

Results are obtained with  $h_0^P$  estimated

CALIBRATED PARAMETERS ON WEDNESDAYS USING OPTIONS LIKELIHOOD, $h_0^Q = h_t^P$									
$\theta$	2010	2011	2012	2013	2014	2015	2016	2017	2018
$\omega$	$2.9373e-07$	$8.3428e-06$	$2.0557e-09$	$1.4603e-06$	$1.9938e-06$	$4.7113e-07$	$6.9592e-07$	$3.5608e-07$	$2.8373e-07$
<b>std</b>	$(1.5899e-06)$	$(2.7177e-05)$	$(4.0487e-09)$	$(4.9823e-06)$	$(6.7867e-06)$	$(2.5578e-06)$	$(3.0411e-06)$	$(2.0030e-06)$	$(1.8910e-06)$
<b>ci</b>	$(\pm 4.3822e-07)$	$(\pm 7.4910e-06)$	$(\pm 1.1272e-09)$	$(\pm 1.4013e-06)$	$(\pm 1.8706e-06)$	$(\pm 7.0501e-07)$	$(\pm 8.3824e-07)$	$(\pm 5.5763e-07)$	$(\pm 5.2647e-07)$
<b>median</b>	$4.4080e-10$	$2.1679e-09$	$1.1257e-09$	$1.5347e-09$	$1.3127e-09$	$1.3856e-09$	$7.3148e-10$	$2.7972e-10$	$4.9914e-10$
$\alpha$	$2.6506e-05$	$2.2808e-05$	$2.0436e-05$	$1.5988e-05$	$1.4776e-05$	$1.3678e-05$	$1.3866e-05$	$9.2340e-06$	$1.6279e-05$
<b>std</b>	$(2.1430e-05)$	$(2.2449e-05)$	$(1.7810e-05)$	$(1.2247e-05)$	$(9.2665e-06)$	$(6.8892e-06)$	$(8.7406e-06)$	$(4.9557e-06)$	$(1.1036e-05)$
<b>ci</b>	$(\pm 5.9068e-06)$	$(\pm 6.1876e-06)$	$(\pm 4.9583e-06)$	$(\pm 3.4444e-06)$	$(\pm 2.5542e-06)$	$(\pm 1.8989e-06)$	$(\pm 2.4092e-06)$	$(\pm 1.3797e-06)$	$(\pm 3.0725e-06)$
<b>median</b>	$2.1958e-05$	$2.0325e-05$	$1.4954e-05$	$1.5884e-05$	$1.4270e-05$	$1.2722e-05$	$1.2912e-05$	$9.1517e-06$	$1.5918e-05$
$\beta$	0.4708	0.3164	0.4553	0.3331	0.1703	0.1908	0.2374	0.1474	0.2896
<b>std</b>	(0.3272)	(0.3221)	(0.3657)	(0.3768)	(0.2815)	(0.2349)	(0.3108)	(0.2931)	(0.3377)
<b>ci</b>	$(\pm 0.0902)$	$(\pm 0.0888)$	$(\pm 0.1018)$	$(\pm 0.1060)$	$(\pm 0.0776)$	$(\pm 0.0647)$	$(\pm 0.0857)$	$(\pm 0.0816)$	$(\pm 0.0940)$
<b>median</b>	0.5549	0.3131	0.6192	0.0023	0.0002	0.0090	0.0007	0.0001	0.0010
$\gamma^*$	155.5027	256.7574	176.9894	247.3834	225.9295	224.0573	257.7868	275.5854	191.7579
<b>std</b>	(149.9840)	(289.5641)	(121.4388)	(267.6261)	(201.9510)	(48.8853)	(247.1550)	(187.7364)	(108.0334)
<b>ci</b>	$(\pm 41.3407)$	$(\pm 79.8138)$	$(\pm 33.8088)$	$(\pm 75.2711)$	$(\pm 55.6646)$	$(\pm 13.4744)$	$(\pm 68.1243)$	$(\pm 52.2661)$	$(\pm 30.0767)$
