

# Diameter of MyAnimeList

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In CS224 lecture, we discussed the concept of a small world - the idea that the shortest path between any two individuals is relatively small. This has been attributed to the principle that the likelihood that two individuals know each other correlates significantly with the geographical distance between them. Effectively, this allows each step in the shortest path to travel a percentage of the remaining distance, which causes the shortest path to grow logarithmically with geographical distance, rather than linearly.

We are curious if these principles extend to less web networks, which are generally considered to be networks that don't use humans as nodes, but can use their interactions to define edges. In particular, we want to study the degrees of separation between differing Anime, using "myanimelist.net" as our dataset. MyAnimeList (MAL) provides a unique opportunity to take a single set of nodes (anime), and multiple sets of edges that we can analyze. For example, edges can be recommendations from one anime to another, or a shared cast.

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## 1. INTRODUCTION

The question

"If you chose any two people in the world at random, how many acquaintances are needed to create a chain between them?" [Kochen, 1989; Garfield 1979]

describes the small world problem in a succinct manner. Stanley Milgram's famous postcard experiment [citation??] was the first experiment that attempted to measure the degrees of separation between people in the world. To do so, he selected a broker in Boston to be a target, and had a group of individuals send letters to acquaintances, seeing if those letters could eventually be routed to the Boston broker. From the results of Milgram's experiment is derived the famous "six degrees of separation" phrase.

Although there are heavy criticisms regarding the veracity of Milgram's experiments, his work clearly demonstrates two ideas. The first is that the degrees of separation in a human social graph are far smaller than one would intuitively think, and the other is that the graph is *navigatable*, that is, there exists some algorithm that can

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traverse from any node  $s$  to destination node  $t$  only knowing the edges of the current node in  $O(\log(N)^\beta)$  time.

The intuition for both of these properties derives from the idea that the likelihood two people know each other is strongly correlated with their geographical distance. That is, in general, as long as the next hop is geographically closer, then our new node has a shorter path to the destination node than our current one. However, this isn't sufficient to explain the results of Milgram's experiments. For example, if every individual knows every other individual within a one mile radius, but knows no one else, then the shortest path between two nodes eight hundred miles apart requires eight hundred hops – order of magnitudes greater than what was observed in Milgram's study. Thus the second requirement is that with high probability, our current node will be connected to another node whose distance to the destination is no more than  $\alpha \ll 1$  times the distance from our current node to the destination node.

- To the best of our knowledge, the MMSN protocol is the first multifrequency MAC protocol especially designed for WSNs, in which each device is equipped with a single radio transceiver and the MAC layer packet size is very small.
- Instead of using pairwise RTS/CTS frequency negotiation [Adya 2001, Culler 2001; Tzamaloukas 2001; Zhou 2006], we propose lightweight frequency assignments, which are good choices for many deployed comparatively static WSNs.
- We develop new toggle transmission and snooping techniques to enable a single radio transceiver in a sensor device to achieve scalable performance, avoiding the non-scalable “one control channel + multiple data channels” design [Natarajan 2001].

## 2. MMSN PROTOCOL

### 2.1. Frequency Assignment

We propose a suboptimal distribution to be used by each node, which is easy to compute and does not depend on the number of competing nodes. A natural candidate is an increasing geometric sequence, in which

$$P(t) = \frac{b^{\frac{t+1}{T+1}} - b^{\frac{t}{T+1}}}{b - 1}, \quad (1)$$

where  $t = 0, \dots, T$ , and  $b$  is a number greater than 1.

In our algorithm, we use the suboptimal approach for simplicity and generality. We need to make the distribution of the selected back-off time slice at each node conform to what is shown in Equation (1). It is implemented as follows: First, a random variable  $\alpha$  with a uniform distribution within the interval  $(0, 1)$  is generated on each node, then time slice  $i$  is selected according to the following equation:

$$i = \lfloor (T + 1) \log_b[\alpha(b - 1) + 1] \rfloor.$$

It can be easily proven that the distribution of  $i$  conforms to Equation (1).

So protocols [Bahl 2002, Culler 2001, Zhou 2006, Adya 2001, Culler 2001; Tzamaloukas-01; Akyildiz-01] that use RTS/CTS controls<sup>1</sup> for frequency negotiation and reservation are not suitable for WSN applications, even though they exhibit good performance in general wireless ad hoc networks.

**2.1.1. Exclusive Frequency Assignment.** In exclusive frequency assignment, nodes first exchange their IDs among two communication hops so that each node knows its two-

<sup>1</sup>RTS/CTS controls are required to be implemented by 802.11-compliant devices. They can be used as an optional mechanism to avoid Hidden Terminal Problems in the 802.11 standard and protocols based on those similar to [Akyildiz 2001] and [Adya 2001].

