

Plot in python:

1. Create a line plot of the function  $y = \sin(x)$  with a solid blue line and circle markers.
2. Plot  $y = \cos(x)$  with a dashed green line and square markers.
3. Create a line plot of  $y = e^x$  with a dotted red line and triangle markers.
4. Plot  $y = \log(x)$  with a dash-dot black line and star markers.
5. Create a subplot with two line plots: one for  $y = \sin(x)$  and one for  $y = \cos(x)$ .
6. Plot  $y = x^2$  with a thick purple line and plus markers.
7. Create a line plot with a figure size of 10x5 inches, plotting  $y = \sqrt{x}$  with a solid orange line and diamond markers.
8. Plot  $y = \tan(x)$  with a thin gray line and 'x' markers.
9. Create a line plot of  $y = \sin(x) + \cos(x)$  with a dash-dot blue line and cross markers.
10. Plot  $y = \frac{1}{x}$  with a solid green line and hexagon markers.
11. Create a subplot with two rows and one column. In the first subplot, plot  $y = x^3$  with a solid red line. In the second subplot, plot  $y = x^4$  with a dashed blue line.
12. Create a line plot of  $y = \sin(x)$  with a figure size of 12x6 inches, using a dotted black line and 'o' markers.
13. Plot  $y = e^{-x}$  with a thick orange line and 'D' markers.

14. Create a subplot with two line plots: one for  $y = \sin(x)$  with a dashed green line and one for  $y = \cos(x)$  with a solid blue line.

15. Plot  $y = \sin(2x)$  with a dash-dot purple line and 's' markers.

16. Create a line plot of  $y = \cos(2x)$  with a thick black line and 'o' markers.

17. Create a subplot with three rows and one column. In the first subplot, plot  $y = \sin(x)$  with a solid red line. In the second subplot, plot  $y = \cos(x)$  with a dashed green line. In the third subplot, plot  $y = \sin(x) + \cos(x)$  with a dash-dot blue line.

18. Plot  $y = x^2 - 2x + 1$  with a solid blue line and 'x' markers.

19. Create a line plot of  $y = \sqrt{x}$  with a figure size of 8x4 inches, using a dotted green line and '+' markers.

20. Plot  $y = \sin(x) \cos(x)$  with a thick red line and diamond markers.

21. Create a subplot with the function  $y = \sin(x)$ , its first derivative  $y' = \cos(x)$ , and its second derivative  $y'' = -\sin(x)$ . Use a solid line for the function and dashed lines for the derivatives.

22. Create a subplot with the function  $y = x^2$ , its first derivative  $y' = 2x$ , and its second derivative  $y'' = 2$ . Use different line styles and markers for each plot.

23. Plot  $y = e^x$  with subplots showing its first derivative  $y' = e^x$  and second derivative  $y'' = e^x$ . Use solid lines for the function and dashed lines for the derivatives.

24. Create a subplot with  $y = \log(x)$ , its first derivative  $y' = \frac{1}{x}$  and its second derivative  $y'' = -\frac{1}{x^2}$ . Use different colors and line styles for each.

25. Plot  $y = \tan(x)$  with subplots showing its first derivative  $y' = \sec^2(x)$  and its second derivative  $y'' = 2\sec^2(x) \tan(x)$ .

### Steepest Descent Method

1. Implement the Steepest Descent Method to minimize the function  $f(x, y) = x^2 + y^2$ .

Initialize the starting point at  $(1, 1)$ , set the step size  $\alpha = 0.1$ , and use a convergence tolerance of  $1e-6$ .

2. Apply the Steepest Descent Method to minimize the following functions:

-  $f(x, y) = x^2 + 2xy + y^2$

-  $f(x, y) = \sin(x) + \cos(y)$

Initialize at  $(0, 0)$  and use a step size  $\alpha = 0.01$  and a convergence tolerance of  $1e-6$ .

3. Convergence Analysis

Implement the Steepest Descent Method for the function  $f(x, y) = (x - 1)^2 + (y - 2)^2$  with different step sizes ( $\alpha = 0.1$ ,  $\alpha = 0.01$ ,  $\alpha = 0.001$ ).

4. Implement the Steepest Descent Method to minimize the function  $f(x, y) = x^2 + 2xy + y^2$ .

5. Apply the Steepest Descent Method to minimize the non-quadratic function  $f(x, y) = e^{-(x^2 + y^2)}$ .

Use a starting point  $(1, 1)$ , a step size  $\alpha = 0.1$ , and a convergence tolerance of  $1e-6$ .