<b>median</b>	115.7838	148.3374	137.7486	166.2098	189.4759	226.1581	205.5256	237.1314	159.7501
$h_0^Q = h_t^P$	$1.2843e-04$	$1.5885e-04$	$8.8858e-05$	$6.0313e-05$	$6.5265e-05$	$1.1085e-04$	$9.9075e-05$	$4.0828e-05$	$1.1258e-04$
<b>std</b>	$(8.7675e-05)$	$(1.0228e-04)$	$(4.2482e-05)$	$(3.1009e-05)$	$(3.7863e-05)$	$(6.5832e-05)$	$(7.2668e-05)$	$(2.3485e-05)$	$(8.8642e-05)$
<b>ci</b>	$(\pm 2.4166e-05)$	$(\pm 2.8191e-05)$	$(\pm 1.1827e-05)$	$(\pm 8.7213e-06)$	$(\pm 1.0436e-05)$	$(\pm 1.8145e-05)$	$(\pm 2.0030e-05)$	$(\pm 6.5382e-06)$	$(\pm 2.4678e-05)$
<b>median</b>	$1.1288e-04$	$1.3446e-04$	$8.4289e-05$	$4.8973e-05$	$5.5260e-05$	$9.2823e-05$	$7.8758e-05$	$3.3053e-05$	$9.1614e-05$
<b>MSE</b>	1.3115	4.7861	2.6162	4.2244	8.4450	6.3652	10.9788	23.0601	13.4936
<b>IVRMSE</b>	0.0639	0.0955	0.0867	0.0890	0.0933	0.0939	0.1111	0.1248	0.0897
<b>MAPE</b>	0.0741	0.0936	0.1184	0.1292	0.1568	0.1523	0.1709	0.2464	0.1414
<b>OptLL</b>	215.4291	208.3681	251.0076	333.0039	351.3072	436.8099	513.2066	555.4006	684.7143

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CALIBRATED PARAMETERS ON WEDNESDAYS, $h_0^Q = \frac{\omega_0 + \alpha_0}{1 - \beta_0 - \alpha_0 \gamma_0^{*2}}$ , WITH $\omega_0, \alpha_0, \beta_0, \gamma_0^{*2}$ FROM MLE UNDER P AND UPDATED UNDER Q									
$\theta$	2010	2011	2012	2013	2014	2015	2016	2017	2018
$\omega$	8.5029e-08	9.2714e-06	1.9246e-07	2.2129e-06	1.9389e-06	4.1610e-07	5.9987e-07	3.5299e-07	5.5812e-07
<b>std</b>	(4.4877e-07)	(2.7968e-05)	(1.0856e-06)	(6.4184e-06)	(6.6239e-06)	(2.4952e-06)	(2.9189e-06)	(2.0142e-06)	(2.7146e-06)
<b>ci</b>	( $\pm 1.2370e-07$ )	( $\pm 7.7090e-06$ )	( $\pm 3.0224e-07$ )	( $\pm 1.8052e-06$ )	( $\pm 1.8258e-06$ )	( $\pm 6.8777e-07$ )	( $\pm 8.0455e-07$ )	( $\pm 5.6074e-07$ )	( $\pm 7.5576e-07$ )
<b>median</b>	4.8556e-10	1.1932e-09	9.6775e-10	1.6296e-09	1.4218e-09	1.6699e-09	8.8906e-10	3.4979e-10	6.2288e-10
$\alpha$	2.5394e-05	2.1003e-05	1.8778e-05	1.3908e-05	1.3646e-05	1.3883e-05	1.3858e-05	8.2692e-06	1.5954e-05
<b>std</b>	(2.2029e-05)	(2.0947e-05)	(1.6410e-05)	(1.1489e-05)	(8.5375e-06)	(5.9109e-06)	(8.0356e-06)	(4.8704e-06)	(9.4418e-06)