**ALGORITHM 1:** Frequency Number Computation

**Input:** Node  $\alpha$ 's ID ( $ID_\alpha$ ), and node  $\alpha$ 's neighbors' IDs within two communication hops.

**Output:** The frequency number ( $FreNum_\alpha$ ) node  $\alpha$  gets assigned.

$index = 0$ ;  $FreNum_\alpha = -1$ ;

**repeat**

$Rnd_\alpha = \text{Random}(ID_\alpha, index)$ ;

$Found = \text{TRUE}$ ;

**for** each node  $\beta$  in  $\alpha$ 's two communication hops **do**

$Rnd_\beta = \text{Random}(ID_\beta, index)$ ;

**if** ( $Rnd_\alpha < Rnd_\beta$ ) or ( $Rnd_\alpha == Rnd_\beta$  and  $ID_\alpha < ID_\beta$ );

**then**

$Found = \text{FALSE}$ ; **break**;

**end**

**end**

**if**  $Found$  **then**

$FreNum_\alpha = index$ ;

**else**

$index++$ ;

**end**

**until**  $FreNum_\alpha > -1$ ;

hop neighbors' IDs. In the second broadcast, each node beacons all neighbors' IDs it has collected during the first broadcast period.

*Eavesdropping.* Even though the even selection scheme leads to even sharing of available frequencies among any two-hop neighborhood, it involves a number of two-hop broadcasts. To reduce the communication cost, we propose a lightweight eavesdropping scheme.

## 2.2. Basic Notations

As Algorithm 1 states, for each frequency number, each node calculates a random number ( $Rnd_\alpha$ ) for itself and a random number ( $Rnd_\beta$ ) for each of its two-hop neighbors with the same pseudorandom number generator.

Bus masters are divided into two disjoint sets,  $\mathcal{M}_{RT}$  and  $\mathcal{M}_{NRT}$ .

*RT Masters.*  $\mathcal{M}_{RT} = \{\vec{m}_1, \dots, \vec{m}_n\}$  denotes the  $n$  RT masters issuing real-time constrained requests. To model the current request issued by an  $\vec{m}_i$  in  $\mathcal{M}_{RT}$ , three parameters—the recurrence time ( $r_i$ ), the service cycle ( $c_i$ ), and the relative deadline ( $d_i$ )—are used, with their relationships.

*NRT Masters.*  $\mathcal{M}_{NRT} = \{\vec{m}_{n+1}, \dots, \vec{m}_{n+m}\}$  is a set of  $m$  masters issuing nonreal-time constrained requests. In our model, each  $\vec{m}_j$  in  $\mathcal{M}_{NRT}$  needs only one parameter, the service cycle, to model the current request it issues.

Here, a question may arise, since each node has a global ID. Why don't we just map nodes' IDs within two hops into a group of frequency numbers and assign those numbers to all nodes within two hops?

## 3. SIMULATOR

If the model checker requests successors of a state which are not created yet, the state space uses the simulator to create the successors on-the-fly. To create successor states the simulator conducts the following steps.

- (1) Load state into microcontroller model.
- (2) Determine assignments needed for resolving nondeterminism.

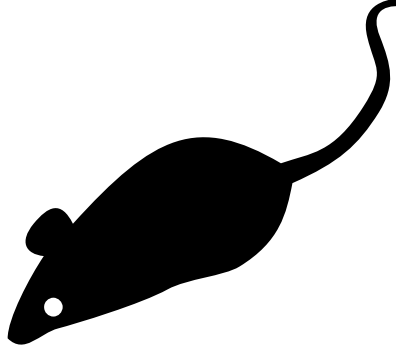


Fig. 1. Code before preprocessing.

- (3) For each assignment.
  - (a) either call interrupt handler or simulate effect of next instruction, or
  - (b) evaluate truth values of atomic propositions.
- (4) Return resulting states.

Figure 1 shows a typical microcontroller C program that controls an automotive power window lift. The program is one of the programs used in the case study described in Section 3. At first sight, the programs looks like an ANSI C program. It contains function calls, assignments, if clauses, and while loops.

### 3.1. Problem Formulation

The objective of variable coalescence-based offset assignment is to find both the coalescence scheme and the MWPC on the coalesced graph. We start with a few definitions and lemmas for variable coalescence.

*Definition 3.1 (Coalesced Node (C-Node)).* A C-node is a set of live ranges (webs) in the AG or IG that are coalesced. Nodes within the same C-node cannot interfere with each other on the IG. Before any coalescing is done, each live range is a C-node by itself.

*Definition 3.2 (C-AG (Coalesced Access Graph)).* The C-AG is the access graph after node coalescence, which is composed of all C-nodes and C-edges.

