Assignment 2

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1. Data Wrangling

1.1 (Q1)

```
hSF <- Hawks %>% filter(Species=="RT", Weight>=1000) %>% select("Wing", "Weight", "Tail") print(head(hSF, 10))
```

```
##
     Wing Weight Tail
           1090 230
## 1
     412
## 2
      412
           1210 210
## 3
      405
           1120 238
## 4
      393
           1010 222
## 5
      371
           1010 217
## 6
      390
           1120 213
## 7
      416
           1170 243
## 8
      436
            1390 232
## 9
      418
           1150 238
## 10 396
           1010 227
```

1.1 (Q2)

there are 3 variables in hSF, show it how many columns it has

There are 4 examples nrow(), dim(), length(rownames()), summary() or str()

obervations: print(nrow(hSF)) 398

dim(hSF) 398 3 dim(hSF)[1] 398 dim(hSF)[2] 3

length(rownames(hSF)) 398

summary(hSF) overview of the data, str(hSF) all the data and the number of rows

1.2 (Q1)

```
sorthSF <- hSF %>% arrange(Wing)
print(sorthSF %>% head(10))
```

```
##
       Wing Weight Tail
       37.2
               1180
## 1
                     210
      111.0
## 2
               1340
                     226
      199.0
               1290
                     222
## 3
      241.0
               1320
                     235
## 4
## 5
      262.0
               1020
                     200
## 6
      277.0
               1500
                     207
               1000
## 7
      330.0
                     220
## 8
      331.0
               1055
                     210
## 9
      345.0
               1000
                     200
## 10 350.0
               1115
                     199
```

1.3 (Q1)

```
species_code <- c("CH", "RT", "SS")
species_name_full <- c("Cooper's", "Red-tailed", "Sharp-shinned")
hawkSpeciesNameCodes <- data.frame(species_code, species_name_full)
print(hawkSpeciesNameCodes)</pre>
```

1.3 (Q2)

```
hawksFullName <- hawkSpeciesNameCodes %>% rename(Species = species_code)
hawksFullName <- left_join(Hawks, hawksFullName) %>% select(-Species) %>% rename(Species = species_name_full)
```

```
## Joining with `by = join_by(Species)`
```

```
print(hawksFullName %>% head(5))
```

```
Month Day Year CaptureTime ReleaseTime BandNumber Age Sex Wing Weight Culmen
##
                                                877-76317
                                                                                   25.7
## 1
         9
             19 1992
                            13:30
                                                              Ι
                                                                     385
                                                                             920
                                                                             930
         9
            22 1992
                            10:30
                                                877-76318
                                                              Ι
                                                                     376
## 2
                                                                                     NA
         9
            23 1992
                            12:45
                                                877-76319
                                                              Ι
                                                                     381
                                                                             990
                                                                                   26.7
## 3
## 4
         9
            23 1992
                            10:50
                                                745-49508
                                                              Ι
                                                                  F
                                                                     265
                                                                             470
                                                                                   18.7
                                                                             170
## 5
         9
            27 1992
                            11:15
                                                1253-98801
                                                              Ι
                                                                     205
                                                                                   12.5
     Hallux Tail StandardTail Tarsus WingPitFat KeelFat Crop
##
                                                                        Species
## 1
       30.1
             219
                             NA
                                    NA
                                                NA
                                                         NA
                                                                     Red-tailed
                                                              NA
## 2
         NA
             221
                             NA
                                    NA
                                                NA
                                                         NA
                                                              NA
                                                                     Red-tailed
       31.3
                                                                     Red-tailed
## 3
             235
                             NA
                                    NA
                                                NA
                                                         NA
                                                              NA
## 4
       23.5
             220
                             NA
                                    NA
                                                NA
                                                         NA
                                                              NA
                                                                       Cooper's
## 5
       14.3
             157
                             NA
                                    NA
                                                NA
                                                         NA
                                                              NA Sharp-shinned
```

1.3 (Q3)

```
print(hawksFullName %>% select(Species, Wing, Weight) %>% head(7))
```

```
##
           Species Wing Weight
## 1
        Red-tailed 385
## 2
        Red-tailed 376
                           930
## 3
        Red-tailed 381
                           990
## 4
          Cooper's 265
                           470
## 5 Sharp-shinned 205
                           170
        Red-tailed 412
## 6
                          1090
## 7
        Red-tailed 370
                           960
```

1.4 (Q1)

```
hawksWithBMI <- Hawks %>% mutate(bird_BMI = 1000*Weight/Wing^2) %>% select(Species, bird_BMI) % arrange(desc(bird_BMI)) print(hawksWithBMI %>% head(8))
```

```
##
     Species bird_BMI
## 1
          RT 852.69973
## 2
          RT 108.75741
## 3
              32.57493
          RT
## 4
          RT
              22.72688
## 5
          CH 22.40818
## 6
          RT 19.54932
## 7
          CH
             15. 21998
## 8
          RT 14.85927
```

1.5 (Q1)

```
## # A tibble: 3 \times 6
##
     Species
                    num_rows mn_wing nd_wing t_mn_wing b_wt_ratio
     <chr>
                       <int>
                                <db1>
                                         <db1>
                                                    <db1>
                                                                <db1>
## 1 Cooper's
                           70
                                                                  1.67
                                  244.
                                           240
                                                     243.
## 2 Red-tailed
                          577
                                  383.
                                           384
                                                     385.
                                                                 3.16
## 3 Sharp-shinned
                          261
                                  185.
                                           191
                                                     184.
                                                                  1.67
```