<b>ci</b>	( $\pm 6.0720e-06$ )	( $\pm 5.7736e-06$ )	( $\pm 4.5685e-06$ )	( $\pm 3.2313e-06$ )	( $\pm 2.3532e-06$ )	( $\pm 1.6292e-06$ )	( $\pm 2.2149e-06$ )	( $\pm 1.3559e-06$ )	( $\pm 2.6286e-06$ )
<b>median</b>	1.7658e-05	1.9181e-05	1.2068e-05	1.2723e-05	1.3239e-05	1.3217e-05	1.3228e-05	8.3302e-06	1.4242e-05
$\beta$	0.5032	0.3363	0.4882	0.3724	0.1836	0.1643	0.2466	0.1768	0.2450
<b>std</b>	(0.3188)	(0.3212)	(0.3411)	(0.3801)	(0.2898)	(0.2274)	(0.3159)	(0.3270)	(0.3193)
<b>ci</b>	( $\pm 0.0879$ )	( $\pm 0.0885$ )	( $\pm 0.0950$ )	( $\pm 0.1069$ )	( $\pm 0.0799$ )	( $\pm 0.0627$ )	( $\pm 0.0871$ )	( $\pm 0.0910$ )	( $\pm 0.0889$ )
<b>median</b>	0.5759	0.3823	0.5857	0.3025	0.0003	0.0007	0.0018	0.0001	0.0023
$\gamma^*$	152.7405	213.9027	178.3425	268.5595	254.9716	221.9130	209.9787	301.8938	202.9867
<b>std</b>	(136.5742)	(168.6915)	(140.6359)	(295.7190)	(239.7515)	(41.5011)	(73.9368)	(189.9283)	(132.2615)
<b>ci</b>	( $\pm 37.6445$ )	( $\pm 46.4971$ )	( $\pm 39.1533$ )	( $\pm 83.1723$ )	( $\pm 66.0837$ )	( $\pm 11.4391$ )	( $\pm 20.3795$ )	( $\pm 52.8764$ )	( $\pm 36.8218$ )
<b>median</b>	112.0207	155.9251	147.8898	169.4020	202.0041	228.8470	208.6253	261.8796	167.7543
$h_0^Q = h_t^P$	1.2504e-04	1.6094e-04	8.8020e-05	6.3516e-05	6.4968e-05	1.0677e-04	9.4593e-05	4.2065e-05	1.2042e-04
<b>std</b>	(8.4350e-05)	(1.0127e-04)	(3.9993e-05)	(3.0169e-05)	(3.7802e-05)	(5.3934e-05)	(6.6163e-05)	(2.5624e-05)	(9.2499e-05)
<b>ci</b>	( $\pm 2.3250e-05$ )	( $\pm 2.7914e-05$ )	( $\pm 1.1134e-05$ )	( $\pm 8.4851e-06$ )	( $\pm 1.0419e-05$ )	( $\pm 1.4866e-05$ )	( $\pm 1.8237e-05$ )	( $\pm 7.1338e-06$ )	( $\pm 2.5752e-05$ )
<b>median</b>	1.0398e-04	1.3887e-04	7.9893e-05	5.2671e-05	5.4472e-05	8.9209e-05	6.9330e-05	3.6036e-05	1.0226e-04
<b>MSE</b>	1.1660	4.6442	2.4437	4.3159	7.5939	6.1701	10.7231	20.7106	13.3130
<b>IVRMSE</b>	0.0633	0.0921	0.0863	0.0894	0.0927	0.0927	0.1089	0.1237	0.0887
<b>MAPE</b>	0.0734	0.0906	0.1179	0.1315	0.1531	0.1484	0.1669	0.2416	0.1395
<b>OptLL</b>	216.3430	211.5388	252.2146	334.4711	356.0208	438.7128	515.4908	559.3221	688.0683