**LEMMA 3.3.** *The C-MWPC problem is NP-complete.*

**PROOF.** C-MWPC can be easily reduced to the MWPC problem assuming a coalescence graph without any edge or a fully connected interference graph. Therefore, each C-node is an uncoalesced live range after value separation and C-PC is equivalent to PC. A fully connected interference graph is made possible when all live ranges interfere with each other. Thus, the C-MWPC problem is NP-complete.  $\square$

**LEMMA 3.4 (LEMMA SUBHEAD).** *The solution to the C-MWPC problem is no worse than the solution to the MWPC.*

**PROOF.** Simply, any solution to the MWPC is also a solution to the C-MWPC. But some solutions to C-MWPC may not apply to the MWPC (if any coalescing were made).  $\square$

Table I. Simulation Configuration

TERRAIN <sup>a</sup>	(200m×200m) Square
Node Number	289
Node Placement	Uniform
Application	Many-to-Many/Gossip CBR Streams
Payload Size	32 bytes
Routing Layer	GF
MAC Layer	CSMA/MMSN
Radio Layer	RADIO-ACCNOISE
Radio Bandwidth	250Kbps
Radio Range	20m–45m

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<sup>a</sup>This is a table footnote. This is a table footnote. This is a table footnote.

#### 4. PERFORMANCE EVALUATION

During all the experiments, the Geographic Forwarding (GF) [Akyildiz 2001] routing protocol is used. GF exploits geographic information of nodes and conducts local data-forwarding to achieve end-to-end routing. Our simulation is configured according to the settings in Table I. Each run lasts for 2 minutes and repeated 100 times. For each data value we present in the results, we also give its 90% confidence interval.

#### 5. CONCLUSIONS

In this article, we develop the first multifrequency MAC protocol for WSN applications in which each device adopts a single radio transceiver. The different MAC design requirements for WSNs and general wireless ad-hoc networks are compared, and a complete WSN multifrequency MAC design (MMSN) is put forth. During the MMSN design, we analyze and evaluate different choices for frequency assignments and also discuss the nonuniform back-off algorithms for the slotted media access design.

#### 6. TYPICAL REFERENCES IN NEW ACM REFERENCE FORMAT

A paginated journal article [Abril and Plant 2007], an enumerated journal article [Cohen et al. 2007], a reference to an entire issue [Cohen 1996], a monograph (whole book) [Kosiur 2001], a monograph/whole book in a series (see 2a in spec. document) [Harel 1979], a divisible-book such as an anthology or compilation [Editor 2007] followed by the same example, however we only output the series if the volume number is given [Editor 2008] (so Editor00a's series should NOT be present since it has no vol. no.), a chapter in a divisible book [Spector 1990], a chapter in a divisible book in a series [Douglass et al. 1998], a multi-volume work as book [Knuth 1997], an article in a proceedings (of a conference, symposium, workshop for example) (paginated proceedings article) [Andler 1979], a proceedings article with all possible elements [Smith 2010], an example of an enumerated proceedings article [Gundy et al. 2007], an informally published work [Harel 1978], a doctoral dissertation [Clarkson 1985], a master's thesis: [Anisi 2003], an online document / world wide web resource [Thornburg 2001], [Ablamowicz and Fauser 2007], [Poker-Edge.Com 2006], a video game (Case 1) [Obama 2008] and (Case 2) [Novak 2003] and [Lee 2005] and (Case 3) a patent [Scientist 2009], work accepted for publication [Rous 2008], 'YYYYb'-test for prolific author [Saeedi et al. 2010a] and [Saeedi et al. 2010b]. Other cites might contain 'duplicate' DOI and URLs (some SIAM articles) [Kirschmer and Voight 2010]. Boris / Barbara Beeton: multi-volume works as books [Hörmander 1985b] and [Hörmander 1985a].

## APPENDIX

In this appendix, we measure the channel switching time of Micaz [CROSSBOW] sensor devices. In our experiments, one mote alternately switches between Channels 11 and 12. Every time after the node switches to a channel, it sends out a packet immediately and then changes to a new channel as soon as the transmission is finished. We measure the number of packets the test mote can send in 10 seconds, denoted as  $N_1$ . In contrast, we also measure the same value of the test mote without switching channels, denoted as  $N_2$ . We calculate the channel-switching time  $s$  as

$$s = \frac{10}{N_1} - \frac{10}{N_2}.$$

By repeating the experiments 100 times, we get the average channel-switching time of Micaz motes:  $24.3\mu s$ .

## ELECTRONIC APPENDIX

The electronic appendix for this article can be accessed in the ACM Digital Library.

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## Online Appendix to: Diameter of MyAnimeList

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### A. THIS IS AN EXAMPLE OF APPENDIX SECTION HEAD

Channel-switching time is measured as the time length it takes for motes to successfully switch from one channel to another. This parameter impacts the maximum network throughput, because motes cannot receive or send any packet during this period of time, and it also affects the efficiency of toggle snooping in MMSN, where motes need to sense through channels rapidly.

By repeating experiments 100 times, we get the average channel-switching time of Micaz motes:  $24.3 \mu\text{s}$ . We then conduct the same experiments with different Micaz motes, as well as experiments with the transmitter switching from Channel 11 to other channels. In both scenarios, the channel-switching time does not have obvious changes. (In our experiments, all values are in the range of  $23.6 \mu\text{s}$  to  $24.9 \mu\text{s}$ .)

### B. APPENDIX SECTION HEAD

The primary consumer of energy in WSNs is idle listening. The key to reduce idle listening is executing low duty-cycle on nodes. Two primary approaches are considered in controlling duty-cycles in the MAC layer.