1.5 (Q2)

```
## # A tibble: 3 \times 8
  Species
                   Wing Weight Culmen Hallux Tail StandardTail Tarsus
  <chr>
                   <int> <int> <int> <int> <int>
                                                           <int> <int>
## 1 Cooper's
                       1
                              0
                                    0
                                            0
                                                              19
                                                                     62
## 2 Red-tailed
                       0
                              5
                                                  0
                                     4
                                            3
                                                             250
                                                                    538
## 3 Sharp-shinned
                              5
                                                              68
                                                                    233
```

2. Random experiments, events and sample spaces, and the set theory

2.1 (Q1)

A Random experiment is a procedure (real or imagined) which: 1. has a well-defined set of possible outcomes 2. could (at least in principle) be repeated arbitrary many times

An event is a set of possible outcomes of an experiments An event is any subset of the sample space, including the empty set and the sample space itself.

A sample space is the set of all possible outcomes of interest for a random experiment

2.1 (Q2)

event: {1,2}

sample space: {(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),...,(6,6)}

total number of different events: $2^{6 imes 6}=2^{36}$

Yes, the empty set is considered an event. It represents the impossible event

2.2 (Q1)

1.
$$A \cup B = \{1, 2, 3, 4, 6\}$$
 $A \cup B = \{1, 2, 3, 4, 5, 6\}$

2.
$$A \cap B = \{2\}$$
 $A \cap B = \{\}$

3.
$$A ackslash B = \{1,3\}$$
 $A ackslash B = \{1,2,3\}$

- 4. A and B are not disjoint, A and C are disjoint
- 5. Yes, B and $A \backslash B$ are disjoint

6. two sets: $\{\{1,2,3\},\{4,5,6\}\}$ three sets:\$ $\{\{1,2\},\{3,4\},\{5,6\}\}$

2.2 (Q2)

1. A

2. empty

3.
$$A^c = \Omega \backslash A, B^c = \Omega \backslash B$$
 because $A \subseteq B, then$ $B^c \subseteq A^c$

4.
$$\bigcup_{k=1}^{K} A_k^c$$

5.
$$(A\cup B)^c=\Omegaackslash(A\cup B)=(\Omegaackslash A)\cap(\Omegaackslash B)=A^c\cap B^c$$

6.
$$\cap_{k=1}^K A_k^c$$

2.2 (Q3)

$$|E|=2^K$$

2.2 (Q4)

1. empty set: \emptyset

2.
$$S_1 \cup S_2 \cup S_3 \cup S_4 = A_1 \cup A_2 \cup A_3 \cup A_4$$

$$S_1\cap S_2=\emptyset \qquad S_2\cap S_3=\emptyset$$

$$S_1\cap S_3=\emptyset \qquad S_2\cap S_4=\emptyset$$

$$S_1\cap S_4=\emptyset \qquad S_3\cap S_4=\emptyset$$

So S_1, S_2, S_3, S_4 form a partition of $A_1 \cup A_2 \cup A_3 \cup A_4$

2.2 (Q5)

1.
$$1_{A^c}(w) = 1 - 1_A(w)$$

2. Ω

3.

Step 1:
$$1_{(A \cap B)^c} = 1 - 1_{(A \cap B)} = 1 - 1_A \cdot 1_B$$

Step 2:
$$1_{A^c \cup B^c} = 1_{A^c} + 1_{B^c} - 1_{A^c} \cdot 1_{B^c} = (1 - 1_A) + (1 - 1_B) - (1 - 1_A)(1 - 1_B) = 1 - 1_A \cdot 1_B$$
 So $(A \cap B)^c = A^c \cup B^c$

2.2 (Q6)

the real number between 0 and 1 is infinite

3. Probability theory

3.1 (Q1)

$$P(x) = egin{cases} 0, & A = \emptyset \ 0.5, & A = a \ 0.1, & A = b \ 0.4, & A = c \ 0.6, & A = a, b \ 0.9, & A = a, c \ 0.5, & A = b, c \ 1, & A = a, b, c \end{cases}$$

3.1 (Q2)

1.
$$\mathbb{P}(A) \geq 0$$
 for any event A

$$\mathbb{P}(\emptyset)=0, \mathbb{P}(0)=1-q, \mathbb{P}(0,1)=1$$

2.
$$\mathbb{P}(\Omega)=\mathbb{P}(0,1)=1$$

3.
$$\mathbb{P}(\cup_{i=1}^{\infty}A_i)=\mathbb{P}(0)+\mathbb{P}(1)=1$$

$$\sum_{i=1}^{\infty} \mathbb{P}(A_i) = \mathbb{P}(0) + \mathbb{P}(1) = 1$$

3.2 (Q1)

$$\mathbb{P}(\cup_{i=1}^n A_i) = \mathbb{P}(A_1) {+} \ldots {+} \mathbb{P}(A_n)$$

$$\sum_{i=1}^n \mathbb{P}(A_i) = \mathbb{P}(A_1) {+} \ldots {+} \mathbb{P}(A_n)$$

3.2 (Q2)

$$\mathbb{P}(S) \cup \mathbb{P}(S^c) = \Omega, \quad \mathbb{P}(S) \cap \mathbb{P}(S^c) = \emptyset$$

$$So \quad \mathbb{P}(S^c) = 1 - \mathbb{P}(S)$$

3.2 (Q3)

S_1={1,2},S_2={2,3},S_3={3,4}

3.2 (Q4)

Draw a diagram