becomes $A = \{x \mid x \in \mathbb{N} \text{ and } x \text{ is a multiple of } 3\}$

Set-Builder Notation

Write the following in set-builder notation $A = \{a, e, i, o, u\}$

Answer: $A = \{x \mid x \text{ is an English vowel}\}$

(Q) $E = \{2, 4, 8, 16, \dots\}$

Answer: $E = \{x \mid x \in \mathbb{N} \text{ and } x = 2^y, y \in \mathbb{N}, y > 0\}$

- **Equal sets** - Two sets are equal sets if and only if they contain the same elements and order doesn't matter and quantity doesn't matter. For ex $A = \{1, 2, 2, 3, 4, 5\}$ is equal set to set $B = \{1, 2, 3, 3, 4, 5\}$
- **Equivalent sets** - two sets are equivalent if they contain the same number of distinct elements. Ex-set $A = \{a, e, i, o, u\}$ is equivalent to $\{1, 2, 3, 4, 5\}$ because both contain 5 different elements
- **Subset** - The set A is a subset of the set B, denoted $A \subseteq B$, if and only if every element in A is also in B
- **Empty or Null set** - The set consisting of no elements is called the empty, or null, set, denoted by the symbol \emptyset or the empty braces $\{\}$. null set is a subset of every set.

(Q) List the subset of $\{4, 6, 7\} = \{4\}, \{6\}, \{7\}, \{4, 6\}, \{4, 7\}, \{6, 7\}, \{4, 6, 7\}, \{\}$

subsets = 2^n where n is the number of elements in the set.

- **proper subset** - The set A is a proper subset of the set B, denoted $A \subset B$, if and only if $A \subseteq B$ and $B \neq A$. $2^n - 1$ is the equation to find no of proper subset.
- **Universal subset** - The universal set U is the set of all items under consideration.

Simple statement – a sentence that is either true or false. eg: It is snowing outside.

Compound statements are combination of simple statements by the use of connectives. (and/or/not)

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we generally start with the letter p, q, and r. For conjunction (“and”), we'll use the symbol \wedge , for disjunction (“or”), we'll use the symbol \vee , and for negation (“not”), we'll use the symbol \sim .

When we use conjunction in a compound statement, the compound statement is true only if both simple statements are true whereas, when we use disjunction in a compound statement, the compound statement is true if one (or both) of the simple statements is true.

A **negation** simply turns a statement into its opposite meaning.

p : Sleep is good for you. $\sim p$: Sleep is not good for you.

NAND is "Not AND". It is the negation of a conjunction. $p \wedge q$.

NOR is "Not OR". It is the negation of a disjunction $p \vee q$

EOR is "Exclusive OR". The EOR statement is true whenever exactly one of p or q is true. $p \oplus q$

Commutative

$$A + B = B + A$$

$$A \cdot B = B \cdot A$$

Associative

$$A + (B + C) = (A + B) + C$$

$$A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

Identity

$$A + 0 = A$$

$$A \cdot 1 = A$$

Distributive Properties

$$A \cdot (B + C) = (A \cdot B) + (A \cdot C)$$

$$A + (B \cdot C) = (A + B) \cdot (A + C)$$

complement

$$A + A' = 1$$

$$A \cdot A' = 0$$

Idempotent

$$A + A = A$$

$$A \cdot A = A$$

0 and 1 Properties

$$A \cdot 0 = 0$$

$$A + 1 = 1$$