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CALIBRATED PARAMETERS ON WEDNESDAYS USING OPTIONS LIKELIHOOD, $h_0^Q$ IS REALIZED VOLATILITY									
$\theta$	2010	2011	2012	2013	2014	2015	2016	2017	2018
$\omega$	$4.4390e-06$	$1.6421e-05$	$1.2371e-06$	$2.3916e-06$	$1.6398e-06$	$1.0287e-06$	$1.3292e-06$	$1.7818e-07$	$5.5739e-06$
<b>std</b>	$(2.1202e-05)$	$(3.7688e-05)$	$(4.8847e-06)$	$(6.4010e-06)$	$(5.4933e-06)$	$(3.6010e-06)$	$(3.7767e-06)$	$(9.9009e-07)$	$(2.3025e-05)$
<b>ci</b>	$(\pm 5.8441e-06)$	$(\pm 1.0388e-05)$	$(\pm 1.3599e-06)$	$(\pm 1.8003e-06)$	$(\pm 1.5141e-06)$	$(\pm 9.9256e-07)$	$(\pm 1.0410e-06)$	$(\pm 2.7564e-07)$	$(\pm 6.4101e-06)$
<b>median</b>	$7.1991e-10$	$2.7245e-09$	$1.0594e-09$	$3.2019e-09$	$8.7991e-10$	$1.5623e-09$	$1.0905e-09$	$2.9135e-10$	$8.2769e-10$
$\alpha$	$3.6449e-05$	$3.0352e-05$	$2.6117e-05$	$1.0640e-05$	$1.3074e-05$	$1.1916e-05$	$1.3060e-05$	$4.4963e-06$	$1.2185e-05$
<b>std</b>	$(2.8777e-05)$	$(2.8048e-05)$	$(2.0832e-05)$	$(1.0869e-05)$	$(1.3823e-05)$	$(1.0055e-05)$	$(1.1191e-05)$	$(5.0144e-06)$	$(1.3058e-05)$
<b>ci</b>	$(\pm 7.9318e-06)$	$(\pm 7.7309e-06)$	$(\pm 5.7997e-06)$	$(\pm 3.0568e-06)$	$(\pm 3.8100e-06)$	$(\pm 2.7716e-06)$	$(\pm 3.0846e-06)$	$(\pm 1.3960e-06)$	$(\pm 3.6355e-06)$
<b>median</b>	$2.7865e-05$	$2.0508e-05$	$1.8591e-05$	$7.1029e-06$	$7.8547e-06$	$8.9842e-06$	$8.6525e-06$	$3.1924e-06$	$9.4728e-06$
$\beta$	0.4154	0.3178	0.4034	0.5183	0.4359	0.3807	0.3932	0.5989	0.4758
<b>std</b>	(0.3534)	(0.3373)	(0.3495)	(0.3480)	(0.3691)	(0.3181)	(0.3109)	(0.3133)	(0.3576)
<b>ci</b>	$(\pm 0.0974)$	$(\pm 0.0930)$	$(\pm 0.0973)$	$(\pm 0.0979)$	$(\pm 0.1017)$	$(\pm 0.0877)$	$(\pm 0.0857)$	$(\pm 0.0872)$	$(\pm 0.0996)$
<b>median</b>	0.5079	0.2049	0.4684	0.6798	0.5937	0.5059	0.4466	0.7443	0.6481
$\gamma^*$	122.4610	172.1046	148.9414	316.1972	260.0664	244.0577	251.5891	307.1280	256.7916
<b>std</b>	(110.7548)	(153.0932)	(118.6459)	(375.3863)	(259.3262)	(132.3480)	(243.2757)	(172.5592)	(228.0918)
<b>ci</b>	$(\pm 30.5278)$	$(\pm 42.1977)$	$(\pm 33.0312)$	$(\pm 105.5791)$	$(\pm 71.4792)$	$(\pm 36.4796)$	$(\pm 67.0551)$	$(\pm 48.0408)$	$(\pm 63.5012)$
