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FINAL GRADE: 100%

COMMENTS:

“task 3: calculation errors -1 point (the info gain calculation is incorrect)”

Task 1:

Each run ~10 times

decision_tree.py pendigits_training pendigits_test optimized 50 = .8393(1 minute)

decision_tree.py pendigits_training pendigits_test 1 50 = .6933 - .7573(5 Seconds)

decision_tree.py pendigits_training pendigits_test 3 50 = .8209 – 8789(1 minute)

Task 2:

a) $H(0.8, 0.2) = -0.8\log_2(0.8) - 0.2\log_2(0.2) = .7219$

b) $\text{Entropy}(\text{Wait}) = -[(20/35) * \log_2(20/35) + (15/35) * \log_2(15/35)] = .4134$

$\text{Entropy}(\text{NW}) = -[(60/65) * \log_2(60/65) + (5/65) * \log_2(5/65)] = .2058$

$\text{Weight}(\text{W}) = 35 / 100$

$\text{Weight}(\text{NW}) = 65 / 100$

$\text{Gain} = \text{Initial Entropy (Entropy(A))} - [\text{Weight}(\text{W}) * \text{Entropy}(\text{W}) + \text{Weight}(\text{NW}) * \text{Entropy}(\text{NW})]$
 $= 0.44354$

c) $\text{Gain} = -0.3291$

d) Node F, Will Wait

e) Node E, Will Not Wait

Task 3:

$A1 = x, x, x$

$A2 = x, y, y, y$

$A3 = x, y, y$

$H(E) = 1 \rightarrow \text{even amount of 'X' and 'Y'}$

$H((A1/10), (A2/10), (A3/10)) = H(E) - [(3/10) * (1.0 * \log_2(1) + 0 * \log_2(0)) +$
 $(4/10) * (-0.25 * \log_2(0.25) - 0.75 * \log_2(0.75)) +$

$$(3/10*(-0.33*\log_2(0.33) - 0.67*(\log_2(0.67))) = \text{Gain_A}$$

$$H(E) - (0 + (.32451) + (-.04221))$$

$$1 - .2823 = .7177$$

$$B1 = x, y, y, y$$

$$B2 = x, x, x, y$$

$$B3 = x, y$$

$$H(E) = 1 \rightarrow \text{even amount of 'X' and 'Y'}$$

$$H((B1/10), (B2/10), (B3/10)) = H(E) - [(4/10)*(-.25 * \log_2(.25) - .75*\log_2(.75)) +$$

$$(4/10)*(-0.75*\log_2(0.75) - 0.25*\log_2(0.25)) +$$

$$(2/10*(-0.5*\log_2(0.5) - 0.5*\log_2(0.5))] = \text{Gain_B}$$

$$H(E) - ((.32451) + (.32451) + .2)$$

$$1 - .84902 = .15098$$

$$C1 = x, y, y, y, y$$

$$C2 = x, x, x, y$$

$$C3 = x$$

$$H(E) = 1 \rightarrow \text{even amount of 'X' and 'Y'}$$

$$H((C1/10), (C2/10), (C3/10)) = H(E) - [(5/10)*(-.2 * \log_2(.2) - .8*\log_2(.80) +$$

$$(4/10)*(-0.75\log_2(0.75) - 0.25\log_2(0.25)) +$$

$$(1/10*(-1.0\log_2(1.0) - 0(\log_2(0))) = \text{Gain_CH(E)} - ((.36096) + (.32451) + (0))$$

$$1 - .68547 = .31453$$

A is the highest so choose it

Task 4:

$$\begin{aligned} \text{a. } H(A, B, C, D)_{\max} &= -(250/1000)\log_2(250/1000) - (250/1000)\log_2(250/1000) - \\ &(250/1000)\log_2(250/1000) - (250/1000)\log_2(250/1000) = 2 \end{aligned}$$

$$\begin{aligned} \text{b. } H(A, B, C, D)_{\min} &= -(1000/1000)\log_2(1000/1000) - (0/1000)\log_2(0/1000) - \\ &(0/1000)\log_2(0/1000) - (0/1000)\log_2(0/1000) = 0 \end{aligned}$$

Task 5:

If your classifier correctly predicts if the home team will win 28% of the time, using the contrapositive, it also means that it incorrectly predicts if the “away” team will lose 72% of the time.

By switching the classifier to predict if the “away” team will lose, and then outputting the opposite of the given answer, you essentially have a classifier that can predict if the “home” team will win 72% of the time.