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Task 1:

a. M->Sensor in Maine; Mn->compliment

S->Sensor in Sahara; Sn->compliment

T->temp>=80; Tn->compliment

$$P(Tn) = P(M) * P(Hn|M) + P(S) * P(Hn|S) = .05 * .8 + .95 * .1 = .135$$

$$P(M|Tn) = [P(M) * P(Tn|M)] / P(Tn) = [.05 * .8] / .135 = .2963$$

b. E1->first email indicates high under 80 degrees

E2->second email indicates high under 80 degrees

$$P(E2|E1, M) = P(Hn|M) = 1 - .2 = .8$$

$$P(E2|E1, S) = P(Hn|S) = 1 - .9 = .1$$

Using Product Rule, Chained Version

$$P(E2|E1) = P(M|T) * P(E2|E1, M) + P(S|Tn) * P(E2|E1, S)$$

$$= (.2963 * .8) + (1 - .2963) * (.1) = .3074$$

c. E3->third email indicates high under 80*

$$P(E3 | E1, E2) = P(E3) * P(E1, E2) = .6828 * .3074 = .20989$$

Task 2:

The 2 Conditions for a function to be valid are

- The probability of any event cannot be less than 0 or greater than 1.
- The sum of probabilities of all possible atomic events is 1.

In this case only 2 of the probabilities are given, adding up to .9. The individual values of each of the probabilities also stay under 1. Given this, we can conclude that it is possibly a function, but we can't be certain until P(C) and P(D) are given.

Task 3:

The 2 Conditions for a function to be valid are

- The probability of any event cannot be less than 0 or greater than 1.
- The sum of probabilities of all possible atomic events is 1. We are given $P(x) = .3$ if $0 \leq x \leq 10$.

Based on this information we can integrate the function to find the final value. When integrating .3 from 0 to 10, we get a value of 3, which exceeds the limit of 1. From here we can conclude that P(x) is not a function.

Task 4:

$$p(a) = p(a|r) * p(r) + p(a|b) * p(b) = .25 * .4 + .75 * .6 = .55$$

$$p(o) = 1 - p(a) = 1 - .546 = .45$$

Task 5:

$$\text{Classification accuracy} = .4483$$

FINAL GRADE: 85%

COMMENTS:

Task 1: part c is incorrect, -5 points task 4: we want the total probability that the classifier is correct. so the probability that it is correct when the fruit is an orange + the probability that it is correct when the fruit is an apple