<b>median</b>	100.2388	132.6313	126.5910	161.2021	177.3985	221.2115	194.6935	287.6256	179.1764
$h_0^Q = h_t^P$	$8.6011e-05$	$1.5683e-04$	$5.7150e-05$	$4.7600e-05$	$4.2269e-05$	$7.3948e-05$	$5.8848e-05$	$1.2876e-05$	$5.7619e-05$
<b>std</b>	$(7.7213e-05)$	$(2.4253e-04)$	$(4.8172e-05)$	$(5.7769e-05)$	$(7.5395e-05)$	$(1.1377e-04)$	$(8.1886e-05)$	$(7.9046e-06)$	$(5.6720e-05)$
<b>ci</b>	$(\pm 2.1283e-05)$	$(\pm 6.6849e-05)$	$(\pm 1.3411e-05)$	$(\pm 1.6248e-05)$	$(\pm 2.0782e-05)$	$(\pm 3.1358e-05)$	$(\pm 2.2571e-05)$	$(\pm 2.2006e-06)$	$(\pm 1.5791e-05)$
<b>median</b>	$6.0175e-05$	$6.9450e-05$	$4.1358e-05$	$3.3327e-05$	$2.2715e-05$	$4.5815e-05$	$2.6906e-05$	$1.1264e-05$	$3.6139e-05$
<b>MSE</b>	1.7891	5.3716	2.5919	3.0224	4.9591	3.6728	4.0827	4.0435	14.2469
<b>IVRMSE</b>	0.0710	0.1004	0.0897	0.0873	0.0936	0.0975	0.1014	0.1046	0.0966
<b>MAPE</b>	0.0802	0.1010	0.1322	0.1310	0.1535	0.1631	0.1585	0.1894	0.1503
<b>OptLL</b>	211.2856	207.1647	247.0419	341.4580	363.2253	438.8849	538.5336	625.4260	679.0972

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CALIBRATED PARAMETERS ON WEDNESDAYS, $h_0^Q$ IS CALIBRATED WITH RESPECT TO OPTIONS LIKELIHOOD									
$\theta$	2010	2011	2012	2013	2014	2015	2016	2017	2018
$\omega$	$1.2384e-08$	$4.0086e-07$	$3.1333e-08$	$1.3755e-07$	$6.9525e-08$	$2.3119e-08$	$4.5524e-08$	$1.5096e-08$	$1.8178e-08$
<b>std</b>	$(7.1945e-08)$	$(1.5924e-06)$	$(1.6514e-07)$	$(4.7604e-07)$	$(3.7729e-07)$	$(1.2129e-07)$	$(2.3641e-07)$	$(7.4217e-08)$	$(8.3026e-08)$
<b>ci</b>	$(\pm 1.9830e-08)$	$(\pm 4.3891e-07)$	$(\pm 4.5975e-08)$	$(\pm 1.3389e-07)$	$(\pm 1.0399e-07)$	$(\pm 3.3431e-08)$	$(\pm 6.5163e-08)$	$(\pm 2.0662e-08)$	$(\pm 2.3115e-08)$
<b>median</b>	$4.2614e-10$	$1.2486e-09$	$7.9886e-10$	$1.2631e-09$	$7.7874e-10$	$1.1199e-09$	$8.6919e-10$	$5.7281e-10$	$7.1012e-10$
$\alpha$	$1.8162e-05$	$1.4839e-05$	$8.9367e-06$	$6.2985e-06$	$8.1050e-06$	$7.2957e-06$	$4.6588e-06$	$2.9109e-06$	$1.3426e-05$
<b>std</b>	$(1.9355e-05)$	$(2.0035e-05)$	$(1.2221e-05)$	$(7.9525e-06)$	$(9.8222e-06)$	$(7.3411e-06)$	$(4.0920e-06)$	$(4.0307e-06)$	$(1.6537e-05)$
<b>ci</b>	$(\pm 5.3349e-06)$	$(\pm 5.5222e-06)$	$(\pm 3.4023e-06)$	$(\pm 2.2367e-06)$	$(\pm 2.7073e-06)$	$(\pm 2.0235e-06)$	$(\pm 1.1279e-06)$	$(\pm 1.1222e-06)$	$(\pm 4.6039e-06)$
<b>median</b>	$1.0695e-05$	$7.6836e-06$	$4.7572e-06$	$3.3952e-06$	$2.8549e-06$	$4.3648e-06$	$2.9570e-06$	$1.4933e-06$	$4.5110e-06$
$\beta$	0.6465	0.5668	0.7271	0.7325	0.6222	0.5594	0.6426	0.7106	0.5391
<b>std</b>	(0.2643)	(0.2919)	(0.2165)	(0.2499)	(0.3072)	(0.2501)	(0.2077)	(0.2807)	(0.3762)
<b>ci</b>	$(\pm 0.0728)$	$(\pm 0.0805)$	$(\pm 0.0603)$	$(\pm 0.0703)$	$(\pm 0.0847)$	$(\pm 0.0689)$	$(\pm 0.0573)$	$(\pm 0.0781)$	$(\pm 0.1047)$
<b>median</b>	0.7430	0.6600	0.8060	0.8158	0.7748	0.6585	0.6903	0.8071	0.6888
$\gamma^*$	134.3603	195.1009	191.4698	217.4109	237.1588	270.9957	276.1619	324.0345	227.4457
<b>std</b>	(48.5942)	(98.6148)	(95.9266)	(146.4449)	(111.0569)	(123.2736)	(75.2875)	(114.3511)	(110.3211)
<b>ci</b>	$(\pm 13.3942)$	$(\pm 27.1816)$	$(\pm 26.7061)$	$(\pm 41.1883)$	$(\pm 30.6111)$	$(\pm 33.9784)$	$(\pm 20.7518)$	$(\pm 31.8355)$	$(\pm 30.7136)$
<b>median</b>	127.2052	175.8919	171.5645	181.2201	221.1372	254.0407	294.1570	327.0867	198.2446
$h_0^Q$	$1.2662e-04$	$2.2087e-04$	$8.4211e-05$	$4.9742e-05$	$4.9380e-05$	0.0001	$6.8390e-05$	$1.8939e-05$	$1.3543e-04$
<b>std</b>	$(1.3048e-04)$	$(2.2980e-04)$	$(5.8095e-05)$	$(4.5784e-05)$	$(5.8697e-05)$	$(1.1334e-04)$	$(7.6510e-05)$	$(1.9366e-05)$	$(1.7217e-04)$
<b>ci</b>	$(\pm 3.5965e-05)$	$(\pm 6.3341e-05)$	$(\pm 1.6174e-05)$	$(\pm 1.2877e-05)$	$(\pm 1.6179e-05)$	$(\pm 3.1241e-05)$	$(\pm 2.1089e-05)$	$(\pm 5.3916e-06)$	$(\pm 4.7933e-05)$
<b>median</b>	$9.2058e-05$	$1.1459e-04$	$6.0478e-05$	$3.5047e-05$	$2.7422e-05$	$5.5033e-05$	$3.8411e-05$	$1.3835e-05$	$4.6850e-05$
<b>MSE</b>	0.6622	1.0575	1.0914	0.6991	1.0554	1.3990	1.6195	2.2744	4.8658
<b>IVRMSE</b>	0.0559	0.0659	0.0806	0.0776	0.0798	0.0917	0.0983	0.1006	0.0792
<b>MAPE</b>	0.0662	0.0726	0.1098	0.1032	0.1205	0.1355	0.1307	0.1651	0.1233
<b>OptLL</b>	226.0306	234.8200	265.2162	363.1728	389.5383	469.0620	572.8691	650.3873	729.6044